Forward and Backward Private **DSSE** for Range Queries

Cong Zuo[®], Shi-Feng Sun[®], Joseph K. Liu[®], Jun Shao[®], Josef Pieprzyk[®], and Lei Xu[®]

Abstract—Due to its capabilities of searches and updates over the encrypted database, the dynamic searchable symmetric encryption (DSSE) has received considerable attention recently. To resist leakage abuse attacks, a secure DSSE scheme usually requires forward and backward privacy. However, the existing forward and backward private DSSE schemes either only support single keyword queries or require more interactions between the client and the server. In this article, we first give a new leakage function for range queries, which is more complicated than the one for single keyword queries. Furthermore, we propose a concrete forward and backward private DSSE scheme by using a refined binary tree data structure. Finally, the detailed security analysis and extensive experiments demonstrate that our proposal is secure and efficient, respectively.

Index Terms—Dynamic searchable symmetric encryption, forward privacy, backward privacy, range queries

INTRODUCTION

UTSOURCING data to the cloud is a cost-effective and reliable way to store large amounts of data. However, at the same time, it exposes data to a server that is not always trusted. Hence, the security and privacy of outsourced data should be addressed before using cloud storage. A simple method to mitigate these problems is to encrypt data before outsourcing. Unfortunately, encryption reduces the usability, especially the searchability, of the data due to the nature of encryption. To solve this problem, searchable symmetric encryption (SSE) has been introduced [1], [2]. It encrypts the data while preserving the searchability of the data. Compared with other techniques for enabling searchability over ciphertexts [3], [4], the clear advantages of SSE is its efficiency.

Traditional SSE schemes cannot support updates over an encrypted database. This substantially limits its applications. To support updates of encrypted databases, dynamic SSE (DSSE) has been proposed in [5], [6]. However, updates leak information about data (see [7]). Zhang et al. [8]

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demonstrated file-injection attacks that break the privacy of client queries by injecting a small number of files to an encrypted database. To deal with the attacks, forward and backward privacy notions have been introduced informally in [9]. Later, the notions have been formalized in [10] and [11], respectively. In particular, Bost et al. [11] defined three different levels of backward privacy, namely, Type-I, Type-II and Type-III, where Type-I is the most secure and Type-III is the least secure. Many other forward and backward private DSSE schemes have also been proposed (see [11], [12] for instance). Unfortunately, a majority of published forward and backward private DSSE schemes support single keyword queries only. This greatly reduces their useability. In many applications, we need more expressive search queries, such as range queries, for instance.

Consider range queries. In a naïve solution, one could query all possible values in a range. This solution is not efficient if the range is large as it requires a large communication overhead. To process range queries more efficiently and reduce communication cost, Faber et al. [13] applied a binary tree to the OXT scheme of Cash et al. [14]. Their solution works for static databases only and does support updates. Zuo et al. [15] designed two DSSE schemes using a new binary tree data structure. Their schemes support both range queries and updates. Their first scheme (SchemeA) based on the framework of [10] achieves forward privacy. However, it inherits low efficiency of the scheme from [10] due to the application of computationally expensive public-key cryptographic operations. For the second scheme (SchemeB), the authors combined the bit string representation with the Paillier encryption [16]. The second scheme achieves backward privacy. The maximum number of files the scheme can support is equal to the length of the message space for the Paillier encryption. For a typical implementation, the message length is very small (around 1,024 bits) and therefore a scheme can support a limited number of files. To reduce storage requirements, the authors homomorphically add the

