Language & Logic - Assignment III

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1 Question 1

1.1 Brief

$$(P \land Q) \rightarrow \neg R : R \rightarrow (P \rightarrow \neg Q)$$

1.2 Answer

1 | R | Hypothesis
$$\{1\}$$

2 | P | Hypothesis $\{1,2\}$
3 | Q | Hypothesis $\{1,2,3\}$
4 | $P \wedge Q$ | \wedge -Introduction(2,3) $\{1,2,3\}$
5 | $(P \wedge Q) \rightarrow \neg R$ | Premise $\{1,2,3,5\}$
6 | $\neg R$ | \rightarrow Elimination(4,5) $\{1,2,3,5\}$
7 | R | Iteration $\{1,2,3\}$
8 | $\neg Q$ | Reductio Ad Absurdum(3,6,7) $\{1,2,5\}$
9 | $P \rightarrow \neg Q$ | \rightarrow Introduction(2,8) $\{1,5\}$
10 | $R \rightarrow (P \rightarrow \neg Q)$ | \rightarrow Introduction(1,9) $\{5\}$

2 Question 2

2.1 Brief

$$\neg R, P \rightarrow \neg Q, R \rightarrow Q, P \lor R : \neg Q$$

2.2 Answer

3 Question 3

3.1 Brief

$$: ((A \vee B) \wedge (\neg B)) \to A$$

3.2 Answer

1

$$((A \lor B) \land (\neg B))$$
 Hypothesis $\{1\}$

 2
 $A \lor B$
 \land - Elimination(1) $\{1\}$

 3
 A
 Hypothesis $\{1,3\}$

 4
 A
 Iteration(3) $\{1,3\}$

 5
 B
 Hypothesis $\{1,5\}$

 6
 $\neg A$
 Hypothesis $\{1,5,6\}$

 7
 B
 Iteration(5) $\{1,5,6\}$

 8
 $\neg B$
 \land -Elimination(1) $\{1,5,6\}$

 9
 A
 Reductio Ad Absurdum(5,6,7,8) $\{1,5,6\}$

 10
 A
 \lor -Elimination(2,3,4,5,9) $\{1\}$

 11
 $((A \lor B) \land (\neg B)) \rightarrow A$
 \rightarrow Introduction(1,10) $\{\}$