

# Neutral Territory Decomposition for Parallel MD

---

**Aiichiro Nakano**

*Collaboratory for Advanced Computing & Simulations  
Department of Computer Science  
Department of Physics & Astronomy  
Department of Chemical Engineering & Materials Science  
Department of Biological Sciences  
University of Southern California*

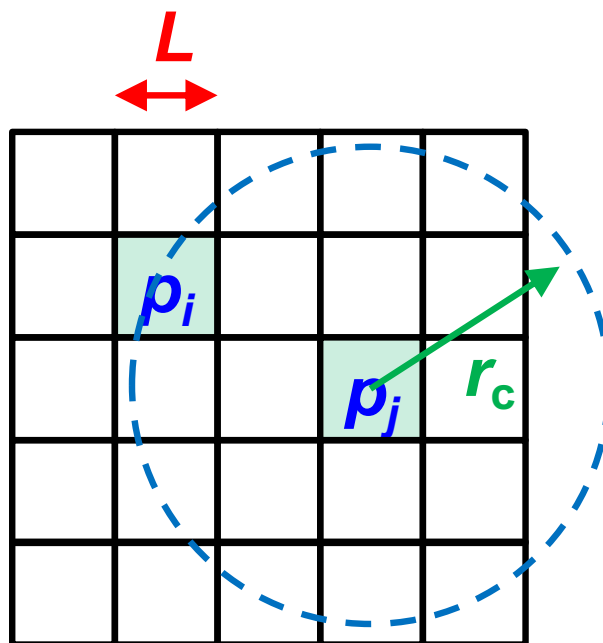
**Email: [anakano@usc.edu](mailto:anakano@usc.edu)**

D. E. Shaw, [A fast, scalable method for the parallel evaluation of distance-limited pairwise particle interactions](#), *J. Comput. Chem.* **26**, 1318 ('05)



# Fine Granularity

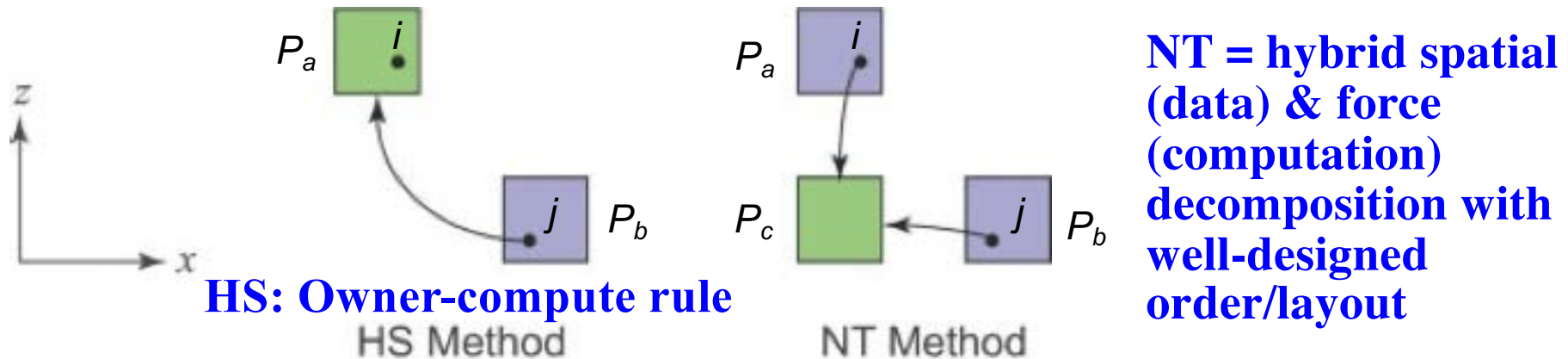
Number of atoms per process ( $N/P$ )  $\sim 1$   
*cf.* Biomolecular simulations



spatial subsystem length ( $L$ )  $\ll$  interaction cutoff ( $r_c$ )

