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HW1

Pseudocode:

int binaryCount(1D matrix, low, high)

```
{ initial sum = 0
  mid = (low + high) / 2

  if (low or high equals to mid (that means if 2 index left for search))
  { if (low == a) sum ++
    if (high == a) sum ++
    return sum }

  if (mid == a)
  { if ((high - low) / 2 == 0) sum ++
    sum += (high - low) / 2
    sum ++
    return sum + binaryCount(matrix, mid + 1, high) }

  if (mid == b)
  { return binaryCount(matrix, low, mid) }

  }
  return sum
}
```

int binarySearchForA(1D matrix)

```
{ return binaryCount(matrix, 0, matrix.length - 1)
}
```

int aCount(2D matrix)

```
result = 0
for (i = 0; i < n; i++)
{ result += binarySearchForA(i'th row of 2D matrix) }
return result
```

Time complexity analysis

Binary count

in the if statements, another recursive function is been called with half searching range of the original function, and other lines costs constant time so,

$$T(N) = C + T(N/2)$$

$$= T(N/2) = C + T(N/4)$$

$$T(N/4) = C + T(N/8)$$

⋮

$$T(N) = k \cdot C + T(N/2^k)$$

$$T(N) = \log N \cdot C + T(1) = C(\log N + 1)$$

$$T(N) \text{ is } O(\log N) \text{ because } C \log N + C \leq (C+1) \log N$$

$$= C \leq \log N$$

$$= 2^C \leq N \quad \forall N \geq 2^C$$

it can be anything greater than $(C+1)$

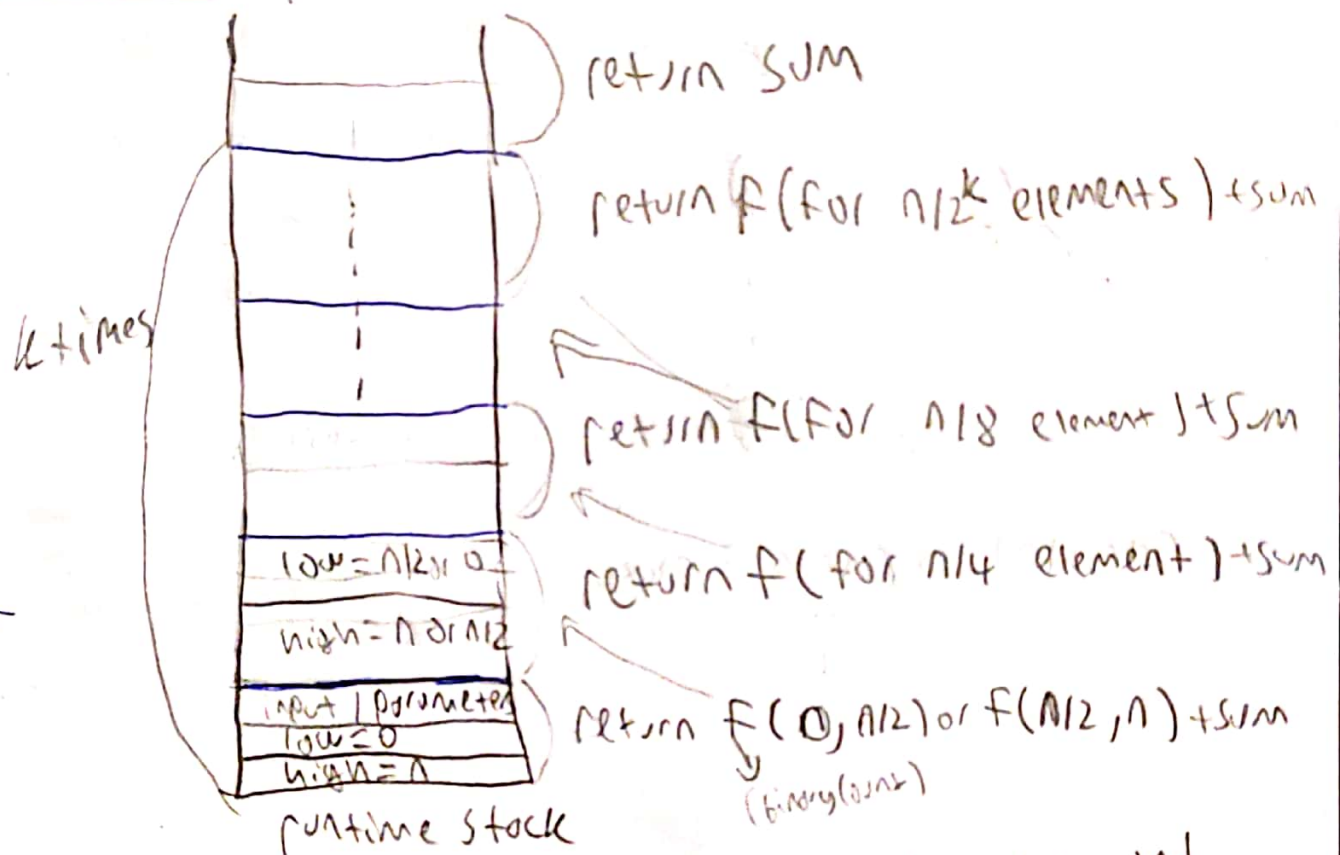
constant

Acco dcount

In this function, binaryCount function iterates N times, so time complexity for that function would be $O(N \cdot \log N)$

Space Complexity Analysis

Binary Count



$n/2^k$ should be 1 so function returns sum, and it can be seen that k should be $\log n$ to achieve that, so it costs $\log n$ c memory, so space complexity is $O(\log n)$

ACount

it's an iterative function, even though it includes a function in the for loop, before ACount returns, all that functions was deleted from runtime stack so space complexity is $O(1)$

Honor code

I have completed this assignment individually, without support from anyone else. I hereby accept that only the below listed sources are approved to be used during this assignment:

- (i) course textbook,
- (ii) All material that is made available to me by the professor (e.g., via Blackboard for this course, course website, email from professor/TA),
- (iii) Notes taken by me during lectures.

I have not used, accessed or taken any unpermitted information from any other source. Hence, all effort belongs to me.

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