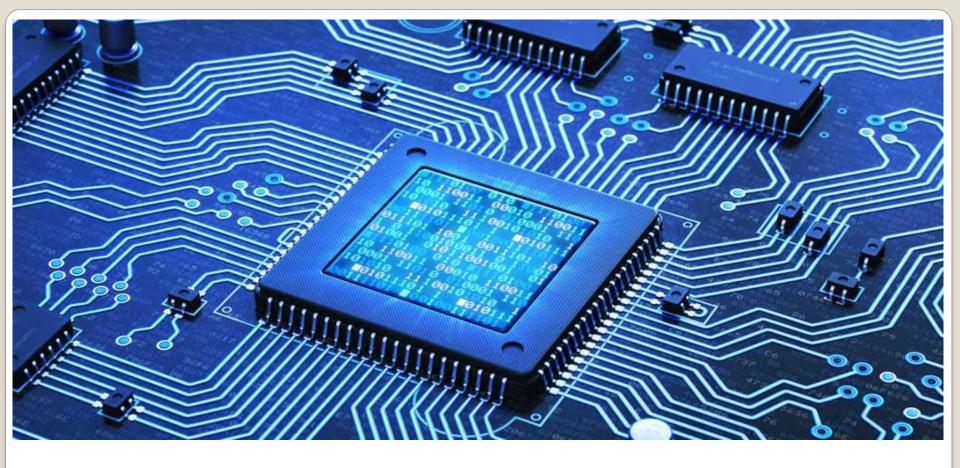


Session 1.4

Module 1a: Capacitors and Inductors

Session 1.4: Focus

- Introduction to Capacitors
- Capacitance Value
 - V-I Relationship
- Construction of Inductors
 - V-I Relationship
- Passive Filters
- Use of Capacitors and Inductors



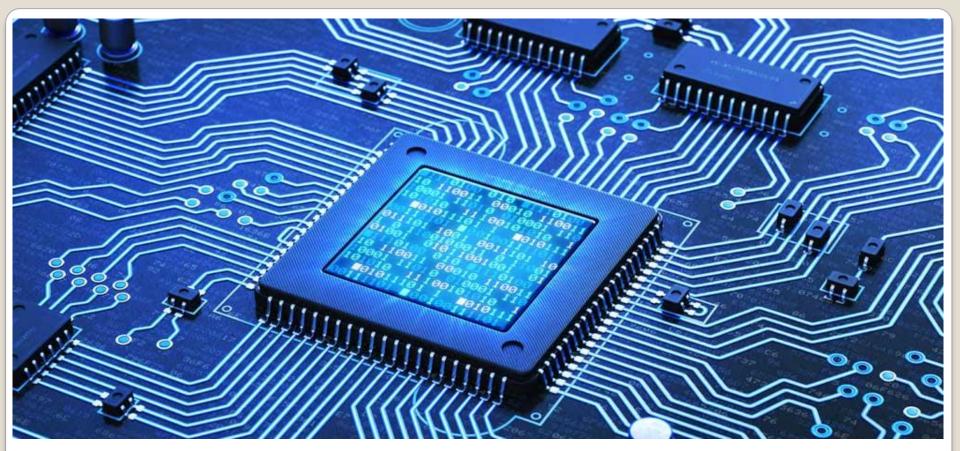
Introduction to Capacitors

Capacitors



What is a Capacitor?

- Capacitors (sometimes known as condensers) are energy-storing devices that are used widely in various products.
 - Television, Radios, electronic equipment, etc.
 - To construct Filters (frequency based)
- Tune a radio into a station, take a flash photo with a digital camera, you're making use of capacitors.
- Capacitors have the ability to both store and deliver *finite amounts* of energy.
- They differ from ideal voltage sources because Capacitors cannot sustain a finite average power flow over an infinite time interval.



