# Pair Distribution Computation on GPU

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Goal: Using multidimensional Grid & Block

See B. G. Levine et al., J. Comput. Phys. 230, 3556 (2011)

https://aiichironakano.github.io/cs596/Levin-RDFonGPU-JCP11.pdf

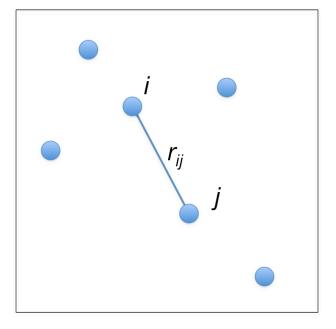


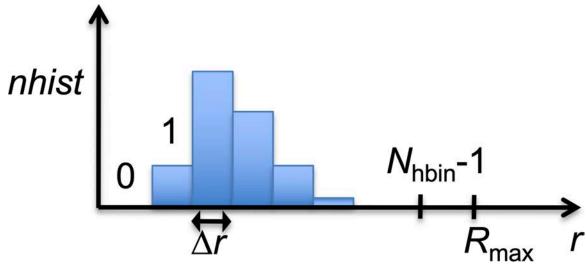


### **Pair Distribution**

• Pair-distance histogram, nhist[Nhbin]

```
for all histogram bins i nhist[i] = 0 for all atomic pairs (i,j) ++nhist[\lfloor |\vec{r}_{ij}|/\Delta r \rfloor] count
```





### **Pair Distribution Function**

### • Pair-distribution function, g(r)

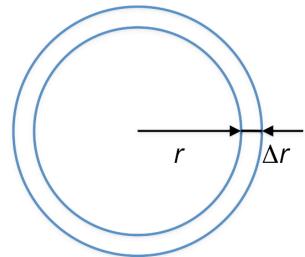
$$g(r_i) = \frac{nhist(i)}{2\pi r_i^2 \Delta r \rho N} N: \text{# of atoms} \\ \rho: \text{# density}$$

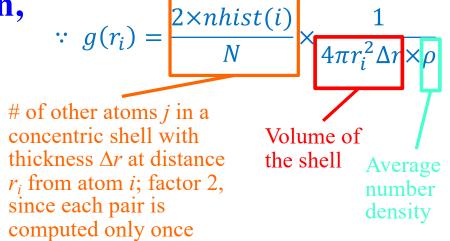
g(r): For each atom, how many other atoms are distance r apart, normalized by # of atoms expected from average density; deviation from 1 signifies correlation with an atom at r = 0

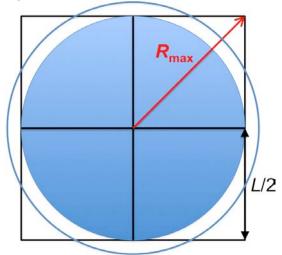
#### With minimum-image convention,

$$R_{\text{max}} = \sqrt{\sum_{\alpha = x, y, z} \left(\frac{\text{al}[\alpha]}{2}\right)^2}$$

$$\Delta r = R_{\text{max}}/N_{\text{hbin}}; r_i = (i+1/2)\Delta r$$







### Big Loops over Atomic Pairs

input: r[], n Program: pdf0.c (atomic positions in pos.d)

#### output: nhis[]

- n: Number of atoms
- r[3\*n]: r[3\*i|3\*i+1|3\*i+2] is the xlylz coordinate of the i-th atom
- alth[a] = al[a]/2: Half the simulation box lengths

```
float SignR(float v, float x) {if (x > 0) return v; else return -v;}
```