TABLE 1
Comparison to Previous Works

Scheme	Forward Privacy	Backward Privacy	Range Queries	Number of Roundtrips
FIDES [11]	√	Type-II	×	2
$DIANA_{del}$ [11]	\checkmark	Type-III	×	2
Janus [11]	\checkmark	Type-III	×	1
Janus++ [12]	\checkmark	Type-III	×	1
MONETA [11]	\checkmark	Ťype-I	×	3
FB-DSSE [18]	\checkmark	Type-I ⁻	×	1
SchemeA[15]	\checkmark	×	\checkmark	1
SchemeB[15]	×	Unknown	\checkmark	1
Generic [17]	\checkmark	×	\checkmark	1
Extension [17]	\checkmark	Type-II	\checkmark	2
Our scheme	\checkmark	Type-R	\checkmark	1

ciphertexts and consequently their scheme loses forward privacy. In addition, they did not provide a detailed backward privacy analysis. Later, Wang et al. [17] suggested a generic forward private DSSE with range queries by adapting the ShemeA from [15]. To achieve backward privacy, they extended their scheme by applying the generic backward private construction of [11]. Unfortunately, to support the backward privacy, their scheme requires another roundtrip between the client and the server. In other words, the client needs to re-encrypt the matched files and send them back to the server, which is not efficient.

Recently, Zuo *et al.* [18] designed an efficient DSSE scheme with forward and stronger backward privacy by combining the bitmap index with simple symmetric encryption with homomorphic addition. To support very large databases, they extended their first scheme to multiple block setting. However, their schemes support single keyword queries only.

Our Contributions. We develop an efficient forward and backward private DSSE scheme that supports range queries by extending the scheme from the work [18]. The scheme is further called FBDSSE-RQ. It requires one roundtrip only. The comparison with previous works is given in Table 1. The list given below details our contributions.

- First, we refine the construction of the binary tree from [15]. For our binary tree, we label all nodes by keywords. Names of nodes are derived from their leaf nodes rather than from the order of node insertion (see Section 2.2 for more details). We also modify algorithms for the binary tree.
- We define a new backward privacy for our range queries named Type-R. Compared with single keyword queries, range queries introduce more leakages. We map a range query into several keywords that are assigned to nodes of our binary tree. For a range search query [a, b], a query leaks the number of keywords, the total number of updates and update time for each keyword, the repetition of these keywords and the final results for the range query, ¹ and

- for the update with value v, it leaks the number of keywords that have been updated (the number of levels of the binary tree). See Sections 4 and 5 for details.
- We describe a forward and Type-R backward private DSSE for range queries. The scheme called FBDSSE-RQ uses our refined binary tree and is based on the FB-DSSE from [18]. In addition, it only requires one roundtrip. Our scheme is more efficient than the extension scheme from [19]. For every search, the scheme from [19] needs to re-encrypt the search results and send them back to the server, which incurs high computational and communication costs. See Section 5 for details.
- Finally, the security analysis and implementation experiments demonstrate that the scheme achieves claimed security goals and is practical.

1.1 Related Work

Searchable symmetric encryption (SSE) was introduced by Song *et al.* [1]. In their scheme, a client encrypts every keyword of a file. For a search query, the client first encrypts a keyword and then finds a match by comparing the (encrypted) keyword to (encrypted) keywords of all the files. As a result, the search time is linear with the number of file/keyword pairs. To reduce the search time, Curtmola *et al.* [2] deployed an inverted index data structure. Consequently, their SSE scheme obtains sublinear search time. In [2], the authors formally defined the SSE security model. There is a large number of followup papers studying different aspects of SSE. For instance, SSE with expressive queries is examined in [13], [14], [15], SSE for multi-client setting is explored in [2], [19], dynamic SSE – in [5], [6] and locality SSE – in [20], [21].

Once a database is encrypted, SSE schemes do not allow to update the encrypted database. To support updates of the encrypted database, dynamic SSE (DSSE) schemes have been introduced in [5], [6]. Early DSSE schemes are, however, vulnerable to file-injection attacks [7], [8]. To deal with the attacks, forward and backward privacy have been informally introduced in [9]. Bost [10] formalized the forward privacy. Later Bost *et al.* [11] defined three levels of backward privacy (Type-I to Type-III, ordered from the most to the least secure). Sun *et al.* [12] designed a DSSE called Janas++, which achieves Type-III backward privacy by replacing (public-key) puncturable encryption (PE) with symmetric puncturable encryption (SPE).

