

# Neutral Territory Decomposition for Parallel MD

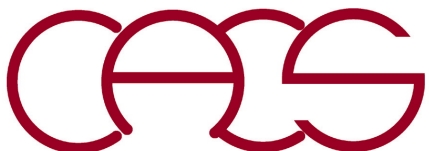
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University of Southern California*

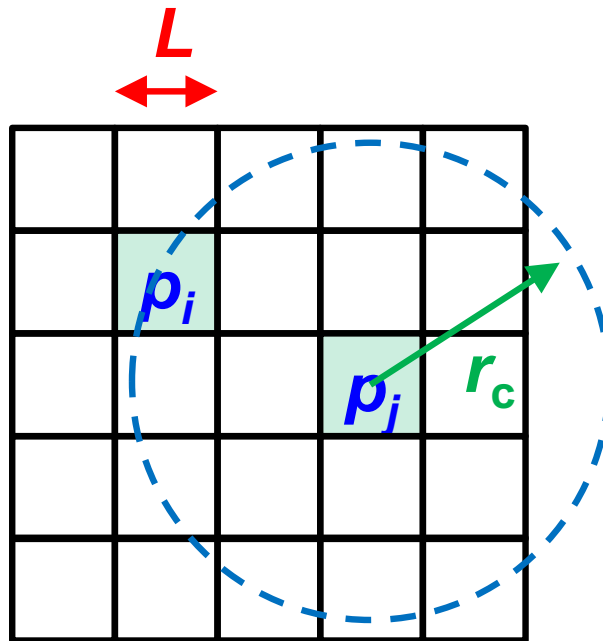
**Email: [anakano@usc.edu](mailto:anakano@usc.edu)**

D. E. Shaw, “A fast, scalable method for the parallel evaluation of distance-limited pairwise particle interactions,” *J. Comput. Chem.* **26**, 1318 ('05)



# Fine Granularity

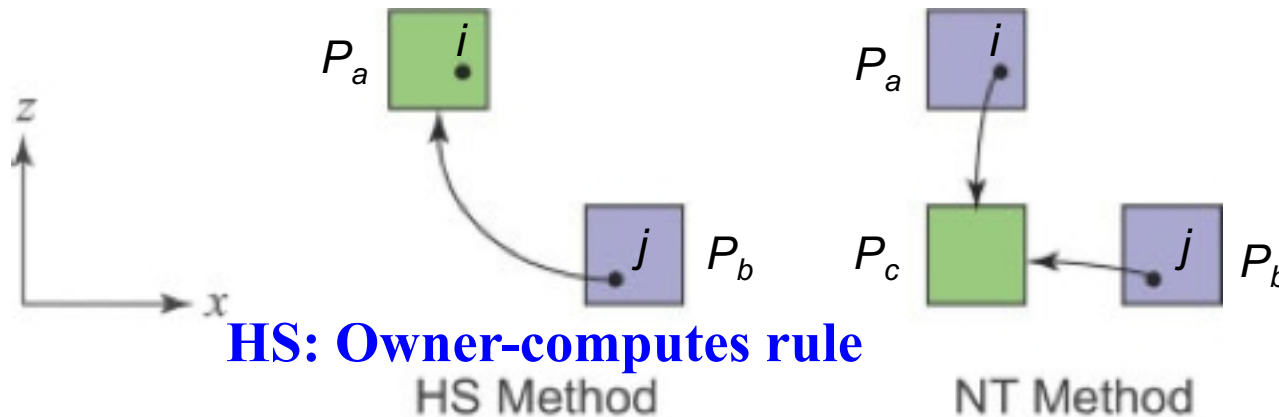
Number of atoms per process ( $N/P$ )  $\sim 1$



spatial subsystem length ( $L$ )  $\ll$  interaction cutoff ( $r_c$ )

# Spatial (Half-Shell) vs. NT Decompositions

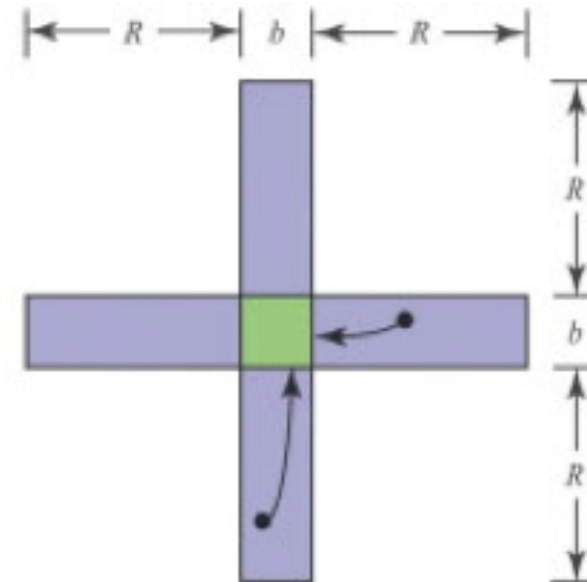
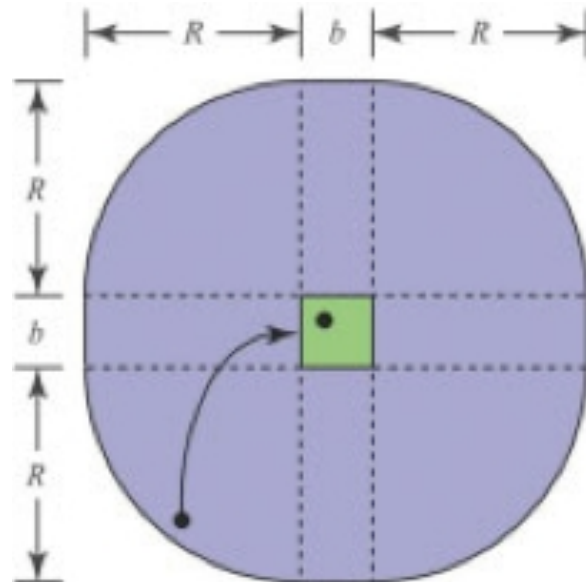
**Locus of interaction — who does what (2-dimensional example)**



