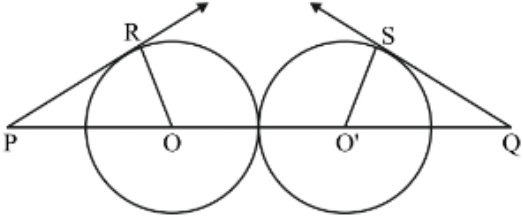


# MBA PRO 2024

## QUANTITATIVE APTITUDE

DPP: 20

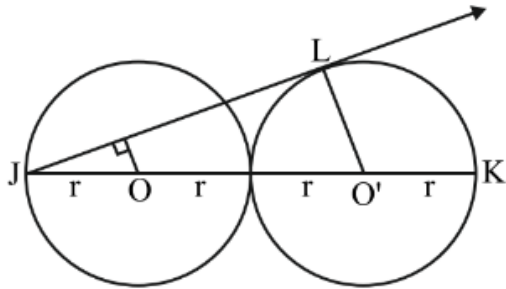
### Circles 3

- Q1** What if one circle lie completely outside the other circle then the number of direct common tangent (D) and Transverse common tangent (T) will be :
- (A)  $D = 2, T = 2$                       (B)  $D = 1, T = 2$   
 (C)  $D = 2, T = 1$                       (D)  $D = 0, T = 1$
- Q2** What if two other circle touch each other externally then the number of direct common tangent and transverse common tangent will be :
- (A)  $D = 2, T = 2$                       (B)  $D = 2, T = 1$   
 (C)  $D = 2, T = 0$                       (D)  $D = 0, T = 0$
- Q3** What if two circles touch each other internally then the number of direct and transverse common tangent will be :
- (A)  $D = 1, T = 0$   
 (B)  $D = 2, T = 1$   
 (C)  $D = 2, T = 2$   
 (D)  $D = 0, T = 0$
- Q4** What if two circles intersect each other at two points then the number of direct and transverse common tangent will be :
- (A)  $D = 2, T = 0$                       (B)  $D = 1, T = 1$   
 (C)  $D = 2, T = 2$                       (D)  $D = 0, T = 0$
- Q5** What if one circle is entirely inside the other circle without touching the outer circle then the number of direct and transverse common tangent.
- (A)  $D = 0, T = 0$                       (B)  $D = 1, T = 1$   
 (C)  $D = 2, T = 2$                       (D)  $D = 2, T = 1$
- Q6** Ritesh a Mathematician draw a pair of circle whose radius are  $9\text{cm}$  and  $5\text{cm}$ . The distance of the center of the circle is  $18\text{cm}$  then the length of transverse tangent will be :
- (A)  $6\sqrt{3}\text{cm}$   
 (B)  $8\sqrt{2}\text{cm}$   
 (C)  $4\sqrt{3}\text{cm}$   
 (D)  $4\sqrt{2}\text{cm}$
- Q7** Ritesh a Mathematician draw a pair of circle of radius  $13\text{ cm}$  and  $15\text{ cm}$ . The distance between the centre of the circle is  $35\text{ cm}$ . Find the length of direct common tangent (in cm)
- (A)  $17\sqrt{21}$                                       (B)  $12\sqrt{21}$   
 (C)  $\sqrt{1221}$                                       (D)  $\sqrt{1421}$
- Q8** Ritesh a Mathematician draw a pair of circle whose direct common tangent and transverse common tangent are  $35$  and  $25$  respectively. Find the product of radius of bigger circle to the smaller circle.
- (A)  $100\text{ cm}$                                       (B)  $150\text{ cm}$   
 (C)  $180\text{ cm}$                                       (D)  $210\text{ cm}$
- Q9**
- 
- Find the length of  $PQ$  (in cm) if we have  $OR = 5\text{ cm}$ ,  $PR = 12\text{ cm}$ ,  $O'S = 7\text{ cm}$  and  $QS = 24\text{ cm}$ . Also,



it is given that  $O$  and  $O'$  are the centres of the two circles respectively.

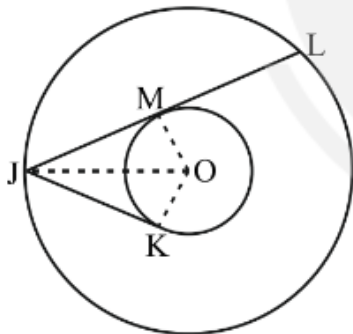
**Q10**



Two equal circle in which  $JL$  is a tangent. Find the ratio between the length of  $JL$  and  $JO'$ .