A majority of forward and/or backward private DSSE schemes support single keyword queries only. Faber *et al.* [13] constructed an SSE scheme that accepts range queries. The scheme applies a binary tree data structure to the OXT scheme of Cash *et al.* [14]. However, the scheme is static (does not allow updates). To design a DSSE for range queries, Zuo *et al.* [15] deployed a new binary tree data structure. They described two solutions. The first one is based on the scheme by Bost [10]. It achieves forward privacy. The second solution applies the Paillier cryptosystem [16], and it is backward private. Unfortunately, the solution can support a limited number of files only. This weakness is due to a limited length of the message space of the Paillier

^{1.} If a=b, the leakage of the search query would be same as Type-I $^-$. Moreover, Type-R does not leak the insertion time of each file identifier while Type-II does.

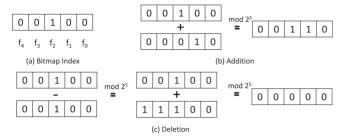


Fig. 1. Illustration of bitmap index operations.

cryptosystem. Wang et al. [17] designed a generic forward private DSSE for range queries. The generic construction applies the framework of SchemeA from [15]. They also extended their first scheme by integrating the generic backward private construction from [11]. The scheme achieves Type-II backward privacy. The scheme, however, requires two roundtrips between the client and the server, which is not efficient. Independently, Demertzis et al. [22] developed several SSE schemes for range queries with different security and efficiency tradeoffs by using the binary tree data structure. To support updates, they deploy several independent SSE instances and periodically consolidate them. As far as information leakage is concerned, the schemes leak not only the number of keywords queried but also the level of each keyword in the binary tree.

Recently, Zuo *et al.* [18] introduced a forward and stronger backward private DSSE, which requires one roundtrip only. Moreover, they introduced a new notion of backward privacy (named Type-I⁻). Compared to Type-I [11], Type-I⁻ does not leak the insertion time of matching files. This is achieved by deploying a bitmap index and a simple symmetric encryption with homomorphic addition. Experiments show that the DSSE scheme is efficient and practical. Nevertheless, it can support single keyword queries only. To the best of our knowledge, there is no forward and backward private DSSE that can process range queries with one roundtrip only.

There is also another line of investigation that explores the usage of trusted hardware (SGX) in order to obtain secure DSSE (see [23], [24], for example). In this paper, we focus on constructing a secure DSSE without a trusted third party. The readers, who are interested in this aspect of DSSE design, are referred to [23], [24].

1.2 Organization

The remaining sections are organized as follows. In Section 2, we give the necessary background information and preliminaries. In Section 3, we define our DSSE model. The forward and backward privacy notions for our range queries are given in Section 4. In Section 5, we give our forward and backward private DSSE for range queries. The security analysis is given in Section 3.2. Section 7 discusses implementation of our scheme and its efficiency. Finally, Section 8 concludes the work.

2 PRELIMINARIES

let λ be the security parameter. We use a bitmap index to represent file identifiers in the same way as in [18]. For a database with y files, we set a bit string bs of length y. If there

exists file f_i , we set the ith bit of bs to 1. Otherwise, it is set to 0. Fig. 1 illustrates setup, addition and deletion of file identifiers. In particular, Fig. 1a shows a bitmap index for a database that can store up to y=5 files. The index tells us that the database contains a single file f_2 . Fig. 1b illustrates addition of file f_1 to the database, i.e., the bit string 00010 (that corresponds to f_1) is added to the index. Fig. 1c displays operations on the index, when the file f_2 is deleted from the database. This can be done either by subtracting the string 00100 from the index or by adding $-(00100)_2 = (11100)_2$ to the index (note that operations are performed modulo 2^5).

