Optimizing Molecular Dynamics

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- Intranode optimization: CPU & memory access
- Internode optimization: Communication



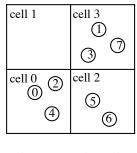
Data/computation locality!



Intranode: Memory Access

Data re-ordering

• Linked-list cells—irregular memory access pattern

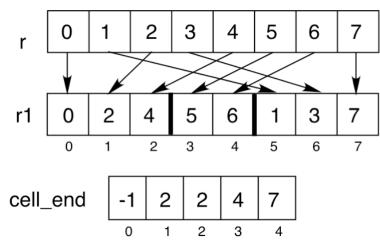


	0	1	2	3	_			
head	4	Е	6	7				
	0	1	2	3	4	5	6	7
lscl	Е	Е	0	1	2	Е	5	3

• Data locality: Regular data layout

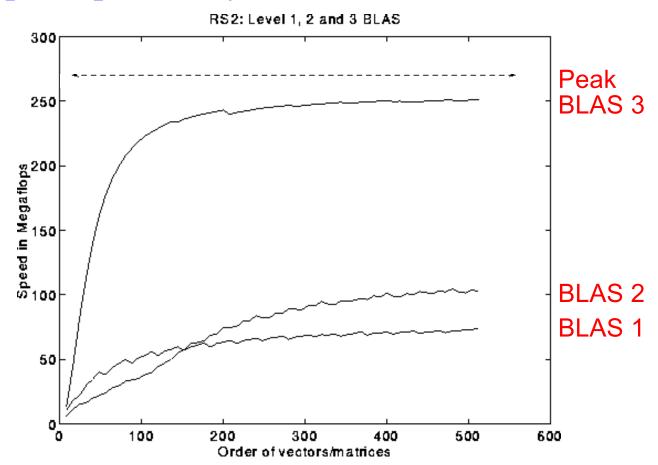
for i = cell_end[c]+1 to cell_end[c+1]

access r1[i] endfor



BLAS3-Performance Molecular Dynamics?

• BLAS3: $q = \text{flop/memory access} = (\text{block size})^{1/2}$



- Molecular dynamics: $q = O(n^2)/O(n) = O(n)$: block size)
 - > Use of SIMD (single instruction multiple data) instructions on Cell, multicore (AVX)?

Floating Point Performance

- BLAS-ification: Transform from band-by-band to all-band computations to utilize a matrix-matrix subroutine (DGEMM) in the BLAS3 library for the quantum molecular dynamics application
- Algebraic transformation of computations

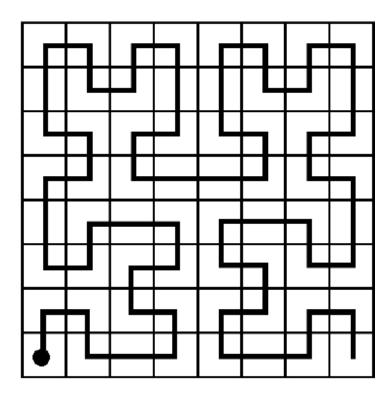
Example: Nonlocal pseudopotential operation D. Vanderbilt, Phys. Rev. B 41, 7892 ('90) $\hat{v}_{\text{nl}}|\psi_{n}^{\alpha}\rangle = \sum_{l}^{N_{\text{atom}}} \sum_{ij}^{L_{\text{max}}} |\beta_{i,l}\rangle D_{ij,l}\langle\beta_{j,l}|\psi_{n}^{\alpha}\rangle \quad (n=1,\ldots,N_{\text{band}})$ $\Psi = \left[|\psi_{1}^{\alpha}\rangle,\ldots,|\psi_{N_{\text{band}}}^{\alpha}\rangle\right] \widetilde{\mathbf{B}}(i) = \left[|\beta_{i,1}\rangle,\ldots,|\beta_{i,N_{\text{atom}}}\rangle\right] \left[\widetilde{\mathbf{D}}(i,j)\right]_{l,J} = D_{ij,l}\delta_{lJ}$ $\hat{v}_{\text{nl}}\Psi = \sum_{i,j}^{L} \widetilde{\mathbf{B}}(i)\widetilde{\mathbf{D}}(i,j)\widetilde{\mathbf{B}}(j)^{T}$

- 50.5% of the theoretical peak FLOP/s performance on 786,432 Blue Gene/Q cores (entire Mira at the Argonne Leadership Computing Facility)
- 55% of the theoretical peak FLOP/s on Intel Xeon E5-2665

Computation Locality

Data to computation re-ordering: How to traverse cells?