**NT = hybrid spatial  
(data) & force  
(computation)  
decomposition with  
well-designed  
order/layout**

**Import regions or communication volume (2-dimensional example)**

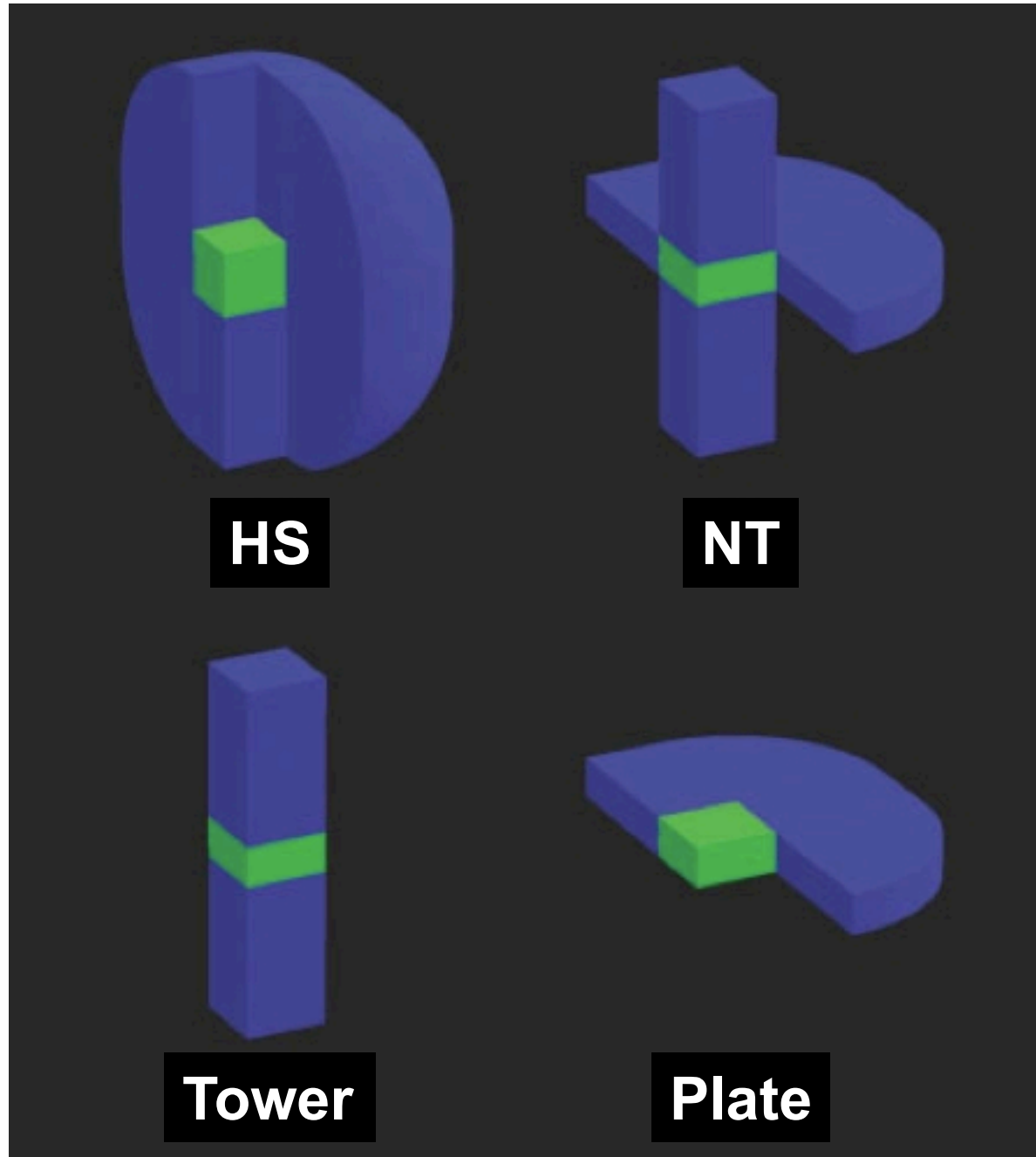
**HS**  
 $4bR + \pi R^2$   
 $\rightarrow \text{const.}$   
 $(b \rightarrow 0)$