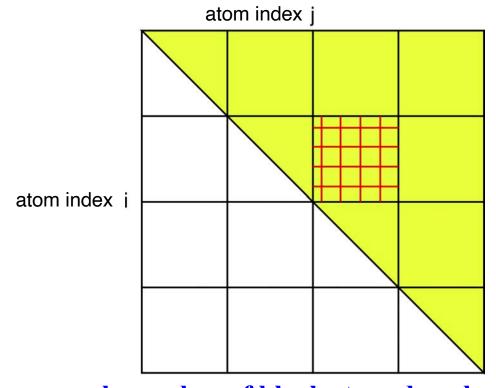
### Variables in Device Memory

```
constant float DALTH[3];
                              In read-only constant memory
             int DN;
 constant
 constant float DDRH;
float* dev r;
               // Atomic positions
float* dev nhis; // Histogram
cudaMalloc((void**)&dev r,sizeof(float)*3*n);
cudaMalloc((void**)&dev nhis,sizeof(float)*NHBIN);
cudaMemcpy(dev r,r,3*n*sizeof(float),cudaMemcpyHostToDevice);
cudaMemset(dev_nhis,0.0,NHBIN*sizeof(float));
cudaMemcpyToSymbol(DALTH, alth, sizeof(float)*3,0,cudaMemcpyHostToDevice);
cudaMemcpyToSymbol(DN,&n,sizeof(int),0,cudaMemcpyHostToDevice);
cudaMemcpyToSymbol(DDRH, &drh, sizeof(float), 0, cudaMemcpyHostToDevice);
// Compute dev nhis on GPU: dev r[] -> dev nhis[]
cudaMemcpy(nhis,dev nhis,NHBIN*sizeof(float),cudaMemcpyDeviceToHost);
                                   Grid
cudaFree(dev r);
cudaFree(dev nhis);
                                   Block (0, 0)
                                                     Block (1, 0)
cudaMemcpyToSymbol:
                                      Shared Memory
                                                        Shared Memory
 Destination (in device) is either an
 address or variable name
 Memory offset (in bytes) is added to
 destination
                           Host
                                   Global Memory
                                                      1. dev nhis[1
         r[], nhis[], alth[], n, drh
```

### Who Does What: Nested Decompositions

- Nested block & thread decompositions
  - > Spatial decomposition among blocks
  - > Loop-index interleaving among threads within each block

```
In host program:
```

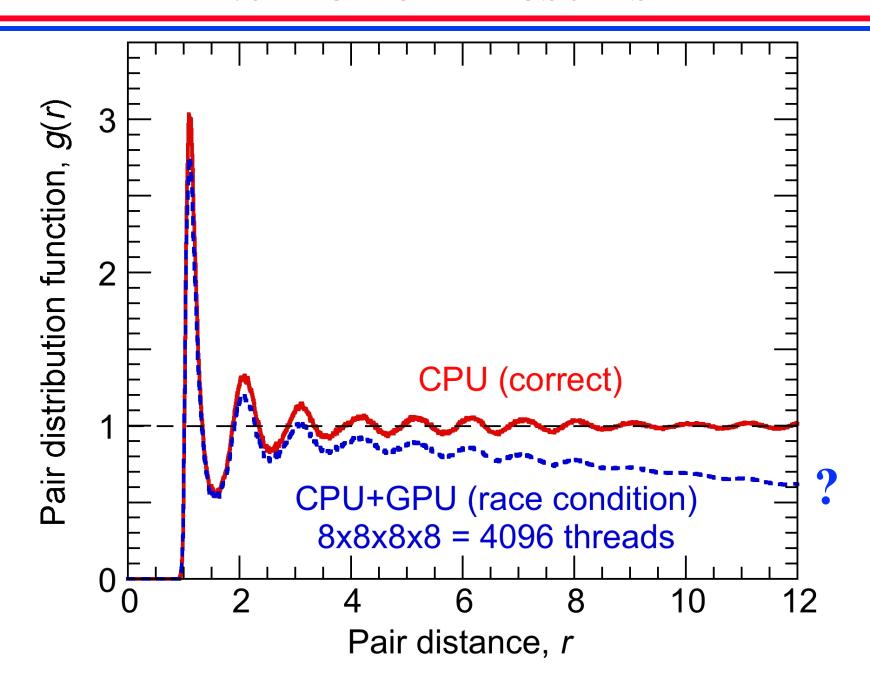


• Use a large enough number of blocks to reduce load imbalance among streaming multiprocessors (SMs)

