

### Exercise 1

Exercise 1.

$$5a^2 \cdot 1.5a^4 - 3a^2 \cdot 6a^2 + a^3 \cdot (-4a^2) - a^2 \cdot (-a^2) - 12 \cdot (-3) =$$

$$= 7.5a^6 - 18a^4 - 4a^5 + a^4 + 36 = 7.5a^6 - 2a^4 - 4a^5 + a^4 + 36 \quad \checkmark$$

Standard form of a polynomial should be in descending order of degrees

### Exercise 2

Exercise 2.

$$3x^3 + 2y + 4 \quad \text{при } y = 3x^3 + x - 5$$

$$\downarrow$$

$$3x^3 + 2(3x^3 + x - 5) + 4 = 3x^3 + 6x^3 + 2x - 10 + 4 = 9x^3 + 2x - 6 \quad \checkmark$$

### Exercise 3

$$4x - 1.5x + 7 + 1\frac{1}{7}x = 0$$
~~$$2.5 + 7 + 1\frac{1}{7}x + 8 = 0$$~~
~~$$2\frac{1}{2} + 1\frac{1}{7}x + 8 = -7$$~~
~~$$2\frac{7}{14} + 1\frac{2}{14}x + 8 = -7$$~~

$$x = 3\frac{9}{14}$$

$$4x - \frac{3}{2}x + 7 + \frac{8}{7}x = 7 \xrightarrow{\text{solve, } -} \frac{-(51 \cdot x)}{14}$$

### Exercise 4

Exercise 4

$$p_1(b) = 12b^4 - 10b^2 + 7 \quad p_2(b) = 1.4b^3 - 5b^4 + b + 1.2$$

a)

$$p(b) = 2(12b^4 - 10b^2 + 7) + 1.4b^3 - 5b^4 + b + 1.2$$

$$p(b) = 24b^4 - 20b^2 + 14 + 1.4b^3 - 5b^4 + b + 1.2$$

$$p(b) = 19b^4 + 1.4b^3 - 20b^2 + b + 15.2 \quad \checkmark$$

b)

$$p(b) = 12b^4 - 10b^2 + 7 - 3(1.4b^3 - 5b^4 + b + 1.2)$$

$$p(b) = 12b^4 - 10b^2 + 7 - 4.2b^3 + 15b^4 - 3b - 3.6$$

$$p(b) = 26b^4 - 4.2b^3 - 10b^2 - 3b + 3.4 \quad \checkmark$$

### Exercise 5

Exercise 5

$$3a(5ab^3 - 3) + 5a^2b^2(3b - 2a) = 15a(2ab^3 - 1) + 18$$

$$15a^2b^3 - 9a + 15a^2b^3 - 10a^3b^2 = 30a^2b^3 - 15a + 18$$

$$30a^2b^3 - 9a - 10a^3b^2 = 30a^2b^3 - 15a + 18$$

$$-9a + 15a - 10a^3b^2 = 18$$

$$-10a^3b^2 + 6a = 18 \quad | : 2$$

$$-5a^3b^2 + 3a = 9$$

I did not get the solution but I tried

Exercise 5.

$$3a(5a^2b^3-3)+5a^2b^2(3b-2a)=15a(2ab^3-1)+18$$

$$15a^2b^3-9a+15a^2b^3-10a^3b^2=30a^2b^3-15a+18$$

$$30a^2b^3-9a-10a^3b^2=30a^2b^3-15a+18$$

$$-9a+15a-10a^3b^2=18$$

$$6a-10a^3b^2=18$$

$$-10a^3b^2+6a=18$$

$$-5a^3b^2+3a=9$$

$$a(-5a^2b^2+3)=9$$

$$\begin{cases} a=3 \\ 3-5(3)^2b^2=9 \end{cases}$$

$$3-45b^2=9$$

$$-45b^2=6$$

$$b^2=-\frac{2}{15}$$

$$b=\pm\sqrt{-\frac{2}{15}}$$

$$a(6-10a^2b^2)=18$$

$$b^2=\frac{3}{5}\frac{(a-3)}{a^3}$$

$$a(3-5a^2b^2)=9$$

$$a\in(-\infty;0)\cup(0;+\infty)$$

$$3a-5a^3b^2=9$$

$$5a^3b^2=3a-9$$

$$b^2=\frac{3a-9}{5a^3}$$

$$\begin{aligned}
 & \begin{cases} a=3 \\ -5(3)^2 b^2 = 3 \\ -5 \cdot 9 b^2 = 3 \\ -45 b^2 = 3 \\ -15 b^2 = 1 \\ b^2 = \pm \frac{1}{15} \\ b = \pm \sqrt{\frac{1}{15}} \end{cases} \\
 & (a-b)(a+b)^2 \\
 & = \cancel{(a-b)} \cancel{(a^2 - b^2)} \\
 & (a-b)(a+b)(a+b) = \\
 & = (a+b)(a^2 - b^2) \\
 & \left(2 - \frac{3a}{6}\right) \left(2 + \frac{3}{6}\right)^2
 \end{aligned}$$

Exercise 6

$$\begin{aligned}
 & \text{Exercise 6} \\
 & (90-1)^2 = 8100 + 1 - 180 = 7921 = 89^2 \quad \checkmark \\
 & (100+2)^2 = 10000 + 4 + 400 = 10404 = 102^2 \quad \checkmark
 \end{aligned}$$

Exercise 7

$$\begin{aligned}
 & \text{Exercise 7} \\
 & (3x+2)(3x-2) - 32 = 9x^2 - 2^2 \\
 & 9x^2 - 4 - 32 = 9x^2 - 36x + 36 - 36 \\
 & 9x^2 - 36 = 9x^2 - 36x + 36 \\
 & 36x = 72 \\
 & x = 2 \quad \checkmark
 \end{aligned}$$

Exercise 8



Exercise 8.

при  $a = \frac{1}{6}$

$$(2-3a)(4+6a+9a^2) = (2-3a)(2+3a)^2 = (2-3a)(2+3a)(2+3a)$$

$$= 1.5 \cdot 2.5^2 = 1.5 \cdot 6.25 = \frac{15^2 \cdot 25}{1000} = \frac{75}{8} = 9.375$$

$$= \frac{3}{2} \cdot \frac{25}{4} = \frac{75}{8} \quad \times$$

$$(2-3a) \cdot (4+6a+9a^2) = 2^3 - (3a)^3$$

$$a = \frac{1}{6}$$

$$2^3 - \left(3 \cdot \frac{1}{6}\right)^3 = 8 - \left(\frac{1}{2}\right)^3 = 8 - \frac{1}{8} = \frac{63}{8} \quad +$$

Exercise 9

Exercise 9

$$(3b+2)^2 + (7+3b)(7-3b) - 12b =$$

$$= \underline{9b^2 + 12b + 4} + \underline{49 - 9b^2} - \underline{12b} =$$

$$= 53 \quad \checkmark$$