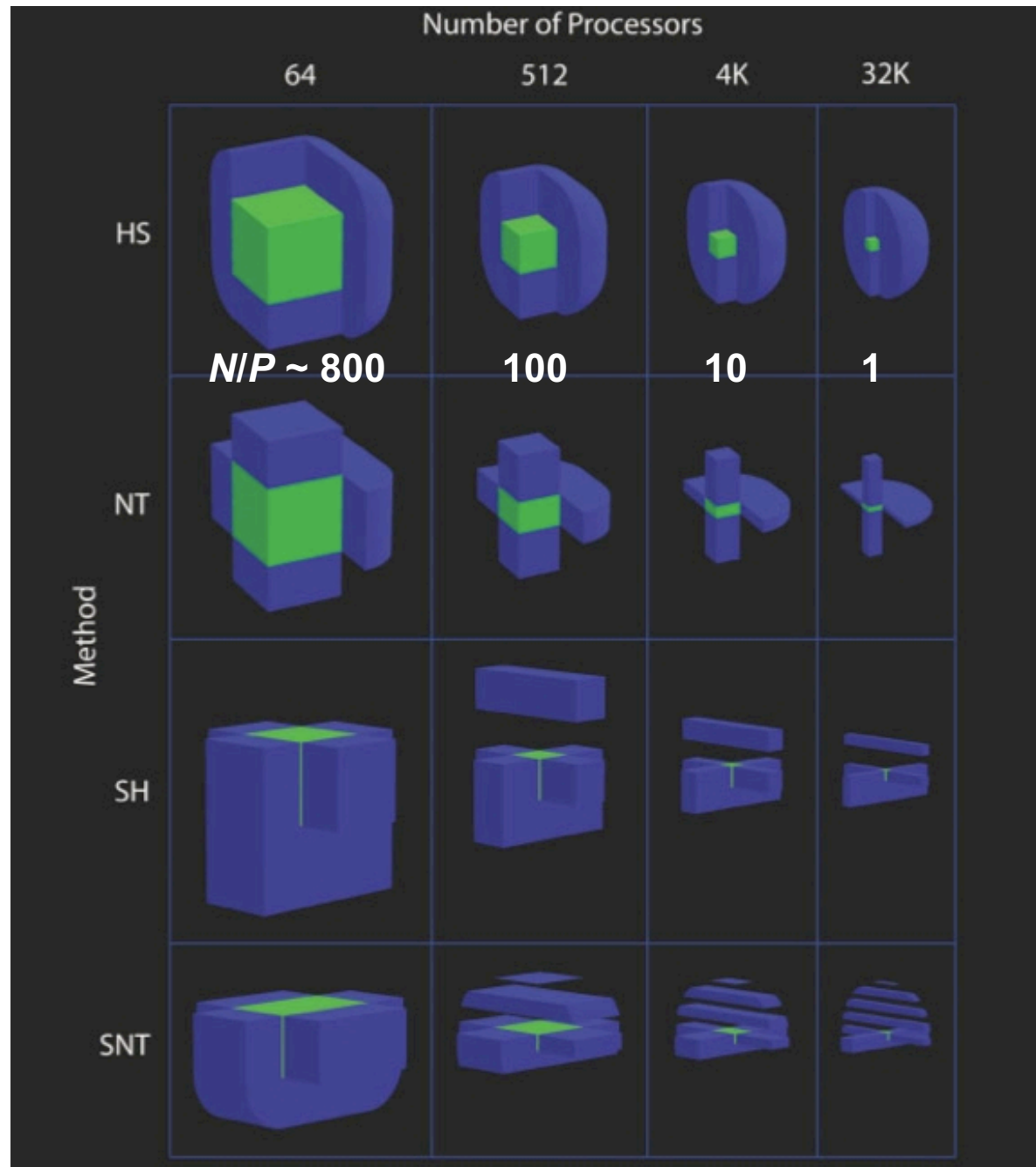
**NT**  
 $4bR$   
 $\rightarrow 0$   
 $(b \rightarrow 0)$