# **Device Program for Histogram**

```
device float d SignR(float v, float x) {if (x > 0) return v; else return -v;}
       This is only called from the device program
global void gpu histogram kernel(float *r,float *nhis) {
int iBlockBegin = (DN/gridDim.x)*blockIdx.x;
int iBlockEnd = (DN/gridDim.x)*(blockIdx.x+1);
if (blockIdx.x == gridDim.x-1) iBlockEnd = DN;
int jBlockBegin = (DN/gridDim.y)*blockIdx.y;
int jBlockEnd = (DN/gridDim.y)*(blockIdx.y+1);
if (blockIdx.y == gridDim.y-1) jBlockEnd = DN;
for (i=iBlockBegin+threadIdx.x; i<iBlockEnd; i+=blockDim.x) {</pre>
  for (j=jBlockBegin+threadIdx.y; j<jBlockEnd; j+=blockDim.y) {</pre>
    if (i<j) {
      // Process (i,j) atom pair
      rij = 0.0;
                               Thread interleaving
                               by skipping indices
      nhis[ih] += 1.0;
    } // end if i<j
                        Block spatial decomposition
  } // end for j
                        via index offset
} // end for i
```

### **Numerical Results**



### **Race Condition**

#### We just "saw" race condition in action!

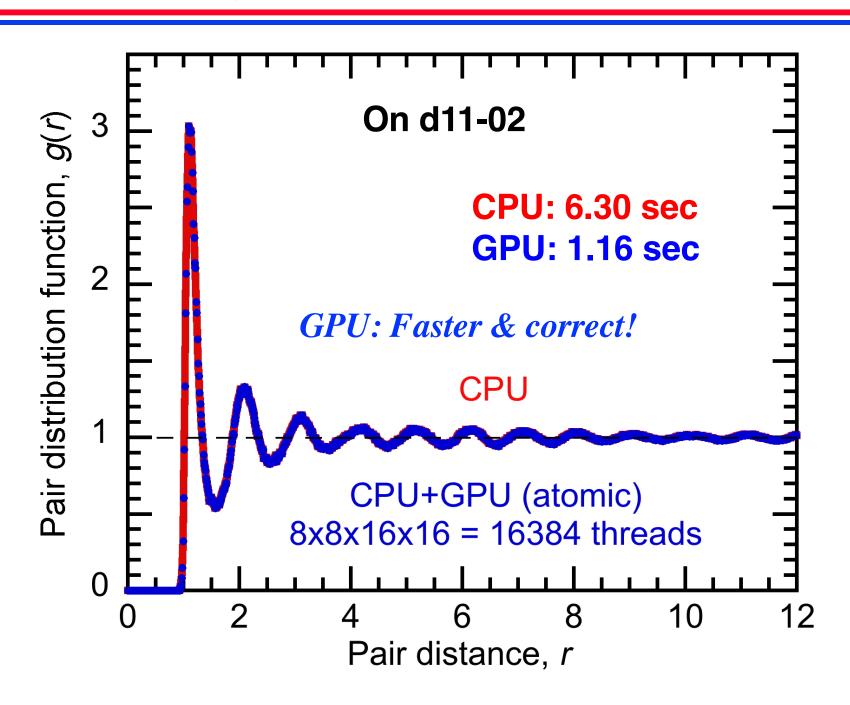
```
for (i=iBlockBegin+threadIdx.x; i<iBlockEnd; i+=blockDim.x) {</pre>
  for (j=jBlockBegin+threadIdx.y; j<jBlockEnd; j+=blockDim.y) {</pre>
    if (i<j) {
      rij = 0.0;
      for (a=0; a<3; a++) {
        dr = r[3*i+a]-r[3*j+a];
        /* Periodic boundary condition */
        dr = dr-d SignR(DALTH[a], dr-DALTH[a])-d SignR(DALTH[a], dr+DALTH[a]);
        rij += dr*dr;
      rij = sqrt(rij); /* Pair distance */
      ih = rij/DDRH;
      nhis[ih] += 1.0; /* Entry to the histogram */
    } // end if i<i/
  } // end for j
} // end for i
```

 In newer versions of CUDA, use atomic update atomicAdd(&nhis[ih],1.0);