Nature's Huge Capacitors

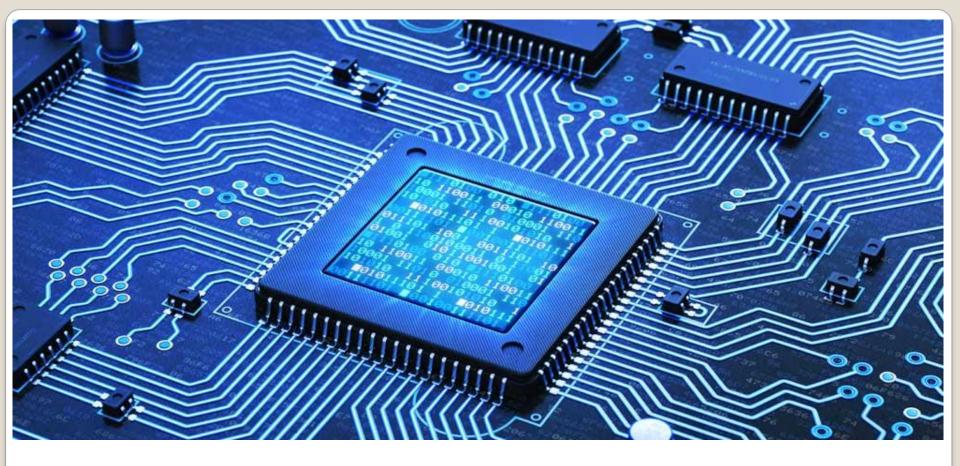
Huge Capacitors in Nature!!!



Clouds are the floating Huge Capacitors!!!



Discharging of Nature's Huge Capacitors is Lightning!!

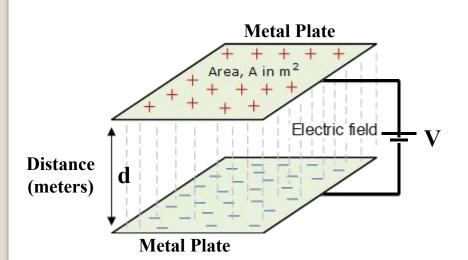


Construction of Capacitors

Definition of a Capacitor

• Capacitor is a component which has the ability or "capacity" to store energy in the form of an electrical energy producing a potential difference (static voltage) across its plates, much like a small rechargeable battery.

Construction of a Capacitor



- Two electrical plates are separated with an insulator.
 - Which is a **dielectric material** that doesn't allow electricity to flow through it very well.
- A capacitor is made!!

- Capacitor is capable of **storing electrical energy**.
- There are basically two operations that can be done on a Capacitor:
 - Adding electrical energy to a capacitor is called as charging;
 - Releasing the energy from a capacitor is known as discharging.

Unit of Capacitor (Farad)

- Capacitance is the electrical property of a capacitor.
- It is a measure of a capacitor's ability to store electrical energy onto its two plates.
- The unit of capacitance is the Farad (abbreviated to F) named after the British physicist Michael Faraday.
- A capacitor has the capacitance of One Farad when electrical energy equivalent to One Coulomb of charge stored in it by a voltage of One volt.

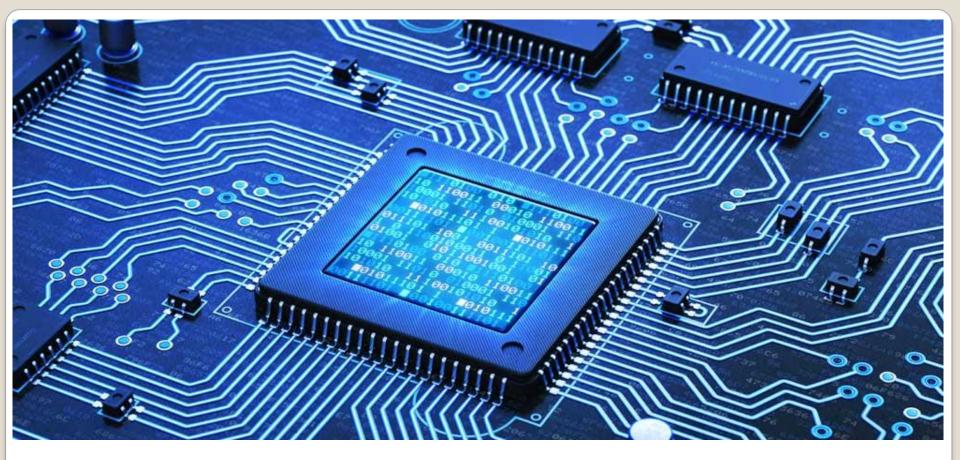
$$\mathbf{C} = \mathbf{Q}/\mathbf{V}$$

Unit of Capacitor and Symbols

- Capacitance, C is always positive and has no negative units.
- However, Farad is a very large unit of measurement to use.
 - One Coulomb of charge = 6.25×10^{18} electrons.
- So, **sub-multiples** of the **Farad** are generally **used**, such as:
 - 1 micro-farads (μ F) = 10-6 F
 - 1 nano-farads (nF) = 10^{-9} F
 - 1 pico-farads (pF) $= 10^{-12}$ F

