THE SAGE ENGINE

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1. Sage

Sage is an open source alternative to Magma, Maple, Mathematica, and Matlab. It is available as free download from http://www.sagemath.org/. The program provides all of the standard features expected from a mathematics software system: arbitrary precision arithmetic, symbolic integration and differentiation, two-dimensional plotting of functions, matrix algebra, and much more.

The SageTeX LaTeX style is an extra utility available from the Sage site. It allows users to embed and process Sage code from within TeX files. The last three pages of this document show this style file in action. One page of source is followed by two pages of output. In the source file, the initial line

%!TEX TS-program = sage

tells TeXShop to process the file using the sage engine; this engine first calls pdflatex, then calls sage, and finally calls pdflatex again. The remaining lines in the preamble are standard LaTeX commands, except the required line

\usepackage{sagetex}

In the remaining source, sage commands are entered within lines of the form

These line cause sage to process commands and output LaTeX source, which becomes part of the LaTeX document.

Notice in particular that sage can plot standard functions. Look carefully at the command which processes $\int \frac{x^2+x+1}{(x-1)^3(x^2+x+2)}$. This commands contains standard LaTeX code to display the integral, but then Sage actually integrates and returns a typeset copy of the result.

2. Setting Up the Engine

This folder contains an engine file named "sage.engine". Move this file to the active portion of /Library/TeXShop/Engines. This engine file assumes that Sage was installed in

/Applications, producing a folder named sage which contains a script named sage. If Sage was installed in a different location, edit sage.engine appropriately.

This folder also contains a Python file named "sagetex.py". Move this to /Applications/sage/. If you do not have write permission for this location, move the file to a different location of your choosing, for instance a location in your home folder. You can also place sagetex.py directly in the folder containing your source, but this is awkward if you have several folders containing different source files.

Finally, this folder contains a style file named "sagetex.sty". This file should be installed in a texmf tree in your system; it is easiest to put it in \sim /Library/texmf/tex/latex. Here \sim /Library is the Library folder in your home directory. You may have to create the subfolders texmf, tex, and latex.

The sagetex.sty file contains a line giving a path to sagetex.py. If you didn't put this Python file in /Applications/sage/, you will need to edit sagetex.sty as follows. Examine the section between lines 46 and 53 of the file. If the "iffalse" and "fi" lines at the beginning and end are uncommented, then sagetex.sty fill look for sagetex.py in the folder containing your TeX source. Otherwise, edit the line

\ST@wsf{sys.path.insert(0, '/Applications/sage')}

replacing "/Applications/sage" with a complete path to the folder containing your sagetex.py file.

The files "sagetex.py" and "sagetex.sty" are available in the Utilities section of the Sage download page, see http://www.sagemath.org/download-mac.html. It is likely that these files will change as Sage and the SageTeX packages are updated. Consequently, it would be safest to download the latest versions rather than using the files provided in this folder. If you do that, you will definitely need to edit sagetex.sty to point to the correct install location for sagetex.py.

3. Final Remarks

Although spaces are permitted in LaTeX source file names, Sage does not like such spaces. So LaTeX source file names which call SageTeX should not contain spaces.

A Sage tutorial is available for download at the Sage page http://www.sagemath.org/help.html. It is definitely recommended. Extensive additional documentation is available from the same web page.

```
% !TEX TS-program = sage
```

% The following lines are standard LaTeX preamble statements.

