

CS363 Networks & Collective Behavior - Homework 2

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1. There is a question here.

Solution: From the question we have,

$$n = 1 \times 10^9$$

$$p = 1 \times 10^{-5}$$

(a)

$$\langle m \rangle = n \cdot p$$

$$\langle m \rangle = 1 \times 10^9 \cdot 1 \times 10^{-5}$$

$$\langle m \rangle = 1 \times 10^4$$

(b)

$$\langle k \rangle = (n - 1) \cdot p$$

$$\langle k \rangle = (1 \times 10^9 - 1) \cdot 1 \times 10^{-5}$$

$$\langle k \rangle = 9999.99$$

(c)

$$\langle k \rangle = (n - 1) \cdot p$$

$$1 \times 10^5 = (1 \times 10^9 - 1) \cdot p$$

$$p = \frac{1 \times 10^5}{1 \times 10^9 - 1} = 1 \times 10^{-4}$$

(d)

$$APL = \frac{\ln(n)}{\ln(\langle k \rangle)}$$

$$\frac{\ln(1 \times 10^9)}{\ln(9999.99)} = 2.25$$

- (e) No, all the nodes will not be a part of the giant component. This is because the probability p is near to 0 rather than 1, thus, not all nodes will be connected.