

Q: Hashing

1. Problem Understanding

- Hashing is a technique to map data (key) â†' a fixed-size array (hash table) using a hash function.
 - Used to quickly:
 - Insert
 - Delete
 - Search
 - usually in $O(1)$ average time.
 - A hash function converts keys into indexes in an array.
- Why Hashing?
 - Array search = $O(n)$
 - Binary Search = $O(\log n)$
 - Hashing = $O(1)$ average, $O(n)$ worst-case (if many collisions)
- **Hash Function**
 - A formula that maps a key â†' index.
 - Example:
 - `int index = key % size;`
 - Should:
 - Distribute keys uniformly.
 - Avoid collisions.
 - Be deterministic (same key â†' same index).
- **Collisions**
 - Occur when two keys hash to the same index.
 - Handled by:
 - Chaining: Each array cell stores a `LinkedList` (or list) of keys with the same hash.
 - Open Addressing: Find the next available cell (Linear / Quadratic probing).
- **Common Hash-Based Data Structures (Java)**
 - `HashMap<K,V>` â†' keyâ€“value mapping
 - `HashSet` â†' stores unique elements (backed by `HashMap`)
 - `LinkedHashMap` â†' maintains insertion order
 - `TreeMap` â†' sorted order (Red-Black Tree, not hash-based)
- **DSA Use Cases of Hashing**
 - Count frequencies (numbers or characters)
 - Check duplicates
 - Track seen prefix sums / subarrays

- Map relations (like Roman numeral → value)
 - Fast lookup or existence check
 - String mappings (isomorphic, anagrams)
 - Unique collections (union, intersection)
- **Hash Arrays (Static Hashing)**
 - When elements are numeric and within range, use arrays as hash tables (common in CP / DSA problems).
 - Example:
 - `int[] hash = new int[1000000]; // 10^6 size`
 - `int[] arr = {1,4,2,4,2};`
 - `for (int x : arr) hash[x]++;`
 - `System.out.println(hash[4]); // prints 2`
 - **Memory Constraints in Java (This is Important for DSA)**
 - Inside main():
 - `int[] up to 10^6`
 - `boolean[] up to 10^7`
 - Outside main (static/global):
 - `int[] up to 10^7`
 - `boolean[] up to 10^8`
 - Reason:
 - Local variables are stored on stack (limited memory).
 - Static/global arrays are stored on heap (larger memory).
 - Exceeding limits causes:
 - `java.lang.OutOfMemoryError: Java heap space`
 - **Types of Hashing in DSA**
 - Direct Address Table: Use the key directly as index (when range is small).
 - Hash Table: Use hash function to map large keys to smaller indexes.
 - Double Hashing: Use two hash functions to minimize clustering in open addressing
 - **Implementation Snippets**
 - Frequency of characters:


```
* String s = "aabbcc"; * int[] freq = new int[26]; * for (char c : s.toCharArray()) freq[c - 'a']++; * System.out.println(freq['b' - 'a']); // freq of 'b'
```
 - Frequency using HashMap:


```
* HashMap<Integer, Integer> map = new HashMap<>(); * for (int x : arr) * map.put(x, map.getOrDefault(x, 0) + 1);
```
 - **Time & Space Complexity**
 - Average Case:
 - Insert → O(1)
 - Search → O(1)
 - Delete → O(1)
 - Worst Case: O(n) (many collisions)
 - Space: O(N)

- **Real-World Analogy**

- Like a library shelf system:
 - Hash function = shelf number
 - Book = key/value
 - You go directly to that shelf → fast retrieval.

- **Common Interview Problems (Hashing-Based)**

- Two Sum → LeetCode #1
 - → Store complement in HashMap.
- Subarray Sum Equals K → LeetCode #560
 - → Store prefix sums in HashMap.
- Longest Consecutive Sequence → LeetCode #128
 - → Use HashSet for fast existence checks.
- Group Anagrams → LeetCode #49
 - → HashMap with sorted string as key.
- Top K Frequent Elements → LeetCode #347
 - → HashMap + MinHeap.
- Valid Anagram → LeetCode #242
 - → Count frequency via array or HashMap.
- Intersection of Two Arrays → HashSet for membership check.