Capacitor Symbols

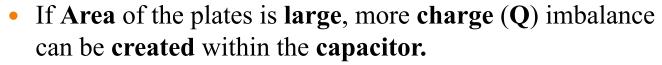




Capacitance Value

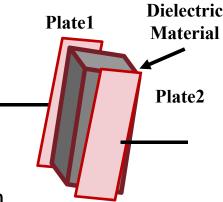
Capacitance Value

ε: Dielectric constant of dielectric material used







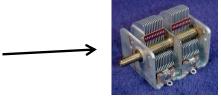


Capacitor Types (Different Dielectrics)

- Electrolytic Capacitors (Aluminium/Tantalum)
 - Large capacitance (~10μF with smaller size)
 - Polarized (has +v & -ve terminals)
 - Permanently damaged, if connected incorrectly





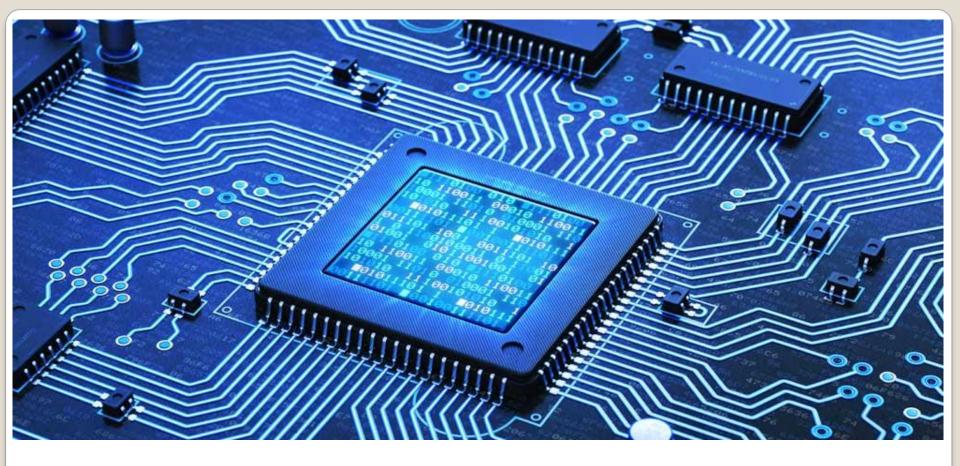


← Air as dielectric

- Paper Capacitors
- Ceramic Capacitors:
 - A few pF to 1or 2 μF







V-I Relationship

V-I Relationship of a Capacitor

Capacitor Symbol:

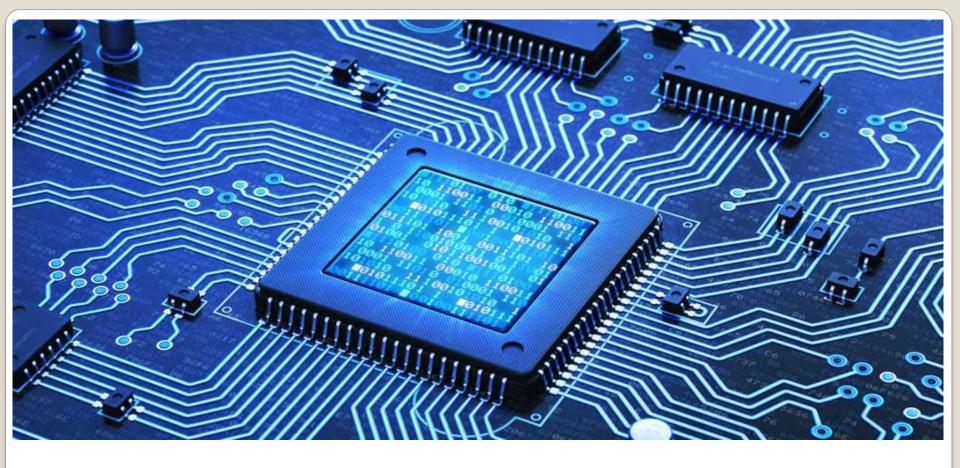


Note the signs of potential across C

- C satisfies the conventions for a passive element.
- Voltage-Current Relationship:

$$i = C \frac{dv}{dt}$$

- This equation tells us that when the voltage doesn't change across the capacitor, current doesn't flow;
- To have a current flow through the capacitor, the voltage must change.
- For a constant **DC voltage source**, **capacitors** act as **open-circuit** because there is no change in the voltage, thus **no current can flow** though it.