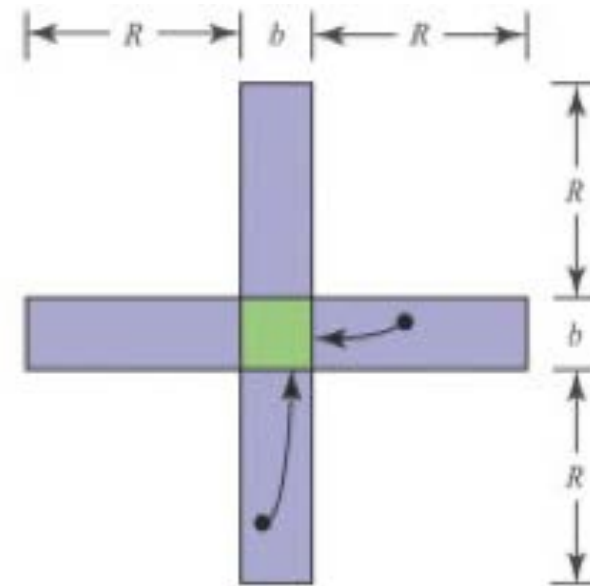
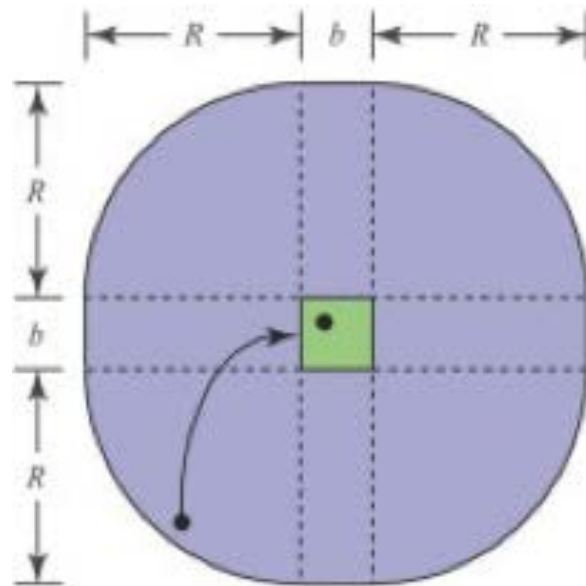
# Spatial (Half-Shell) vs. NT Decompositions

**Locus of interaction — who does what (2-dimensional example)**



**Import regions or communication volume (2-dimensional example)**

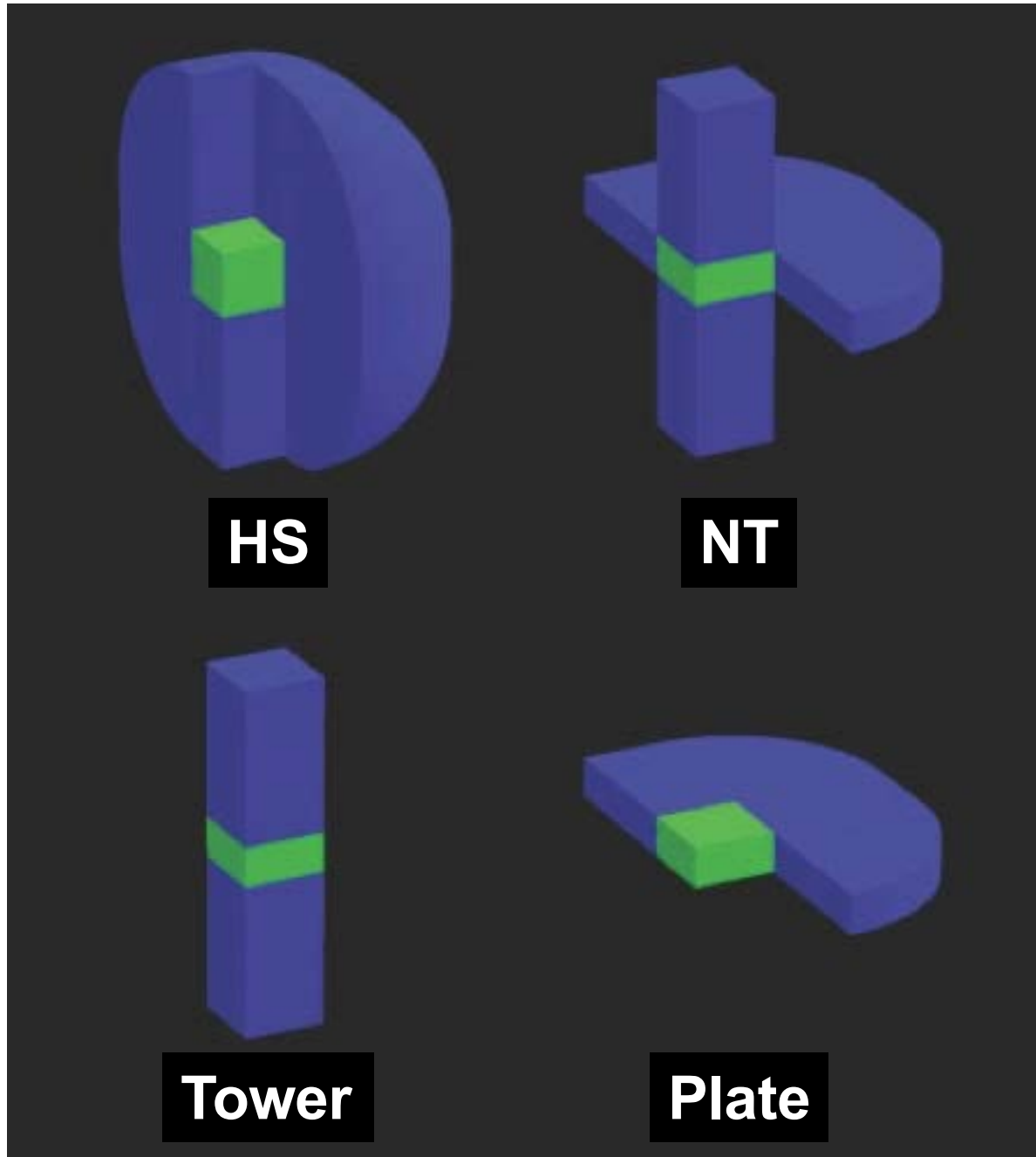
**HS**  
 $4bR + \pi R^2$   
 $\rightarrow \text{const.}$   
 $(b \rightarrow 0)$