- **Best Practices for Hashing in DSA**

- For characters: use arrays (int[26] or int[256])
- For numbers: use HashMap or static arrays.
- Always offset negative numbers by $+10^{15}$ or $+10^{11}$ before indexing.
- Avoid large arrays if range is unknown → use HashMap.
- Clear hash structures between test cases in coding challenges.
- Use long as key for larger integers (e.g. prefix sums).
- Be aware of hash collisions → use .equals() and hashCode() properly for custom objects.

- **Internal Working of HashMap (Java Internals)**

- 1. Structure
 - Backed by an array of buckets (Node<K,V>[]).
 - Each bucket holds a linked list (or tree) of key-value pairs.
- 2. Node<K,V> Structure
 - static class Node<K,V> {
 - final int hash;
 - final K key;
 - V value;
 - Node<K,V> next;
 - }
- 3. hashCode()
 - Every key has a hashCode() (integer value).
 - HashMap refines this using bit manipulation:
 - `int hash = (key == null) ? 0 : (key.hashCode() ^ (key.hashCode() >>> 16));`

- $\hat{+}$ spreads hash bits to avoid collisions.
- 4. Index Calculation
 - Index in array = hash & (n - 1) (where n = capacity, always power of 2)
- 5. Collision Handling
 - Before Java 8: LinkedList chaining.
 - After Java 8: Converts to balanced tree (TreeNode) if chain length > 8.
- 6. Load Factor
 - Ratio of number of elements to array size (default = 0.75).
 - When load factor exceeds threshold $\hat{+}$ rehashing (array size doubles).
- 7. equals() and hashCode()
 - Both must be correctly overridden for user-defined keys.
 - Two keys are equal if:
 - key1.hashCode() == key2.hashCode() && key1.equals(key2)
- 8. Null Keys and Values
 - HashMap allows one null key and multiple null values.
 - Null key is stored in index 0.

- **Common Interview Questions on HashMap Internals**

- How does HashMap achieve O(1) complexity?
- What happens if two keys have same hashCode()?
- How does Java 8 improve collision handling?
- What is load factor and resizing?
- Why is capacity a power of 2?
- Why should hashCode() and equals() be consistent?

- **Optimization Tips**

- Use HashSet for unique element lookups.
- Use LinkedHashMap when insertion order matters.
- Use TreeMap when you need sorted keys.
- Avoid large primitive arrays if the key range is sparse.
- For competitive programming:
 - Prefer static arrays (faster than HashMap).
 - Use HashMap when input constraints are large or negative.

- **Quick Recap (Key Takeaways)**

- Hashing = fast lookup using key $\hat{+}$ index mapping.
 - Use arrays for small ranges, HashMap for generic data.
 - Memory matters:
 - Inside main: 10^6
 - Static/global: 10^7 (int), 10^8 (boolean)
 - Handle collisions smartly.
 - Understand hashCode() + equals() for interviews.
 - Practice problems: Two Sum, Subarray Sum, Anagrams.
-

Q95: Longest Consecutive Sequence in an Array

1. Problem Understanding

- You are given an integer array `nums`.
 - You must find the length of the longest consecutive elements sequence, where the sequence numbers appear in any order.
 - A consecutive sequence means numbers that come one after another with a difference of 1 (like 1,2,3,4).
 - Important: You only care about the length, not the sequence itself.
-

2. Constraints

- $1 \leq \text{nums.length} \leq 10^5$
 - $-10^9 \leq \text{nums}[i] \leq 10^9$
-

3. Edge Cases

- Empty array → return 0
 - Array with duplicates → count only unique numbers
 - Array already consecutive → return full length
 - Negative and mixed values handled normally
-

4. Examples

```
Input: nums = [100, 4, 200, 1, 3, 2]
Output: 4
Explanation: Longest consecutive sequence is [1, 2, 3, 4].
```

5. Approaches

Approach 1: Sorting-Based

Idea:

- Sort the array and then count consecutive elements. Skip duplicates and reset when the sequence breaks.

