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In[15]:= Clear["Global`*"]
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(* Initial Conditions *)
 $\bar{x}_0 = 0;$           (*Initial x-position*)
 $\dot{\bar{x}}_0 = 6;$        (*Initial x-velocity*)
 $\bar{y}_0 = 18;$        (*Initial y-position*)
 $\dot{\bar{y}}_0 = 20;$      (*Initial y-velocity*)
 $g = 9.81;$         (*Acceleration due to gravity*)
 $\theta_0 = \text{Pi} / 2;$  (*Initial angle*)
 $\dot{\theta}_0 = .9 * \text{Pi};$  (*Initial angular velocity,e.g.,rad/s*)
 $L = 20;$ 
```

```
(*COM Position Equations*)
xposition[t_] :=  $\dot{\bar{x}}_0 t + \bar{x}_0$ 
yposition[t_] :=  $-(1/2) g * t^2 + \dot{\bar{y}}_0 t + \bar{y}_0$ 
 $\theta$ position[t_] :=  $\dot{\theta}_0 t + \theta_0$ 
(*COM Velocity Equations*)
xvelocity[t_] := xposition'[t]
yvelocity[t_] := yposition'[t]
 $\theta$ velocity[t_] :=  $\theta$ position'[t]
(*COM Position Equations*)
xaccel[t_] := xposition''[t]
yaccel[t_] := yposition''[t]
 $\theta$ accel[t_] :=  $\theta$ position''[t]
```

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(* Link Tip Coordinates*)
 $y_{atip}[t_] := yposition[t] + (L/2) * \text{Sin}[\theta position[t]]$ 
 $y_{btip}[t_] := yposition[t] - (L/2) * \text{Sin}[\theta position[t]]$ 
 $x_{atip}[t_] := xposition[t] + (L/2) * \text{Cos}[\theta position[t]]$ 
 $x_{btip}[t_] := xposition[t] - (L/2) * \text{Cos}[\theta position[t]]$ 
```

```
In[37]:= (*---Find the Time of A Tip Impact---*)
impactSolutionA = FindRoot[ $y_{atip}[t] == 0$ , {t, 4}];
impactTimeA = t /. impactSolutionA;
impactPointA = { $x_{atip}[impactTimeA]$ , 0};
```

```
(*---Find the Time of B Tip Impact---*)
impactSolutionB = FindRoot[ $y_{btip}[t] == 0$ , {t, 4}];
impactTimeB = t /. impactSolutionB;
impactPointB = { $x_{btip}[impactTimeB]$ , 0};
```

```
(*-----What Tip Hit First-----*)
If[impactTimeB > impactTimeA,
  {impactTimeFirst = impactTimeA, impactPointFirst = impactPointA, firstTip = "A"},
```

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    {impactTimeFirst = impactTimeB, impactPointFirst = impactPointB, firstTip = "B"}
];

Print["Tip ", firstTip, " hits the ground first at t = ", impactTimeB, " seconds."];
Print["Impact location: ", impactPointFirst];
Print["Center of Mass Parameters: "];
Print["COM Coordinates: ", impactPointFirst];
Print["Impact angle: ",  $\theta$ position[impactTimeFirst]];
Print["Impact Velocities: x-velocity: ", xvelocity[impactTimeFirst], " y-velocity: ",
      yvelocity[impactTimeFirst], "  $\theta$ -velocity: ",  $\theta$ velocity[impactTimeFirst]];

(*-----Animation-----*)
Manipulate[
  Graphics[
    {(*Objects to Draw*)

      (*1. The Trajectory of the Center of Mass*)
      {Dashed, Black,
       ParametricPlot[{xposition[tau], yposition[tau]}, {tau, 0, t}, PlotStyle  $\rightarrow$  Yellow][[1]]},

      (*2. The Link Itself*)
      {White, Thickness[0.012],
       Line[{xatip[t], yatip[t]}, {xbtip[t], ybtip[t]}]}},

      (*3. The Tips and COM points*)
      {PointSize[0.020],
       Green, Point[{xatip[t], yatip[t]}], Red, Point[{xbtip[t], ybtip[t]}],
       Black, Point[{xposition[t], yposition[t]}]},

