

Discrete Mathematics

Home Work 3

Dead Line : Wednesday 16 JAN 2013, 4:30 PM

Take $T(1) = 1$ for all the questions below,

Q - 1 [Marks 60]

Find tight asymptotic bounds for the following:

1. $T(n) = 2T\left(\frac{n}{2}\right) + \frac{n}{\lg n}$
2. $T(n) = 2T(\sqrt{n}) + 1$
3. $T(n) = \sqrt{n}T(\sqrt{n}) + n$
4. $T(n) = \frac{1}{4}T\left(\frac{n}{4}\right) + \frac{3}{4}T\left(\frac{3n}{4}\right) + 1$
5. $T(n) = 2T\left(\frac{n}{2}\right) + n \lg n$
6. $T(n) = T\left(\frac{n}{5}\right) + T\left(\frac{3n}{4}\right) + n$

Q - 2 [Marks 50]

Find exact solution to the following:

- (a) $T(n) = 8T(n/2) + n$
- (b) $T(n) = 8T(n/2) + n^3$
- (c) $T(n) = 3T(n/2) + n$
- (d) $T(n) = T(n/4) + 1$
- (e) $T(n) = 3T(n/3) + n^2$