Steps:

- Sort the array.

- Use variables currLen and maxLen to track streaks.
- Compare consecutive elements and update counts.

Java Code:

```
public int longestConsecutive(int[] nums) {
    if (nums.length == 0) return 0;
    Arrays.sort(nums);
    int maxLen = 1, currLen = 1;

    for (int i = 1; i < nums.length; i++) {
        if (nums[i] == nums[i - 1]) continue;
        if (nums[i] == nums[i - 1] + 1) currLen++;
        else currLen = 1;
        maxLen = Math.max(maxLen, currLen);
    }
    return maxLen;
}
```

Complexity (Time & Space):

- Time Complexity
 - Sorting: $O(n \log n)$
 - Single traversal: $O(n)$
 - Total: $O(n \log n)$
- Space Complexity
 - $O(1)$ (ignoring sort overhead)

Approach 2: Using HashSet (Optimal)

Idea:

- Use a HashSet to check existence of consecutive numbers quickly.
- Start counting only when the current number is the start of a sequence (i.e., $\text{num} - 1$ is not present).

Steps:

- Add all numbers to a HashSet.
- For each number, if $\text{num} - 1$ doesn't exist, start a new sequence.
- Keep counting $\text{num} + 1, \text{num} + 2, \dots$ until break.
- Track the maximum streak length.

Java Code:

```
public int longestConsecutive(int[] nums) {
    HashSet<Integer> set = new HashSet<>();
    for (int num : nums) set.add(num);

    int maxLen = 0;
```

```

for (int num : set) {
    if (!set.contains(num - 1)) { // sequence start
        int curr = num;
        int len = 1;

        while (set.contains(curr + 1)) {
            curr++;
            len++;
        }
        maxLen = Math.max(maxLen, len);
    }
}
return maxLen;
}

```

Complexity (Time & Space):

- Time Complexity
 - Insert all elements: O(n)
 - Traverse and count sequences: O(n) (each element checked once)
 - Total: O(n)
- Space Complexity
 - O(n) for HashSet storage

Approach 3: Using HashMap (Alternate)

Idea:

- Use a HashMap to dynamically merge sequences.
- Each number connects to the length of its current sequence, and merging happens when neighboring sequences exist.

Steps:

- For each element, get lengths of left and right neighboring sequences.
- New sequence length = left + right + 1.
- Update boundaries (num - left and num + right) with new length.
- Keep track of the longest sequence.

Java Code:

```

public int longestConsecutive(int[] nums) {
    HashMap<Integer, Integer> map = new HashMap<>();
    int maxlen = 0;

    for (int num : nums) {
        if (map.containsKey(num)) continue;

        int left = map.getOrDefault(num - 1, 0);

```

```

        int right = map.getOrDefault(num + 1, 0);
        int len = left + right + 1;

        map.put(num, len);
        map.put(num - left, len);
        map.put(num + right, len);

        maxLen = Math.max(maxLen, len);
    }
    return maxLen;
}

```

Complexity (Time & Space):

- Time Complexity
 - Each element processed once: $O(n)$
 - HashMap operations: $O(1)$ average
 - Total: $O(n)$
 - Space Complexity
 - $O(n)$ for HashMap
-

6. Justification / Proof of Optimality

- Sorting is simpler but slower ($O(n \log n)$).
 - HashSet is optimal and easy to reason about.
 - HashMap approach is powerful for merging intervals (advanced variant).
-

7. Variants / Follow-Ups

- Longest consecutive subsequence in a sorted array.
 - Longest sequence with given difference k .
 - Used in problems like “Longest Band” or “Union of consecutive ranges.”
-

8. Tips & Observations

- Always check $num - 1$ to find the start of a sequence.
 - HashSet avoids unnecessary duplicate counting.
 - The logic applies for negative, positive, and unordered values.
 - This is a great example of how to convert $O(n \log n)$ sorting logic into $O(n)$ using hashing.
-