2.1 Simple Symmetric Encryption With Homomorphic Addition

Following [25], a simple symmetric encryption with homomorphic addition $\Pi = (\texttt{Setup}, \texttt{Enc}, \texttt{Dec}, \texttt{Add})$ is described by following four algorithms:

- $n \leftarrow \text{Setup}(1^{\lambda})$: For a security parameter λ , it outputs a public parameter n, where $n = 2^{y}$ and y is the maximum number of files a scheme can support.
- $c \leftarrow \operatorname{Enc}(sk, m, n)$: For a message m $(0 \le m < n)$, a public parameter n and a random secret key sk $(0 \le sk < n)$, it computes a ciphertext $c = sk + m \mod n$. For every encryption, the secret key sk needs to be stored, and it can be used once only.
- m ← Dec(sk, c, n): For a ciphertext c, a public parameter n and a secret key sk, it recovers the message m = c sk mod n.
- $\hat{c} \leftarrow \operatorname{Add}(c_0, c_1, n)$: For two ciphertexts c_0 , c_1 and a public parameter n, it computes $\hat{c} = c_0 + c_1 \operatorname{mod} n$, where $c_0 \leftarrow \operatorname{Enc}(sk_0, m_0, n)$, $c_1 \leftarrow \operatorname{Enc}(sk_1, m_1, n)$, $n \leftarrow \operatorname{Setup}(1^{\lambda})$ and $0 \leq sk_0, sk_1 < n$.

We claim that the above defined encryption supports homomorphic addition, in the sense that, knowing two ciphertexts $c_0 = m_0 + sk_0 \bmod n$ and $c_1 = m_1 + sk_1 \bmod b$, anybody can create $\hat{c} = c_0 + c_1 \bmod n$. However, to decrypt \hat{c} and recover $m_0 + m_1 \bmod n$, one needs to know $sk_0 + sk_1 \bmod n$. To prove validity of the claim, it is enough to check that

$$Dec(\hat{sk}, \hat{c}, n) = \hat{c} - \hat{sk} \bmod n = m_0 + m_1 \bmod n,$$

where $\hat{sk} = sk_0 + sk_1 \mod n$.

Note that Π enjoys perfect security as long as secret keys are used once only. To see that this is true is enough to note that our encryption becomes the well-know one-time pad (OTP) when the secret key is chosen randomly and uniformly for each new message.

Perfectly Security [25]. We say Π is perfectly secure if for any adversary A, its advantage is negligible or

$$\begin{split} \mathbf{Adv}^{\mathrm{PS}}_{\Pi,\mathcal{A}}(\lambda) &= |\Pr[\mathcal{A}(\mathsf{Enc}(sk,m_0,n)) = 1] \\ &- \Pr[\mathcal{A}(\mathsf{Enc}(sk,m_1,n)) = 1]| \leq \epsilon, \end{split}$$

where $n \leftarrow \text{Setup}(1^{\lambda})$, the secret key sk ($0 \le sk < n$) is kept secret and \mathcal{A} chooses m_0, m_1 s.t. $0 \le m_0, m_1 < n$.

2.2 Binary Tree

We revisit the binary tree BT from [15]. For simplicity, we always use a perfect (a.k.a. full) binary tree and denote its root root as BT. A perfect binary tree is a binary tree with 2^{ℓ}

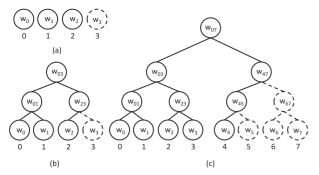


Fig. 2. Binary tree.

leaf nodes, where $\ell+1$ is the number of levels. The root exists at the level 0 and leaves belong to the level ℓ . For range queries on attribute A (e.g., age) with range $R = \{0, 1, \dots, d-1\}$, each leaf of BT is associated with a value v from R. For example, in Fig. 2a, d is 3. To form a perfect binary tree, we need to add an additional leaf (the dotline node in Fig. 2a). For Fig. 2c, d is 5. Every node in BT has three pointers, which are initially set to null. The three pointers are parent, left and right. The parent links the node with its parent. The pointers left and right connect the node with its left and right children, respectively. We also define the leftmost child and righmost child. The leftmost leaf is a node, which is the left child of its parent and all parents are left children of their ancestors. The rightmost leaf is defined similarly but for right child. For example, in Fig. 2b, w_0 is the *leftmost* leaf of w_{03} and w_3 is the *rightmost* leaf of w_{03} . Now, we are ready to describe a collection of algorithms for BT (see Algorithm 1 for precise definition).

