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Project 4 – Degradation of Data Integrity

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CST-305: Benchmark – Project 5 – Self-Organized Criticality

Objective: Use a dynamical system to model the deterministically chaotic behavior of a file system.

Description:

Repeated file creations and deletions on a storage device impact the efficiency of allocating memory to store files. This results in many gaps between the files and causes a number of files to become fragmented because of insufficient contiguous space. In turn, this affects the time needed to save, load, and access a file. At some critical point, when a certain threshold of fragmentation is reached, the system becomes too slow to operate (i.e., below a predetermined threshold).

Create a model for the dynamic system that illustrates the deterministic chaos phenomenon and the self-organized criticality characteristics of a file system. Define variables for storage size, file sizes, file load time, file access time, file save time, fragmentation time, fragments assembly time, critical threshold that triggers a “system too slow” alert, and other variables as needed.

Implement the model as a computer program. The program should display a visualization of the fragmentation process as a sequence of save and delete commands are received. While you have a certain measure of freedom to choose your techniques for visualization, consult the instructor to ensure that your approach is acceptable.

Your program should also display a graph showing the appropriate metrics approaching the critical point (e.g. a line chart).

Note: *The Lab Questions in this topic provide the opportunity to reflect and experiment with mathematical and programming implementation of concepts referred to in this assignment.*

Deliverables:

1. Documentation
 - a. Cover page
 - b. Responsibilities and completed tasks by each team member
 - c. System performance context description
 - d. Specific problem solved
 - e. The mathematical approach for solving it
 - f. The approach for implementation in code (e.g., algorithm, flowchart)
 - g. Screenshots depicting key phases in the program execution
 - h. References for theory and code sources
 - i. README document written in Markdown detailing how to install and run the program
2. Code
 - a. Full code submitted to GitHub



- b. Code executes correctly:
 - i. Reads a sequence of save and delete commands as input
 - ii. Performs the commands
 - iii. Saves the files as fragments if not enough contiguous space is available
 - iv. Assembles files from fragments when needed
 - v. Measures the overall fragmentation of the file system
 - vi. Measures the time to perform tasks and the delay due to fragmentation
 - vii. Creates graph showing approaching the critical point
 - viii. Solution is presented using terminology and units in the context of the problem
 - c. Include a header comment, including name of programmers, code packages used, and approach to implementation
 - d. Include comments in key areas of the code
3. Note: Refer to the instructor for additional clarifications for the requirements of this assignment.

Responsibilities:

Code: Grant

Documentation: Ben

System performance context description

The code runs. there isn't really any loops so it should be $O(n)$ where n is user input and the equation for time and space complexity.

Specific Problem Solved: Graphed a series of equations known as the Lorenz system in three dimensions to visualize the fragmentation of a file system due to repeated creation and deletion of files to help understand storage efficiency.

Mathematical Approach: The three equations that are collectively known as the Lorenz system are as follows: $x' = \sigma(y - x)$, $y' = rx - y - xz$, $z' = xy - bz$