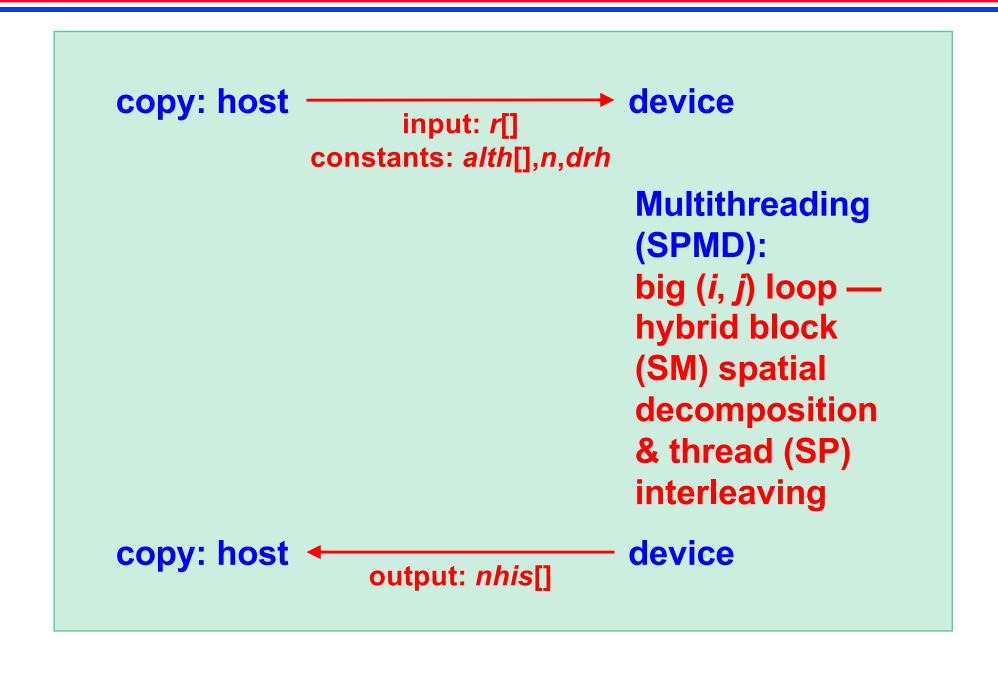
### Running CPU & GPU Versions at HPC

```
Script
#!/bin/bash
#SBATCH --nodes=1
#SBATCH --ntasks-per-node=1
#SBATCH -- gres = gpu: 1
#SBATCH --time=00:00:59
#SBATCH --output=pdf.out
#SBATCH -A anakano 429
echo '##### CPU: gcc -o pdf0 pdf0.c -lm #####'
./pdf0
echo '##### GPU: nvcc -o pdf pdf.cu #####'
./pdf
Output
##### CPU: gcc -o pdf0 pdf0.c -lm #####
Execution time (s) = 6.300000e+00
##### GPU: nvcc -o pdf pdf.cu #####
Execution time (s) = 1.160000e+00
```

