



Computer Vision

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Course Details

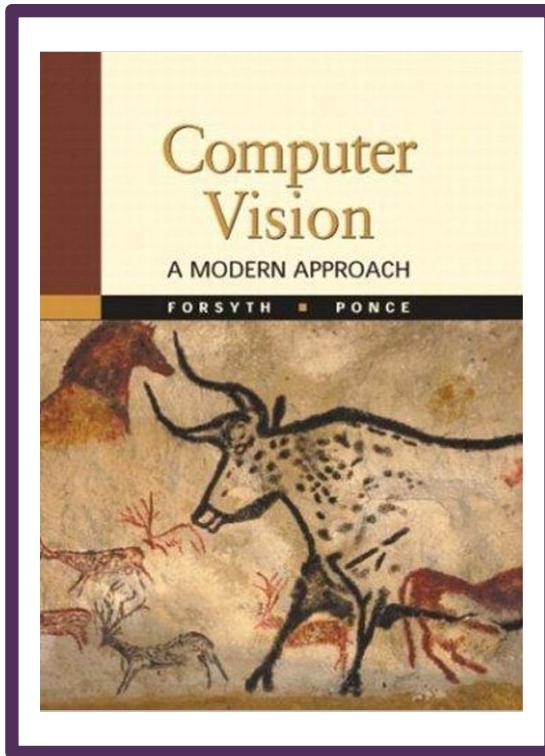
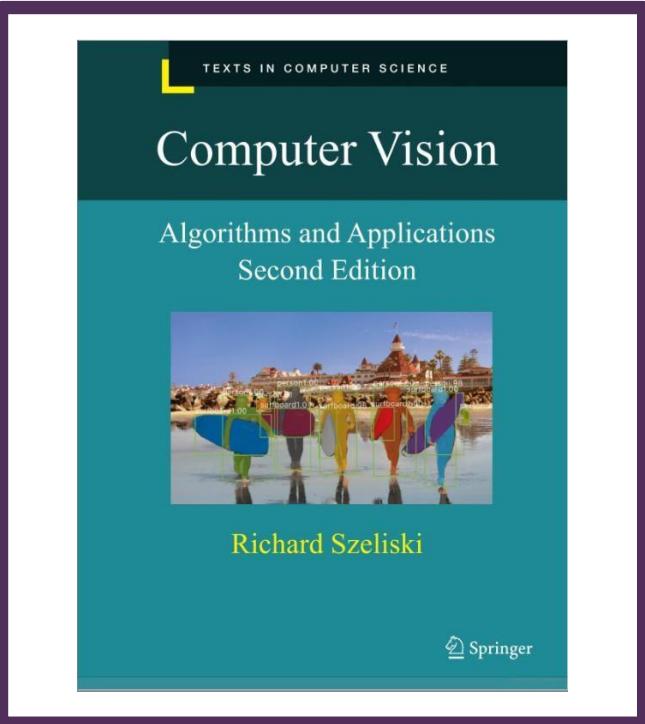
LECTURES: Monday
& Wednesday

TIMINGS:
9:30 am – 11:00 am

MY OFFICE:

OFFICE HOURS:

EMAIL: m.tahir@nu.edu.pk



References

The material in these slides are based on:

1

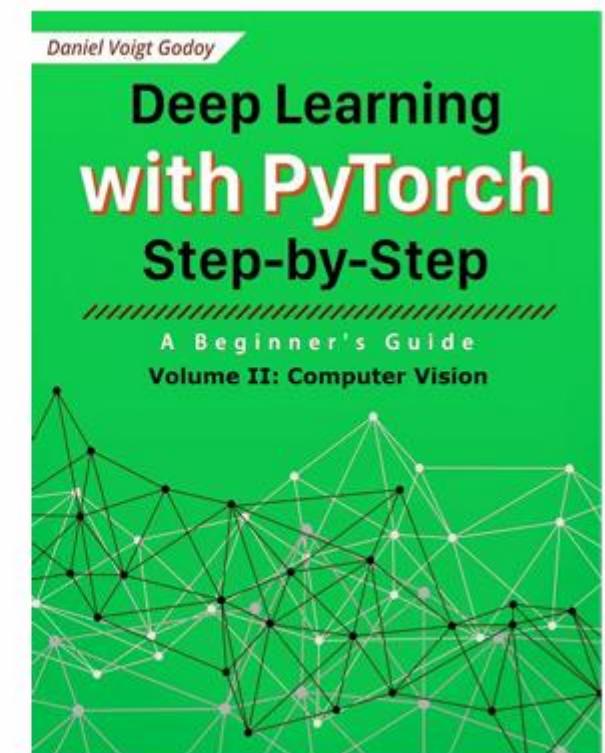
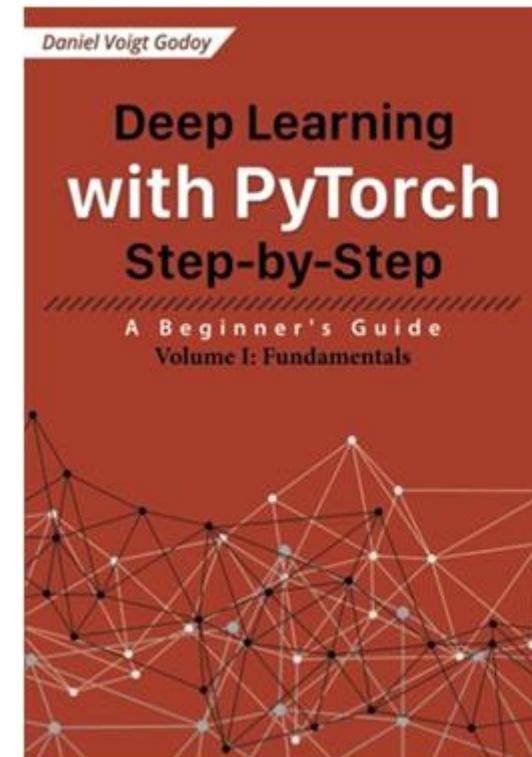
Rick Szeliski's book: [Computer Vision: Algorithms and Applications](#)

