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In[15]:= Clear["Global`*"]

(* Initial Conditions *)
 $\bar{x}_0 = 0$ ; (*Initial x-position*)
 $\dot{x}_0 = 6$ ; (*Initial x-velocity*)
 $\bar{y}_0 = 18$ ; (*Initial y-position*)
 $\dot{y}_0 = 20$ ; (*Initial y-velocity*)
g = 9.81; (*Acceleration due to gravity*)
 $\theta_0 = \frac{\pi}{2}$ ; (*Initial angle*)
 $\dot{\theta}_0 = .9\pi$ ; (*Initial angular velocity,e.g.,rad/s*)
L = 20;

(*COM Position Equations*)
xposition[t_] :=  $\bar{x}_0 t + \dot{x}_0$ 
yposition[t_] := -(1/2) g * t^2 +  $\dot{y}_0 t + \bar{y}_0$ 
θposition[t_] :=  $\dot{\theta}_0 t + \theta_0$ 
(*COM Velocity Equations*)
xvelocity[t_] := xposition'[t]
yvelocity[t_] := yposition'[t]
θvelocity[t_] := θposition'[t]
(*COM Position Equations*)
xaccel[t_] := xposition''[t]
yaccel[t_] := yposition''[t]
θaccel[t_] := θposition''[t]

(* Link Tip Coordinates*)
yatip[t_] := yposition[t] + (L/2) * Sin[θposition[t]]
ybtip[t_] := yposition[t] - (L/2) * Sin[θposition[t]]
xatip[t_] := xposition[t] + (L/2) * Cos[θposition[t]]
xbtip[t_] := xposition[t] - (L/2) * Cos[θposition[t]]

In[37]:= (*---Find the Time of A Tip Impact---*)
impactSolutionA = FindRoot[yatip[t] == 0, {t, 4}];
impactTimeA = t /. impactSolutionA;
impactPointA = {xatip[impactTimeA], 0};

(*---Find the Time of B Tip Impact---*)
impactSolutionB = FindRoot[ybtip[t] == 0, {t, 4}];
impactTimeB = t /. impactSolutionB;
impactPointB = {xbtip[impactTimeB], 0};

(*-----What Tip Hit First-----*)
If[impactTimeB > impactTimeA,
  {impactTimeFirst = impactTimeA, impactPointFirst = impactPointA, firstTip = "A"},


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{impactTimeFirst = impactTimeB, impactPointFirst = impactPointB, firstTip = "B"}
];

Print["Tip ", firstTip, " hits the ground first at t = ", impactTimeB, " seconds."];
Print["Impact location: ", impactPointFirst];
Print["Center of Mass Parameters: "];
Print["COM Coordinates: ", impactPointFirst];
Print["Impact angle: ", eposition[impactTimeFirst]];
Print["Impact Velocities: x-velocity: ", xvelocity[impactTimeFirst], " y-velocity: ",
yvelocity[impactTimeFirst], " e-velocity: ", evelocity[impactTimeFirst]];

(*-----Animation-----*)
Manipulate[
Graphics[
{(*Objects to Draw*)

(*1. The Trajectory of the Center of Mass*)
{Dashed, Black,
ParametricPlot[{xposition[tau], yposition[tau]}, {tau, 0, t}, PlotStyle -> Yellow][[1]]}, 

(*2. The Link Itself*)
{White, Thickness[0.012],
Line[{{xatip[t], yatip[t]}, {xbtip[t], ybtip[t]}}]}, 

(*3. The Tips and COM points*)
{PointSize[0.020],
Green, Point[{xatip[t], yatip[t]}], Red, Point[{xbtip[t], ybtip[t]}],
Black, Point[{xposition[t], yposition[t]}]}, 

(*4. The Impact Markers (appears only after impact) *)
If[t > impactTimeFirst,
If[firstTip == "A",
{PointSize[0.015], Green, Point[impactPointFirst]}, (*Use Green for Tip A*)
{PointSize[0.015], Red, Point[impactPointFirst]} (*Use Red for Tip B*)]
]
],
},
(*Graphics Options*)
PlotRange -> {{0, 65}, {-20, 75}},
Axes -> True, AxesLabel -> {"x (m)", "y (m)" },
GridLines -> Automatic, ImageSize -> Medium, AspectRatio -> Automatic
],
(*Animation Controls*)
{{t, 0, "Time (s)"}, 0, 5.5, 0.01, Animator}
]
]

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Tip B hits the ground first at $t = 4.44444$ seconds.

Impact location: {26.6667, 0}

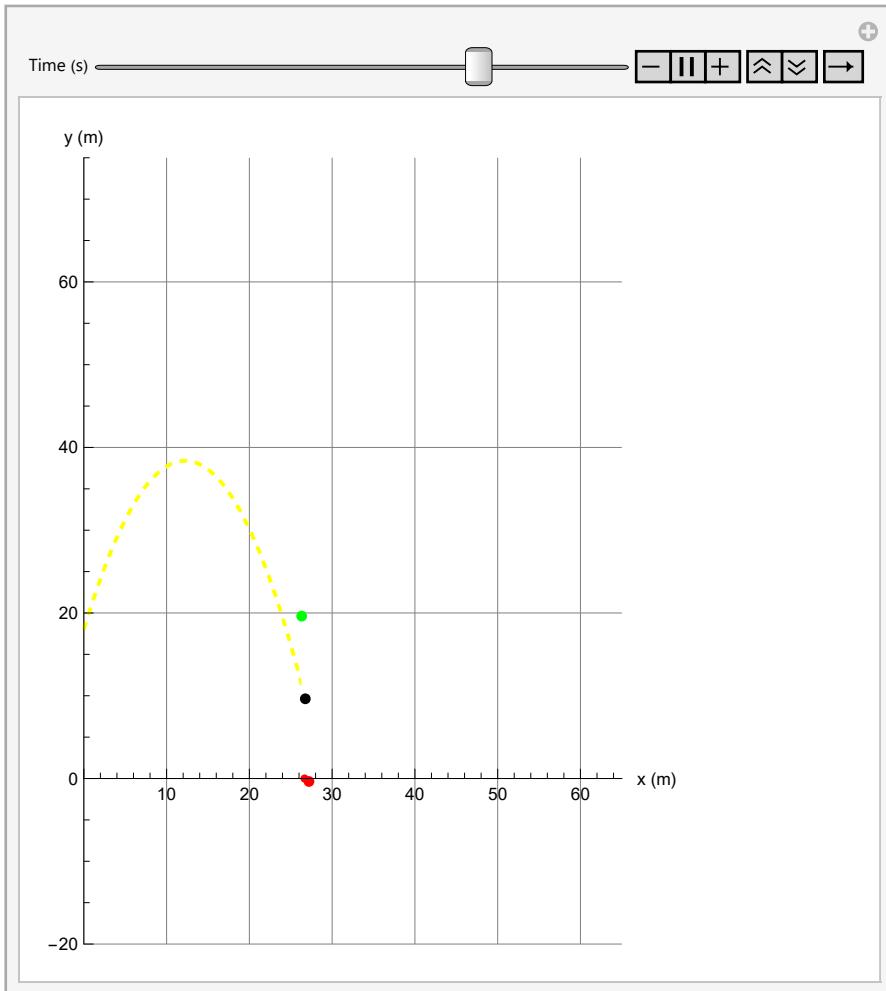
Center of Mass Parameters:

COM Coordinates: {26.6667, 0}

Impact angle: 14.1372

Impact Velocities: x-velocity: 6 y-velocity: -23.6 θ-velocity: 2.82743

Out[50]=



In[51]:=