- (A)  $2\sqrt{2} : 1$
- (B)  $2\sqrt{2} : \sqrt{3}$
- (C)  $2\sqrt{2} : 5$
- (D)  $2\sqrt{2} : 2$

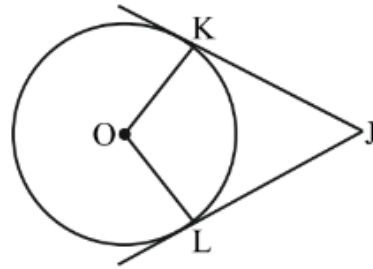
- Q11** Rahul draws two concentric circles in such a way that the tangent drawn from a point lying at outer circle, to the inner circle. Find  $JL$  if the radius of inner circle and distance between centre ( $O$ ) and point  $J$  is  $5\text{cm}$  and  $12\text{cm}$  respectively.



- (A)  $24\text{cm}$
- (B)  $25\text{cm}$
- (C)  $2 \times \sqrt{119}\text{cm}$
- (D)  $27\text{cm}$

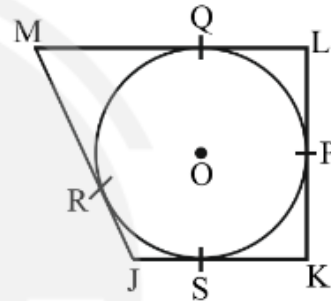
- Q12** Sujeet draw a circle in which tangent from point  $J$  is draw as shown in the figure. If  $OK = 7.5\text{cm}$  and  $KJ$  and  $JL$  are

perpendicular to each other. Find the length of  $JK$  given that  $O$  is the centre of the circle.



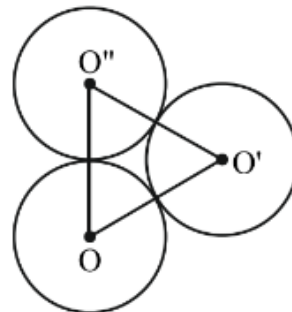
- (A)  $7.5\text{cm}$
- (B)  $8\text{cm}$
- (C)  $8.5\text{cm}$
- (D)  $9\text{cm}$

- Q13** Praful billore drawn a quadrilateral to circumscribe a circle as shown in figure then which of the following is true :



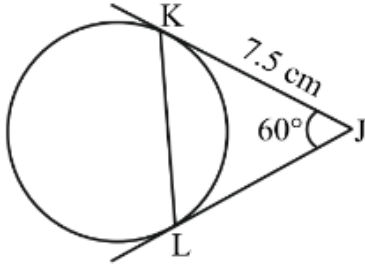
- (A)  $JK + LM = JM + KL$
- (B)  $JK = LK$
- (C)  $JS - LP = MR$
- (D)  $MR + SK = PL$

- Q14** Aniket draws three circles which touch each other externally as shown in figure. Find the radius of the circle (in  $\text{cm}$ ) with center  $O'$  if  $OO' = 11\text{cm}$ ,  $O'O'' = 12\text{cm}$  and  $O''O = 13\text{cm}$ .



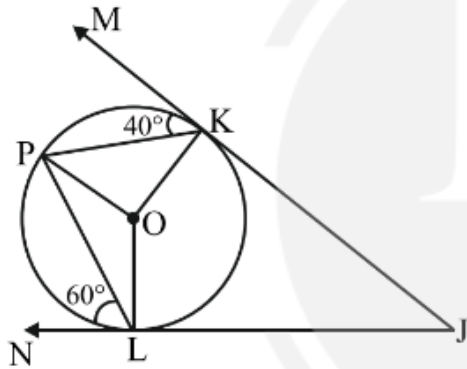
- (A) 5  
(C) 7
- (B) 6  
(D) 8

**Q15** JK and JL are tangents to the circle given below. Find the length of KL.



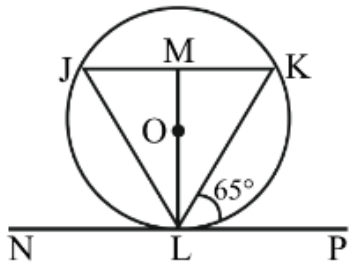
- (A) 7.5 cm  
(C) 8 cm
- (B) 6 cm  
(D) 9.5 cm

**Q16** In the figure, JM and JN are tangent at K and L respectively.  $\angle MKP = 40^\circ$  and  $\angle NLP = 60^\circ$ . Find the measure of  $\angle LPK$ .