2

Forsythe and Ponce: [Computer Vision: A Modern Approach](#)

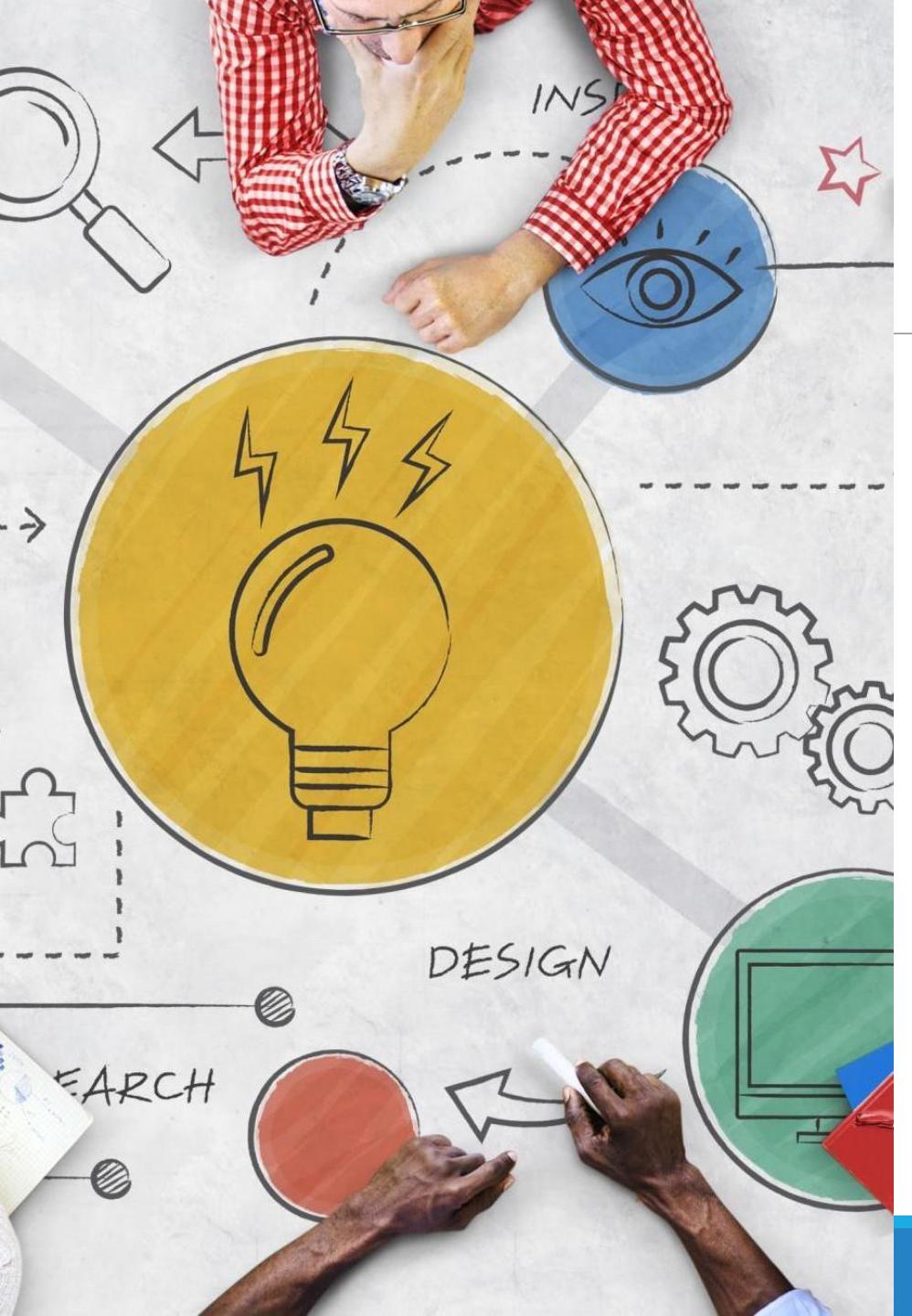
Recommended Books

Deep Learning with PyTorch Step-by-Step by Daniel Voigt Godoy



Course Learning Outcomes

| No | CLO (Tentative) | Domain | Taxonomy Level | PLO |
|----|--|-----------|----------------|-----|
| 1 | Understanding basics of Computer Vision: algorithms, tools, and techniques | Cognitive | 2 | |
| 2 | Develop solutions for image/video understanding and recognition | Cognitive | 3 | |
| 3 | Design solutions to solve practical Computer Vision problems | Cognitive | 3 | |