- Pair-interaction computation: Preserve nearest-neighbor cells' proximity in memory
- Spacefilling curve: Mapping from the *d*-dimensional space to one-dimensional list to preserve spatial proximity of consecutive list elements



J. Mellor-Crummey et al., Int'l J. Parallel Prog. 29, 217 ('01)

Hilbert-Peano Curve

• Gray code: a sequence of numbers such that successive numbers have Hamming <u>distance</u> 1

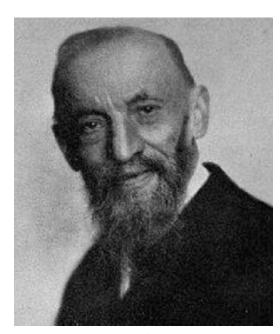
Algorithm: Recursive generation of k-bit Gray code G(k)

of bits where two binary numbers differ

- (2)G(k+1) is constructed from G(k) as follows:
 - a. Construct a new sequence by appending a 0 to the left of all members of G(k).
 - b. Construct a new sequence by reversing G(k) & then appending a 1 to the left of all members of the sequence.
 - c. G(k+1) is the concatenation of the sequences defined in steps a & b.
- G(3): 000 001 011 010 110 111 101 100



000 010 1110 001

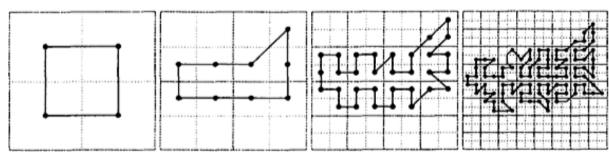


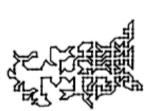
David Hilbert (1862-1943)

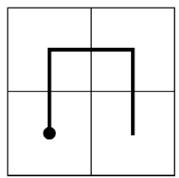
Giuseppe Peano (1858–1932)

Hilbert-Peano Curve

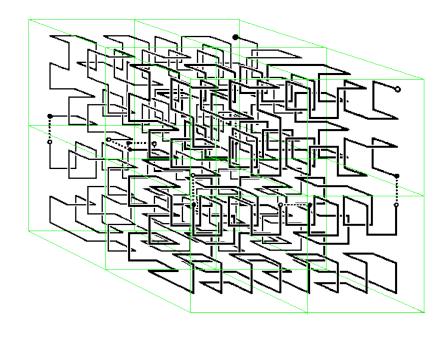
- Hilbert curve: recursive application of the *d*-dimensional Gray codes
- 2-dimensional Hilbert curve





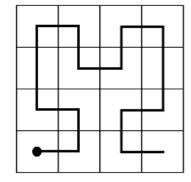


• 3-dimensional Hilbert curve

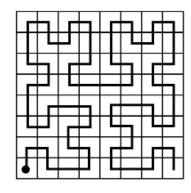


level 2

level 1



level 3

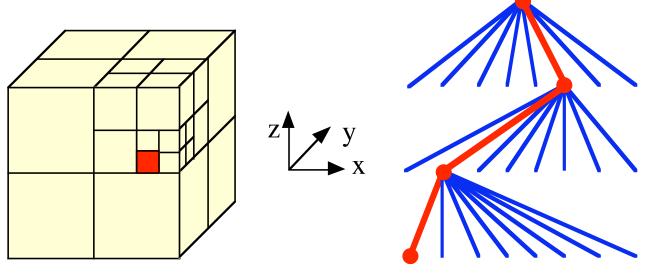


Morton (Z) Curve

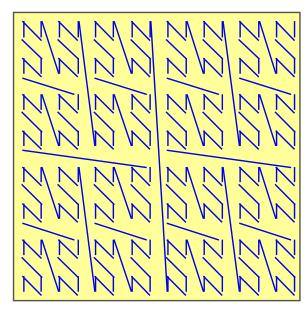
Spacefilling curve based on octree index