# 3D Import Regions

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# Scaling of Import Regions



Marc Snir

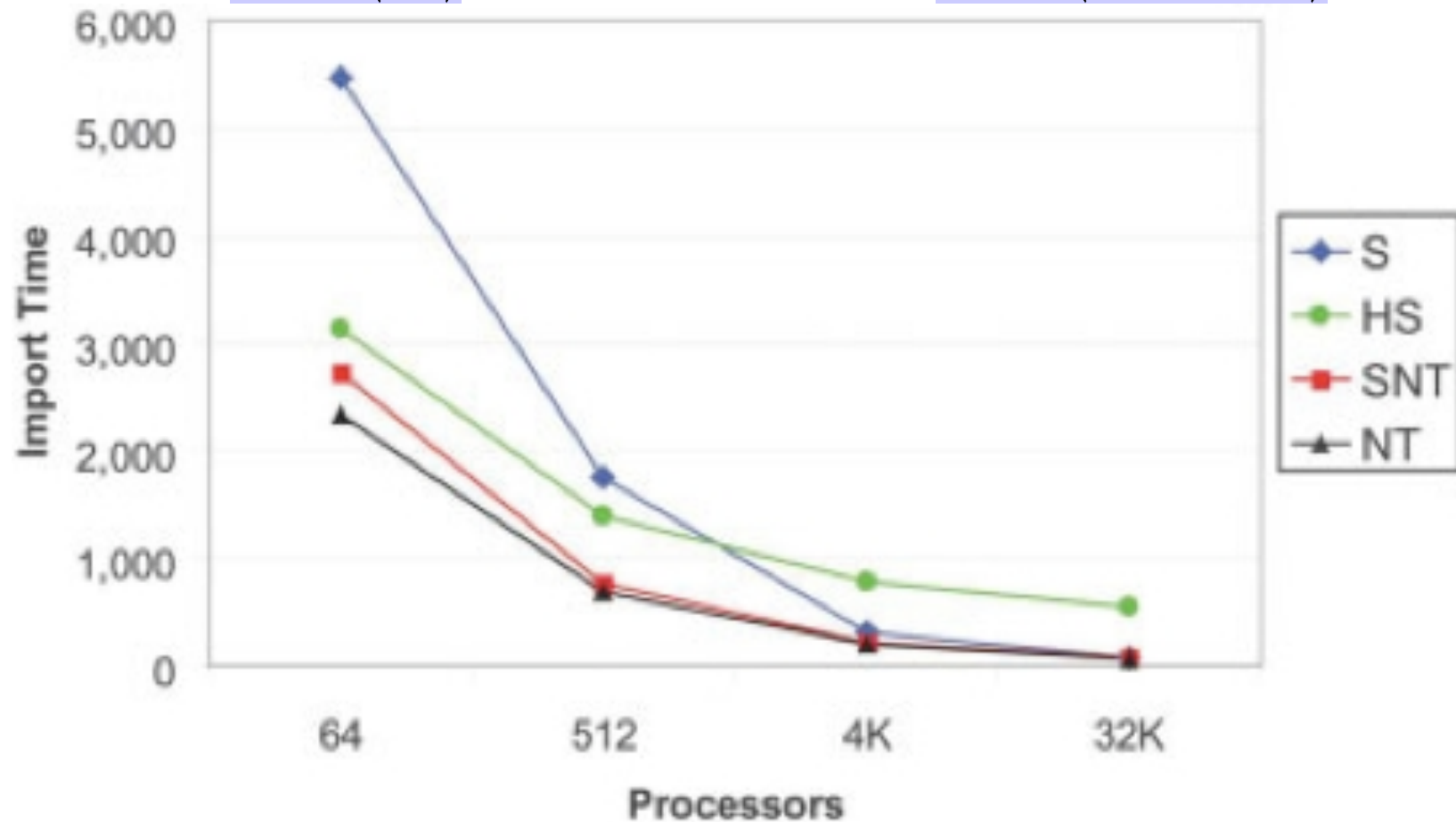
# Scaling of the Volume of Import Regions

HS decomposition

$$V_i = O(R^3)$$

NT decomposition

$$V_i = O(R^{3/2} p^{-1/2})$$



**Communication time**

$$T_{\text{comm}} = t_{\text{latency}} \overset{\text{\# of messages}}{N_{\text{message}}} + \frac{1}{b_{\text{bandwidth}}} \overset{\text{volume (Bytes) of messages}}{V_{\text{message}}}$$

ns ~ many  $\mu$ s      GB/s

# Combine NT with ...

## Cache-oblivious recursive blocking?

### Cache-Oblivious Algorithms

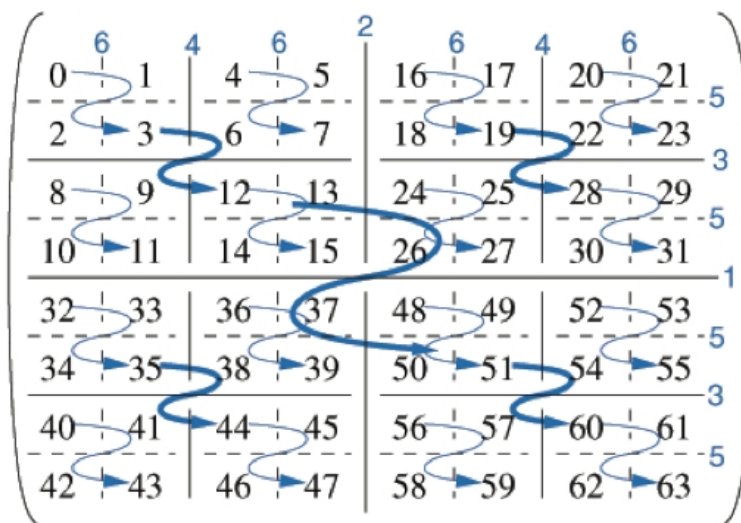
EXTENDED ABSTRACT SUBMITTED FOR PUBLICATION. FOCS99

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## Recursive Blocked Algorithms and Hybrid Data Structures for Dense Matrix Library Software\*



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Isak Jonsson<sup>†</sup>  
Bo Kågström<sup>†</sup>



# Combine NT with ...

## Optimal data/computation layout (on Cell, GPU, multicore,...)?

### Improving Memory Hierarchy Performance for Irregular Applications\*

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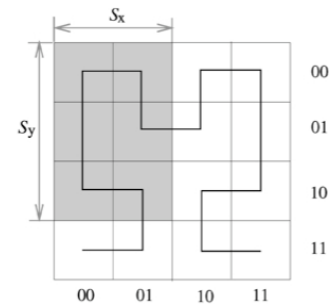
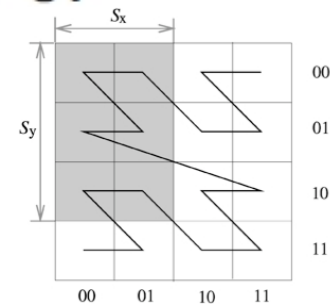
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IEEE TRANSACTIONS ON KNOWLEDGE AND DATA ENGINEERING, VOL. 13, NO. 1, JANUARY/FEBRUARY 2001



## Analysis of the Clustering Properties of the Hilbert Space-Filling Curve

Bongki Moon, H.V. Jagadish, Christos Faloutsos, *Member, IEEE*, and  
Joel H. Saltz, *Member, IEEE*



## Metrics and Models for Reordering Transformations

Morton or Hilbert?