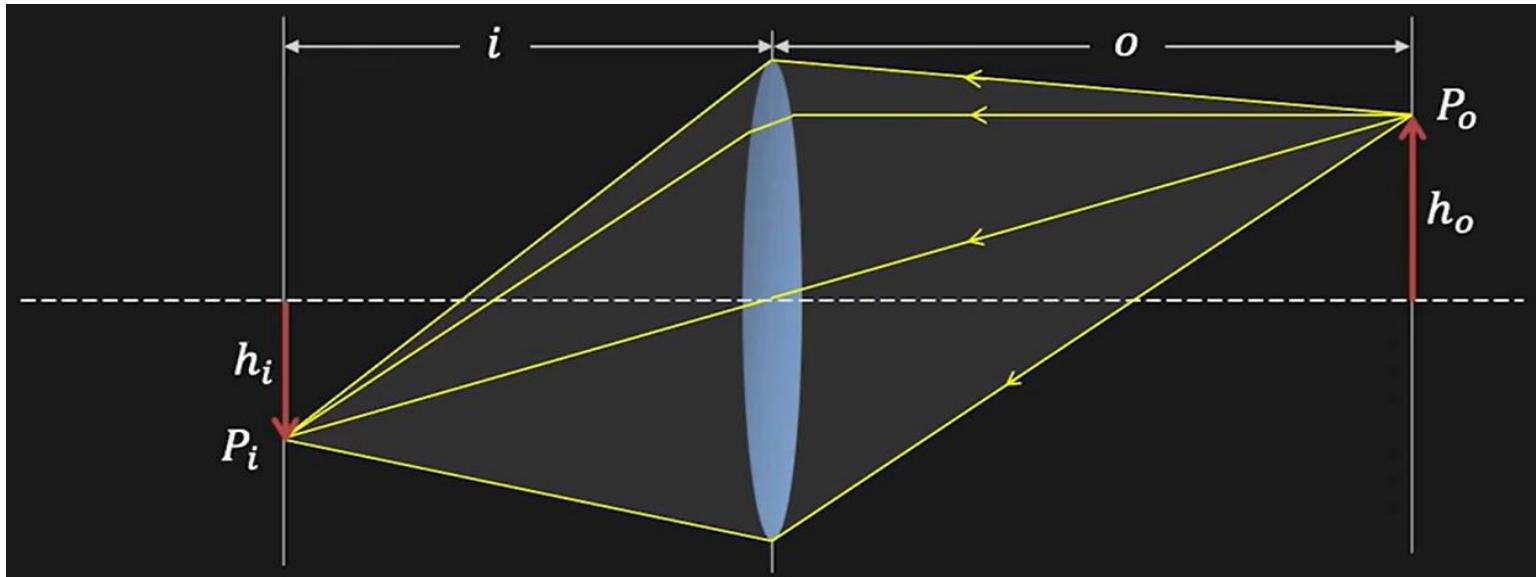


Outline

Image Formation

Image Magnification due to Lens

Image Magnification due to Lens

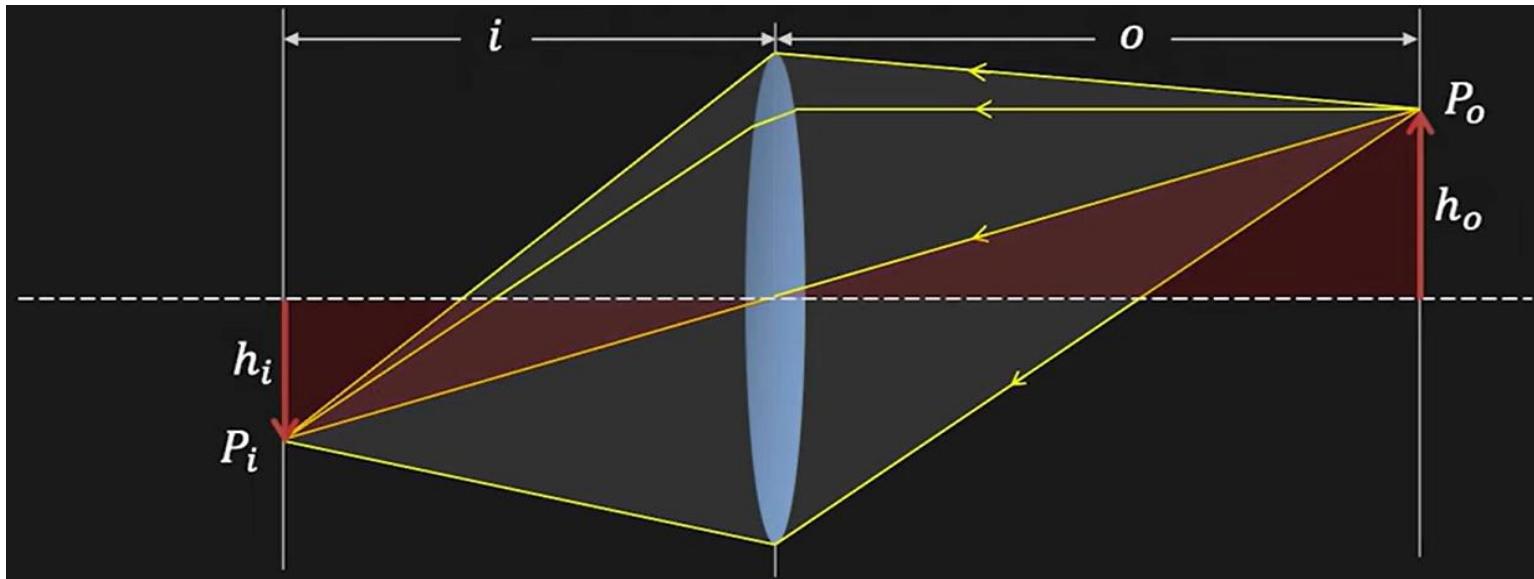


- The distance of the object from the lens is o
- The distance of the image from the lens is i
- The height of the object is h_o
- We want to know what is the height of the image h_i