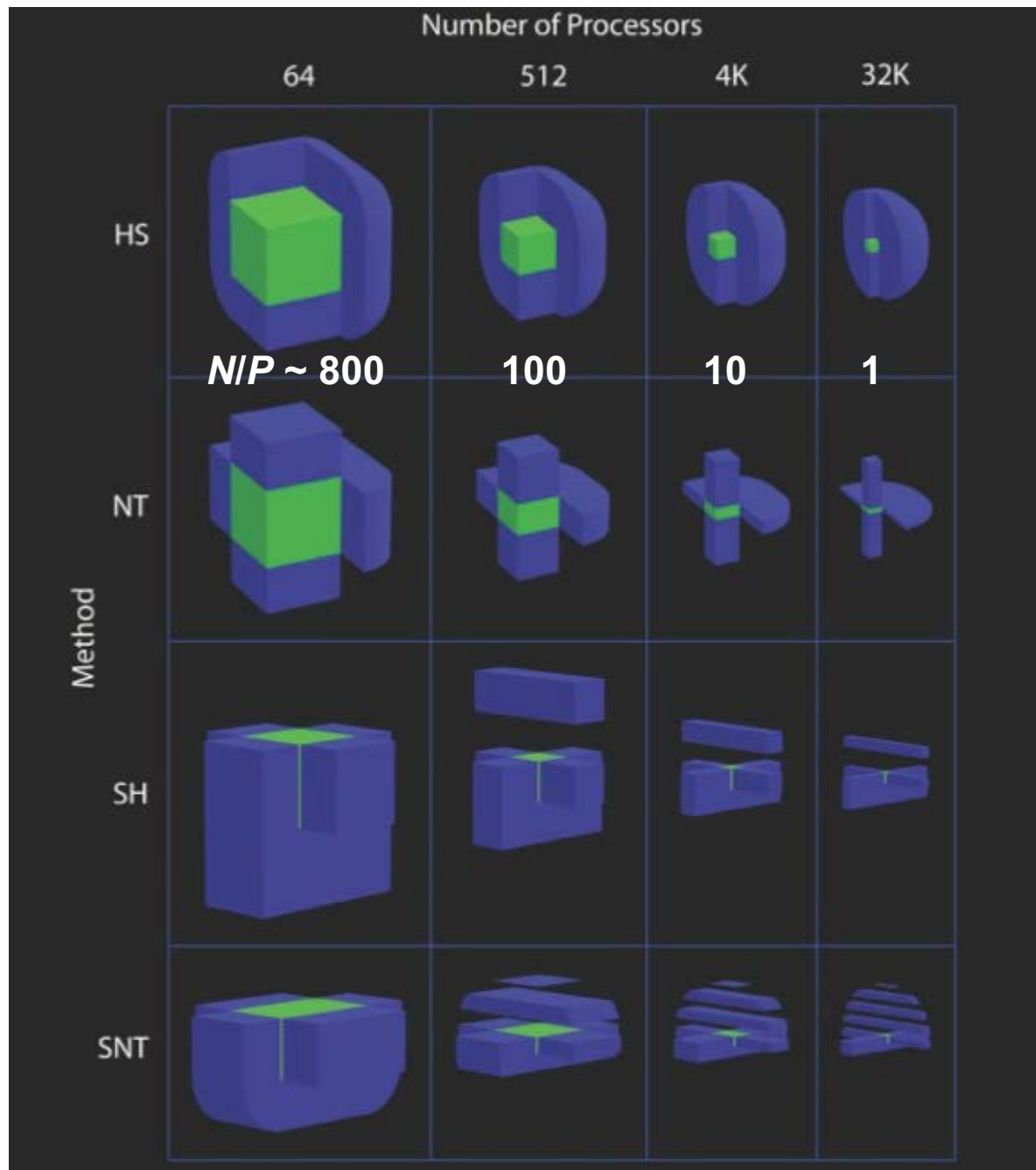
**NT**  
 $4bR$   
 $\rightarrow 0$   
 $(b \rightarrow 0)$