MSP04

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Hypergraph

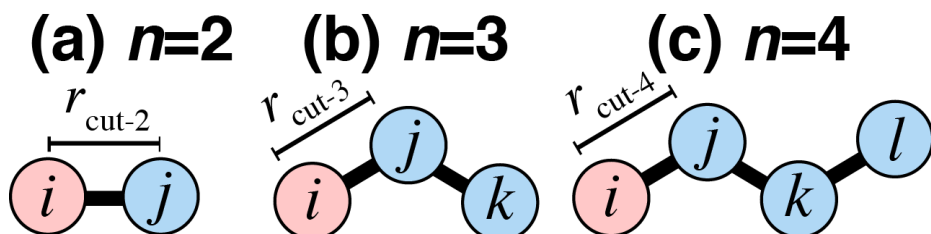
G.M. Morton, "A computer oriented geodetic data base & a new technique in file sequencing,"  
*IBM Tech. Report* ('66)



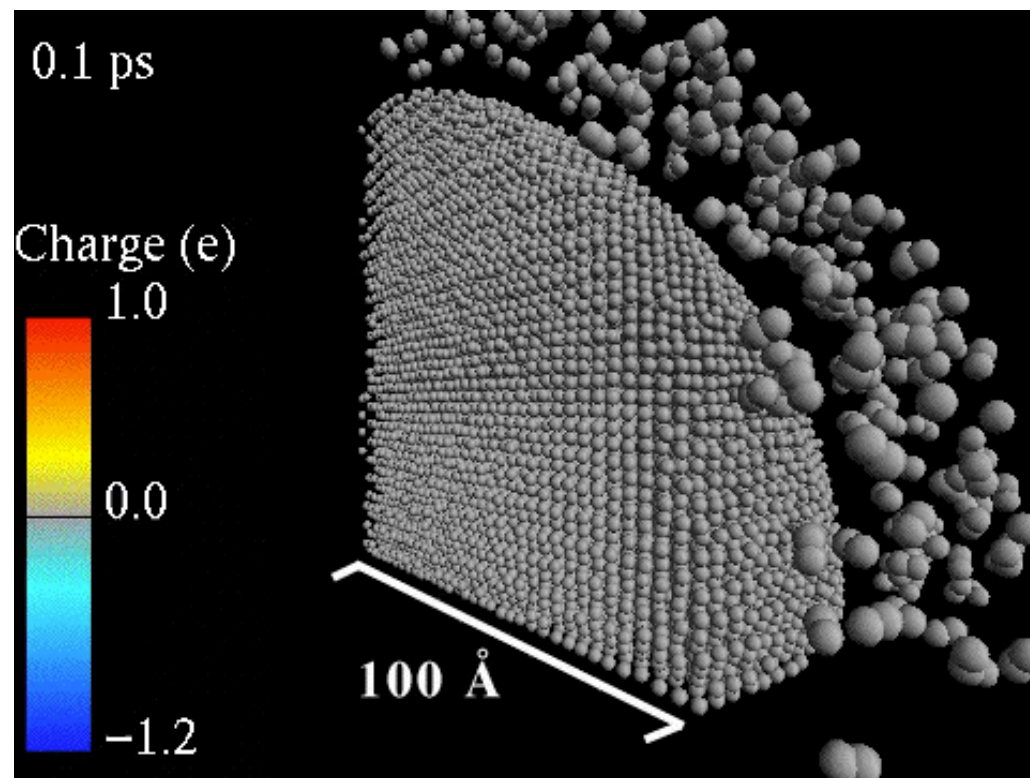
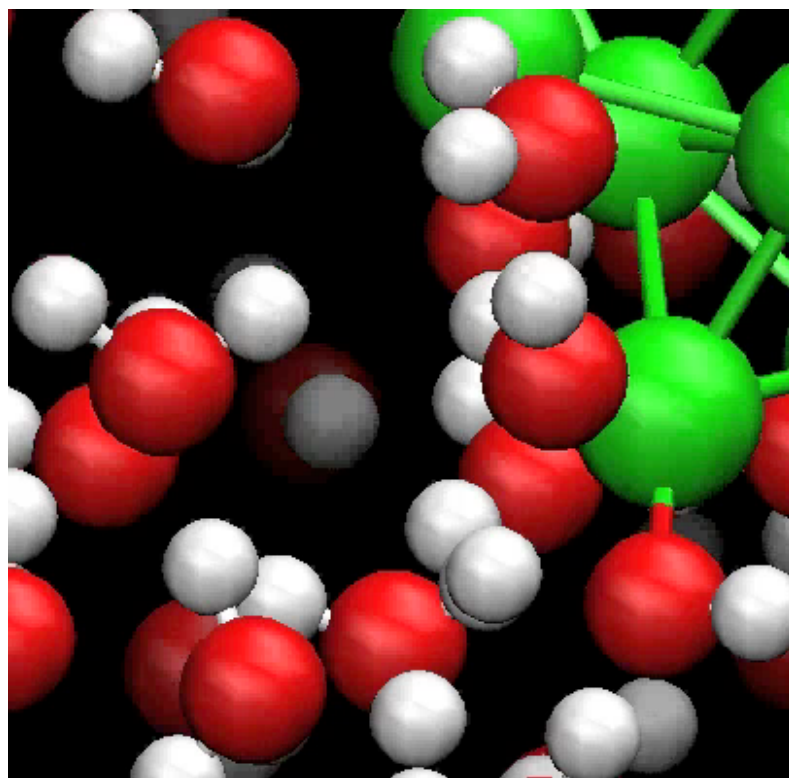
# Reactive Molecular Dynamics (RMD)