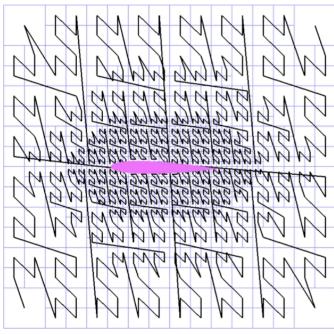
$$x = 1 1 0$$
 $y = 0 0 0$
 $z = 1 0 0$
 $R = 101 001 000$

- 3D → list map preserves spatial proximity
- Multiresolution analysis made easy









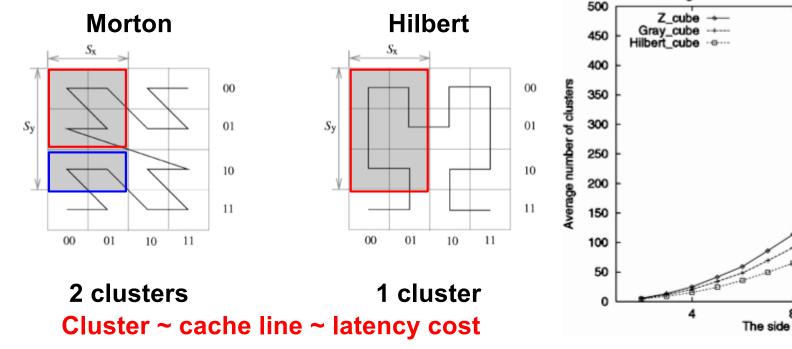
IEEE TRANSACTIONS ON KNOWLEDGE AND DATA ENGINEERING, VOL. 13, NO. 1, JANUARY/FEBRUARY 2001

Average Number of Clusters (Grid: 32768 x 32768 x 32768)

Morton (Z)

Analysis of the Clustering Properties of the Hilbert Space-Filling Curve

Bongki Moon, H.V. Jagadish, Christos Faloutsos, Member, IEEE, and Joel H. Saltz, Member, IEEE



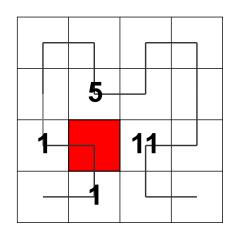
Hilbert 16 12 The side length of query (s)

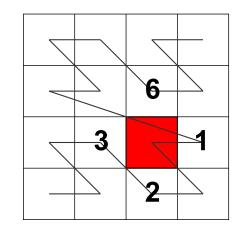
Hilbert curve is better than Morton curve for spatial range query

Alternative Locality Measure for MD

Which curve is better for spatial "pair" query?

- Evaluate curves based on curve distances to neighbors
- Compare number below & above threshold cutoff k_c (like cache)





- 4x4 Hilbert:
 - 30 1s
 - 10 3s
 - 45s
 - 211s
 - 213s
- Lower median, higher variance
- Better for k_c = 1

- 4x4 Z-curve:
 - 161s
 - 16 2s
 - 83s
 - 86s
- Higher median, lower variance
- Better for $2 < k_c < 13$

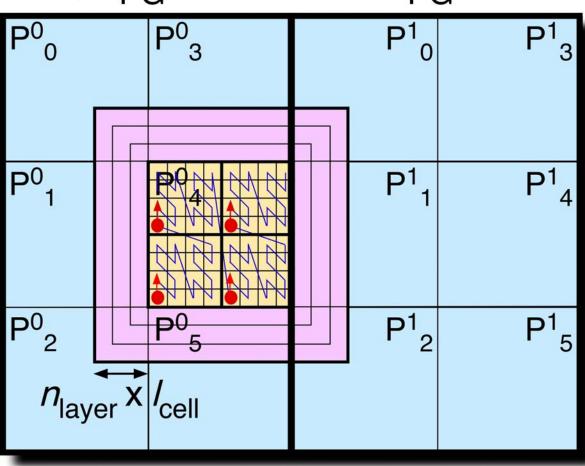
Scott Calaghan (CSCI 596 final project)

Tunable Hierarchical Cellular Decomposition

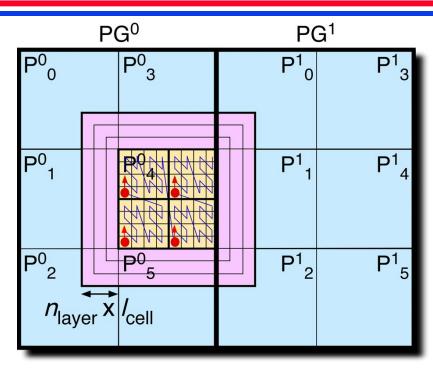
Mapping O(N) divide-&-conquer algorithms onto memory hierarchies