# 3D Import Regions

---



# Scaling of Import Regions



Marc Snir

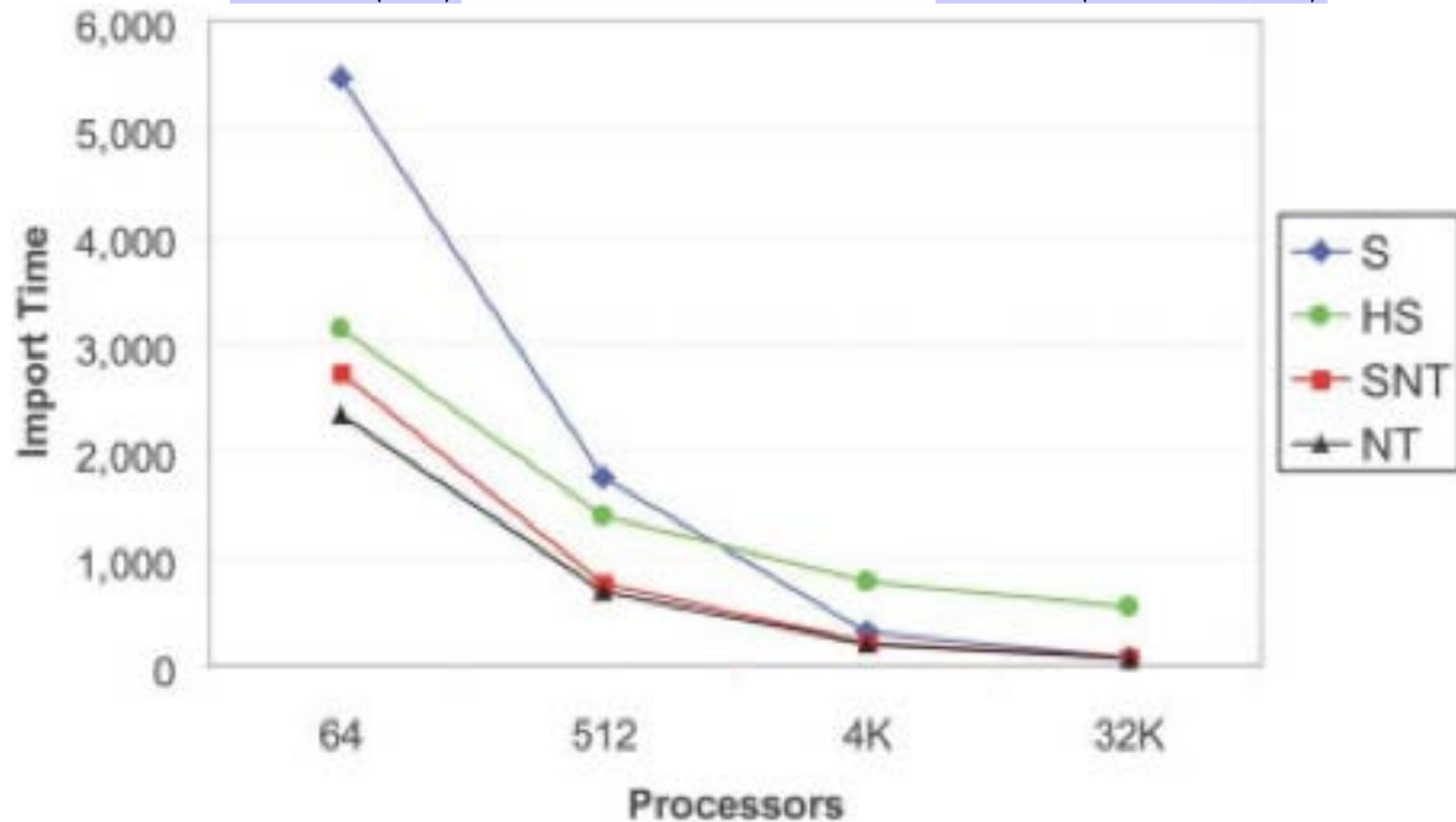
# Scaling of the Volume of Import Regions