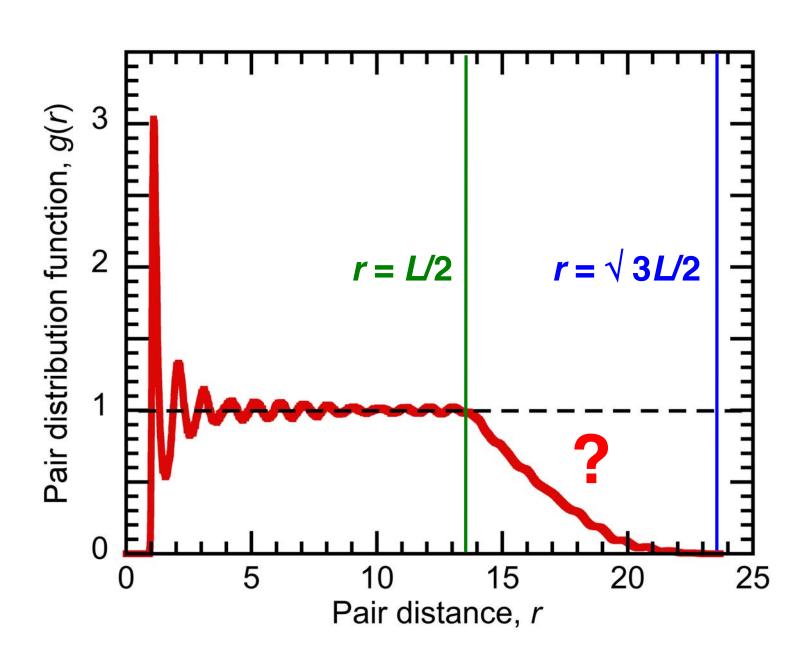
### **Numerical Results**



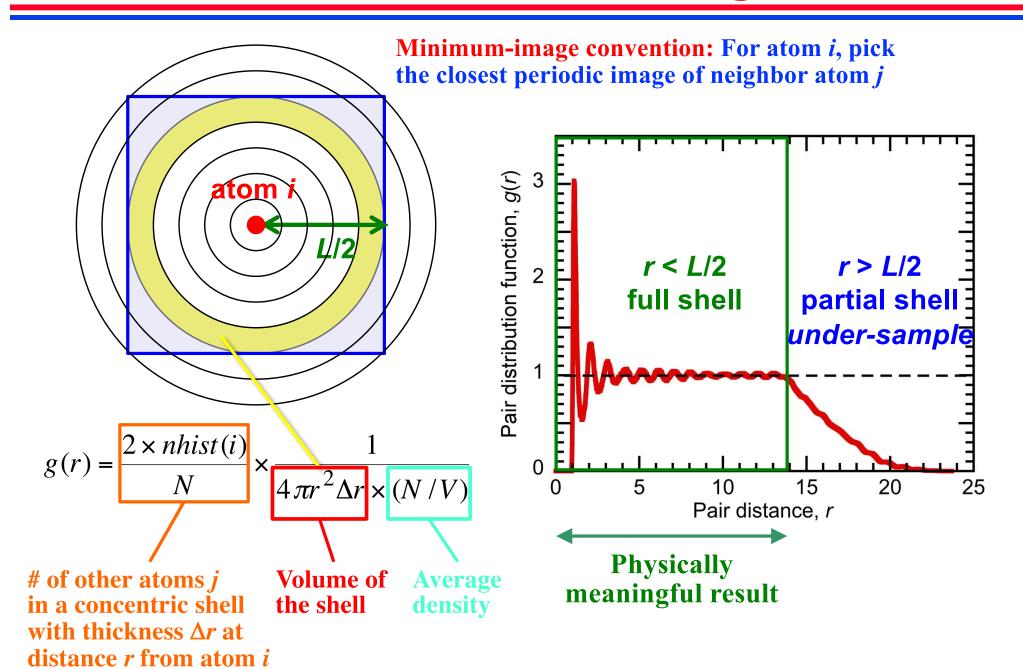
### **Summary: CUDA Pair-Distribution Computing**



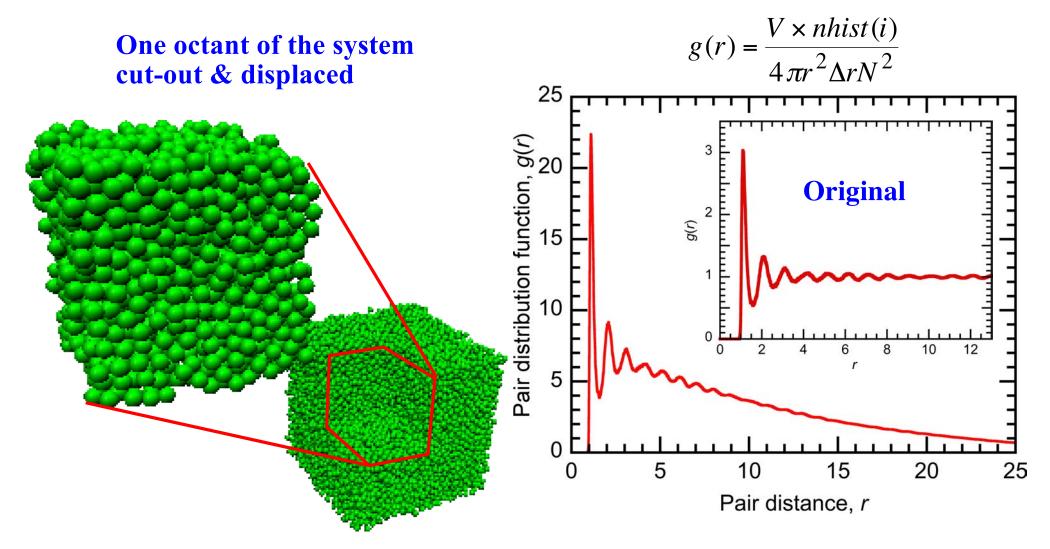
### Finite-Size Effect on g(r)