Q96: Longest Subarray with Sum K

1. Problem Understanding

- You are given an array nums of integers and a target sum k.
 - You need to find the length of the longest contiguous subarray whose sum equals k.
 - If no such subarray exists, return 0.
-

2. Constraints

- $1 \leq n \leq 10^5$
 - $-10^5 \leq \text{nums}[i] \leq 10^5$
 - $-10^5 \leq k \leq 10^5$
-

3. Edge Cases

- All numbers are positive â†’ sliding window approach works.
 - Array contains negative numbers â†’ need prefix sum + HashMap.
 - $k = 0$ (check for subarrays summing to zero).
 - No subarray equals k â†’ return 0.
-

4. Examples

```
Input: nums = [10, 5, 2, 7, 1, 9], k = 15
Output: 4
Explanation: [5, 2, 7, 1] has sum = 15.
```

5. Approaches

Approach 1: Brute Force ($O(n^2)$)

Idea:

- Try every possible subarray and compute its sum.
- Keep track of the longest one equal to k .

Steps:

- Use two loops â€” outer for start index, inner for end index.
- Compute sum for each subarray.
- If sum == k â†’ update longest length.

Java Code:

```
int longestSubarraySumK(int[] nums, int k) {
    int n = nums.length;
    int maxLen = 0;
    for (int i = 0; i < n; i++) {
        int sum = 0;
```

```

        for (int j = i; j < n; j++) {
            sum += nums[j];
            if (sum == k)
                maxLen = Math.max(maxLen, j - i + 1);
        }
    }
    return maxLen;
}

```

Complexity (Time & Space):

- Time Complexity
 - $O(n^2)$ due to nested loops
 - For large n (10^6), not efficient
- Space Complexity
 - $O(1)$

Approach 2: Prefix Sum + HashMap (Optimized $O(n)$)

Idea:

- Use a prefix sum to keep track of cumulative sums, and store the first occurrence of each prefix in a HashMap.
- If $\text{prefixSum} - k$ exists in map → a subarray with sum k exists from that index to current.

Steps:

- Initialize $\text{sum} = 0$, $\text{maxLen} = 0$, and a $\text{HashMap<Integer, Integer>} \text{prefixMap}$.
- For each element:
 - Add it to sum .
 - If $\text{sum} == k$ → update maxLen .
 - If $\text{sum} - k$ exists in map → subarray found, update maxLen .
 - If sum not in map → store it with current index (only first occurrence).
- Return maxLen .

Java Code:

```

int longestSubarraySumK(int[] nums, int k) {
    HashMap<Integer, Integer> map = new HashMap<>();
    int sum = 0, maxLen = 0;

    for (int i = 0; i < nums.length; i++) {
        sum += nums[i];

        if (sum == k) maxLen = i + 1;

        if (map.containsKey(sum - k)) {
            maxLen = Math.max(maxLen, i - map.get(sum - k));
        }
    }
}

```

```

        if (!map.containsKey(sum)) {
            map.put(sum, i);
        }
    }

    return maxLen;
}

```

Complexity (Time & Space):

- $O(n)$ Time Complexity
 - $O(1)$ single pass with $O(1)$ HashMap lookups
- $O(n)$ Space Complexity
 - $O(n)$ HashMap storing prefix sums

Approach 3: Sliding Window (Only for Non-Negative Numbers)

Idea:

- When all elements are non-negative, we can use a sliding window to expand/shrink the subarray.

Steps:

- Maintain two pointers l and r, and a running sum.
- Expand r to increase sum.
- If sum > k → move l forward.
- If sum == k → update maxLen.