- (A)  $60^\circ$   
(C)  $80^\circ$
- (B)  $70^\circ$   
(D)  $90^\circ$

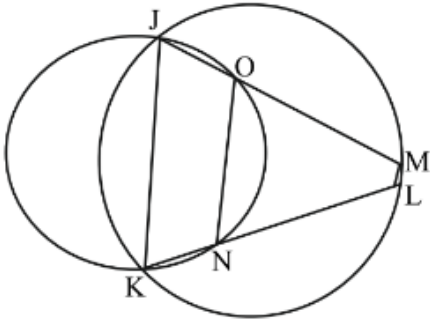
**Q17** In the given figure NLP is a tangent and  $\angle KLP = 65^\circ$  then find the value of  $\angle JLK$  if  $JK \parallel NP$  given that OM is perpendicular to JK.



- (A)  $25^\circ$   
(B)  $30^\circ$

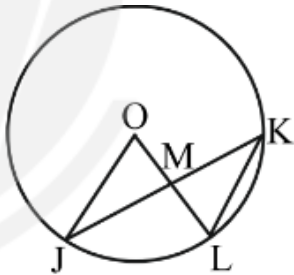
- (C)  $40^\circ$   
(D)  $50^\circ$

**Q18** Kiran draw the above figure in which JKLM is a cyclic quadrilateral. A small circle passing through J and K meets JM and KL at O and N respectively, then which of the following is true.



- (A)  $ON \parallel ML$   
(B)  $\angle JON = \angle JML$   
(C)  $JO = ML$   
(D) Both (a) and (b)

**Q19** Barsha draw the following figure in which  $\angle JOL = 50^\circ$  and  $\angle LMK = 105^\circ$ . Find  $\angle MLK$ .

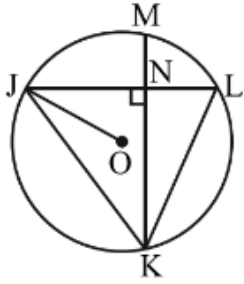


- (A)  $40^\circ$   
(C)  $60^\circ$
- (B)  $50^\circ$   
(D)  $70^\circ$

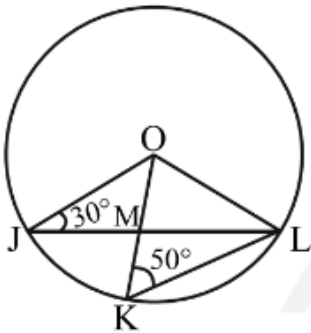
**Q20** In the following figure, chord JL and MK intersect each other at point N. If  $\angle OJK$  is



$30^\circ$ . Find the value of  $\angle NKL$  in degrees.

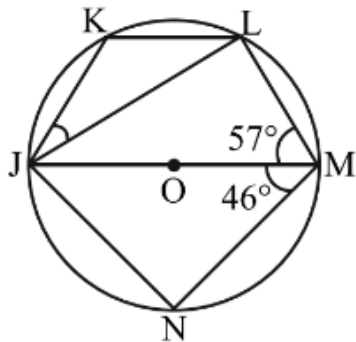


- Q21** In the figure,  $O$  is the centre of the circle,  $\angle OJL = 30^\circ$  and  $\angle OKL = 50^\circ$ , find  $\angle JOK$ .



- (A)  $20^\circ$   
(B)  $30^\circ$   
(C)  $45^\circ$   
(D)  $40^\circ$

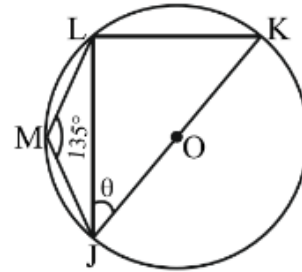
- Q22** Sunil draw the above circle in which JM is the diameter of the circle with centre  $O$ .  $\angle JML = 57^\circ$ ,  $\angle JMN = 46^\circ$  then find the sum of  $\angle MJN$ ,  $\angle MJL$ ,  $\angle JLK$  if  $KL \parallel JM$ .