So, magnification
is defined as h_i
divided by h_o

$$m = \frac{h_i}{h_o}$$

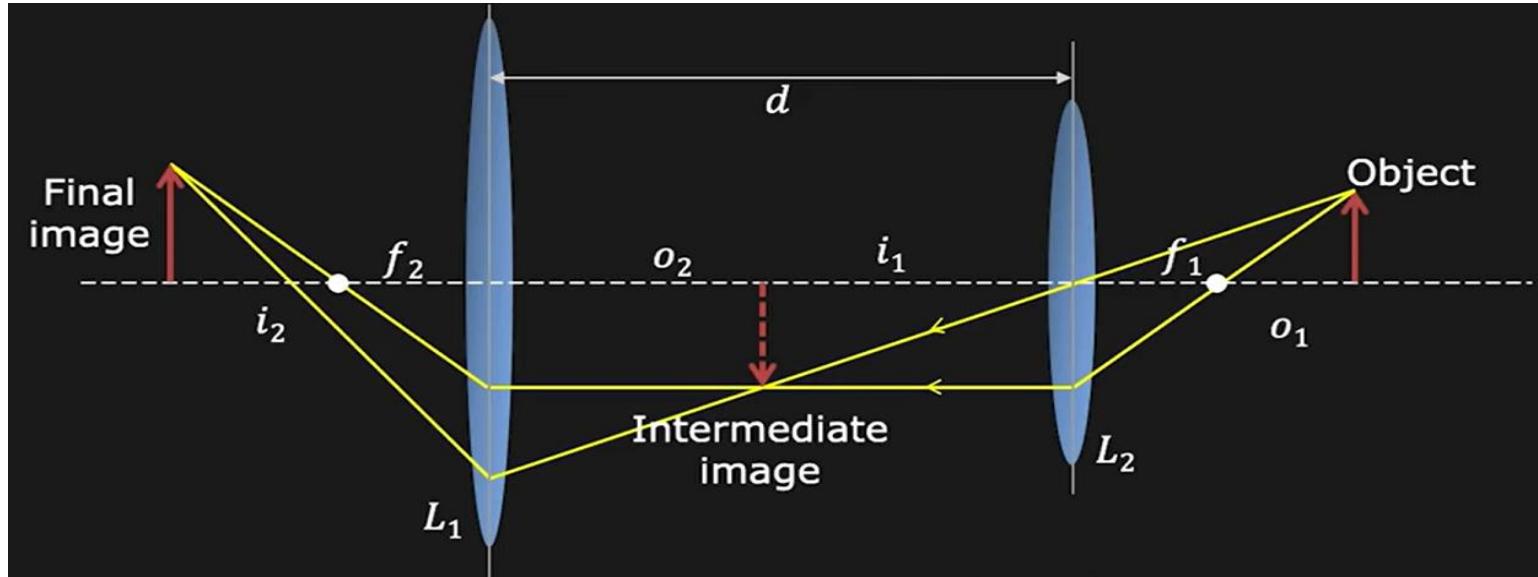
Image Magnification due to Lens



- Consider the two similar triangles, then $\frac{h_i}{h_o} = \frac{i}{o}$

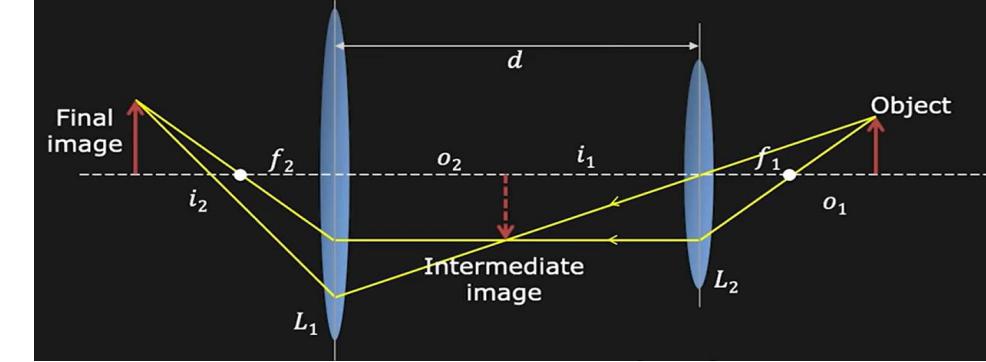
Two Lens System

Two Lens System



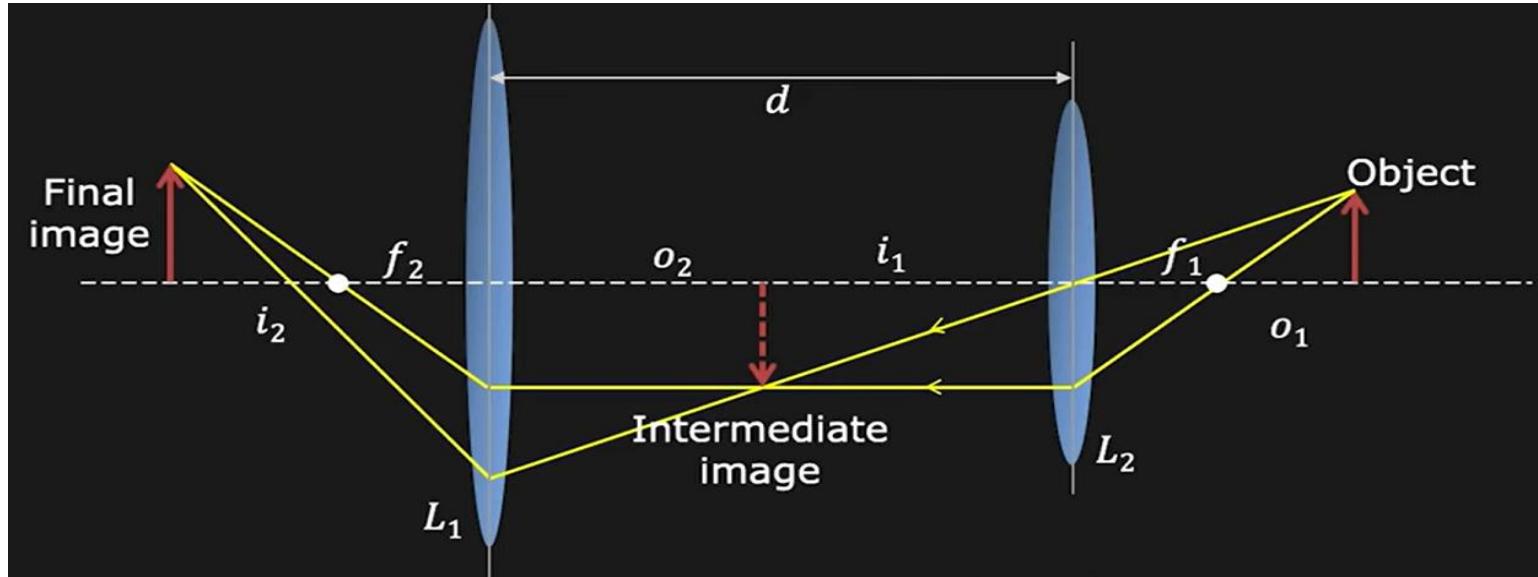
- The magnification of a lens system can be changed by using multiple lenses.

Two Lens System



- Consider the two-lens system where we have lens L_1 and L_2
- Object is placed at distance o_1 from L_2 , which is imaged as an **intermediate image** between L_1 and L_2
- The intermediate image is a new object for the final image that is formed at distance i_2 from L_1
- So, the magnification of the complete system is a **magnification due to lens L_2** times **the magnification due to lens L_1**
