

ANALITIK COZUM"  
q0 = {0, 0, 0};  
dq0 = {1, 0, 0};  
q = Sum[  
(Um[[All, i]].M.q0 \* Cos[wi[[i]] \* t] + 1 / wi[[i]] \* Um[[All, i]].M.dq0 \* Sin[wi[[i]] \* t]) \*  
Um[[All, i]] , {i, 1, 3}]

ANALITIK COZUM

{-0.193239 (0. Cos[0.693019 t] - 0.278837 Sin[0.693019 t]) +  
0.932324 (0. Cos[0.982431 t] + 0.948997 Sin[0.982431 t]) -  
0.305665 (0. Cos[2.07715 t] - 0.147156 Sin[2.07715 t]) ,  
-4.89838 (0. Cos[0.693019 t] - 0.278837 Sin[0.693019 t]) -  
1.00213 (0. Cos[0.982431 t] + 0.948997 Sin[0.982431 t]) +  
0.0400656 (0. Cos[2.07715 t] - 0.147156 Sin[2.07715 t]) ,  
-0.219607 (0. Cos[0.693019 t] - 0.278837 Sin[0.693019 t]) +  
1.22883 (0. Cos[0.982431 t] + 0.948997 Sin[0.982431 t]) +  
3.88695 (0. Cos[2.07715 t] - 0.147156 Sin[2.07715 t])}

"SolutionBySolver "

TIME = 10;

X = {x1[t], x2[t], x3[t]};

D2X = D[X, {t, 2}];

Eqs = {0, 0, 0};

Table[Eqs[[i]] = (M.D2X + K.X)[[i]] == 0, {i, 1, 3}];

Eqs // MatrixForm

vars = {x1, x2, x3}

IC = {x1[0] == 0, x2[0] == 0, x3[0] == 0, x1'[0] == 1, x2'[0] == 0, x3'[0] == 0}

NDSolve[Flatten[{Eqs, IC}], vars, {t, 0, TIME}, AccuracyGoal -> 16,

PrecisionGoal -> 16, Method -> "ExplicitRungeKutta", MaxSteps -> ∞]

Plot[Evaluate[x1[t] /. %], {t, 0, TIME}]

Plot[q[[1]], {t, 0, TIME}]

Plot[q[[1]] - Evaluate[x1[t] /. dsol], {t, 0, TIME}, PlotRange -> All]

SolutionBySolver

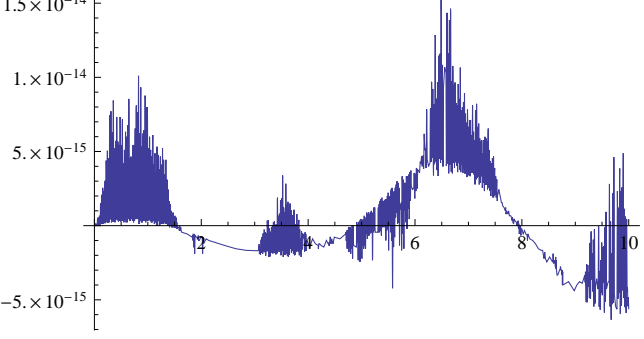
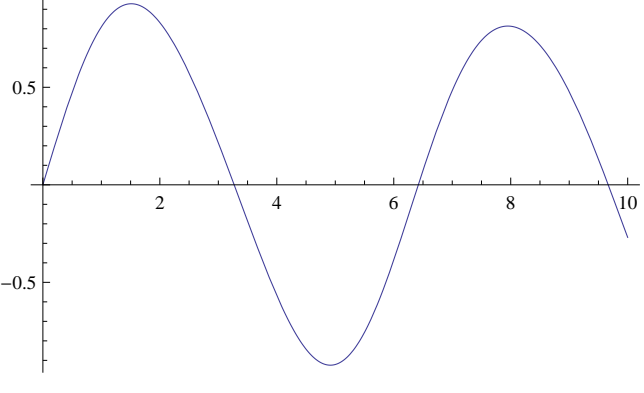
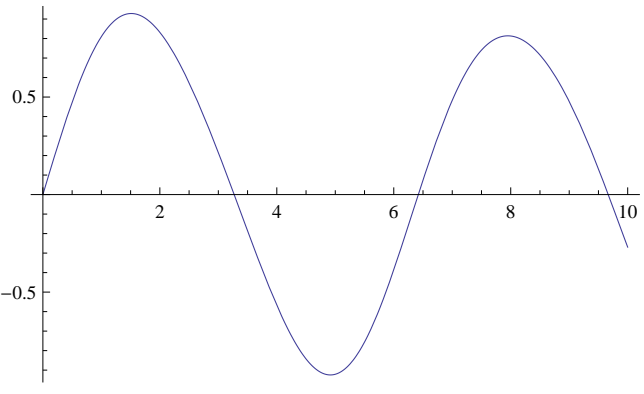
$$\begin{pmatrix} 1.26 x_1[t] - 0.02 x_2[t] - 0.24 x_3[t] + x_1''[t] = 0 \\ -0.02 x_1[t] + 0.02 x_2[t] + 0.04 x_2''[t] = 0 \\ -0.24 x_1[t] + 0.24 x_3[t] + 0.06 x_3''[t] = 0 \end{pmatrix}$$