# Geometric Factor in g(r)



# Large-scale Correlation in g(r)



- Short-range correlation (i.e. peak positions) unchanged, just magnified by the lower average density,  $N/V_{\rm expanded}$
- Superimposed with larger length-scale geometric factors

# **Experimental Connection**

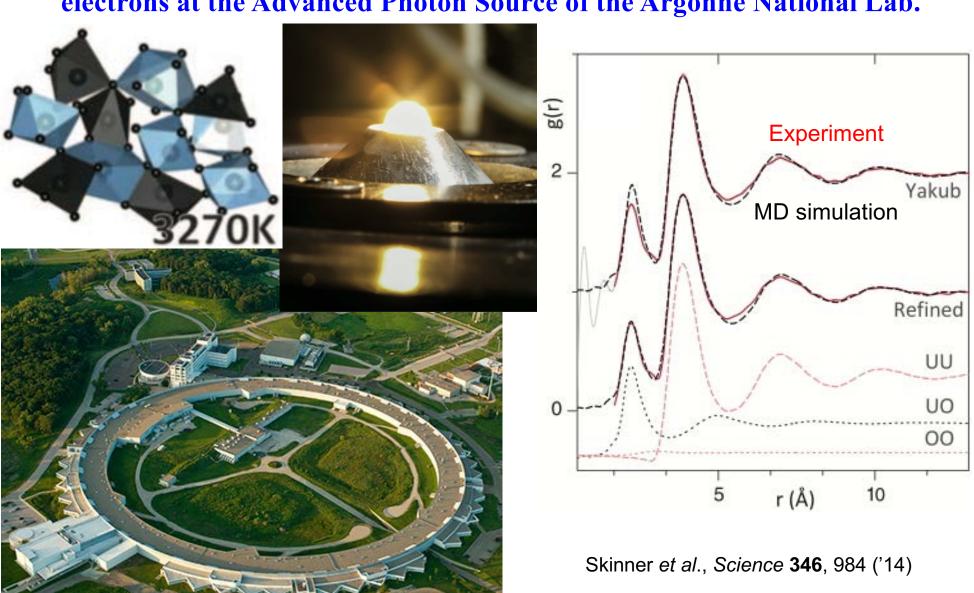
Short-range correlations are directly compared with neutron or X-ray scattering measurements of the structure factor S(q) $S(q) = 1 + 4\pi \frac{N}{V} \int_{V}^{\infty} dr r^2 \frac{\sin(qr)}{r^2} [g(r) - 1]$ Attenuated transmitted Incident beam 2 Amorphous silica Wave vector: 100  $0.1 \text{ g/cm}^3$  $0.4 \text{ g/cm}^3$  $0.8 \, \text{g/cm}^3$  $1.5 \, \text{g/cm}^3$ 100 MD (Nakano et al., JNCS 171, 157, '94) r (Å) Exp't (Johnson et al., JNCS 58, 109, '83) 1000 orous silica 15 10 20  $q(\mathring{A}^{-1})$ 100 S(q) $S(q) \propto q^{-d_{\rm f}}$ **Long-range correlations are** measured by small-angle  $d_{\rm f}$ : Fractal neutron or X-ray scattering dimension structure factors (SANS or 0.01 0.1 SAXS)

Nakano et al., PRL 71, 85 ('93); PRB 49, 9441 ('94)

q (Å-1)

# g(r) of Molten $UO_2$

• X-ray scattering measurement using synchrotron radiation from 7 GeV electrons at the Advanced Photon Source of the Argonne National Lab.



### More Pair-Distribution Computation

<u>Use the force!</u> Reduced variance estimators for densities, radial distribution functions, and local mobilities in molecular simulations •

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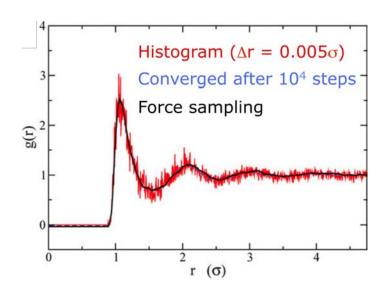




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https://aiichironakano.github.io/cs596/Rotenberg-UseTheForce-JCP20.pdf