- So, $m = \frac{i_2}{o_2} \times \frac{i_1}{o_1}$

Two Lens System



- No need to change the distance between the object and the image plane.
- Instead, the effective magnification of the complete system is achieved by moving the lenses L_1 and L_2 . That is the process of zooming.

Zooming: Move lenses to change magnification

Aperture of Lens

Aperture of Lens



- Aperture is the light receiving area of lens, indicated by lens **diameter**.

Aperture of Lens



- Aperture can be **reduced / increased** to control image brightness

f-number (f-stop, f-ration) of Lens

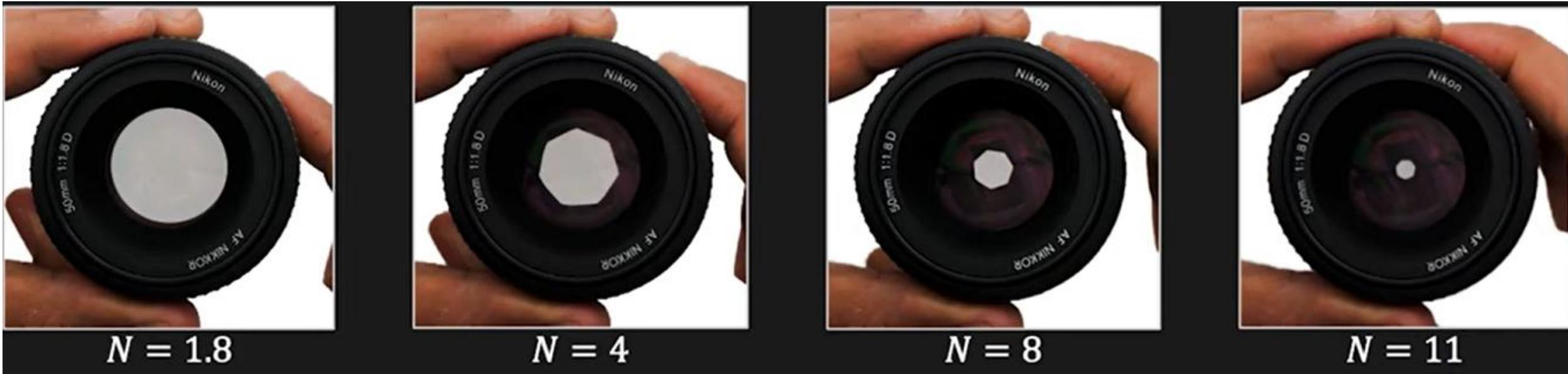
- The aperture of a lens can be expressed **as a fraction of focal length** of the lens that is called the *f – number* represented here by N .

