

TABLE II  
Integration of a Single Gaussian in Nine Dimensions<sup>a</sup>

VEGAS					
Iteration	Per iteration		Cumulative		No. of integrand evaluations
	$I_i$	$\sigma_i$	$I$	$\sigma_I$	
1	0.007	0.005	0.007	0.005	$10^4$
3	0.643	0.070	0.612	0.064	$3 \times 10^4$
5	1.009	0.041	0.963	0.034	$5 \times 10^4$
10	1.003	0.008	1.001	0.005	$10^5$
Crude Monte Carlo			0.843	0.360	$10^5$

  

Gauss-Legendre Integration			
No. of points/axis	Integral	No. of integrand evaluations	
5	71.364	$2.0 \times 10^6$	
6	0.017	$1.0 \times 10^7$	
10	0.774	$10^9$	
15	1.002	$3.8 \times 10^{10}$	

<sup>a</sup> The exact result is 1.

TABLE III  
Integration of a Double Gaussian in  $n$  Dimensions<sup>a</sup>

	VEGAS				
	$n = 2$	$n = 4$	$n = 7$	$n = 7$	$n = 9$
No. function evaluations/iteration	20,000	20,000	32,000	160,000	100,000
No. increments/axis	50	50	50	50	50
Optimal standard deviation	0.007	0.02	0.05	0.02	0.06
Cumulative result after 15 iterations	0.999	1.003	1.015	0.991	0.96
	$\pm 0.002$	$\pm 0.006$	$\pm 0.015$	$\pm 0.007$	$\pm 0.04$

  

	SHEP				
	$n = 2$	$n = 4$	$n = 7$	$n = 7$	$n = 9$
No. function evaluations/iteration	20,000	20,000	32,768	170,000	3,906,250
No. increments/axis	100	10	4	5	5
Optimal standard deviation	0.0008	0.03	$1.0^b$	0.25	$***$
Cumulative result after 15 iterations	1.0001	1.004	*	0.90	**
	$\pm 0.0002$	$\pm 0.008$	*	$\pm 0.04$	**

<sup>a</sup> The exact result is 1.

<sup>b</sup> Algorithm would not converge.

<sup>c</sup> Too large to be tried.