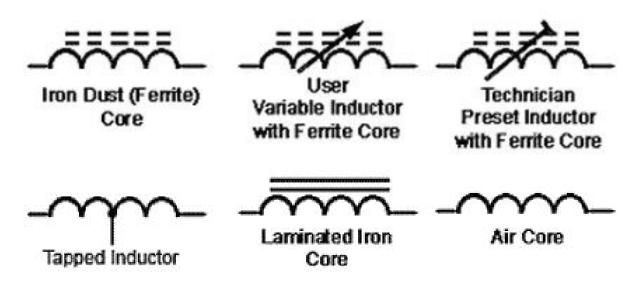


Inductors

What is Inductance?

• Inductance is the property whereby an inductor exhibits opposition to the change of current flowing through it, measured in henrys (H).

Inductor Symbols



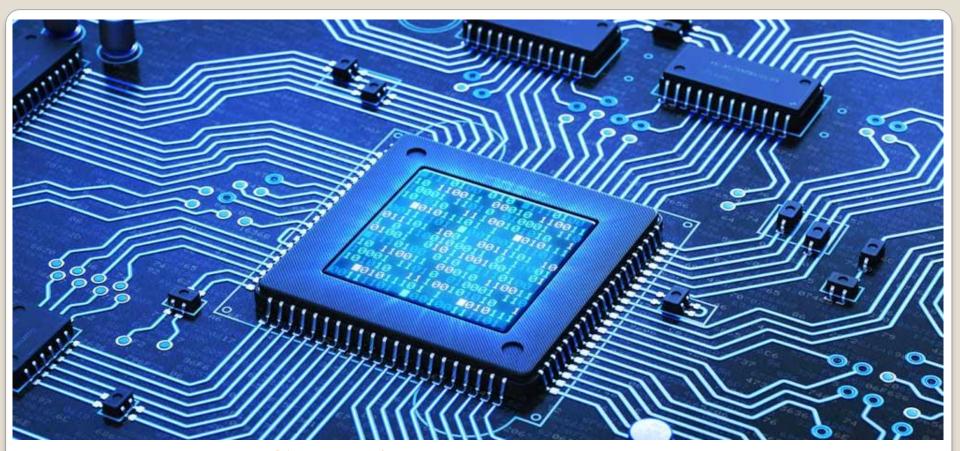
Inductors: Invention

- Michael Faraday and Joseph Henry discovered almost simultaneously that a changing magnetic field could induce a voltage in a neighbouring circuit.
- The voltage induced is proportional to the time rate of change of the current producing the magnetic field.
- The **constant** of **proportionality** is what we call the **inductance**, symbolized by **L**, and therefore

$$v = L \frac{di}{dt}$$

$$+ V_{L} -$$

- The unit in which inductance is measured is the henry (H)
- Equation shows that **henry** is just a **shorter expression** for a **volt-second per ampere**.

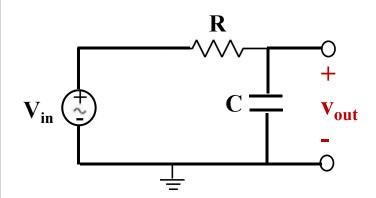


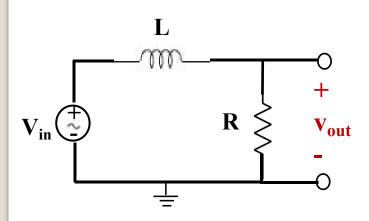
Capacitors and Inductors in AC Circuits

Passive Filters

- Filters are circuits which allow certain input frequency signals to pass through or to get blocked before reaching the output of the circuit.
- Filters which are built only with passive components (Resistors, Capacitors, Inductors) are called passive filters.
- Frequency of the signals is the rate of change of signal amplitude with time.
- What we normally see in real-life are sinusoidal voltages which will be covered shortly.