$$\text{Aperture: } D = \frac{f}{N} \quad \text{f – Number: } N = \frac{f}{D}$$

- Example:** A 50 mm focal length, $\frac{f}{1.8}$ lens implies:
 - $N = 1.8$ ($D = 27.8\text{ mm}$) when aperture is fully open



f – number (f-stop, f-ration) of Lens



$N = 1.8$

$N = 4$

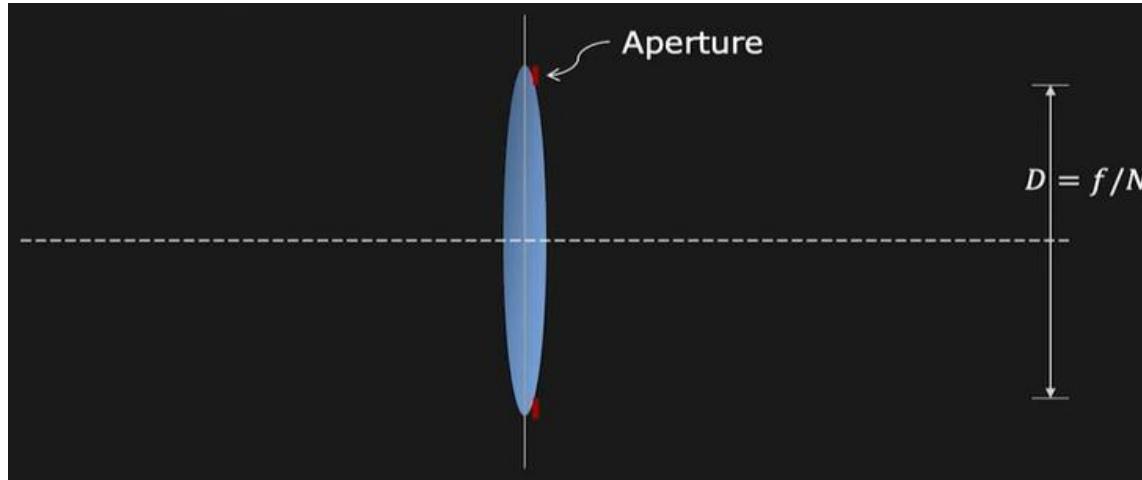
$N = 8$

$N = 11$

- *f – number* goes up, the **diameter** goes down
- The *f – number* tells you **how “open” or “closed”** the camera lens is.
 - A **small *f – number*** → large aperture (wide opening) → more light enters.
 - A **large *f – number*** → small aperture → less light enters.