- Dynamic  $n$ -tuple computation:  $n \leq 4$  explicitly;  $\leq 6$  through bond order

$$\mathbf{f}_i^{(n)} = - \sum_{\forall (\mathbf{r}_0, \dots, \mathbf{r}_{n-1}) \in \Gamma^{(n)}} \left. \frac{\partial}{\partial \mathbf{x}_i} \Phi_n(\mathbf{x}_0, \dots, \mathbf{x}_{n-1}) \right|_{(\mathbf{x}_0, \dots, \mathbf{x}_{n-1}) = (\mathbf{r}_0, \dots, \mathbf{r}_{n-1})}$$

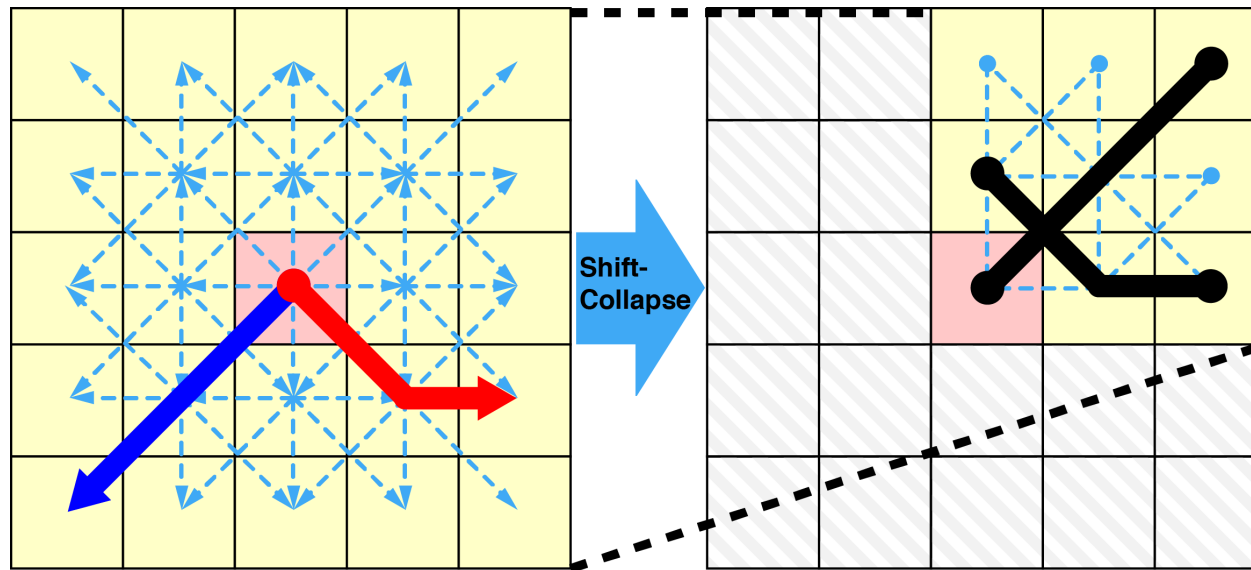


K. Nomura *et al.*,  
*Comp. Phys. Commun.* **192**, 91 ('15)

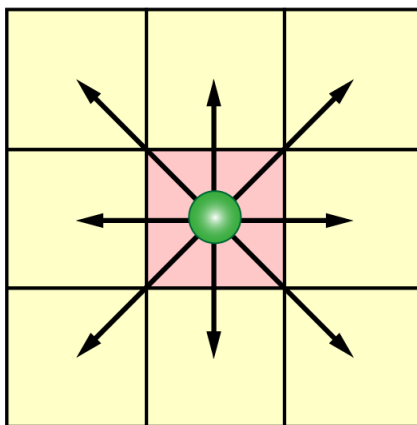


# Shift-Collapse (SC) Algorithm

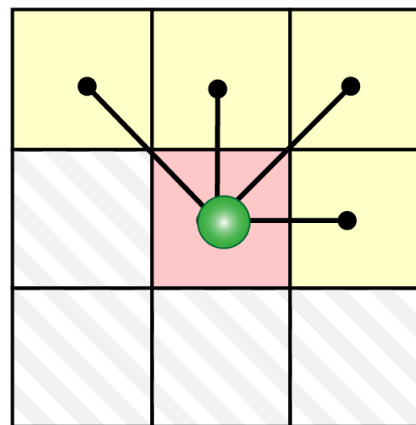
- Generalization of Shaw's eighth-cell method (non-owner-compute method on high-latency cluster) for pair computation to general dynamic range-limited  $n$ -tuples