- BT \leftarrow TGen(d): It takes d and outputs a perfect binary tree BT for 2^ℓ leaf nodes, where $2^{\ell-1} < d \le 2^\ell$ and ℓ is the smallest such integer. For example, Figs. 2b and 2c illustrate a tree constructed for d=3 and d=5 leaves, respectively.
- BRC \leftarrow TGetCover(q, BT): The algorithm takes a range q = [a, b] and a binary tree BT as its input and outputs the best range cover BRC that contains all leaves in the range [a, b], where $0 \le a < b < d$. Note that a BRC has to include the smallest number of parent nodes of leaves in the range. Consider the tree depicted in Fig. 2c, BRC = $\{w_{23}, w_4\}$ for range query q = [2, 4].
- PT ← TPath(v, BT): The algorithm takes a value v and a binary tree BT as its input and outputs a set PT of nodes that belong to the path traversing from the leaf w_v to the root, where 0 ≤ v < d. For instance, consider the tree in Fig. 2c. For v = 1 (or the leaf w₁), the set PT = {w₁, w₀₁, w₀₃, w₀₇}.

2.3 Notations

Notations used in the work are given in Table 2.

3 DSSE DEFINITION AND SECURITY MODEL

For range queries, we assume that each file f is characterised by an attribute A (e.g., age), whose value v belongs to the range $R = \{0, 1, \dots, d-1\}$. We assign the range values

2. If a = b, it becomes a single keyword query for keyword w_a .

to the leaves of our binary tree BT as shown in Fig. 2b. Consequently, each file contains not only the keyword of its leaf but also the keywords associated with its ancestors.

A database DB stores a list of file-identifier/keyword-set pairs or $\mathsf{DB} = (f_i, \mathbf{W}_i)_{i=1}^y$, where $f_i \in \{0,1\}^\lambda$ is the file identifier, \mathbf{W}_i is the keyword set and y is the total number of files in DB. For example, consider the tree from Fig. 2b, the file f_0 is associated with the range value 0 and contains keywords from the set $\mathbf{W}_0 = \{w_0, w_{01}, w_{03}\}$. We denote the collection of all distinct keywords in DB by $\mathbf{W} = \bigcup_{i=1}^y \mathbf{W}_i$. The notation $|\mathbf{W}|$ means the total number of keywords in the set \mathbf{W} (or cardinality of the set). The total number of file-identifier/keyword pairs is denoted by $N = \sum_{i=1}^y |\mathbf{W}_i|$.

Algorithm 1. Binary Tree

TGen(d)

```
1: if d < 0 then
 2: return
 3: else if d = 1 then
      Generate one node n and set this node as BT.
      Associate value 0 to this node and name it as w_0.
      return BT
 6:
 7: else
      Generate 2^{\ell} leaf nodes \gt 2^{\ell-1} < d < 2^{\ell}
      Associate each leaf node with each value v \in 2^{\ell} and name
       the corresponding leaf node as w_v.
10:
      for i = \ell - 1 to 0 do
11.
        Generate 2^i nodes.
12:
        for each node do
13:
             Set its left and right child to two consecutive nodes
             from previous level, where the value of its leftmost
            is even and the value of its rightmost is odd.
            Name this node as w_{ab}, where a and b are the values
14:
            associated with its leftmost and rightmost.
15:
        end for
16:
      end for
      Set the root node as BT
17.
18:
      return BT
19: end if
\mathtt{TGetCover}(q,\mathtt{BT}) \rhd q = [a,b], \mathtt{ where } 0 \leq a < b < d
1: BRC, Temp, Parent ← Empty Set
2: for i = a to b do
    \mathtt{Temp} \leftarrow \mathtt{Temp} \cup w_i

    ▷ Put all the leaf nodes to the temp set

                             Temp.
4: end for
5: while Temp \neq \perp do
     for two nodes in Temp have the same parent do
        Remove these two nodes from Temp, and put the parent
        node to the set Parent.
     end for
     Move the remaining nodes from Temp to BRC.
    \texttt{Temp} \leftarrow \texttt{Parent}, \texttt{Parent} \leftarrow \perp
11: end while
12: return BRC
TPath(v, BT)
1: PT ← Empty Set
2: w \leftarrow w_v
3: while w \neq \perp do
    \mathtt{PT} \leftarrow \mathtt{PT} \cup w
5:
    w \leftarrow w \cdot parent
6: end while
```