- Spatial decomposition with data "caching" & "migration"
- Computational cells (e.g. linked-list cells in MD) < cell blocks (threads) < processes (P_{π}^{γ} , spatial decomposition subsystems) < process groups (P^{γ} , Grid nodes) P_{G}^{0} P_{G}^{1}
- Multilayer cellular decomposition (MCD) for *n*-tuples (n = 2-6)
- Tunable cell data & computation structures:
 Data/computation re ordering & granularity
 parameterized at each
 decomposition level
- Tunable hybrid MPI +
 OpenMP + SIMD
 implementation

Nomura et al., IPDPS 2009

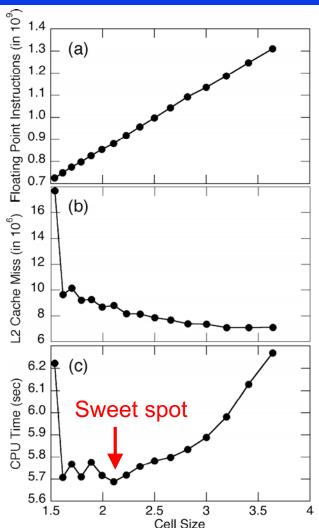


Performance Tunability



Floating-point operation/L2 cache miss trade-off:

331,776-atom silica MRMD on 1.4GHz Pentium III



MPI/OpenMP parallelism trade-off:

8,232,000-atom silica MRMD & 290,304-atom RDX F-ReaxFF on 8-way 1.5 GHz Power4

Number of OpenMP	Number of MPI	Execution time/MD time step (sec)			
threads, $n_{\rm td}$	processes, n_p	MRMD	P-ReaxFF		
1	8	4.19	62.5		
2	4	5.75	58.9		
4	2	8.60	54.9		
8	1	12.5	120		

SIMD Vectorization

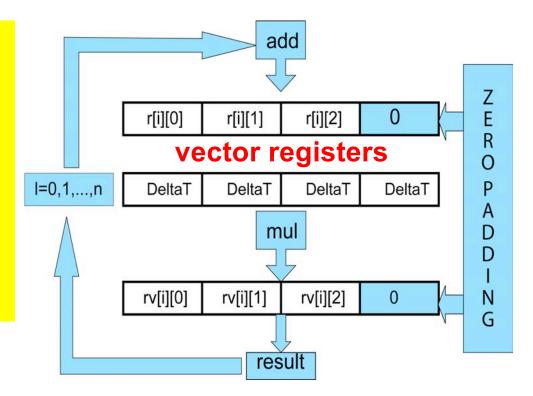
• Single-instruction multiple-data (SIMD) parallelism

(Example) Zero padding to align complex data

Original solution

SIMD solution

```
for (i=0; i<N; i++)
  for (a=0; a<3; a++)
   r[i][a] =
   r[i][a] +
   DeltaT*rv[i][a];</pre>
```

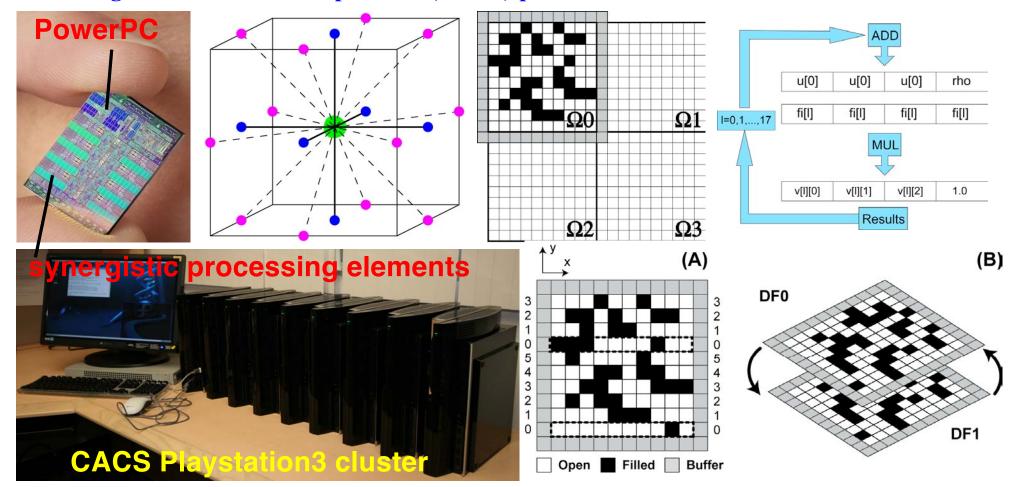


cf. False-sharing avoidance

Peng et al., PDPTA 2009; UCHPC 2010; J. Supercomputing 57, 20 ('11)

