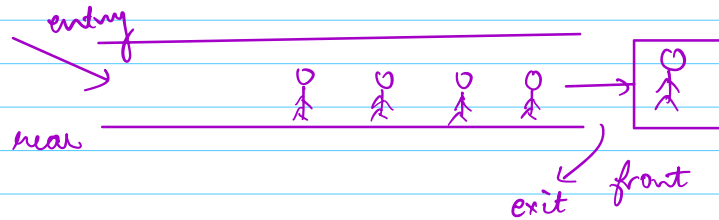


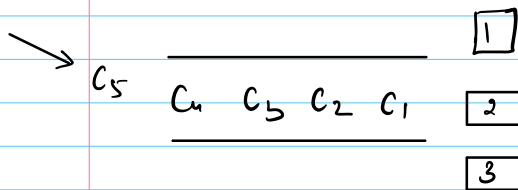
16/1/2024

Queue



customer care

First In First Out



operations

- 1) Enqueue(x) \rightarrow Insert x from rear end.
- 2) Dequeue() \rightarrow remove data from front end
- 3) isEmpty() \rightarrow checks if Q is empty
- 4) Front() \rightarrow get data at front end
- 5) Rear() \rightarrow get data at rear end.

Tc: OCV

Q Implement queue using array.

enqueue(3) ✓

enqueue(5) ✓

enqueue(8) ✓

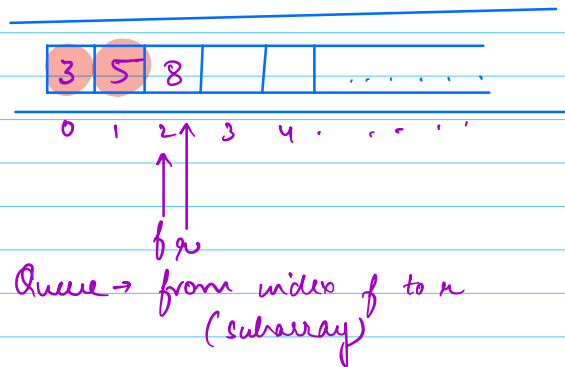
dequeue() → 3

isEmpty() → false

front() → 5

dequeue() → 5

rear() → 8



~~$f = 0$~~
 ~~$r = 0$~~

```
void enqueue(x) {  
    r++;  
    A[r] = x;  
}
```

// overflow → 1) Use dynamic array.
2) Do not insert more than size

```
int dequeue() {  
    if (isEmpty())  
        return -1;  
    f++;  
    return A[f-1];  
}
```

```
boolean isEmpty() {  
    return f > r;  
}
```

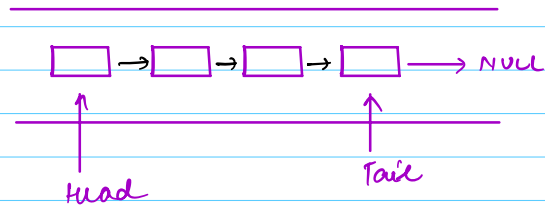
```
int front() {  
    if (isEmpty())  
        return -1;  
    return A[f];  
}
```

```
int rear() {  
    if (isEmpty())  
        return -1;  
    return A[r];  
}
```

✓ O(1)

Q Implement queue using linked list.

TC:	<u>Insertion</u>	<u>Removal</u>
Head	$O(1)$	$O(1)$
Tail	$O(1)$	$O(N)$

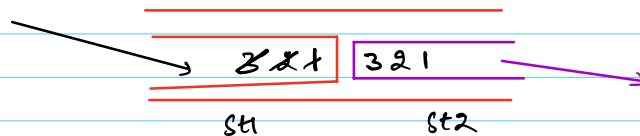
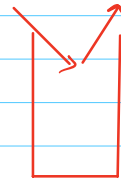


enqueue(x) \rightarrow insert at tail
dequeue() \rightarrow removal of head
isEmpty() \rightarrow head == null
front() \rightarrow head.data
rear() \rightarrow tail.data

Q Implement queue using 2 stacks

$\left. \begin{array}{l} \text{enqueue}(x) \\ \text{dequeue}() \\ \text{isEmpty}() \end{array} \right\} O(1)$

$\rightarrow \text{push}(x)$
 $\rightarrow \text{pop}()$
 $\rightarrow \text{isEmpty}()$



