Poisson_MGWR_univariate_check

May 14, 2020

Notebook Outline:

- Section 0.0.1
- Section 0.0.2
- Section 0.0.3
- Section 0.0.4
- Section 0.0.5
 - Section 0.0.6
 - Section 0.0.7

0.0.1 Set up Cells

```
In [1]: import sys
        sys.path.append("C:/Users/msachde1/Downloads/Research/Development/mgwr")
In [2]: import warnings
        warnings.filterwarnings("ignore")
        import pandas as pd
        import numpy as np
        from mgwr.gwr import GWR
        from spglm.family import Gaussian, Binomial, Poisson
        from mgwr.gwr import MGWR
        from mgwr.sel_bw import Sel_BW
        import multiprocessing as mp
        pool = mp.Pool()
        from scipy import linalg
        import numpy.linalg as la
        from scipy import sparse as sp
        from scipy.sparse import linalg as spla
        from spreg.utils import spdot, spmultiply
        from scipy import special
        import libpysal as ps
        import seaborn as sns
        import matplotlib.pyplot as plt
        from copy import deepcopy
        import copy
        from collections import namedtuple
        import spglm
```

0.0.2 Fundamental equations for Poisson MGWR

$$y = Poisson[E_i exp(\sum \beta_k x_{k,i})] - (1)$$
(1)

$$E_i = Offset - (2) (2)$$

$$\hat{y} = predicted(y) - (3) \tag{3}$$

$$z = (\sum \beta_k x_{k,i}) + ((y - \hat{y})/\hat{y}) - (4)$$
(4)

(5)

0.0.3 Example Dataset

```
In [3]: data_p = ps.io.open(ps.examples.get_path('Tokyomortality.csv'))
    coords = list(zip(data_p.by_col('X_CENTROID'),data_p.by_col('Y_CENTROID')))
    off = np.array(data_p.by_col('eb2564')).reshape((-1,1))
    y = np.array(data_p.by_col('db2564')).reshape((-1,1))
    occ = np.array(data_p.by_col('OCC_TEC')).reshape((-1,1))
    own = np.array(data_p.by_col('OWNH')).reshape((-1,1))
    pop = np.array(data_p.by_col('POP65')).reshape((-1,1))
    unemp = np.array(data_p.by_col('UNEMP')).reshape((-1,1))
    X = np.hstack([occ,own,pop,unemp])
    x = unemp

X_std = (X-X.mean(axis=0))/X.std(axis=0)
    x_std = (x-x.mean(axis=0))/x.std(axis=0)
    y_std = (y-y.mean(axis=0))/y.std(axis=0)
```

0.0.4 Helper functions

Hardcoded here for simplicity in the notebook workflow

Please note: A separate bw_func_p will not be required when changes will be made in the repository

0.0.5 Univariate example

GWPR model with independent variable, x = unemployment

```
In [7]: bw_gwpr=Sel_BW(coords,y_std,x_std,family=Poisson(),offset=off,constant=False).search()
In [8]: gwpr_model=GWR(coords,y_std,x_std,bw=bw_gwpr,family=Poisson(),offset=off,constant=False
```

MGWR Poisson loop with one independent variable, x = unemployment

Edited multi_bw function - original function in https://github.com/pysal/mgwr/blob/master/mgwr/search.j

```
bw_gwr = bw
XB = XB
if rss_score:
    rss = np.sum((err)**2)
iters = 0
scores = []
delta = 1e6
BWs = []
bw_stable_counter = np.ones(k)
bws = np.empty(k)
try:
    from tqdm.auto import tqdm #if they have it, let users have a progress bar
except ImportError:
    def tqdm(x, desc=''): #otherwise, just passthrough the range
        return x
for iters in tqdm(range(1, max_iter + 1), desc='Backfitting'):
    new_XB = np.zeros_like(X)
    params = np.zeros_like(X)
    for j in range(k):
        temp_y = XB[:, j].reshape((-1, 1))
        temp_y = temp_y + err
        temp_X = X[:, j].reshape((-1, 1))
        #The step below will not be necessary once the bw_func is changed in the r
        if isinstance(family,spglm.family.Poisson):
            bw_class = bw_func_p(coords,temp_y, temp_X)
        else:
            bw_class = bw_func(coords,temp_y, temp_X)
        if np.all(bw_stable_counter == bws_same_times):
            #If in backfitting, all bws not changing in bws_same_times (default 3)
            bw = bws[j]
        else:
            bw = sel_func(bw_class, multi_bw_min[j], multi_bw_max[j])
            if bw == bws[j]:
                bw_stable_counter[j] += 1
            else:
                bw_stable_counter = np.ones(k)
        #Changed qwr_func to accept family and offset as attributes
```

```
optim_model = gwr_func(temp_y, temp_X, bw,family,offset)
        err = optim_model.resid_response.reshape((-1, 1))
        param = optim_model.params.reshape((-1, ))
        new_XB[:, j] = optim_model.predy.reshape(-1)
        params[:, j] = param
        bws[j] = bw
    num = np.sum((new_XB - XB)**2) / n
    den = np.sum(np.sum(new_XB, axis=1)**2)
    score = (num / den)**0.5
    XB = new_XB
    if rss_score:
        predy = np.sum(np.multiply(params, X), axis=1).reshape((-1, 1))
        new_rss = np.sum((y - predy)**2)
        score = np.abs((new_rss - rss) / new_rss)
        rss = new_rss
    scores.append(deepcopy(score))
    delta = score
    BWs.append(deepcopy(bws))
    if verbose:
        print("Current iteration:", iters, ",SOC:", np.round(score, 7))
        print("Bandwidths:", ', '.join([str(bw) for bw in bws]))
    if delta < tol:</pre>
        break
print("iters = "+str(iters))
opt_bws = BWs[-1]
print("opt_bws = "+str(opt_bws))
return (opt_bws, np.array(BWs), np.array(scores), params, err, bw_gwr)
```

Running the function with family = Poisson() and offset

```
In [10]: bw_mgwpr = multi_bw(init=None,coords=coords,y=y_std, X=x_std, n=262, k=x.shape[1], far
iters = 2
opt_bws = [178.]
```

Running without family and offset attributes runs the normal MGWR loop

```
In [11]: bw_mgwr = multi_bw(init=None,coords=coords,y=y_std, X=x_std, n=262, k=x.shape[1])
iters = 1
opt_bws = [73.]
```

0.0.6 Parameter check

Difference in parameters from the GWPR model and MGWPR model

```
In [12]: max(bw_mgwpr[3]-gwpr_model.params)
Out[12]: array([1.89357983e-05])
```

The parameters are not identical but the maximum difference in the parameters is to the order of 1e-05

0.0.7 Bandwidths check

```
In [13]: bw_gwpr
Out[13]: 178.0
In [14]: bw_mgwpr[0]
Out[14]: array([178.])
```

Bandwidths from both models is the same