Hierarchical Parallelization

- Developed a hierarchical parallel lattice Boltzmann method (pLBM) for flow simulation on a cluster of Cell Broadband Engine-based Playstation3 consoles & IBM BlueGenes
 - 1. Spatial decomposition via message passing
 - 2. Multithreading through critical section-free, dual representation
 - 3. Single-instruction multiple data (SIMD) parallelism via new vector transforms



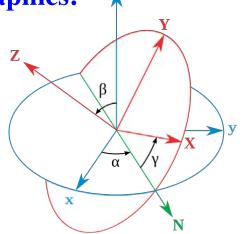
Peng et al., IJCS 08; Euro-Par 08; IPDPS 09; cf. https://en.wikipedia.org/wiki/Four-vector

More Four-Vectors for SIMD

Use SIMD-efficient four-vectors abundant in mathematical physics!

- Special relativity in physics: space (x, y, z)-time (t) four-vector $X^{\mu} = (ct, x, y, z)$; c: light speed
- Quaternion representation of rotation in computer graphics:

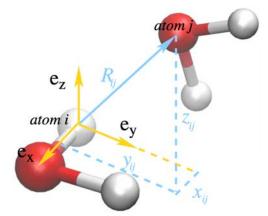
$$\begin{bmatrix} q_0 \\ q_1 \\ q_2 \\ q_3 \end{bmatrix} = \begin{bmatrix} \cos\frac{\theta}{2}\cos\frac{\phi+\psi}{2} \\ \sin\frac{\theta}{2}\cos\frac{\phi-\psi}{2} \\ \sin\frac{\theta}{2}\sin\frac{\phi-\psi}{2} \\ \cos\frac{\theta}{2}\sin\frac{\phi+\psi}{2} \end{bmatrix}; \ (\theta,\phi,\psi): \text{ Euler angles}$$



• Feature vector in deep-learning molecular dynamics:

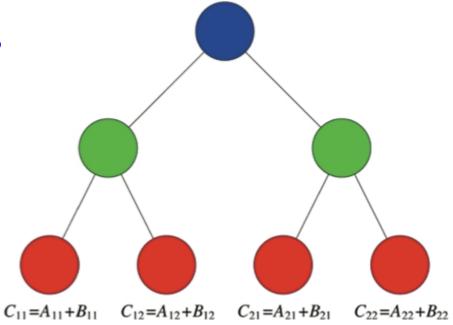
$$D_{ij} = (1/R_{ij}, x_{ij}/R_{ij}, y_{ij}/R_{ij}, z_{ij}/R_{ij})$$

L. Zhang et al., Phys. Rev. Lett. 120, 143001 ('18)



Cache-Oblivious Linked-List Cell MD?

• Recursive blocking for cells?



Cache-Oblivious Algorithms

EXTENDED ABSTRACT SUBMITTED FOR PUBLICATION. In Proc. FOCS99

Matteo Frigo Charles E. Leiserson Harald Prokop Sridhar Ramachandran

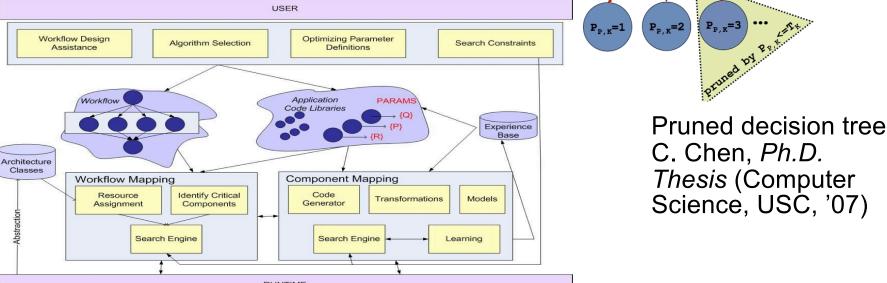
MIT Laboratory for Computer Science, 545 Technology Square, Cambridge, MA 02139

{athena,cel,prokop,sridhar}@supertech.lcs.mit.edu

We introduce an "ideal-cache" model to analyze our algorithms, and we prove that an optimal cache-oblivious algorithm designed for two levels of memory is also optimal for multiple levels.