      (*4. The Impact Markers (appears only after impact)*)
      If[t  $\geq$  impactTimeFirst,
        If[firstTip == "A",
          {PointSize[0.015], Green, Point[impactPointFirst]}, (*Use Green for Tip A*)
          {PointSize[0.015], Red, Point[impactPointFirst]} (*Use Red for Tip B*)
        ]
      ]
    },

    (*Graphics Options*)
    PlotRange  $\rightarrow$  {{0, 65}, {-20, 75}},
    Axes  $\rightarrow$  True, AxesLabel  $\rightarrow$  {"x (m)", "y (m)"},
    GridLines  $\rightarrow$  Automatic, ImageSize  $\rightarrow$  Medium, AspectRatio  $\rightarrow$  Automatic
  ],

  (*Animation Controls*)
  {{t, 0, "Time (s)"}, 0, 5.5, 0.01, Animator}
]

```

Tip B hits the ground first at $t = 4.44444$ seconds.

Impact location: $\{26.6667, 0\}$

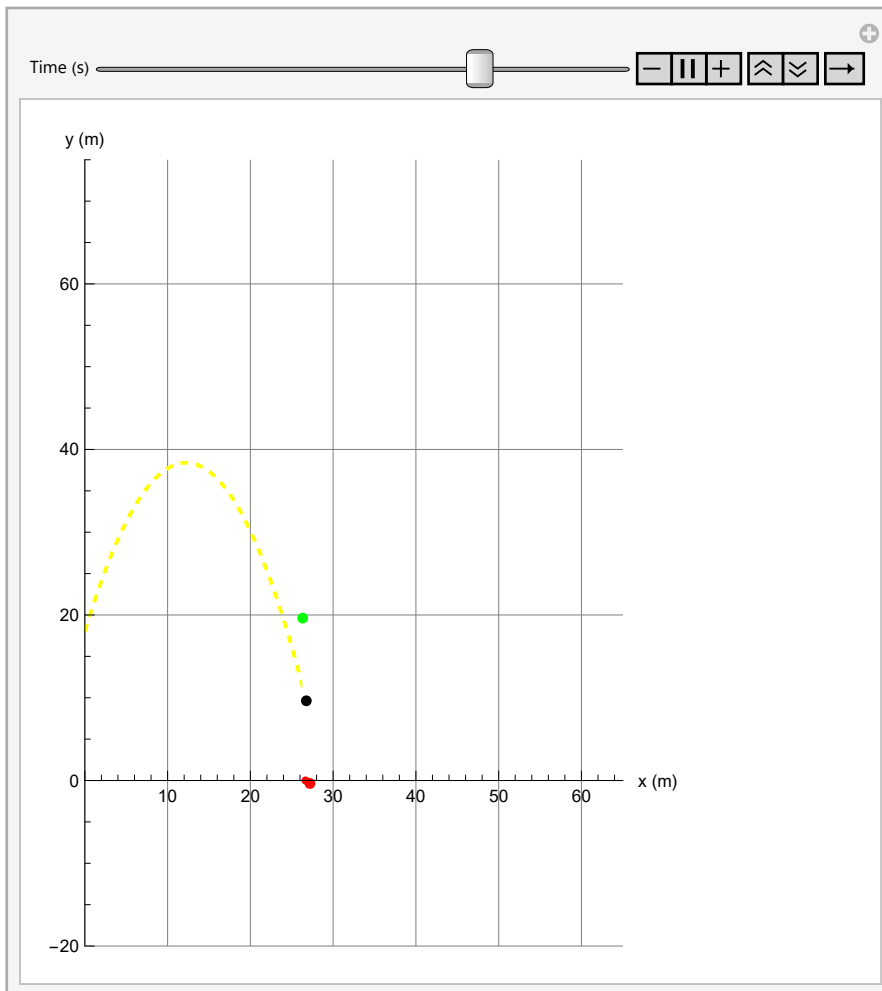
Center of Mass Parameters:

COM Coordinates: $\{26.6667, 0\}$

Impact angle: 14.1372

Impact Velocities: x-velocity: 6 y-velocity: -23.6 θ -velocity: 2.82743

Out[50]=



In[51]:=