$$\sigma = 10$$

$$x = 11.8 \text{ KB}$$

$$dt = 0.01$$

$$b = 2.667$$

$$y = 4.4 \text{ KB}$$

$$r = \text{variable on user input}$$

$$z = 2.4 \text{ KB}$$



Math representation in the code:

```
def lorenz_attractor(x, y, z, dt=0.01, s=10, b=2.667, r=28): 1 usage  TaterTotMan64
    """
    Generates the Lorenz attractor.

    Args:
        x, y, z: Initial values for x, y, and z.
        dt: Time step.
        s, b, r: Lorenz parameters.

    Returns:
        x, y, z: Arrays containing the time series of x, y, and z values.
    """

    x_list, y_list, z_list = [x], [y], [z]

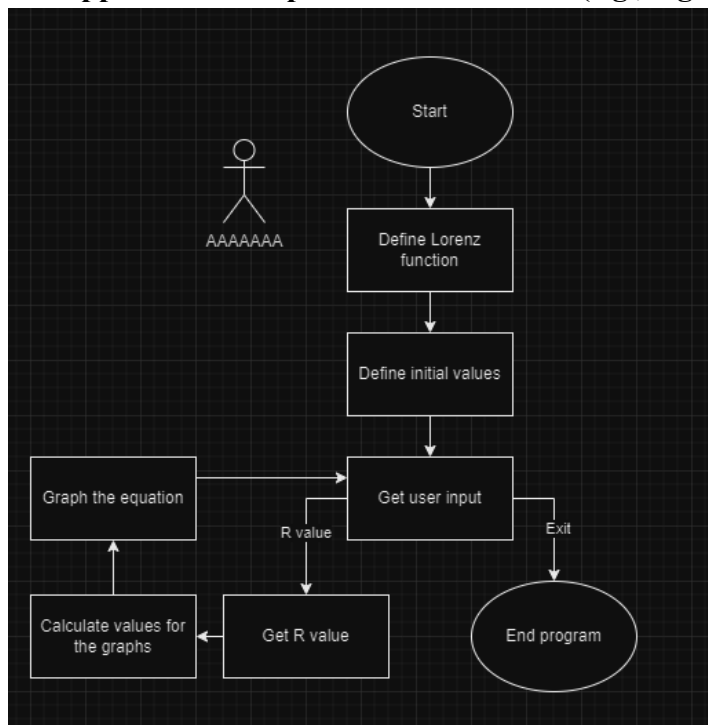
    for i in range(10000):
        dx = s * (y - x)
        dy = x * (r - z) - y
        dz = x * y - b * z

        x += dx * dt
        y += dy * dt
        z += dz * dt

        x_list.append(x)
        y_list.append(y)
        z_list.append(z)

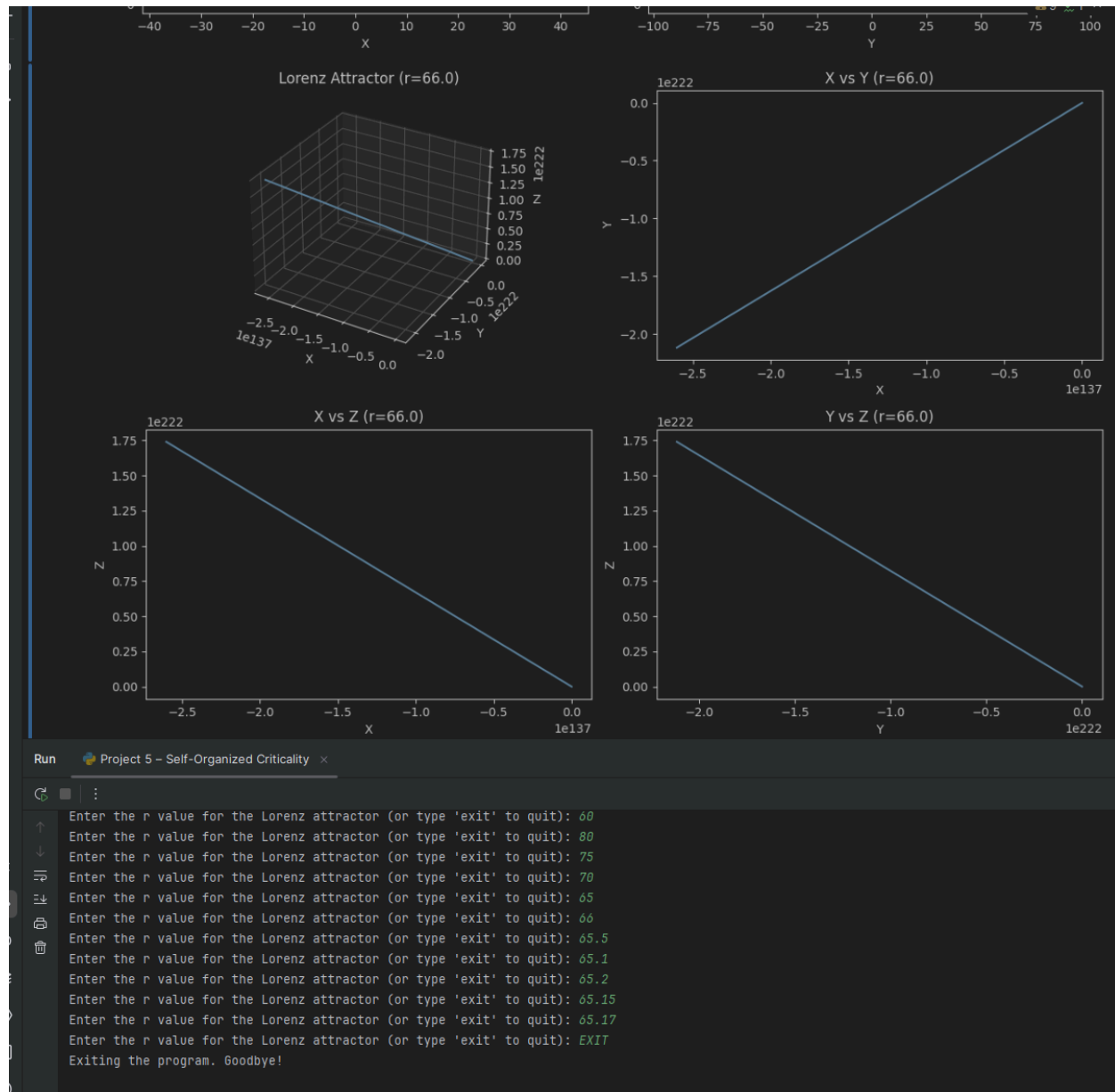
    return np.array(x_list), np.array(y_list), np.array(z_list)
```