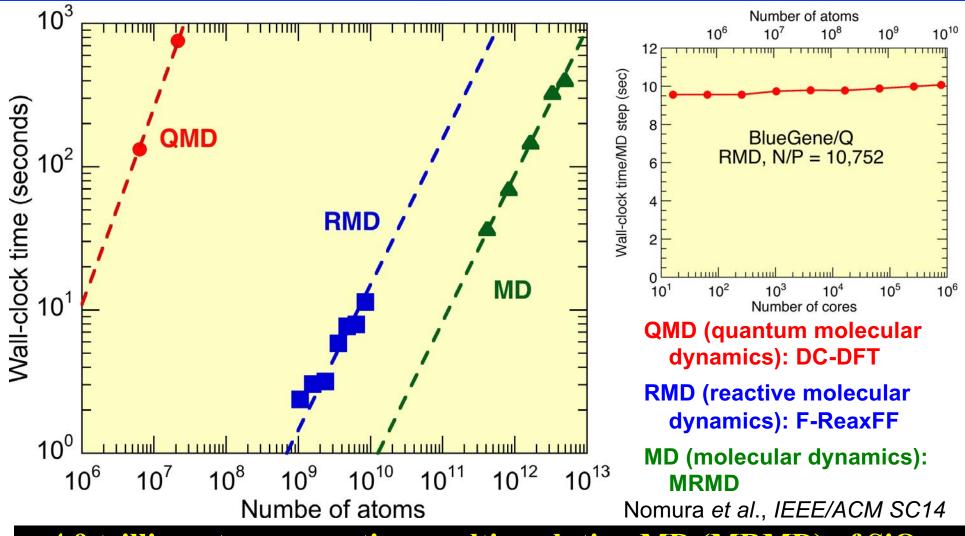
Intelligent Performance Optimization

• Knowledge representation to express concurrency/data locality & machine learning to optimally map them to hardware cf. Tunable hierarchical cellular decomposition exposes maximal data locality



"Intelligent optimization of parallel & distributed applications," B. Bansal, U. Catalyurek, J. Chame, C. Chen, E. Deelman, Y. Gil, M. Hall, V. Kumar, T. Kurc, K. Lerman, A. Nakano, Y. L. Nelson, J. Saltz, A. Sharma, and P. Vashishta, in *Proc. of Next Generation Software Workshop, Int'l Parallel & Distributed Processing Symp. (IPDPS 07)*

Scalable Simulation Algorithm Suite



- 4.9 trillion-atom space-time multiresolution MD (MRMD) of SiO₂
- 8.5 billion-atom fast reactive force-field (F-ReaxFF) RMD of RDX
- 39.8 trillion grid points (50.3 million-atom) DC-DFT QMD of SiC parallel efficiency 0.984 on 786,432 Blue Gene/Q cores

Scalability on Multicore Clusters

Hybrid message-passing (MPI) + multithreading (OpenMP) + single-instruction multiple-data (SIMD) programming

2.6× speedup over MPI by hybrid MPI+OpenMP on 32,768 IBM BlueGene/P cores

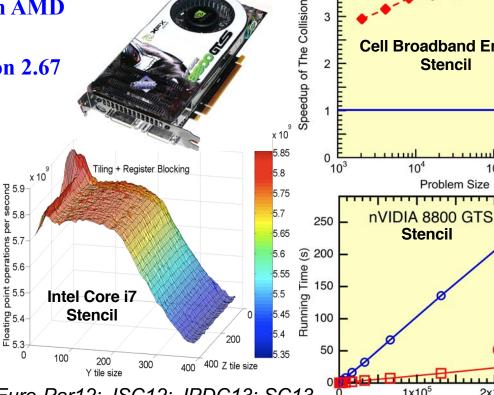
Multithreading parallel efficiency 0.99 for MD on 64-core Godson-T processor

SIMD efficiency 0.93 on PlayStation3

8.8× speedup on an NVIDIA GeForce 8800 GTS graphics processing unit (GPU) over an AMD Sempron CPU