7: return PT

TABLE 2 Notations

\overline{v}	The value in a range query
BT	The full binary tree
$\ell + 1$	The number of levels of the binary tree, where the root
	is in level 0 and the leaves are in level ℓ
d	The boundary of our range query
R	The set of values for our range query $\{0, 1, \dots, d-1\}$
[a,b]	A range query
BRC	The set of least number of nodes to cover range $[a, b]$
PT	The set of nodes in the path from a leaf to the root
DB	A database
λ	The security parameter
ST_c	The current search token for a keyword w
EDB	The encrypted database EDB which is a map
F	A secure PRF
W	The set of all keywords of the database DB
CT	A map stores the current search token ST_c and counter
	c for every keyword in ${f W}$
f_i	The <i>i</i> th file
bs	The bit string which is used to represent the existence
	of files
y	The length of bs
e	The encrypted bit string
Sum_e	The sum of the encrypted bit strings
sk	The one time secret key
Sum_{sk}	The sum of the one time secret keys

A set of files that satisfy a range query q is denoted by DB (q). Note that we use the bitmap index to represent the file identifiers. For a search query q, the result is a bit string bs, which represents a list of file identifiers in $\mathrm{DB}(q)$. For an update query u, a bit string bs is used to update a list of file identifiers. Moreover, we isolate the actual files from the metadata (e.g., file identifiers). We focus on the search of the metadata only. We ignore the retrieval process of encrypted files from the database.

3.1 DSSE Definition

A DSSE scheme consists of an algorithm *Setup* and two protocols *Search* and *Update* that are executed between a client and a server. They are described as follows:

- (EDB, σ) ← Setup(1^λ, DB): For a security parameter λ and a database DB, the algorithm outputs a pair: an encrypted database EDB and a state σ. EDB is stored by the server and σ is kept by the client.
- (I, ⊥) ← Search(q, σ; EDB): For a state σ, the client issues a query q and interacts with the server who holds EDB. At the end of the protocol, the client outputs a set of file identifiers I that match q and the server outputs nothing.
- $(\sigma', \text{EDB}') \leftarrow \text{Update}(\sigma, op, in; \text{EDB})$: For a state σ , the operation $op \in \{add, del\}$ and a collection of $in = (f, \mathbf{w})$ pairs, the client requests the server (who holds EDB) to update database by adding/deleting files specified by the collection in. Finally, the protocol returns an updated state σ' to the client and an updated encrypted database EDB' to the server.

Remark. In literature, there are two result models for SSE schemes. In the first one (considered in the work [14]), the server returns encrypted file identifiers \mathcal{I} , so the client

needs to decrypt them. In the second one (studied in the work [10]), the server returns the file identifiers to the client as a plaintext. In our work, we consider the first variant, where the protocol returns encrypted file identifiers.

3.2 Security Model

DSSE security is modeled by the Real and Ideal worlds called DSSEREAL and DSSEIDEAL, respectively. The behavior of DSSEREAL is exactly the same as the original DSSE. However, DSSEIDEAL reflects a behavior of a simulator \mathcal{S} , which takes the leakages of the original DSSE as input. The leakages are defined by the function $\mathcal{L} = (\mathcal{L}^{Setup}, \mathcal{L}^{Search}, \mathcal{L}^{Update})$, which details what information the adversary \mathcal{A} can learn during execution of the Setup algorithm, Search and Update protocols.