- (A)  $105^\circ$   
(B)  $112^\circ$   
(C)  $117^\circ$

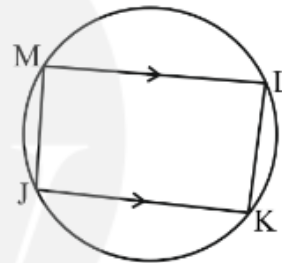
(D)  $110^\circ$

- Q23** Sundar draw the below figure in which JKLM is a cyclic quadrilateral in which JK is the diameter and  $\angle JML = 135^\circ$ . Find the value of  $\angle LJK$ .



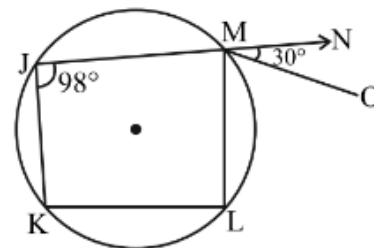
- (A)  $40^\circ$  (B)  $55^\circ$   
(C)  $50^\circ$  (D)  $45^\circ$

- Q24** Suket draw this figure in which JKLM in a cyclic quadrilateral in which  $JK \parallel LM$  and  $\angle KJM = 96^\circ$  then find the difference of  $\angle MLK$  and  $\angle JKL$ .



- (A)  $8^\circ$  (B)  $10^\circ$   
(C)  $14^\circ$  (D)  $12^\circ$

- Q25** Alex draw this figure in which JKLM is a cyclic quadrilateral.  $\angle NMO = 30^\circ$ ,  $\angle MJK = 98^\circ$  and  $MO \parallel KL$ , then find the value of  $\angle JKL$ .

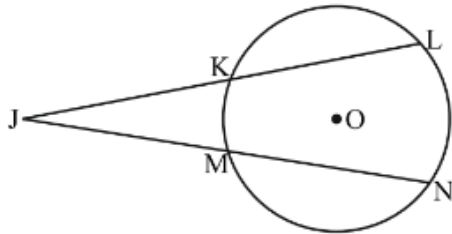


- (A)  $110^\circ$   
(B)  $112^\circ$   
(C)  $114^\circ$



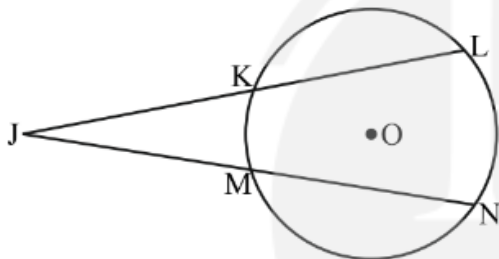
(D)  $116^\circ$ 

- Q26** In the given figure  $JK = 2\text{cm}$ ,  $KL = 6\text{cm}$ ,  $JN = 12\text{ cm}$  then find JM.



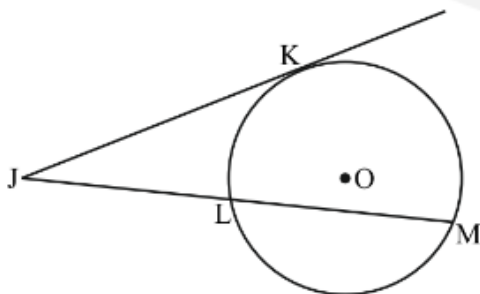
- (A)  $1.5\text{cm}$  (B)  $1.72\text{cm}$   
(C)  $1.33\text{cm}$  (D)  $2\text{cm}$

- Q27** In the given figure  $JL = 12\text{cm}$ ,  $KL = 8\text{cm}$ ,  $JM = 4.5\text{cm}$  then find the value of  $JN$ .



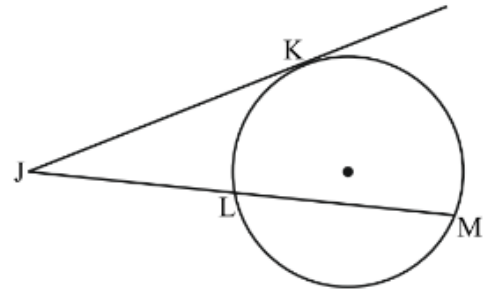
- (A)  $10.67\text{cm}$  (B)  $10\text{cm}$   
(C)  $11\text{cm}$  (D)  $12\text{cm}$

- Q28** In the given figure,  $JK$  is tangent,  $JM$  is secant where  $JK = a$ ,  $JL = b$  and  $LM = c$  then which of the following is true.



