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AI5002 - Assignment 1

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Download code and LaTeX from below hyperlinks

- 1. Codes/RayleighDist CDF PDf Plot.py
- 2. LaTeX

Problem 6.1.4

Find an expression for $F_A(x)$ using the definition. Plot this expression and compare with the result of problem 6.1.3

Solution

Given,

$$A = \sqrt{V} \tag{0.0.1}$$

$$F_A(x) = P (A \le x)$$
 (0.0.2)

$$F_A(x) = P (\sqrt{V} \le x)$$
 (0.0.3)

$$F_A(x) = P (V \le x^2)$$
 (0.0.4)

$$F_A(x) = F_V(x^2)$$
 (0.0.5)

From (6.1.2.1) we get

$$\mathsf{F}_V(x) \ = \ \left\{ 1 \ - \ e^{-\alpha x} \qquad ; \ x \geq 0 \right.$$

Now for x^2 , we substitute x^2 in place of x

$$F_V(x^2) = \begin{cases} 1 - e^{-\alpha x^2} & ; \ x^2 \ge 0 \end{cases}$$
 (0.0.6)

Putting
$$\alpha = \frac{1}{2\sigma^2} = \frac{1}{2}$$
 [: σ^2 is given as 1]

We get,

$$F_V(x^2) = 1 - e^{\frac{-x^2}{2}} \quad ; \ x^2 \ge 0$$
 (0.0.7)

Thus the CDF is derived as

$$F_A(x) = F_V(x^2) = 1 - e^{\frac{-x^2}{2}}$$
 ; $x^2 \ge 0$

Problem 6.1.5

Find an expression for $p_A(x)$ using the definition.

Solution

The PDf can be derived by differentiating the CDF expression from the previous problem 6.1.4

$$f_A(x) = f_V(x^2)$$
 (0.0.8)

$$f_V(x^2) = \frac{d}{dx}(F_V(x^2))$$
 (0.0.9)

$$f_V(x^2) = \frac{d}{dx}(1 - e^{\frac{-x^2}{2}})$$
 (0.0.10)

$$f_V(x^2) = e^{\frac{-x^2}{2}}.x$$
 (0.0.11)

$$p_A(x) = f_A(x) = e^{\frac{-x^2}{2}}.x$$