HS decomposition

$$V_i = O(R^3)$$

NT decomposition

$$V_i = O(R^{3/2} p^{-1/2})$$



**Communication time**

$$T_{\text{comm}} = t_{\text{latency}} \overset{\text{\# of messages}}{N_{\text{message}}} + \frac{1}{b_{\text{bandwidth}}} \overset{\text{volume (Bytes) of messages}}{V_{\text{message}}}$$

ns ~ many  $\mu$ s      GB/s

# Combine NT with ...

## Cache-oblivious recursive blocking?

### Cache-Oblivious Algorithms

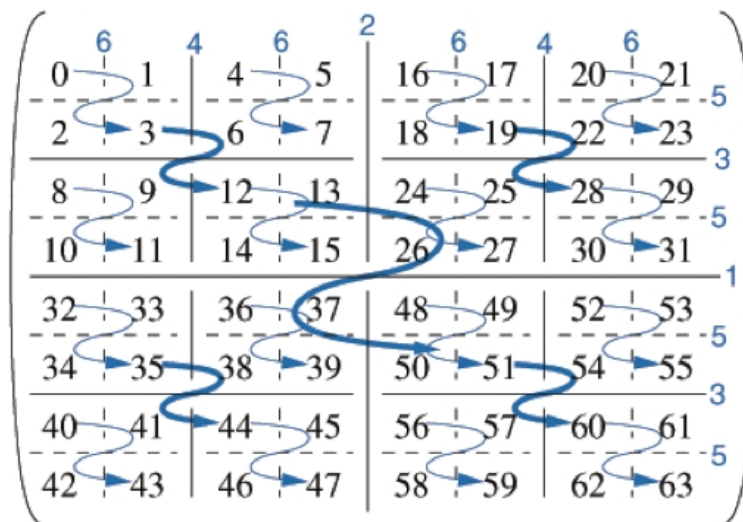
EXTENDED ABSTRACT SUBMITTED FOR PUBLICATION. FOCS99

Matteo Frigo Charles E. Leiserson Harald Prokop Sridhar Ramachandran  
MIT Laboratory for Computer Science, 545 Technology Square, Cambridge, MA 02139  
(athena, cel, prokop, sridhar)@supertech.lcs.mit.edu

SIAM REVIEW  
Vol. 46, No. 1, pp. 3–45

© 2004 Society for Industrial and Applied Mathematics

### Recursive Blocked Algorithms and Hybrid Data Structures for Dense Matrix Library Software\*



Erik Elmroth<sup>†</sup>  
Fred Gustavson<sup>‡</sup>  
Isak Jonsson<sup>†</sup>  
Bo Kågström<sup>†</sup>



# Combine NT with ...

## Optimal data/computation layout (on Cell, GPU, multicore,...)?

### Improving Memory Hierarchy Performance for Irregular Applications\*

John Mellor-Crummey†, David Whalley‡, Ken Kennedy†

† Department of Computer Science, MS 132  
Rice University  
6100 Main  
Houston, TX 77005  
{johnmc,ken}@cs.rice.edu

ISC99

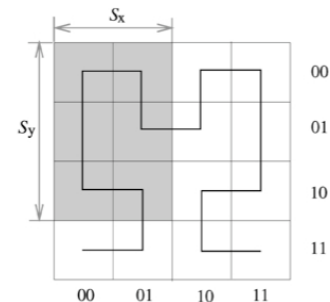
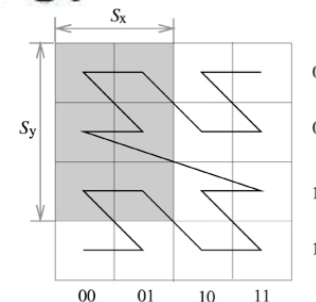
‡ Computer Science Department  
Florida State University  
Tallahassee, FL 32306-4530  
whalley@cs.fsu.edu  
phone: (850) 644-3506

IEEE TRANSACTIONS ON KNOWLEDGE AND DATA ENGINEERING, VOL. 13, NO. 1, JANUARY/FEBRUARY 2001



## Analysis of the Clustering Properties of the Hilbert Space-Filling Curve

Bongki Moon, H.V. Jagadish, Christos Faloutsos, *Member, IEEE*, and  
Joel H. Saltz, *Member, IEEE*



## Metrics and Models for Reordering Transformations

Morton or Hilbert?