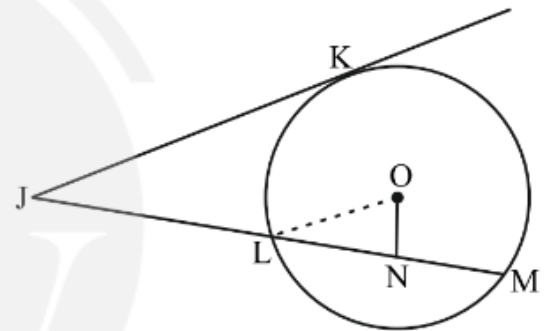
- (A)  $(a + b)(a - b) = 0$   
(B)  $a^2 = b \times c$   
(C)  $(a + b)(a - b) = bc$   
(D)  $a^2 = \frac{bc}{c}$

- Q29** In the given figure,  $JK = 3.5\text{cm}$ ,  $JM = 10\text{cm}$  then find the length of JL.



- (A)  $1.025\text{cm}$  (B)  $2.325\text{cm}$   
(C)  $1.275\text{cm}$  (D)  $1.225\text{cm}$

- Q30** In the given figure,  $JK = 14\text{cm}$ ,  $JL = 7\text{cm}$  and the radius of circle is  $14.5\text{cm}$  then find the length (in cm) of the perpendicular drawn on chord LM from centre O in cm.



## Answer Key

Q1 (A)  
Q2 (B)  
Q3 (A)  
Q4 (A)  
Q5 (A)  
Q6 (B)  
Q7 (C)  
Q8 (B)  
Q9 50  
Q10 (B)  
Q11 (C)  
Q12 (A)  
Q13 (A)  
Q14 (A)  
Q15 (A)

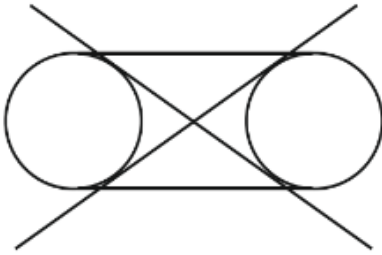
Q16 (C)  
Q17 (D)  
Q18 (D)  
Q19 (B)  
Q20 30  
Q21 (D)  
Q22 (D)  
Q23 (D)  
Q24 (D)  
Q25 (B)  
Q26 (C)  
Q27 (A)  
Q28 (C)  
Q29 (D)  
Q30 10



# Hints & Solutions

**Q1 Text Solution:**

The figure looks like that,

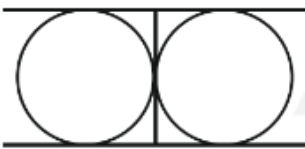


Here direct tangent (D) = 2

Transverse tangent (T) = 2

**Q2 Text Solution:**

The figure looks like that,



Direct tangent = 2

Transverse tangent = 1

**Q3 Text Solution:**

The figure looks like that,

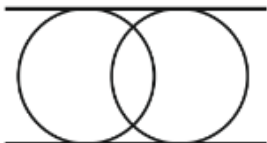


Direct common tangent = 1

Transverse common tangent = 0

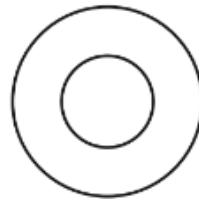
**Q4 Text Solution:**

The figure looks like that,

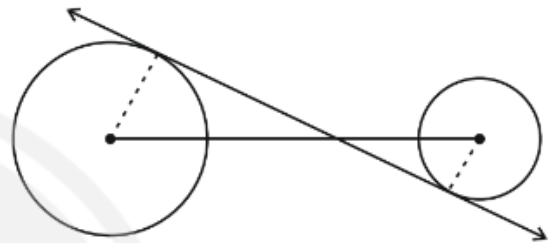


Direct tangent = 2

Transverse = 0

**Q5 Text Solution:**


In this case there is no direct or transverse common tangent.