The approach for implementation in code (e.g., algorithm, flowchart)

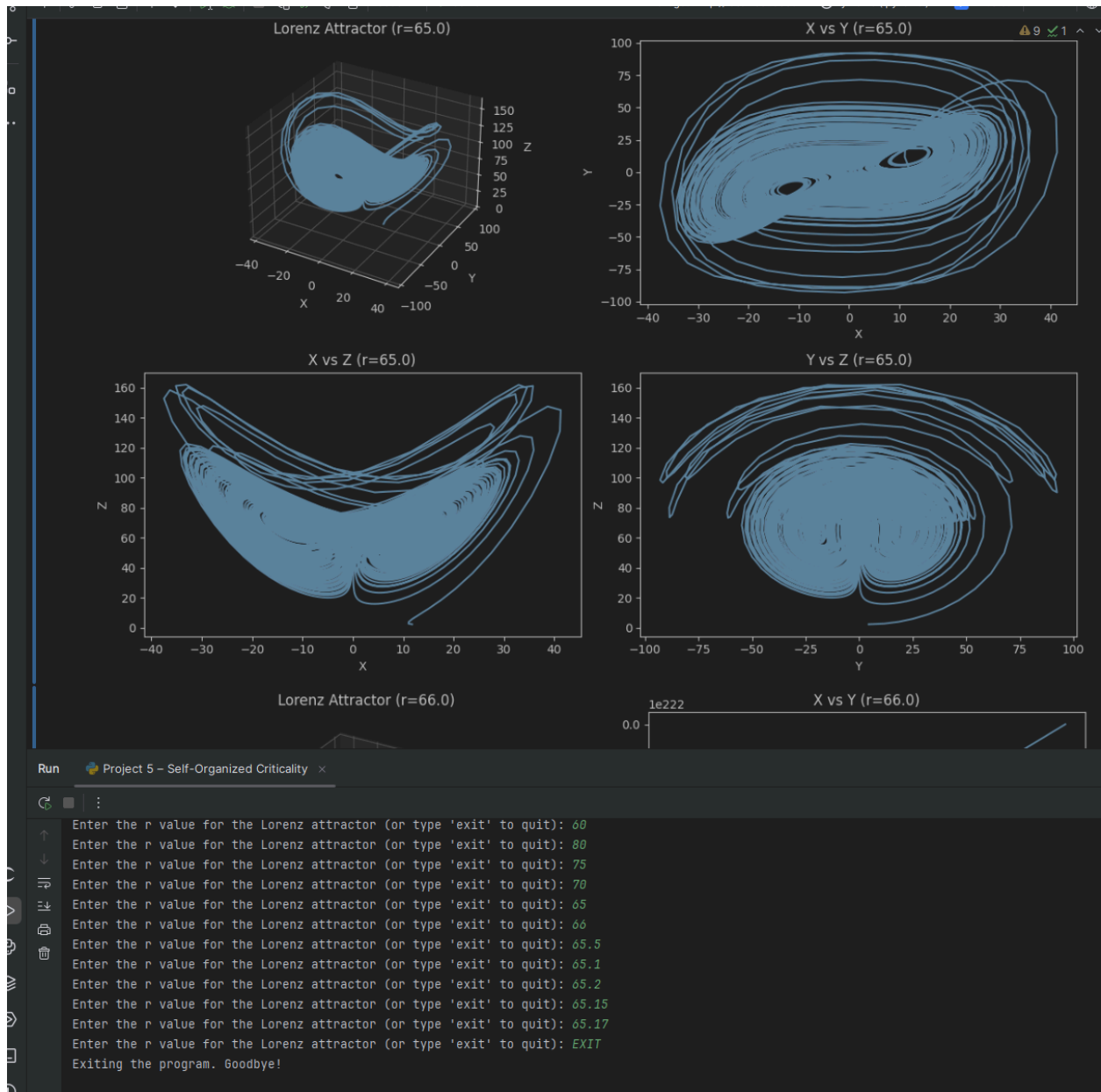




Screenshots depicting key phases in the program execution



(Bottom shows input of r value and eventually an exit that ends the program, the top is the graphs the are outputted from the program)



