

# RuleSet for Distributed Quantum Error Correction

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[name=Bernard Ousmane Sane (BOS)]

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## Research Objectives:

In this work, we propose a solution-based quantum error correction for reducing nodes' memories requirement. Hence, we define a distributed erasure code that can do fast recovery while using a few nodes, unlike existing proposals. This allows:

- To reduce the computational complexity
- To reduce the number of nodes to contact during the recovery process

## Construction of $[n, k, r]$ LRC code

Process 1 : the parameters

1. Prepare  $n, q, r$ , and  $k$  such that  $r + 1/n$  and  $r/k$ .
2. Prepare a polynomial  $g(x) \in \mathcal{F}_q$  such as:
  - $\deg(g)$  is  $r + 1$
  - $\mathcal{A} = \bigcup_{i=1}^n \mathcal{A}_i$  is a partition of  $\mathcal{A} \subseteq \mathcal{F}_q$  with  $n = |\mathcal{A}|$ ,  $r + 1 = |\mathcal{A}_i|$
  - $g$  is constant on each set  $\mathcal{A}_i$  in the partition.
3. Send the result to each node

Process2:  $[n, k, r]$  LRC code codeword

1. Wait for a message  $m = m_1 \dots m_k$  from the system
2. Wait for the code's parameters
3. form the codeword  $c = c_1 \dots c_n$  such as  $c_i$  is a function of a small number (at most  $r$ ) of other symbols
  - Distribute  $c_i$  over the nodes

Process3: recover an erasure symbol  $c_t^d$  of the codeword  $c^d = c_1^d \dots c_n^d$

1. Determine the nodes which contain the symbols  $c_i^d, i \neq t$
2. Wait for symbols  $c_1, \dots, c_r$  from  $r$  Nodes
3. recover  $c_i$  by using at most  $r$  symbols

### Process3: Blocks of qubits

1. Wait for  $N$  qubits from the system
2. Split the  $N$  qubits into  $m$  blocks of  $k$  qubits
3. Build a  $km$  matrix where the  $j^{th}$  column describes the  $j^{th}$  block.

### Process4: Quantum local Recovery code $[[n, k, r]]$

1. Wait for  $\mathcal{C} = [n, k, r]$  LRC code
2. Generates the parity-check and generator matrices
3. Build the quantum code using the theorem given by *A. R. Calderbank et al.*
4. Send the result to every node

### Process5: Encoding a block $\mathcal{B}^i$ from a node $\mathcal{N}^j$

1. Wait for the block  $\mathcal{B}^i = \{q_1^i, \dots, q_k^i\}$
2. Produce a logical state  $|\psi^i\rangle$  which is a combination of states  $|\psi_j^i\rangle$  where  $1 < j \leq n$ .
3. Removes  $\mathcal{B}^i$  and distribute  $|\psi_j^i\rangle$  where  $1 < j \leq n$  over the  $\mathcal{N}$  nodes

### Process 6: Quantum Local recovery code

1. Check the availability of the nodes
2. Determine the state  $|\psi^i\rangle$  which contains the encoding value of  $\mathcal{B}^i$
3. Launch a broadcast request for  $\{|\psi_1^i\rangle, \dots, |\psi_n^i\rangle\}$  from nodes  $\{\mathcal{N}^1, \dots, \mathcal{N}^n\}$  (**remote gate**)
4. Recover the block  $\mathcal{B}^i$  using  $\{|\psi_1^i\rangle, \dots, |\psi_n^i\rangle\}$