MSP04

Michelle Mills Strout  
Mathematics and Computer Science Division  
Argonne National Laboratory  
Argonne, IL 60439 USA  
mstrout@mcs.anl.gov

Paul D. Hovland  
Mathematics and Computer Science Division  
Argonne National Laboratory  
Argonne, IL 60439 USA  
hovland@mcs.anl.gov

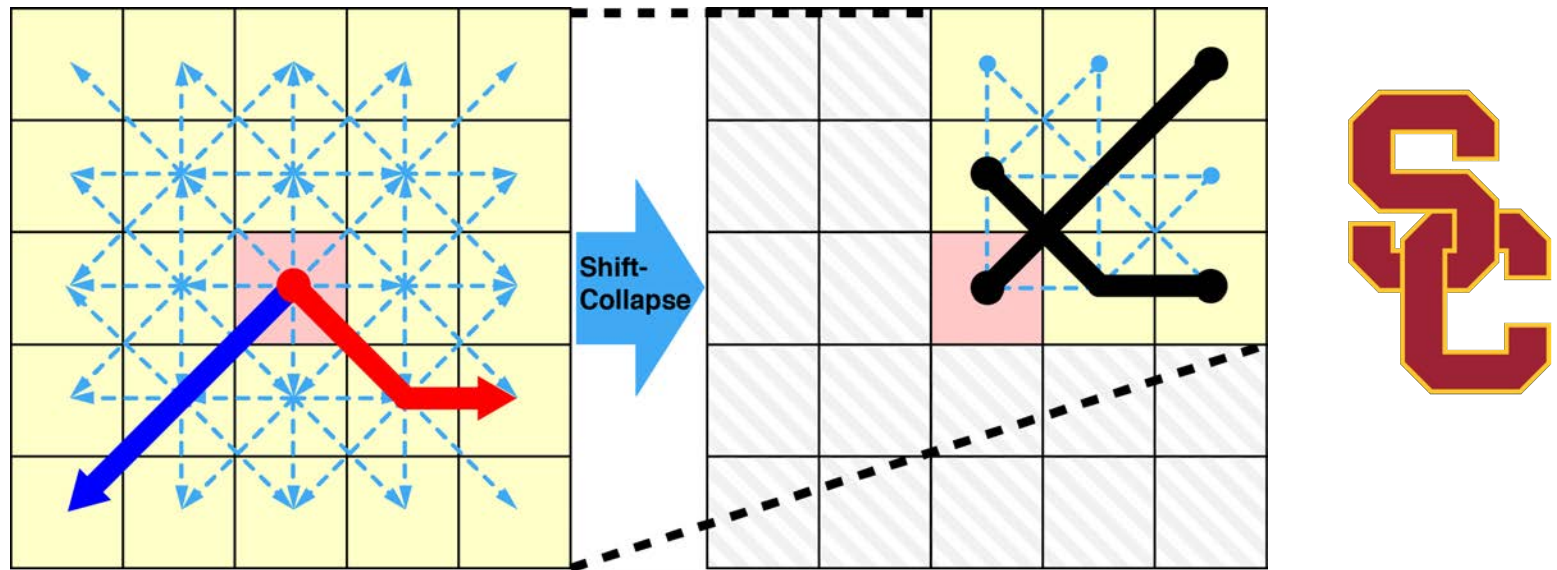
Hypergraph

G.M. Morton, "A computer oriented geodetic data base & a new technique in file sequencing,"  
*IBM Tech. Report* ('66)

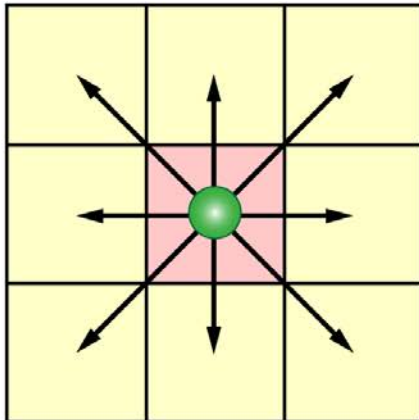


# Shift-Collapse (SC) Algorithm

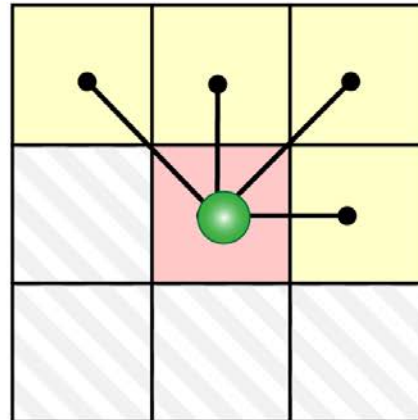
- Generalization of Shaw's eighth-cell method (non-owner-compute method on high-latency cluster) for pair computation to general dynamic range-limited  $n$ -tuples