**Q6 Text Solution:**


Here we have a direct formula to find the length of transverse common tangent.

$$\Rightarrow \sqrt{d^2 - (r_2 + r_1)^2}$$

Where  $d$  = distance between the centres

$r_2$  = radius of smaller circle

$r_1$  = radius of bigger circle

$r_1 = 9\text{cm}$

$r_2 = 5\text{cm}$

$d = 18\text{cm}$

$$\Rightarrow \sqrt{(18)^2 - (9 + 5)^2}$$

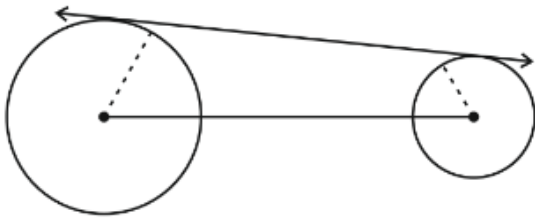
$$\Rightarrow \sqrt{(18)^2 - (14)^2}$$

$$\Rightarrow \sqrt{324 - 196}$$

$$= \sqrt{128}$$

$$= 8\sqrt{2}\text{cm}$$

**Q7 Text Solution:**

Length of direct common tangent,

$$\Rightarrow \sqrt{(d)^2 - (r_1 - r_2)^2}$$

where  $d$  = distance between the centre,

$r_1$  = radius of bigger circle

$r_2$  = radius of smaller circle

$$\Rightarrow \sqrt{(d)^2 - (r_1 - r_2)^2}$$

$$\Rightarrow \sqrt{(35)^2 - (15 - 13)^2}$$

$$\Rightarrow \sqrt{1225 - 4}$$

$$= \sqrt{1221}$$

#### Q8 Text Solution:

For direct common tangent

$$= \sqrt{d^2 - (R - r)^2}$$

For transverse common tangent

$$= \sqrt{d^2 - (R + r)^2}$$

on sq. both equation and subtract second from 1 we get,

$$\left( \sqrt{d^2 - (R - r)^2} \right)^2 - \left( \sqrt{d^2 - (R + r)^2} \right)^2$$

$$\Rightarrow 4Rr \Rightarrow (35)^2 - (25)^2$$

$$\Rightarrow 4Rr = 1225 - 625$$

$$\Rightarrow 4Rr = 600$$

$$\Rightarrow Rr = 150\text{cm}$$

#### Q9 Text Solution:

Topic - Circles

In  $\triangle POR$

$$PO^2 = PR^2 + OR^2 = 12^2 + 5^2 = 169$$

$$PO = 13\text{cm}$$

In  $\triangle QSO'$

$$QO'^2 = QS^2 + O'S^2 = 7^2 + 24^2 = 625$$

$$QO' = 25\text{cm}$$

$$PQ = PO + OO' + O'Q$$

$$= 13 + (5 + 7) + 25$$

$$= 13 + 12 + 25 = 50\text{cm}$$

#### Q10 Text Solution:

In  $\triangle JO'L$ ,

$$JL^2 + O'L^2 = JO'^2$$

$$JL^2 + r^2 = (3r)^2$$

$$JL^2 = 9r^2 - r^2$$

$$JL^2 = 8r^2$$

$$JL = 2\sqrt{2}r$$

$$\text{Required ratio} = JL : JO' \Rightarrow 2\sqrt{2}r : 3r$$

$$= 2\sqrt{2} : 3$$

#### Q11 Text Solution:

In  $\triangle JOK$ ,

$$JO^2 = OK^2 + JK^2$$

$$JK^2 \Rightarrow 12^2 - 5^2 = 119$$

$$JK = \sqrt{119}\text{cm}$$

$$JK = JM(\text{Tangent})$$

$$OM \perp JL$$

$$\text{So, } JM = ML = 13\text{cm}$$

$$JL = JM + ML$$

$$JL = 2 \times \sqrt{119}\text{cm}$$

#### Q12 Text Solution:

Here  $KJ \perp JL$ ,

$OK$  and  $OL$  are radius and perpendicular to the tangent.





$$\begin{aligned}\angle OKJ + \angle KJL + \angle JLO + \angle LOK &= 360 \\ 90 + 90 + 90 + \angle LOK &= 360 \\ \angle LOK &= 360 - 270 = 90\end{aligned}$$

All angles are equal, so it can be a square or a rectangle but  $OK = OL$  as radius. So now we can say that  $OKJL$  is a square.