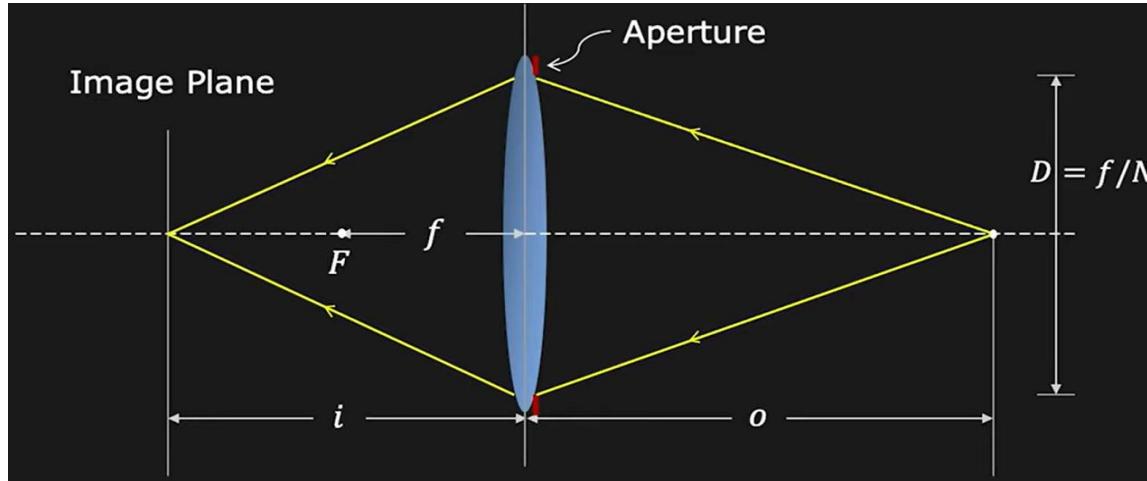
Lens Defocus

Lens Defocus



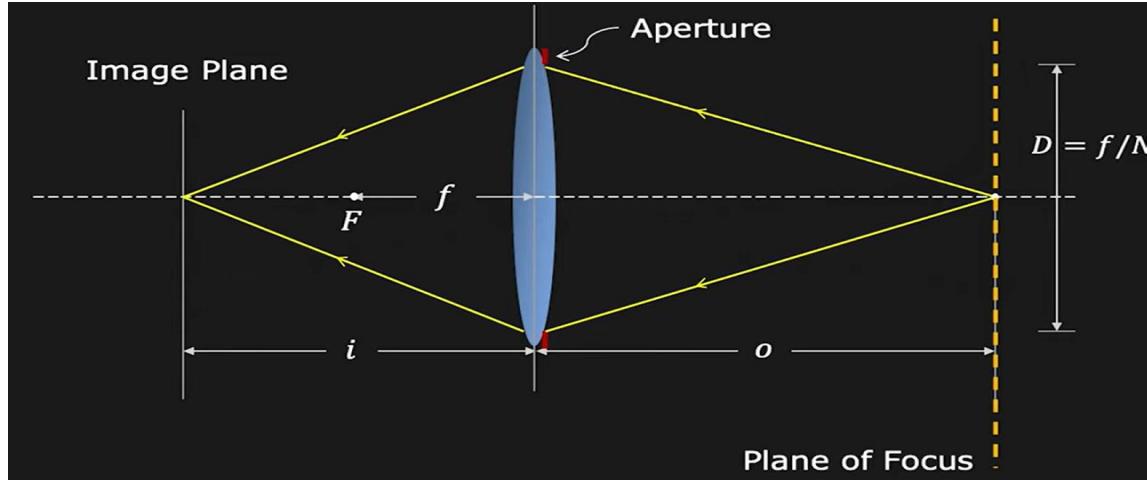
- **Lens defocus** occurs when a point in the scene **is not in perfect focus** on the image sensor.
- Lens gathers more light compared to a pinhole camera
- However, there is only one plane in the scene that is perfectly focused onto the image plane by lens

Lens Defocus



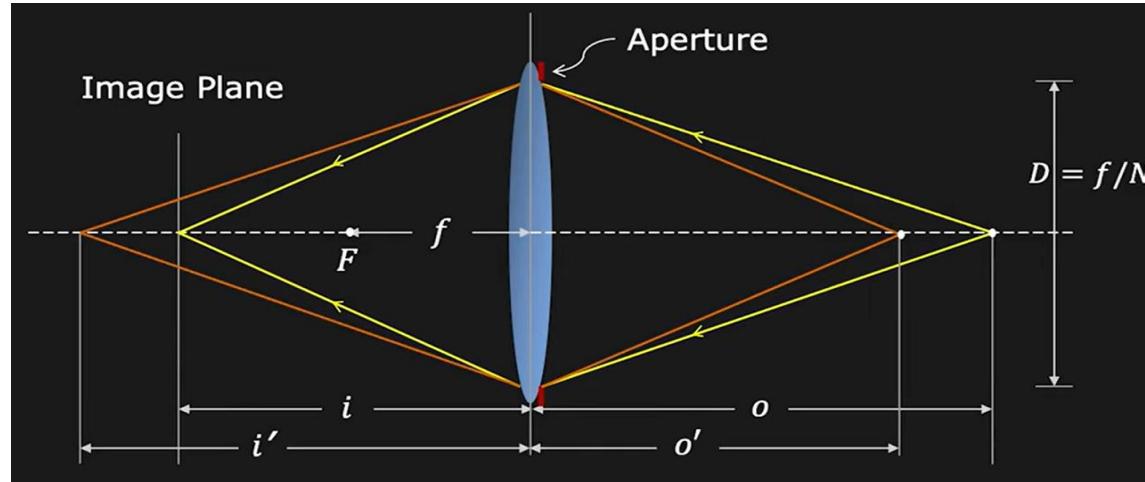
- The point at the distance o will be focused on the distance i
- The image plane is placed exactly at that location

Lens Defocus



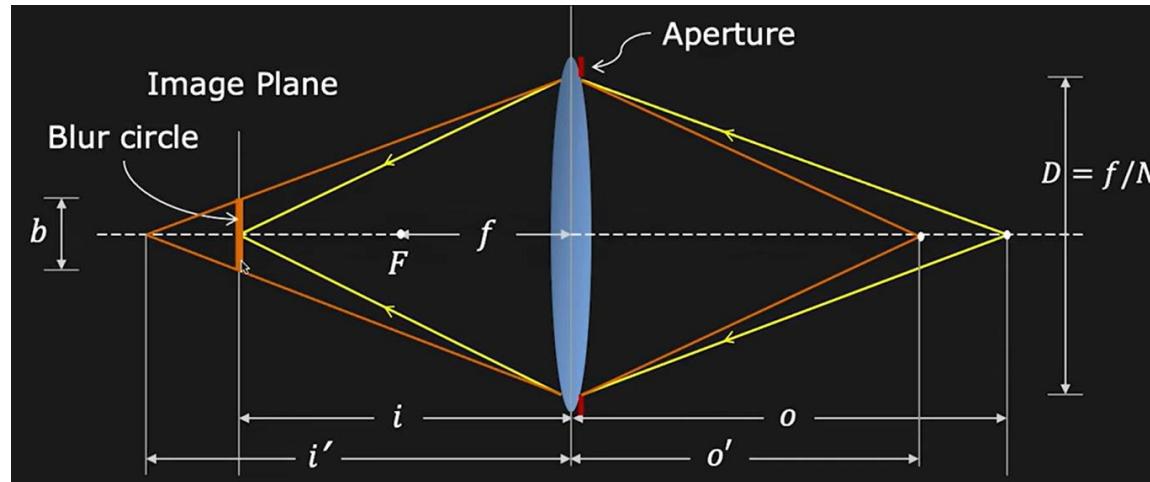
- For this particular position of the image plane, there is exactly one plane which is going to be completely in focus.
- This is called the **plane of focus** corresponding to the lens system

Lens Defocus



- If a point lies out of this plane of focus, For example the point at distance δ from the lens
- Since it is closer to the lens, its image is going to be formed at a distance i' that is behind the image plane

Lens Defocus



- The light that the lens receives from this point is not going to end as a single point on the image plane but rather distributed over a **blur circle** with a **diameter b**.