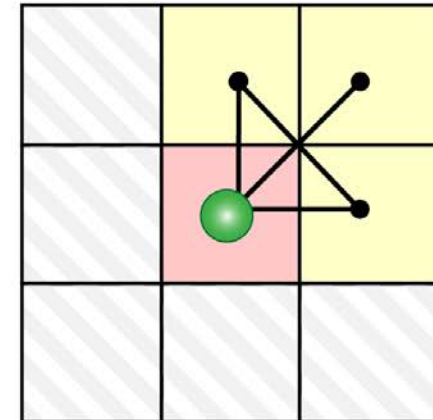
M. Kunaseth *et al.*, *IEEE/ACM Supercomputing (SC13)*



**Full-shell (FS) method**  
[e.g. Rappaport, '88]



**Half-shell (HS) method**  
[e.g. Rappaport, '88]

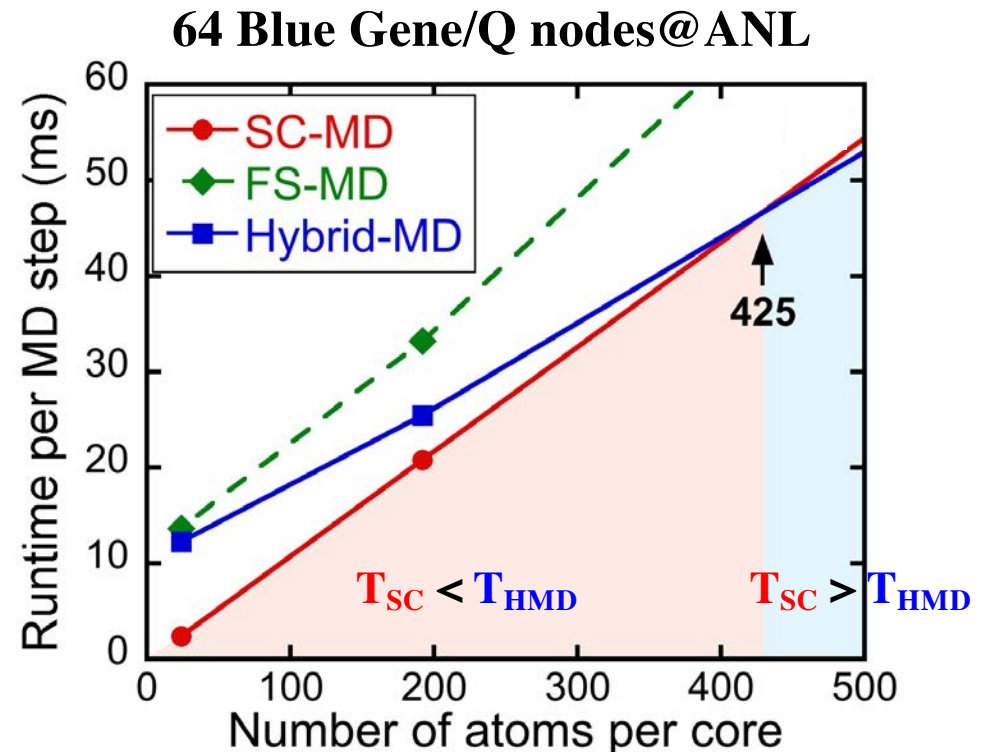
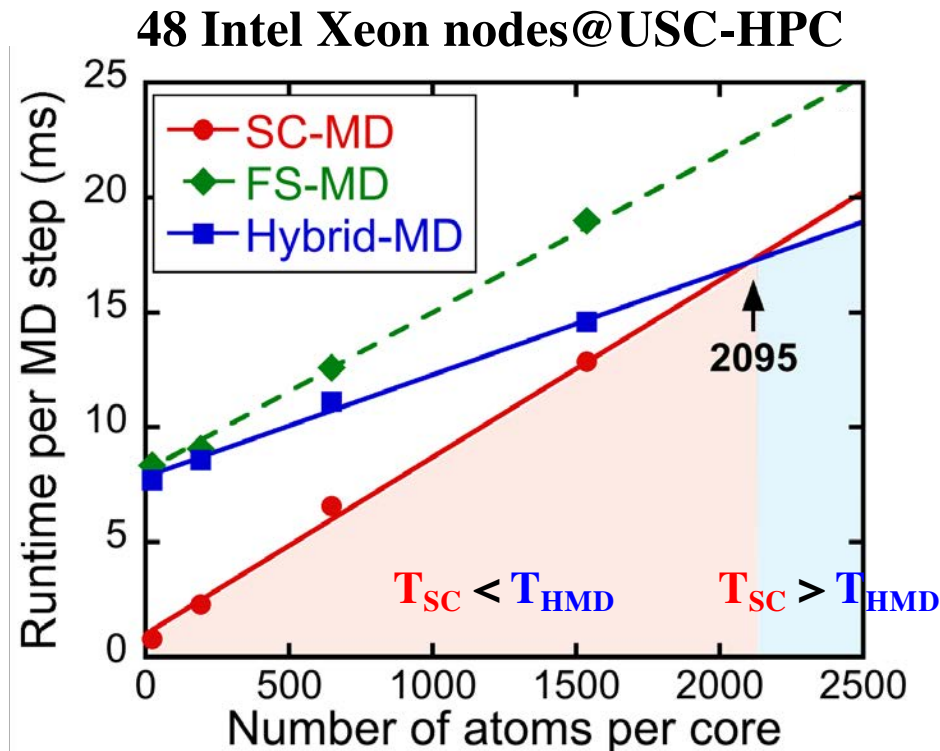