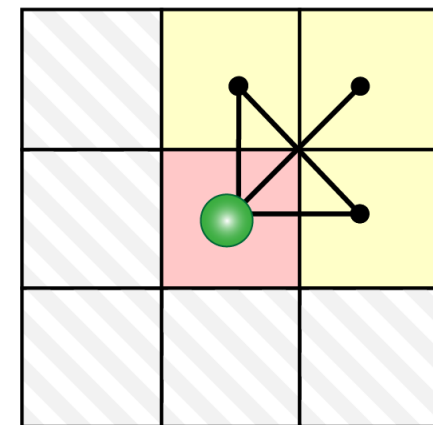
M. Kunaseth *et al.*, *IEEE/ACM Supercomputing (SC13)*



**Full-shell (FS) method**  
[e.g. Rappaport, '88]



**Half-shell (HS) method**  
[e.g. Rappaport, '88]

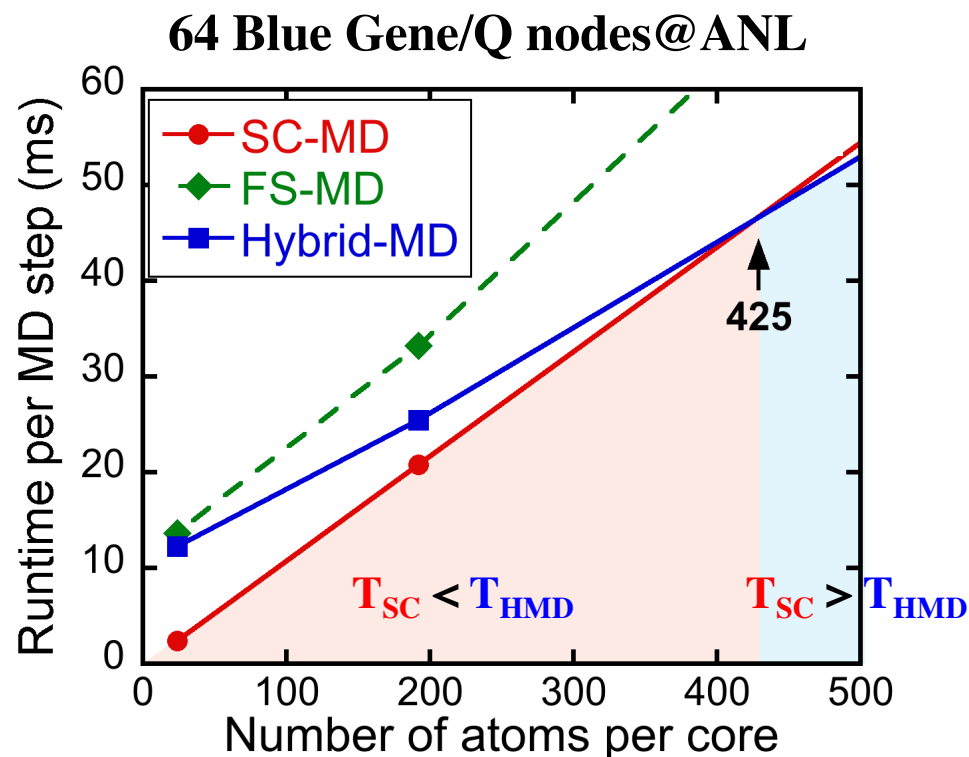
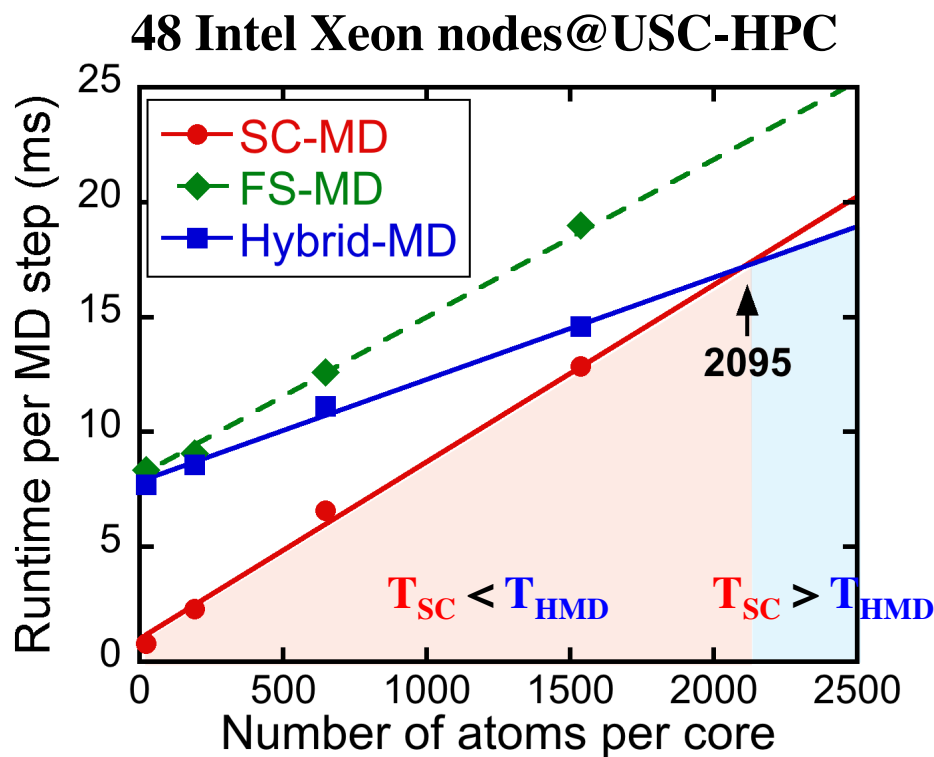