So,  $OK = OL = KJ = JL = 7.5\text{cm}$

**Q13 Text Solution:**

Here,  $MQ = MR$ ,  $LQ = LP$ ,  $JR = JS$ ,  $KS = KP$ .

$$JK + LM = JS + SK + LQ + MQ$$

$$JK + LM = JR + KP + LP + MR$$

$$JK + LM = JM + KL$$

**Q14 Text Solution:**

Let the radius with centre  $O$ ,  $O'$  and  $O''$  are  $a$ ,  $b$  and

$c$ . then

$$a + b = 11\text{ cm}$$

$$b + c = 12\text{ cm}$$

$$c + a = 13\text{ cm}$$

$$2(a + b + c) = 36$$

$$a + b + c = 18$$

Here we have to find the value of  $b$ .

$$b = (a + b + c) - (a + c)$$

$$b = 18 - 13$$

$$b = 5$$

**Q15 Text Solution:**

In the figure,  $JK$  and  $JL$  are tangent and are equal so in  $\triangle JKL$ ,

$$\angle JKL + \angle JLK + \angle KJL = 180^\circ$$

$$2\angle JKL = 180 - 60$$

$$\angle JKL = 60 = \angle JLK$$

each angle of the triangle is equal ( $60^\circ$ ) so  $KL = 7.5\text{ cm}$ .

**Q16 Text Solution:**

$OL$  and  $OK$  are radius and  $\perp$  to  $JM$  and  $NJ$ .

$$\angle PKO = 90 - 40^\circ = 50^\circ$$

$$\angle PLO = 90 - 60^\circ = 30^\circ$$

$$\angle PKO = \angle OPK = \text{radius} = 50^\circ$$

$$\angle PLO = \angle OPL = \text{radius} = 30^\circ$$

$$\angle LPK = 30^\circ + 50^\circ = 80^\circ$$

**Q17 Text Solution:**

Here  $JK \parallel LP$ , So  $\angle JKL = \angle KLP = 65^\circ$

$OM \perp JK$  So,  $JM = MK$

$\triangle LKM \cong \triangle LMJ$  So,  $\angle KLM = \angle MLJ$

$$\angle KLM = 90 - 65^\circ = 25^\circ$$

$$\angle MLJ = 25^\circ$$

$$\angle JLK = 25 + 25 = 50^\circ$$

**Q18 Text Solution:**

In cyclic quadrilateral  $JKNO$

$$\angle JKN + \angle JON = 180^\circ$$

In cyclic quadrilateral  $JKLM$ ,

$$\angle JKL + \angle JML = 180^\circ$$

From eq. (1) and (2) we get

$$\angle JKN + \angle JON = \angle JKL + \angle JML$$

$$\Rightarrow \angle JON = \angle JML$$

It is only possible if  $ON \parallel ML$

**Q19 Text Solution:**

$$\angle JOL = 50^\circ$$

$$\angle JKL = \frac{1}{2} \times 50 = 25^\circ$$

$$\angle LMK = 105^\circ$$

In  $\triangle MLK$ ,

$$\angle MLK + \angle LMK + \angle MKL = 180^\circ$$

$$\angle MLK + 105 + 25 = 180^\circ$$

$$\angle MLK = 180 - 130$$

$$\angle MLK = 50^\circ$$

**Q20 Text Solution:**



Meet  $O$  to  $K$

Then  $OJ = OK$  (radius)

$$\angle OJK = \angle OKJ = 30^\circ$$

$$\angle JOK = 180 - 2 \times 30^\circ = 120^\circ$$

$$\angle JLK = \frac{1}{2} \times \angle JOK = \frac{1}{2} \times 120 = 60^\circ$$

