Calculus I

Section 2.5 Homework

1) Equation (implicit function) : $5x^2 + y^2 = 12$

- a) $D_x(5x^2) = ?$
- b) $D_x(y^2) = ?$
- c) $D_x(12) = ?$

d)Implicit Differentiation Equation: ?

e)
$$y' = \frac{dy}{dx} = ?$$

2) Equation (implicit function): $\sqrt{x} + \sqrt{y} = 8$

- a) $D_x(x^{1/2}) = ?$
- b) $D_x(y^{1/2}) = ?$
- c) $D_x(8) = ?$
- d) Implicit Differentiation Equation: ?

e)
$$y' = \frac{dy}{dx} = ?$$

3) Equation (implicit function) : $2x^3 - xy + y^2 = 12$

- a) $D_x(2x^3) = ?$
- b) $D_x(-xy) = ?$ Hint: Use Product Rule
- c) $D_x(y^2) = ?$
- d) $D_x(12) = ?$
- e)Implicit Differentiation Equation: ?

$$f) y' = \frac{dy}{dx} = ?$$

4) Equation (implicit function): $4x^3 - 3x^2 \cdot y + 2x \cdot y^2 = 10$

a)
$$D_x(4x^3) = ?$$

b)
$$D_x(-3x^2 \cdot y) = ?$$
 Hint: Use Product Rule

c)
$$D_x(2x \cdot y^2) = ?$$
 Hint: Use Product Rule

d)
$$D_x(10) = ?$$

e)Implicit Differentiation Equation: ?

f)
$$y' = \frac{dy}{dx} = ?$$

5) Equation: Equation (implicit function): xy = 14

a)
$$D_x(x \cdot y) = ?$$
 Hint: Use Product Rule

b)
$$D_x(14) = ?$$

c)Implicit Differentiation Equation: ?

d)
$$y' = \frac{dy}{dx} = ?$$

$$e)y'(1, 14) = ?$$

6) Equation (implicit function): $(x + y)^3 + x^3 + y^3 = 2$

a)
$$D_x((x+y)^3) = ?$$

b)
$$D_x(x^3) = ?$$

c)
$$D_x(y^3) = ?$$

d)Implicit Differentiation Equation: ?

$$e) \ y' = \frac{dy}{dx} = ?$$

$$f)y'(0,1) = ?$$

7) Find equation of tangent line at (1, 4).

Equation: Equation (implicit function): $x \cdot y = 4$

- a) $D_x(x \cdot y) = ?$
- b) $D_x(4) = ?$
- c) Implicit Differentiation Equation: ?

$$d) y' = \frac{dy}{dx} = ?$$

- e) Slope of tangent line = y'(1,4) = ?
- f) Equation of Tangent Line:

Hint:
$$y - y_1 = m(x - x_1)$$

8) Find equation of tangent line at (0, 4).

Equation (implicit function): $(3x^2 + 2) \cdot y = 8$

- a) $D_x((x^2+4)\cdot y) = ?$ Hin
 - Hint: Use Product Rule

- b) $D_x(8) = ?$
- c) Implicit Differentiation Equation: ?
- d) $y' = \frac{dy}{dx} = ?$
- e) Slope of tangent line = y'(0,4) = ?
- f) Equation of Tangent Line:_____

Hint:
$$y - y_1 = m(x - x_1)$$

9) Find equation of tangent line at (0, 0).

Equation (implicit function): $(x^2 + y^2)^2 + 6x^2y = 0$

- a) $D_x((x^2 + y^2)^2) = ?$ Hint: Use Power Rule
- b) $D_x(6x^2y) = ?$ Hint: Use Product Rule
- c) Implicit Differentiation Equation: ?

$$d) \ y' = \frac{dy}{dx} = ?$$

- e) Slope of tangent line = y'(0,0) = ?
- f) Equation of Tangent Line:_____

Hint:
$$y - y_1 = m(x - x_1)$$