55% of theoretical peak performance on 2.67 GHz Intel Core i7 920





per MD Step (ms)

Runtime

30

4000

BlueGene/P

MD

0.8 million atoms

10000

Number of cores

Cell Broadband Engine

Stencil

MPI

2.6x

30000

CPU

3x105

2x105

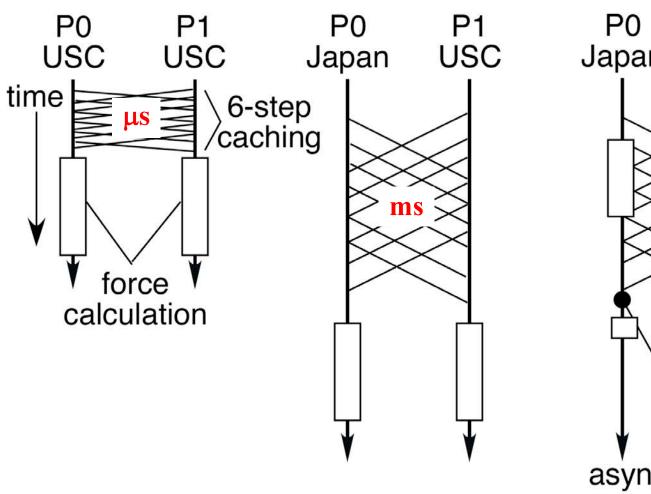
Problem Size

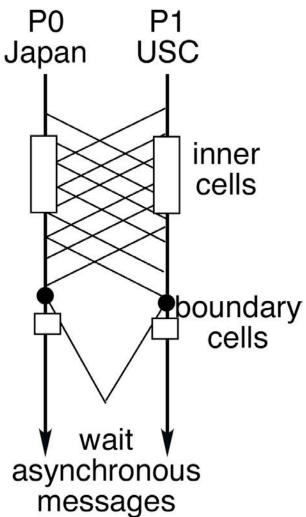
MPI+OpenMP

IJCS08; IPDPS09; PPL09; ICS10; CF11; Euro-Par12; JSC12; JPDC13; SC13

Internode Optimization

• Communication bottleneck in metacomputing on a Grid

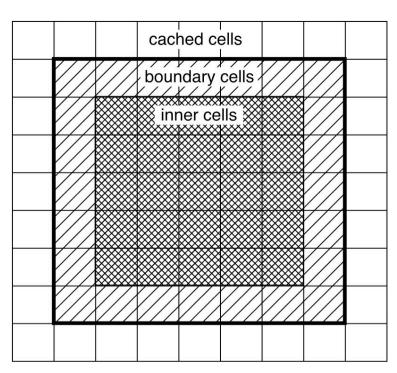




Grid-Enabled MD Algorithm

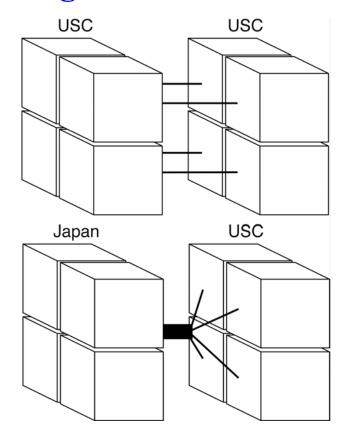
Grid MD algorithm:

- 1. asynchronous receive of cells to be cached MPI_Irecv()
- 2. send atomic coordinates in the boundary cells
- 3. compute forces for atoms in the inner cells
- 4. wait for the completion of the asynchronous receive MPI_Wait()
- 5. compute forces for atoms in the boundary cells