**Eighth-shell (ES) method**  
[Bower *et al.*, '06]

# Shift-Collapse (SC) Performance

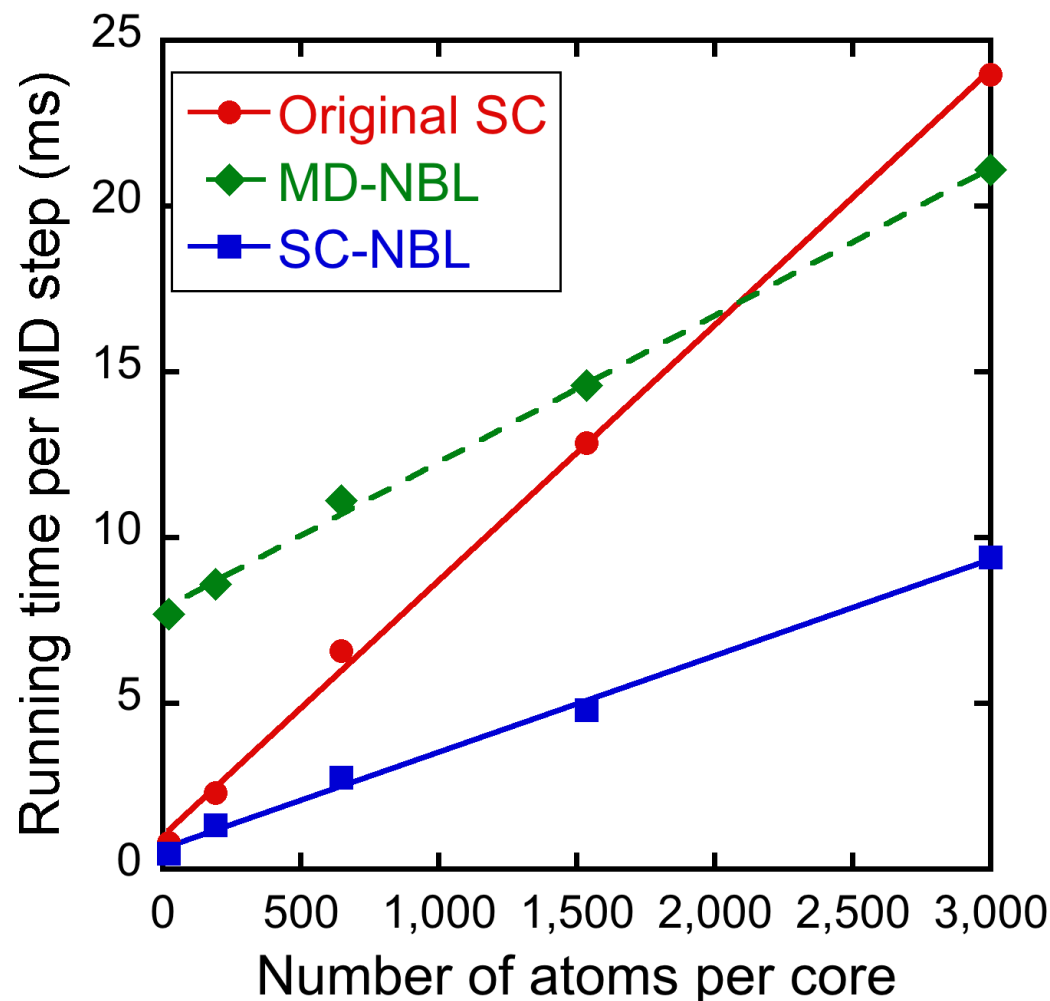
Runtime comparison on 48 Intel-Xeon nodes and 64 Blue Gene/Q nodes

- SC-MD is always faster than FS-MD
- At the smallest grain, SC-MD is **9.7-** and **5.1-fold** speedups over the state-of-the-art hybrid linked-cell & neighbor list code
- Crossover of optimal algorithm from SC-MD to hybrid MD at larger granularity (*i.e.*  $N/P > 2,095$  on Intel Xeon and  $N/P > 425$ )



# Shift-Collapse on Neighbor List (SC-NBL)

- Apply shift-collapse operations to the hybrid linked-cell & neighbor list code (best of both)



“Shift/collapse on neighbor list (SC-NBL): fast evaluation of dynamic many-body potentials in molecular dynamics simulations,” M. Kunaseth, S. Hannongbua, & A. Nakano, *Comput. Phys. Commun.* **235**, 88 (2019)