**Eighth-shell (ES) method**  
[Bower *et al.*, '06]

# Shift-Collapse (SC) Performance

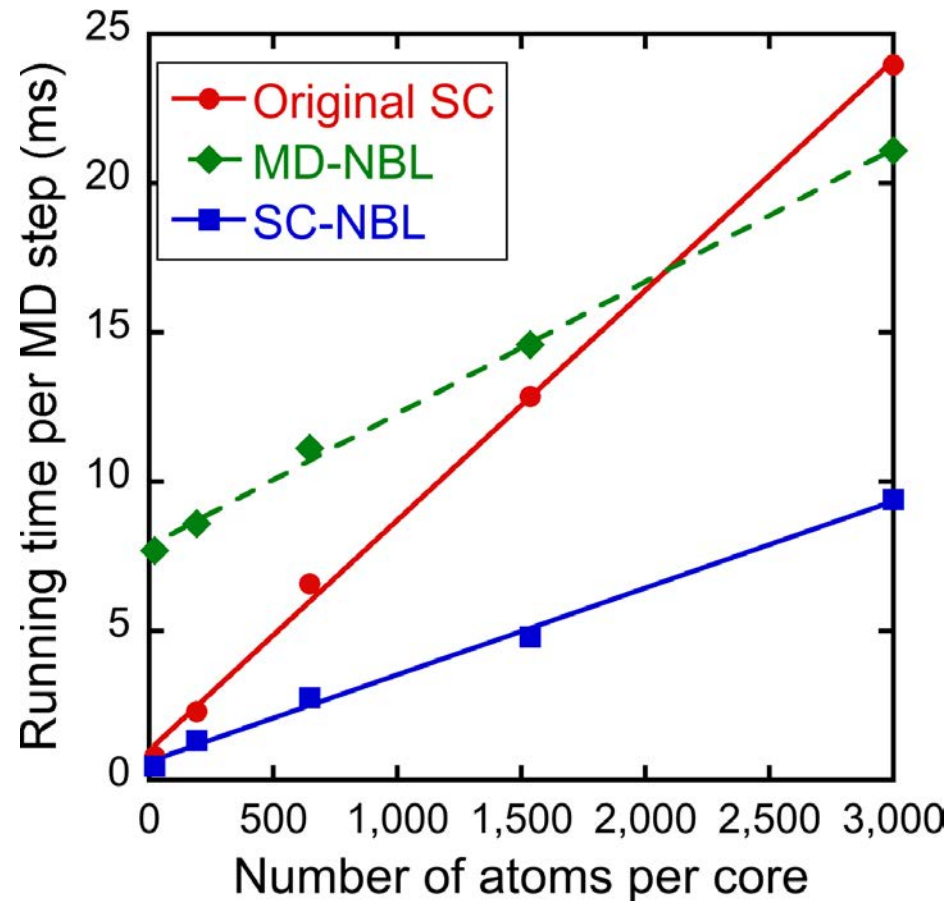
Runtime comparison on 48 Intel-Xeon nodes and 64 Blue Gene/Q nodes

- SC-MD is always faster than FS-MD
- At the smallest grain, SC-MD is **9.7-** and **5.1-fold** speedups over the state-of-the-art hybrid linked-cell & neighbor list code
- Crossover of optimal algorithm from SC-MD to hybrid MD at larger granularity (*i.e.*  $N/P > 2,095$  on Intel Xeon and  $N/P > 425$ )



# Shift-Collapse on Neighbor List (SC-NBL)

- Apply shift-collapse operations to the hybrid linked-cell & neighbor list code (best of both)



[Shift/collapse on neighbor list \(SC-NBL\): fast evaluation of dynamic many-body potentials in molecular dynamics simulations](#), M. Kunaseth, S. Hannongbua, & A. Nakano, *Comput. Phys. Commun.* **235**, 88 (2019)

**Challenge:** Expose massive data parallelism for SC on graphics processing unit (GPU)