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AI5002 - Assignment 5

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Download code and LaTeX from below hyperlinks

- 1. Codes/MiscellaneousDistributions 5 31.py
- 2. LaTeX

Problem 5.31

Two cards are drawn simultaneously (or successively without replacement) from a well shuffled pack of 52 cards. Find the mean, variance and standard deviation of the number of kings.

Solution

Let X be a random variable.

X = Number of kings present in the two cards drawn from a well shuffled pack of 52 cards.

The values that X can have are $= \{0, 1, 2\}$. The probability of X taking each of the above values are -

$$P(X=0) = \frac{\binom{48}{2}}{\binom{52}{2}} = \frac{188}{221} \approx 0.851$$
 (0.0.1)

$$P(X=1) = \frac{\binom{4}{1} * \binom{48}{1}}{\binom{52}{2}} = \frac{32}{221} \approx 0.145 \qquad (0.0.2)$$

$$P(X = 2) = \frac{\binom{4}{2}}{\binom{52}{2}} = \frac{1}{221} \approx 0.004$$
 (0.0.3)

The Mean calculated as E(X) is given by,

$$E(X) = \sum X.P(X)$$
 (0.0.4)
= 0 * $\frac{188}{221}$ + 1 * $\frac{32}{221}$ + 2 * $\frac{1}{221}$

$$= \frac{34}{221} \approx 0.154$$

$$E(X^2) = \sum X^2 . P(X)$$

$$= 0^2 * \frac{188}{221} + 1^2 * \frac{32}{221} + 2^2 * \frac{1}{221} = \frac{36}{221}$$

The Variance calculated as Var(X)is given by,

$$Var(X) = E(X^2) - [E(X)]^2$$
 (0.0.5)

$$=\frac{36}{221} - \left[\frac{34}{221}\right]^2 = \frac{6800}{48841} \approx 0.139$$

The Standard-Deviation calculated as SD(X) is given by,

$$SD(X) = \sqrt{Var(X)} = \sqrt{0.139} \approx 0.373$$
 (0.0.6)

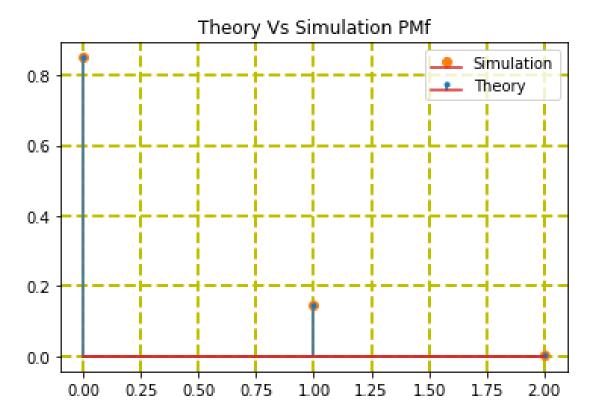


Fig 1.1: Theory Vs Simulation of PMf

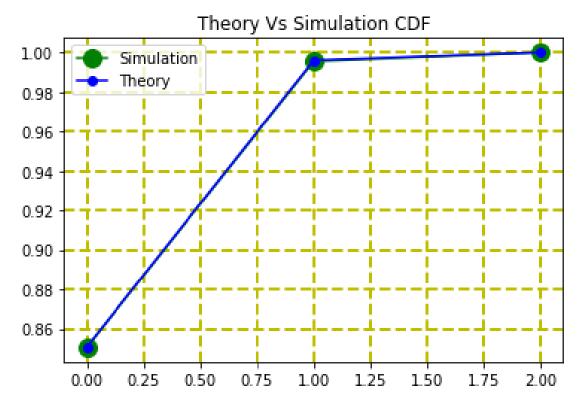


Fig 1.2: Theory Vs Simulation CDF