Lens Defocus

- For any given position of the object in the scene, the diameter b can be calculated
- From similar triangles:

$$\frac{b}{D} = \frac{|\tilde{i} - i|}{\tilde{i}}$$

- So, the blur circle diameter:

$$b = \frac{D}{\tilde{i}} |\tilde{i} - i|$$

$$b \propto D \propto \frac{1}{N}$$

Blur Circle (Defocus)

Focused Point

$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$$

$$i = \frac{of}{o-f}$$

Defocused Point

$$\frac{1}{i'} + \frac{1}{o'} = \frac{1}{f}$$

$$i' = \frac{o'f}{o'-f}$$

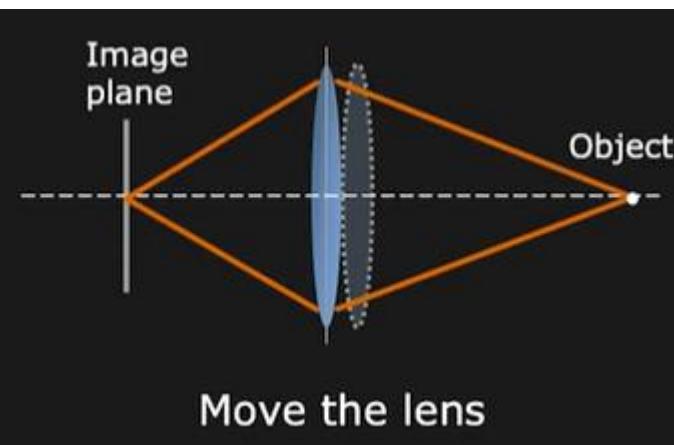
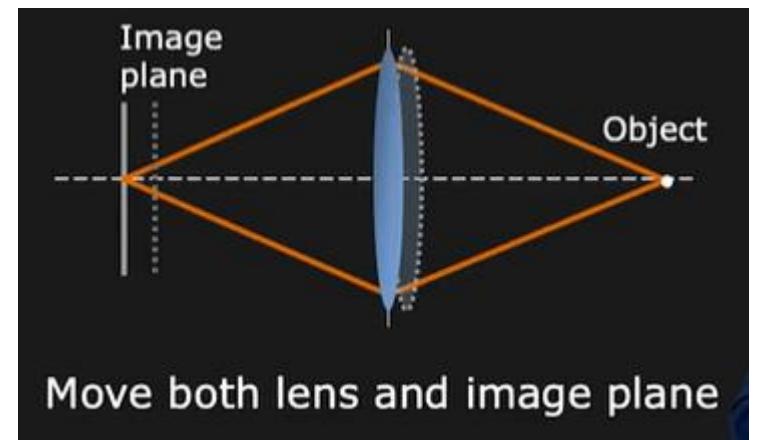
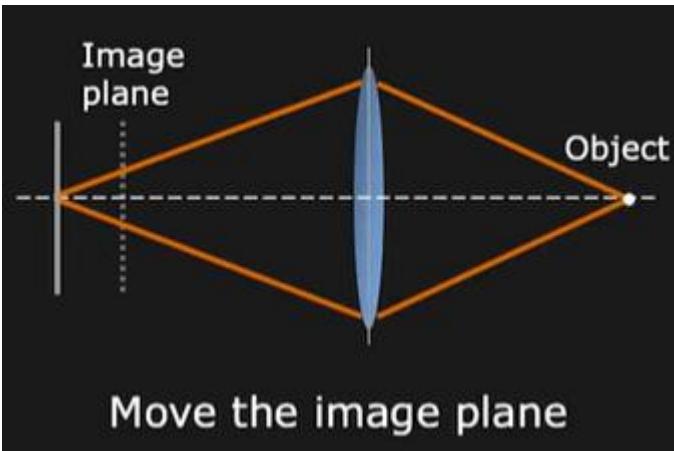
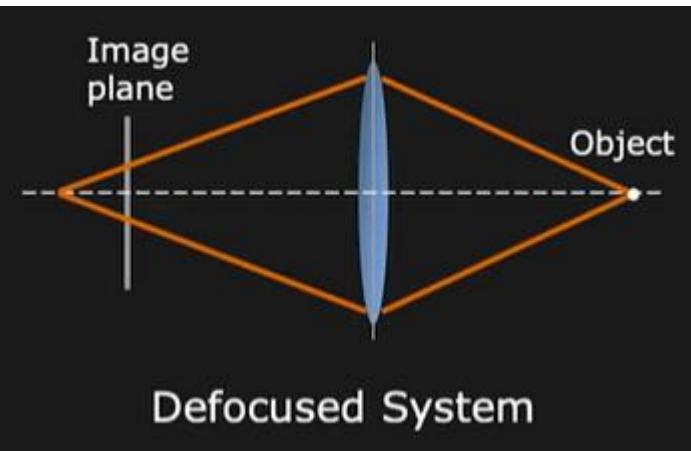
Gaussian Lens Law

$$i' - i = \frac{f}{(o' - f)} \times \frac{f}{(o - f)} \times (o - o')$$

$$b = Df \left| \frac{o - o'}{o'(o - f)} \right|$$

$$b = \frac{f^2}{N} \left| \frac{o - o'}{o'(o - f)} \right|$$

Focusing



Thank you