Java Code:

```

int longestSubarraySumK(int[] nums, int k) {
    int left = 0, right = 0, sum = 0, maxLen = 0;
    int n = nums.length;

    while (right < n) {
        sum += nums[right];

        while (sum > k) {
            sum -= nums[left];
            left++;
        }

        if (sum == k) {
            maxLen = Math.max(maxLen, right - left + 1);
        }

        right++;
    }

    return maxLen;
}

```

Complexity (Time & Space):

- Time Complexity
 - $O(n)$ for each element added/removed once
 - Space Complexity
 - $O(1)$
-

6. Justification / Proof of Optimality

- The HashMap + Prefix Sum approach is the most optimal because:
 - It handles both positive and negative numbers.
 - It gives $O(n)$ time complexity.
-

7. Variants / Follow-Ups

- Count of subarrays with sum K (instead of longest length).
 - Subarray sum divisible by K
 - Longest subarray with sum $\leq K$
-

8. Tips & Observations

- Always store first occurrence of prefix sum as it gives longest subarray.
 - Resetting map or overwriting sums can shorten valid subarrays.
 - For strictly positive arrays the sliding window is even simpler and faster.
-

Q97: Count subarrays with given sum

1. Problem Understanding

- You are given an integer array nums and an integer k.
 - You need to count all subarrays whose sum equals k.
 - Subarrays are contiguous sequences within the array.
-

2. Constraints

- $1 \leq \text{nums.length} \leq 10^5$ implies $O(n^2)$ brute force may TLE, we need $O(n)$.
 - $-1000 \leq \text{nums}[i] \leq 1000$ elements can be negative.
 - $-10^7 \leq k \leq 10^7$.
-

3. Edge Cases

- Array contains negative numbers → prefix sum with hashmap works.
 - Array has all zeros, $k = 0$ → multiple subarrays sum to 0.
 - Single element array equal to k .
-

4. Examples

```
Input: [1, 1, 1], k = 2 → Output: 2 → [1,1], [1,1]
```

```
Input: [1, 2, 3], k = 3 → Output: 2 → [1,2], [3]
```

```
Input: [3, 1, 2, 4], k = 6 → Output: 1 → [2,4]
```

5. Approaches

Approach 1: Brute Force

Idea:

- Check all possible subarrays and sum them.

Steps:

- Initialize count = 0
- Loop i from 0 to $n-1$
- Loop j from i to $n-1$
- Sum $\text{nums}[i..j]$, if sum == k → count++

Java Code:

```
public int subarraySum(int[] nums, int k) {  
    int count = 0;  
    for (int i = 0; i < nums.length; i++) {  
        int sum = 0;  
        for (int j = i; j < nums.length; j++) {  
            sum += nums[j];  
            if (sum == k) count++;  
        }  
    }  
    return count;  
}
```

Complexity (Time & Space):

- Time Complexity:
 - $O(n^2)$
- Space Complexity:

- O(1)

Approach 2: Prefix Sum + HashMap (Optimized) →...

Idea:

- Use a prefix sum and store counts of prefix sums in a hashmap.
- For each new prefix sum currSum, check if $(currSum - k)$ exists in the map → add its frequency to result.

Steps:

- Initialize map = {0:1}, sum = 0, count = 0
- Loop over each element in nums:
- $sum += nums[i]$
- If $(sum - k)$ exists in map → count += map.get(sum - k)
- $map[sum] = map.getOrDefault(sum, 0) + 1$

Java Code:

```
import java.util.HashMap;

public class Solution {
    public int subarraySum(int[] nums, int k) {
        HashMap<Integer, Integer> map = new HashMap<>();
        map.put(0, 1); // base case
        int sum = 0, count = 0;
        for (int num : nums) {
            sum += num;
            if (map.containsKey(sum - k)) {
                count += map.get(sum - k);
            }
            map.put(sum, map.getOrDefault(sum, 0) + 1);
        }
        return count;
    }
}
```

Complexity (Time & Space):

- Time Complexity:
 - O(n) → single pass over array
- Space Complexity:
 - O(n) → hashmap storing prefix sums

6. Justification / Proof of Optimality

- The hashmap keeps track of how many times a prefix sum occurred.
- $sum - k$ exists → there exists a previous prefix sum that forms a subarray summing to k.