Low Pass Filter (LPF): AC





• At lower frequencies the capacitive reactance of the circuit will be higher, having higher voltage drop across the capacitor, where the output is taken.

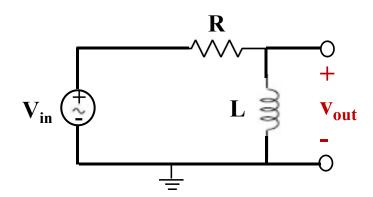
$$X_{\rm C} = \frac{1}{\omega c} = \frac{1}{2\pi f c}$$

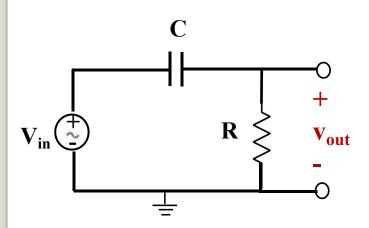
- At higher frequencies reactance of the capacitor becomes very low that no output can be seen at **v**_{out}.
- In the lower circuit with inductor, lower frequency signals are allowed because of inductive reactance being low.

$$^{\circ} \mathbf{X}_{L} = \boldsymbol{\omega} \mathbf{L} = 2\pi f L$$

• At higher frequencies, due to higher X_L no output can be seen at \mathbf{v}_{out} .

High Pass Filter (HPF): AC

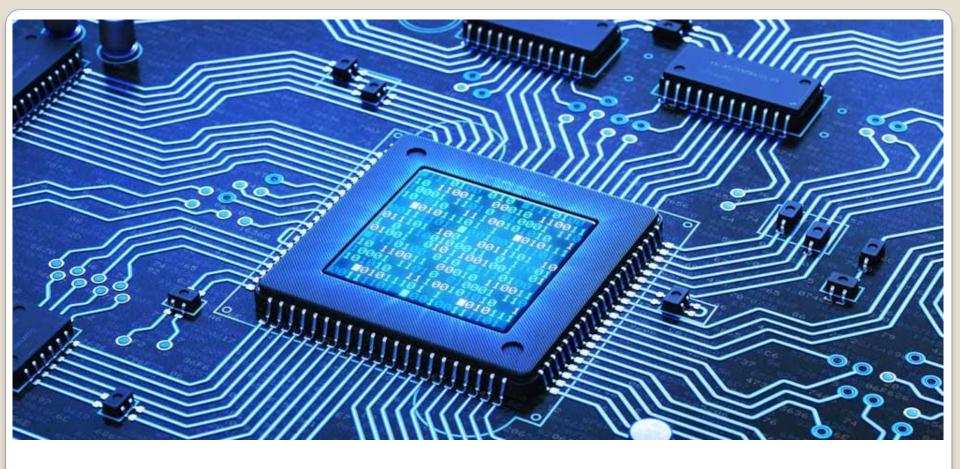




- At higher frequencies the inductive reactance of the circuit will be higher, having higher voltage drop across the inductor, where the output is taken.
 - $X_L = \omega L = 2\pi f L$
- At lower frequencies reactance of the inductor becomes very low that no output can be seen at **v**_{out}.
- In the lower circuit with capacitor, higher frequency signals are allowed because of capacitive reactance being low.

$$X_{\rm C} = \frac{1}{\omega C} = \frac{1}{2\pi fC}$$

• At lower frequencies, due to higher X_C no output can be seen at \mathbf{v}_{out} .