{x1, x2, x3}

{x1[0] == 0, x2[0] == 0, x3[0] == 0, x1'[0] == 1, x2'[0] == 0, x3'[0] == 0}

{{x1 -> InterpolatingFunction[{{0., 10.}}, <>], x2 -> InterpolatingFunction[{{0., 10.}}, <>],

x3 -> InterpolatingFunction[{{0., 10.}}, <>]}}



"FOR HARMONIC EXCITATIONS "

Q0 = {1, 0, 0};

α = 0.5;

Q[t\_] = Q0 \* Cos[α \* t];

% // MatrixForm

NF = Table[Um[[All, i]].Q0 \* Cos[α \* t], {i, 1, 3}];

% // MatrixForm

qharm = Sum[ Um[[All, i]] / wi[[i]] \*  
Integrate[Q[t - τ] \* Sin[wi[[i]] \* τ], {τ, 0, t}].Um[[All, i]] , {i, 1, 3}];

% // MatrixForm

Plot[qharm[[1]], {t, 0, TIME}]

Table[Eqs[[i]] = (M.D2X + K.X)[[i]] == Q0[[i]] \* Cos[α \* t], {i, 1, 3}];

IC = {x1[0] == 0, x2[0] == 0, x3[0] == 0, x1'[0] == 0, x2'[0] == 0, x3'[0] == 0};

NDSolve[Flatten[{Eqs, IC}], vars, {t, 0, TIME}, AccuracyGoal -> 16,

PrecisionGoal -> 16, Method -> "ExplicitRungeKutta", MaxSteps -> ∞];

Plot[Evaluate[x1[t] /. dsol2], {t, 0, TIME}]

Plot[qharm[[1]] - Evaluate[x1[t] /. dsol2], {t, 0, TIME}, PlotRange -> All]

FOR HARMONIC EXCITATIONS

$$\begin{pmatrix} \cos[0.5 t] \\ 0 \\ 0 \end{pmatrix}$$

$$\begin{pmatrix} -0.193239 \cos[0.5 t] \\ 0.932324 \cos[0.5 t] \\ -0.305665 \cos[0.5 t] \end{pmatrix}$$

$$\begin{pmatrix} 0.0538821 (3.00952 \cos[0.5 t] - 3.00952 \cos[0.693019 t] + 0. i \sin[0.5 t] + 0. i \sin[0.693019 t]) + 0.884772 (1.3737 \cos[0.5 t] - 1.3737 \cos[0.982431 t] + 0. i \sin[0.5 t] + 0. i \sin[0.982431 t]) + 0.0449804 (0.51104 \cos[0.5 t] - 0.51104 \cos[2.07715 t] + 0. i \sin[0.5 t] + 0. i \sin[2.07715 t]) \\ 1.36585 (3.00952 \cos[0.5 t] - 3.00952 \cos[0.693019 t] + 0. i \sin[0.5 t] + 0. i \sin[0.693019 t]) - 0.95102 (1.3737 \cos[0.5 t] - 1.3737 \cos[0.982431 t] + 0. i \sin[0.5 t] + 0. i \sin[0.982431 t]) - 0.00589589 (0.51104 \cos[0.5 t] - 0.51104 \cos[2.07715 t] + 0. i \sin[0.5 t] + 0. i \sin[2.07715 t]) \\ 0.0612345 (3.00952 \cos[0.5 t] - 3.00952 \cos[0.693019 t] + 0. i \sin[0.5 t] + 0. i \sin[0.693019 t]) + 1.16616 (1.3737 \cos[0.5 t] - 1.3737 \cos[0.982431 t] + 0. i \sin[0.5 t] + 0. i \sin[0.982431 t]) - 0.571988 (0.51104 \cos[0.5 t] - 0.51104 \cos[2.07715 t] + 0. i \sin[0.5 t] + 0. i \sin[2.07715 t]) \end{pmatrix}$$