In  $\triangle NKL$ ,

$$\angle NKL = 180 - 90 - 60^\circ$$

$$\angle NKL = 30^\circ$$

**Q21 Text Solution:**

$OJ = OL =$  (radius)

$$\angle OJL = \angle OLJ = 30^\circ$$

$$\angle JOL = 180^\circ - 2 \times 30 = 120^\circ$$

$OK = OL =$  (radius)

$$\angle OKL = \angle OLK = 50^\circ$$

$$\angle KOL = 180 - 2 \times 50 = 80^\circ$$

$$\angle JOK = \angle JOL - \angle KOL$$

$$= 120 - 80$$

$$= 40^\circ$$

**Q22 Text Solution:**

In  $\triangle JLM$

$$\angle MJL = 180 - 90 - 57 \Rightarrow 33^\circ$$

In  $\triangle JNM$ ,

$$\angle MJN = 180 - 90 - 46 \Rightarrow 44^\circ$$

$KL \parallel JM$  So,  $\angle KLJ = \angle LJM = 33^\circ$

So, required sum  $\Rightarrow 33 + 44 + 33$

$$\Rightarrow 110^\circ$$

**Q23 Text Solution:**

Here JKLM is a cyclic quadrilateral,

$$\angle JML + \angle JKL = 180^\circ$$

$$\angle JKL = 180 - 135 \Rightarrow 45^\circ$$

In  $\triangle JLK$ ,

$$\begin{aligned}\angle LJK &= 180 - 90 - 45 \\ &= 45^\circ\end{aligned}$$

**Q24 Text Solution:**

$$\angle KJM = 96^\circ$$

$$\angle KLM = 180$$

$- 96$  (Opposite angle sum in cyclic

$\Rightarrow 84^\circ$  quadrilateral)

$$\angle JML = 180 - \angle MJK \text{ (co-interior)}$$

$$= 180 - 96$$

$$= 84^\circ$$

$$\angle JML + \angle JKL$$

$$= 180^\circ \text{ (Opposite angle sum in}$$

cyclic quadrilateral)

$$\angle JKL = 180 - 84 = 96^\circ$$

$$\text{required difference} = 96 - 84 = 12^\circ$$

**Q25 Text Solution:**

$$\angle KJM + \angle KLM = 180^\circ$$

$$\angle KLM = 180 - 98 = 82^\circ$$

$KL \parallel MO$  So,

$$\angle KLM = \angle LMO = 82^\circ$$

$$\angle NMO + \angle OML + \angle LMJ$$

$$= 180^\circ \text{ (Linear Pair)}$$

$$\angle LMJ = 180 - 30 - 82$$

$$\angle LMJ = 68^\circ$$

$$\angle JKL + \angle LMJ = 180$$

$$\angle JKL = 180 - 68$$

$$\angle JKL = 112^\circ$$

**Q26 Text Solution:**

$$\Rightarrow JK \times JL = JM \times JN$$

$$\Rightarrow 2 \times 8 = JM \times 12$$

$$\Rightarrow JM = \frac{16}{12} = \frac{4}{3} = 1.33\text{cm}$$

**Q27 Text Solution:**



$$\begin{aligned}\Rightarrow JK \times JL &= JM \times JN \\ \Rightarrow 4 \times 12 &= 4.5 \times JN \\ \Rightarrow JN &= \frac{4 \times 12}{4.5} = 10.6666 \dots 67 \\ \Rightarrow JN &= 10.67cm\end{aligned}$$

**Q28 Text Solution:**

By Tangent secant theorem

$$\begin{aligned}JK^2 &= JL \times JM \\ JK &= a, JL = b, JM = (b + c) \\ a^2 &= b \times (b + c) \\ a^2 &= b^2 + bc \\ a^2 - b^2 &= bc \\ (a + b)(a - b) &= bc\end{aligned}$$

**Q29 Text Solution:****Topic - Geometry**

By using tangent secant theorem,

$$\begin{aligned}JK^2 &= JL \times JM \\ (3.5)^2 &= JL \times 10cm \\ 12.25 &= JL \times 10cm \\ JL &= \frac{12.25}{10} = 1.225cm\end{aligned}$$

**Q30 Text Solution:**

By using tangent secant theorem,

$$\begin{aligned}\Rightarrow JK^2 &= JL \times JM \\ \Rightarrow (14)^2 &= 7 \times JM \\ JM &= 28cm \\ LM &= JM - JL = 28 - 7 = 21cm \\ ON \perp LM \text{ So } LN &= \frac{CM}{2} = \frac{21}{2} = 10.5cm \\ OL^2 &= ON^2 + LN^2 \\ (14.5)^2 &= ON^2 + (10.5)^2 \\ ON &= 10cm.\end{aligned}$$