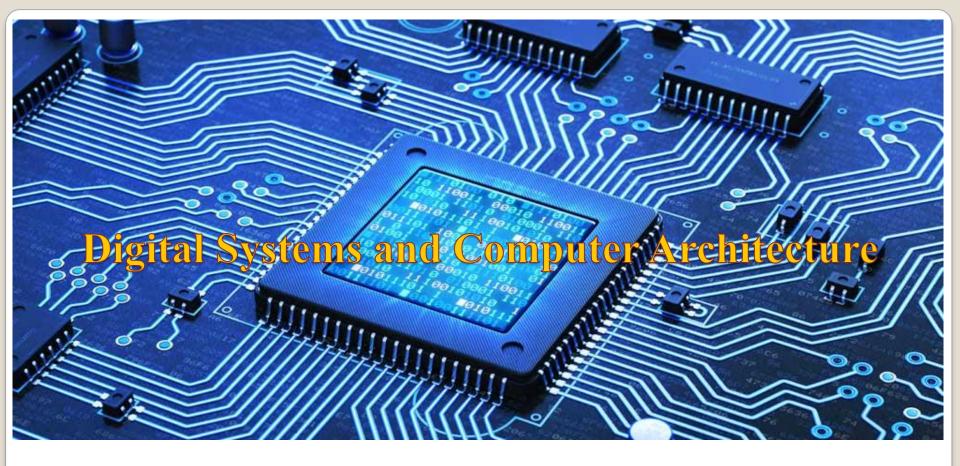
Use of Capacitors and Inductors

Use of Capacitors and Inductors

- Inductors, combined with capacitors and resistors, are used extensively to create **filters** for analogue circuits and in-signal processing.
- **Induction motors** change the electrical energy into mechanical energy.
- Inductors that share the magnetic path are combined together and form a **transformer**.
- Inductors can be used for energy storage.
- Unlike capacitors, they do not store energy for a long time.
- In the case of inductors, energy is stored in the form of the magnetic field; however, this fails when there is no power supply.
- Capacitors act as an insulator for DC circuits.

Session 1.4: Summary

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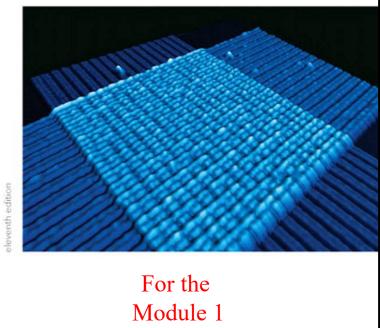


References

Reference 1: DS & CA

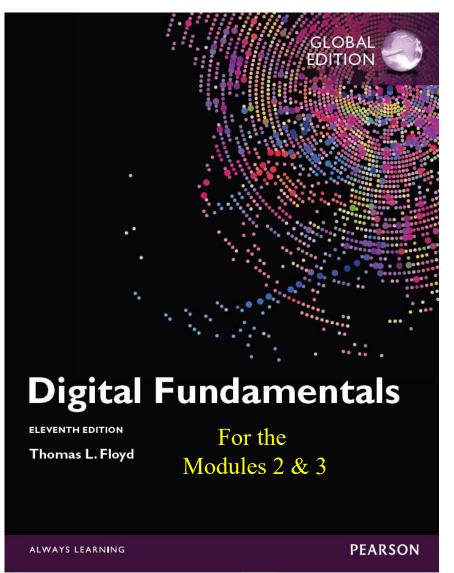
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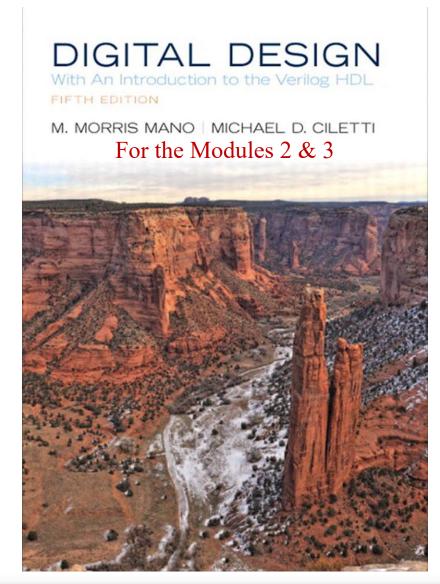




References 2 & 3: DS & CA

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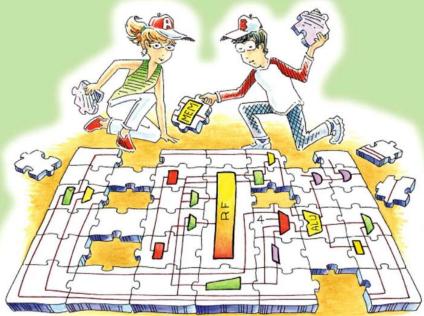


References 4 & 5: DS and CA

Ref 4 Ref 5

Digital Design and Computer Architecture

SECOND EDITION



David Money Harris & Sarah L. Harris



For the Modules 2 to 5