\documentclass[11pt, oneside]{amsart}

\usepackage{geometry}

\geometry{letterpaper}

\usepackage[parfill]{parskip}

\usepackage{graphicx}

\usepackage{amssymb}

\usepackage{epstopdf}

\title{Brief Article}

\author{The Author}

% Only one command is required to use Sage within the LaTeX source:

\usepackage{sagetex}

\begin{document}

\maketitle

\section{Introduction}

This is an example of using Sage within a \TeX\ document. We can compute extended values like

$$$32^{31} = sge{32^31}$$
\$

We can plot functions like \$x \sin x\$:

 $\frac{5 n}{plot(x * sin(30 * x), -1, 1)}$

We can integrate:

 $\pi {(x^2 + x + 1) \circ (x^2 + x + 2)} dx = sage{integrate((x^2 + x + 1) / ((x - 1)^3 * (x^2 + x + 2)))}$

\newpage

We can perform matrix calculations:

\$\$\sage{matrix([[1, 2, 3], [4, 5, 6], [7, 8, 9]])^3}\$\$

 $AB= \sum_{[1, 2], [3, 4]} \sage{Matrix([5, 6], [6, 8]])} = \sage{Matrix([1, 2], [3, 4]]) * Matrix([5, 6], [6, 8]])}$

Plots are fun; here is a second one showing \$x \ln x\$. The ``width" command in the source is sent to the include graphics command in LaTeX rather than to Sage.

 $\square{1} \operatorname{sageplot}[\operatorname{width=5in}] \left\{ \operatorname{plot}(x * \ln(x), 0, 2) \right\}$

Sage understands mathematical constants and writes them symbolically unless it is told to produce a numerical approximation. The term \$e \pi\$ below is not in the LaTeX source; instead it is the result of a Sage calculation, as is the numerical value on the other side of the equal sign.

The product of e and $\phi = \frac{n * e}{n * e} = \frac{N(pi * e)}{.}$

\end{document}

BRIEF ARTICLE

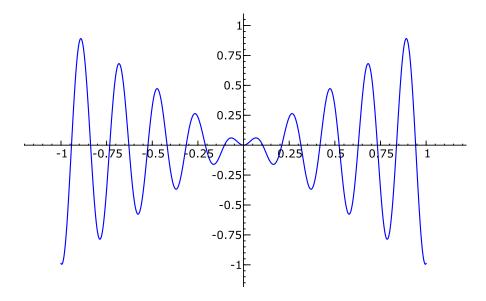
THE AUTHOR

1. Introduction

This is an example of using Sage within a T_EX document. We can compute extended values like

$$32^{31} = 45671926166590716193865151022383844364247891968$$

We can plot functions like $x \sin x$:



We can integrate:

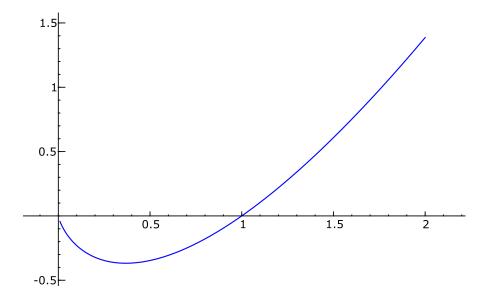
$$\int \frac{x^2 + x + 1}{(x - 1)^3 (x^2 + x + 2)} dx = \frac{5 \log \left(x^2 + x + 2\right)}{128} - \frac{9 \tan^{-1} \left(\frac{2x + 1}{\sqrt{7}}\right)}{64 \sqrt{7}} - \frac{5 \log \left(x - 1\right)}{64} - \frac{3x + 3}{16x^2 - 32x + 16}$$

We can perform matrix calculations:

$$\begin{pmatrix} 468 & 576 & 684 \\ 1062 & 1305 & 1548 \\ 1656 & 2034 & 2412 \end{pmatrix}$$

$$AB = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} 5 & 6 \\ 6 & 8 \end{pmatrix} = \begin{pmatrix} 17 & 22 \\ 39 & 50 \end{pmatrix}$$

Plots are fun; here is a second one showing $x \ln x$. The "width" command in the source is sent to the include graphics command in LaTeX rather than to Sage.



Sage understands mathematical constants and writes them symbolically unless it is told to produce a numerical approximation. The term $e\pi$ below is not in the LaTeX source; instead it is the result of a Sage calculation, as is the numerical value on the other side of the equal sign.

The product of e and π is $e\pi = 8.53973422267357$.