$\text{enqueue}(1)$
 $\text{enqueue}(2)$
 $\text{enqueue}(3)$
 $\text{dequeue}()$
 $\text{enqueue}(4)$
 $\text{enqueue}(5)$

```
void enqueue(x) {
    st1.push(x);
}
```

```
void move() {
    while (!st1.isEmpty()) {
        st2.push(st1.pop());
    }
}
```

```
int dequeue() {
    if (isEmpty())
        return -1;
```

```
    if (st2.isEmpty())
        move();
```

```
    return st2.pop();
```

```
}
```

```
boolean isEmpty() {
    return st1.isEmpty()
        && st2.isEmpty();
}
```

amortized TC

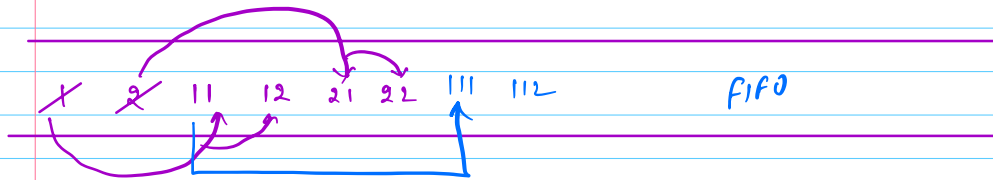
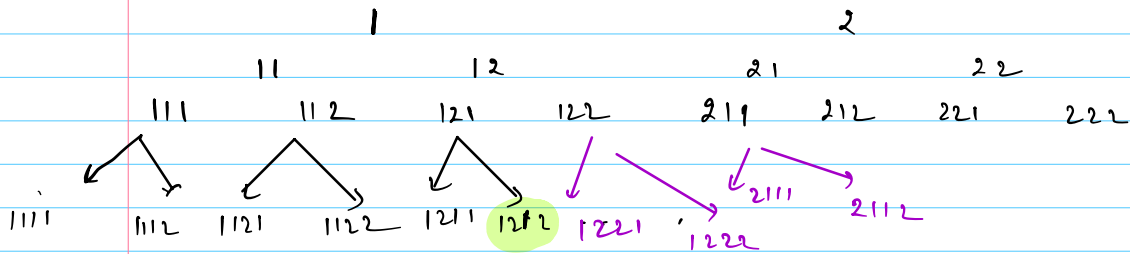
If TC of move() = $O(N)$ \rightarrow next K dequeue() will have TC: $O(1)$

$\hookrightarrow O(2) \approx O(1)$

Met at 8:30 am IST

Q Given an integer N , find N^{th} number that can be formed by digits 1 & 2 only.

<u>N</u>	1	2	3	4	5	6	7	8	...
<u>No</u>	1	2	11	12	21	22	111	112	121 122



$$\begin{aligned}
 x &\rightarrow x * 10 + 1 \\
 &\rightarrow x * 10 + 2
 \end{aligned}$$

mit getNth No (mit N) {

if (N <= 2) return N;

q.enqueue(1); q.enqueue(2)

N = 10

i = 3

while (i <= N) {

x = q.dequeue();

~~1, 2, 1, 2~~, 21, 22 111 112

a = x * 10 + 1;

b = x * 10 + 2;

i = 3

x = ~~1, 2, 1, 2~~ 12

if (i == N) return a;

5

a = ~~11 21 112~~ 121

if (i + 1 == N) return b;

7

b = ~~12 22 112~~ 122

9

q.enqueue(a);

q.enqueue(b);

Tc: O(N)

i += 2;

Sc: O(N)

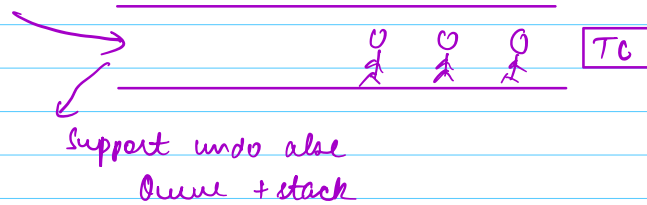
}

return -1;

}

Doubly ended Queue (deque)

- 1> enqueueFront(x)
- 2> enqueueRear(x)
- 3> dequeueFront()
- 4> dequeueRear()
- 5> isEmpty()

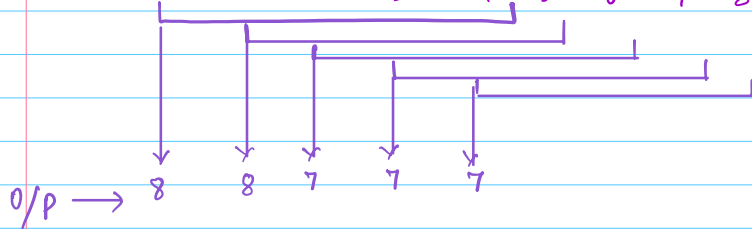


Tc: $O(1)$ #operations.

Q Given an integer array & an integer k.
Find the max element of subarray of size k.

sliding window.

$A = [1, 8, 5, 6, 7, 4, 2, 0, 3]$ $k=5$



$A = [1, 8, 5, 6, 7, 4, 2, 0, 3]$ $k=4$

~~0 1 2 3 4 5 6 7 8~~

l, r
2, 5
~~3~~, 6
4, 7
5, 8

store data \rightarrow index

Tc: $O(N)$
Sc: $O(K)$

remove invalid index () {

}

sliding window + deque

Queue <Integer> q = new Deque();

Deque <Integer> q.

Coding thru Interfaces