

$$k \log[1 + x[t]]$$

Sistemin Toplam Kinetik Enerjisi:

$$\frac{1}{2} \sum_{i=2}^n m_i (x_i)'[t]^2 + \frac{1}{2} M_N (x_N)'[t]^2$$

Sistemin Toplam Potansiyel Enerjisi:

$$\sum_{i=2}^n k_i (-x_i[t] + \log[1 + x_i[t] - x_N[t]] (1 + x_i[t] - x_N[t]) + x_N[t]) + K_N (-x_N[t] + \log[1 + x_N[t]] (1 + x_N[t]))$$

Lagrange Eşitliği:

$$-\sum_{i=2}^n k_i (-x_i[t] + \log[1 + x_i[t] - x_N[t]] (1 + x_i[t] - x_N[t]) + x_N[t]) + \frac{1}{2} \sum_{i=2}^n m_i (x_i)'[t]^2 - K_N (-x_N[t] + \log[1 + x_N[t]] (1 + x_N[t])) + \frac{1}{2} M_N (x_N)'[t]^2$$

Hareketin Diferansiyel Denklemlerinin Euler Lagrange Denklemlerinden Çıkarılması:

$$\frac{\partial L}{\partial x_i(t)} - \frac{\partial}{\partial t} \frac{\partial L}{\partial \frac{\partial x_i(t)}{\partial t}} = 0 \quad \frac{\partial L}{\partial x_N(t)} - \frac{\partial}{\partial t} \frac{\partial L}{\partial \frac{\partial x_N(t)}{\partial t}} = 0$$

$$-\sum_{i=2}^n \log[1 + x_i[t] - x_N[t]] k_i - \frac{1}{2} \sum_{i=2}^n 2 m_i (x_i)''[t] = 0$$

$$-\log[1 + x_N[t]] K_N - \sum_{i=2}^n -\log[1 + x_i[t] - x_N[t]] k_i - M_N (x_N)''[t] = 0$$

Sistemin Lineerize Edilmiş Hali:

Kinetik En:

$$\frac{1}{2} \sum_{i=2}^n m_i (x_i)'[t]^2 + \frac{1}{2} M_N (x_N)'[t]^2$$

Pot En:

$$\sum_{i=2}^n (0.0721318 k_i (x_i[t] - x_N[t]) + 0.333333 k_i (x_i[t] - x_N[t])^2) + 0.0721318 K_N x_N[t] + 0.333333 K_N x_N[t]^2$$

Lagrange Eq:

$$-\sum_{i=2}^n (0.0721318 k_i (x_i[t] - x_N[t]) + 0.333333 k_i (x_i[t] - x_N[t])^2) + \frac{1}{2} \sum_{i=2}^n m_i (x_i)'[t]^2 - 0.0721318 K_N x_N[t] - 0.333333 K_N x_N[t]^2 + \frac{1}{2} M_N (x_N)'[t]^2$$

$$-\sum_{i=2}^n (0.0721318 k_i + 0.666667 k_i (x_i[t] - x_N[t])) - \frac{1}{2} \sum_{i=2}^n 2 m_i (x_i)''[t] = 0$$

$$-0.0721318 K_N -$$

$$\sum_{i=2}^n (-0.0721318 k_i - 0.666667 k_i (x_i[t] - x_N[t])) - 0.666667 K_N x_N[t] - M_N (x_N)''[t] = 0$$

{Spring Force vs Displacement $F = \log(x(t) + 1)$, $F_{lin} = 0.666667 (x(t) - 0.5) + 0.405465$ }