(Another diagram showing a nonlinear result)

References for theory and code sources

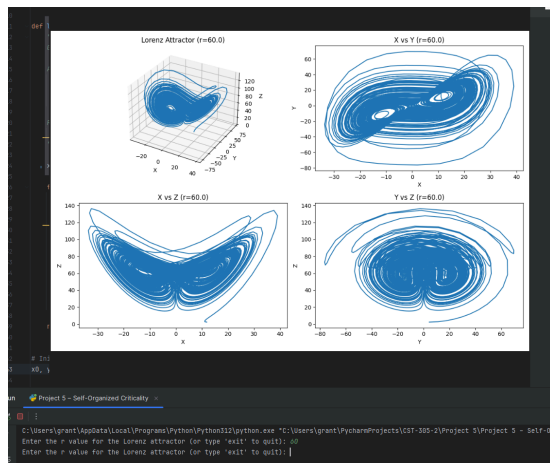
Project reference slides provided to the class.



Employing Scientific Theory + Analysis:

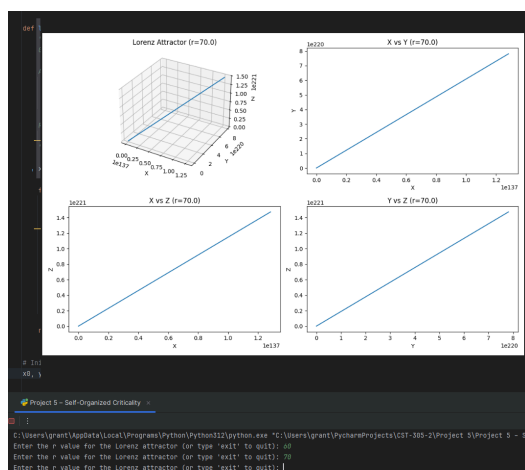
The goal of this experiment was to find the limit R value where the computer's storage was still usable/optimal. To identify the R value the output graphs were studied where a spiral shaped graph indicated that the system was still functioning properly while a linear graph indicates that R reached a critical point so the system doesn't work anymore as the fractionation was too extreme.

Initial test:



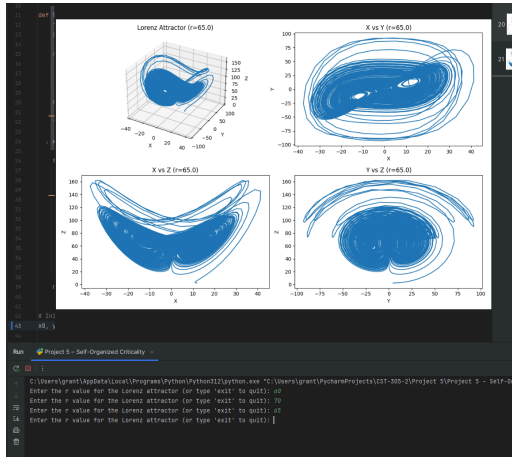
Input: 60

Analysis: as the graph is not linear, the limit is higher.



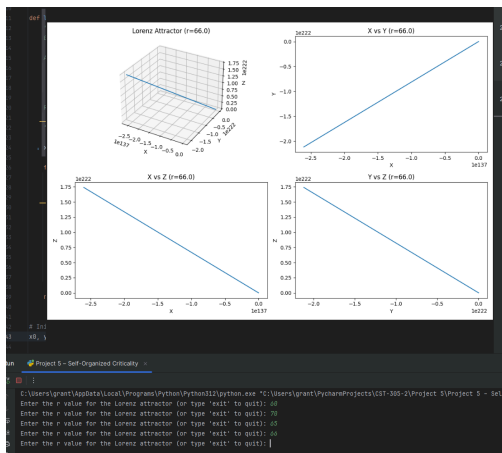
Input: 70

Analysis: the plots are linear, so the limit of the R value is lower.



Input: 65

Analysis: plots are nonlinear, so the R limit must be higher.



Input: 66

Analysis: plots are linear, so the R limit must be lower.

Conclusion:

Since 65 indicates that the limit is higher, and 66 indicates that the limit is lower, the R limit must be 65 or be somewhere between 65 and 66. 65 is the highest recorded integer R value that does not return a linear graph, so 65 is the integer limit of the system.