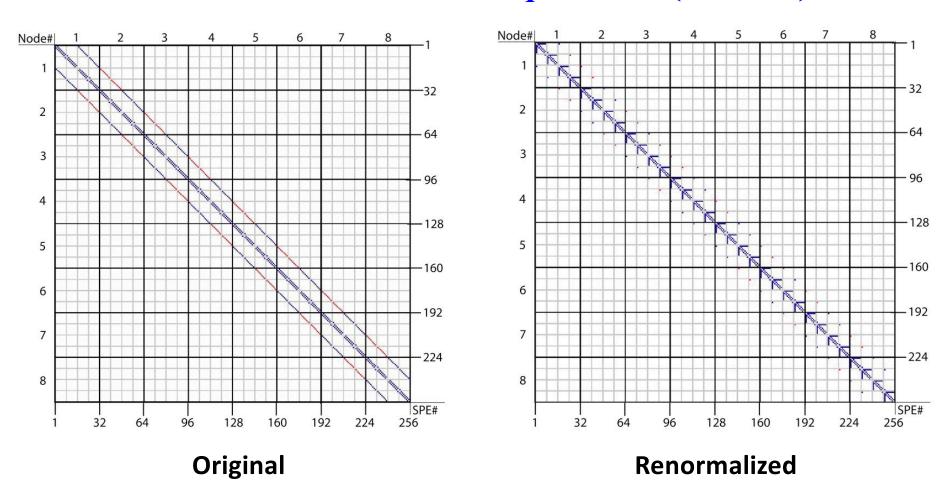
Renormalized Messages:

Latency can be reduced by composing a large cross-site message instead of sending all processor-to-processor messages



Renormalized Messages

Communication pattern of a 3D particle transport simulation code on a cluster of quad-Cell (32 cores) nodes



H. Dursun et al., Parallel Processing Letters 19, 535 ('09)

Where to Go from Here

- Performance profiling: First thing is how well/badly your program is performing in terms of flop/s performance, vectorization, cache miss, etc.
- Use professional tools like Intel VTune if available on your computer:

 https://software.intel.com/content/www/us/en/develop/tools/vtune-profiler.html
 https://www.youtube.com/watch?reload=9&v=ymy139CuAx8

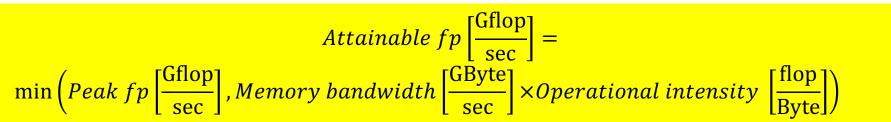
VTune can show you the "roofline" of your application

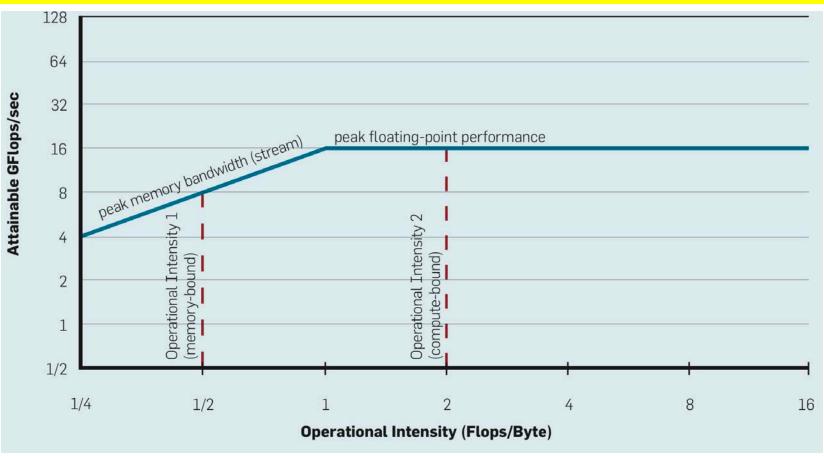
- Off-chip memory bandwidth (from DRAM) is critical for performance (to feed enough data to be operated)
- Operational intensity: Operations per byte of DRAM traffic
- Roofline model: Predicts the floating-point (fp) performance from operation intensity, theoretical peak fp performance & peak memory bandwidth

$$Attainable fp\ performance\ \left[\frac{\text{Gflop}}{\text{sec}}\right] = \\ min \left(\begin{array}{c} Peak\ fp\ performance\ \left[\frac{\text{Gflop}}{\text{sec}}\right],\\ Peak\ memory\ bandwidth\ \left[\frac{\text{GByte}}{\text{sec}}\right] \times Operational\ intensity\ \left[\frac{\text{flop}}{\text{Byte}}\right] \right) \\ \end{array}$$

S. Williams *et al.*, <u>Commun. ACM **52(4)**</u>, 65 ('09) V. Elango *et al.*, <u>ACM. T. Arch. Code Opt. **11**</u>, 67 ('15)

Roofline Model of Performance





Key: Data/computation locality

see Berkeley CS267 lecture on "memory hierarchies & matrix multiplication"