7. Variants / Follow-Ups

- Count subarrays with sum $\leq k$ → need sliding window for positive numbers.
 - Longest subarray with sum = k → similar prefix sum + hashmap, store first index.
-

8. Tips & Observations

- Always initialize map.put(0,1) → handles subarrays starting from index 0.
 - Works for negative numbers too.
 - For longest subarray, store first occurrence of each prefix sum.
-

Q98: Count subarrays with given xor K

1. Problem Understanding

- You are given an integer array nums and an integer k.
 - You need to count all subarrays whose XOR of elements equals k.
 - XOR (^) is bitwise exclusive OR.
-

2. Constraints

- $1 \leq \text{nums.length} \leq 10^5$ → O(n^2) brute force may TLE, need O(n).
 - $1 \leq \text{nums}[i] \leq 10^9$ → elements are positive integers.
 - $1 \leq k \leq 10^9$.
-

3. Edge Cases

- Single element equal to k → counts as one subarray.
 - Multiple subarrays with same XOR.
 - Large numbers → ensure XOR calculations are correct (int is fine in Java).
-

4. Examples

```
Input: [4, 2, 2, 6, 4], k = 6 → Output: 4 → [4,2], [4,2,2,6,4], [2,2,6], [6]
```

```
Input: [5, 6, 7, 8, 9], k = 5 → Output: 2 → [5], [5,6,7,8,9]
```

```
Input: [5, 2, 9], k = 7 → Output: 0
```

5. Approaches

Approach 1: Brute Force

Idea:

- Check XOR for all subarrays.

Steps:

- Initialize count = 0
- Loop i from 0 to n-1
- Loop j from i to n-1 \rightarrow xor = XOR(nums[i..j])
- If xor == k \rightarrow count++

Java Code:

```
public int subarrayXor(int[] nums, int k) {  
    int count = 0;  
    for (int i = 0; i < nums.length; i++) {  
        int xor = 0;  
        for (int j = i; j < nums.length; j++) {  
            xor ^= nums[j];  
            if (xor == k) count++;  
        }  
    }  
    return count;  
}
```

Complexity (Time & Space):

- Time Complexity:
 - $O(n^2)$ \rightarrow TLE for large n
- Space Complexity:
 - $O(1)$

Approach 2: Prefix XOR + HashMap (Optimized) ↴

Idea:

- Let prefixXOR[i] = XOR of all elements from 0 to i.
- For subarray nums[l..i], XOR = prefixXOR[i] ^ prefixXOR[l-1]
- If prefixXOR[i] ^ k exists in map \rightarrow there exists a subarray ending at i with XOR k.

Steps:

- Initialize map = {0:1}, xor = 0, count = 0
- Loop over each element in nums:
 - xor ^= nums[i]
 - If (xor ^ k) exists in map \rightarrow count += map.get(xor ^ k)
 - map[xor] = map.getOrDefault(xor, 0) + 1

Java Code:

```
import java.util.HashMap;

public class Solution {
    public int subarrayXor(int[] nums, int k) {
        HashMap<Integer, Integer> map = new HashMap<>();
        map.put(0, 1); // base case
        int xor = 0, count = 0;
        for (int num : nums) {
            xor ^= num;
            count += map.getOrDefault(xor ^ k, 0);
            map.put(xor, map.getOrDefault(xor, 0) + 1);
        }
        return count;
    }
}
```

Complexity (Time & Space):

- Time Complexity:
 - $O(n)$ for single pass over array
 - Space Complexity:
 - $O(n)$ for hashmap storing prefix XOR counts
-

6. Justification / Proof of Optimality

- The hashmap stores frequency of prefix XORs.
 - $xor \wedge k$ in map implies there exists a previous prefix XOR that will form a subarray with $XOR = k$.
 - Works for large positive integers.
-

7. Variants / Follow-Ups

- Count subarrays with $XOR \wedge k$ needs trie-based approach.
 - Find longest subarray with $XOR k$ use first occurrence of prefix XOR in map.
-

8. Tips & Observations

- XOR is reversible: $a \wedge b = c \Rightarrow a = b \wedge c$
 - Initialize $map.put(0, 1)$ handles subarrays starting from index 0.
 - Similar template to prefix sum with hashmap, just replace $+$ with \wedge .
-