If the adversary \mathcal{A} can distinguish DSSEREAL from DSSEIDEAL with a negligible advantage, we can say that leakage of information is restricted to the leakage \mathcal{L} . More formally, we consider the following security game. The adversary \mathcal{A} interacts with one of the two worlds DSSEREAL or DSSEIDEAL which are described as follows:

- DSSEREAL_A(λ): On input a database DB, which is chosen by the adversary A, it outputs EDB to A by running Setup(λ, DB). A performs search queries q (or update queries (op, in)). Eventually, A outputs a bit b, where b ∈ {0,1}.
- DSSEIDEAL_{A,S}(λ): Simulator S outputs the simulated EDB with the input $\mathcal{L}^{Setup}(\lambda, DB)$). For search queries q (or update queries (op,in)) generated by the adversary A, the simulator S replies by using the leakage function $\mathcal{L}^{Search}(q)$ (or $\mathcal{L}^{Update}(op,in)$). Eventually, A outputs a bit b, where $b \in \{0,1\}$.

Definition 1. Given a DSSE scheme and the security game described above. The scheme is \mathcal{L} -adaptively-secure if for every probabilistic polynomial time (PPT) adversary \mathcal{A} , there exists an efficient simulator \mathcal{S} (with the input \mathcal{L}) such that

$$\begin{split} |\Pr[\texttt{DSSEREAL}_{\mathcal{A}}(\lambda) = 1] - \Pr[\texttt{DSSEIDEAL}_{\mathcal{A},\mathcal{S}}(\lambda) = 1]| \\ &\leq negl(\lambda). \end{split}$$

Leakage Function. Before defining the leakage function, we define a range query $q = (t, [a, b]) = \{t, w\}_{w \in BRC}$, where BRC is the best range cover of range [a, b]. An update query u = $(t, op, (v, bs)) = \{t, op, (w, bs)\}_{w \in PT(v)}$, where t is the timestamp, PT contains all keywords in the path from the leaf node of v to the root, op is the update operation and bsdenotes a list of file identifiers to be updated. For a list of search queries Q, we define a search pattern $sp(q) = \{t : g \in A\}$ $\{t,w\}_{w\in BRC}$, where t is a timestamp and $q\in Q$. The search pattern leaks the repetition of search queries on q. Denote a result pattern rp(q) = bs, where bs represents all file identifiers that match the range query q. Note that, after a search query, we implicitly assume that the server knows the final result \overline{bs} , since the client may retrieve the file identifiers represented by bs which is not described in this paper. Moreover, the server can infer if a range query contains other range queries or not by looking at \overline{bs} .

4 FORWARD AND BACKWARD PRIVACY FOR OUR RANGE QUERIES

To support range queries, we incorporate the binary tree data structure (see Section 2.2 for details). For an update with a value v, we need to update every node (keyword) in the path from the corresponding leaf node to the root node, where the value v is within the boundaries of the current binary tree. For the update with a value v, we need to issue several updates (all keywords from the leaf to the root). Hence the number of updates (the number of levels of the binary tree) is leaked.

4.1 Forward Privacy

Informally, for any adversary who may continuously observe the interactions between the server and the client, forward privacy guarantees that an update does not leak information about the newly added files that match the previously issued queries. The definition given below is taken from [10]:

Definition 2. A \mathcal{L} -adaptively-secure DSSE scheme is forward-private if the update leakage function \mathcal{L}^{Update} can be written as

$$\mathcal{L}^{Update}(op, in) = \mathcal{L}'(op, \{(f_i, \mu_i)\}),$$

where f_i is the identifier of the modified file, μ_i is the number of keywords corresponding to the updated file f_i .

Remark. For our range query, the leakage function will be $\mathcal{L}^{Update}(op,v,bs)=\mathcal{L}'(op,bs,\ell+1)$, where $\ell+1$ is the number of levels of the full binary tree BT.

4.2 Backward Privacy

Given a time interval, in which two search queries for the same range occur. Backward privacy ensures that there is no leak of information about the files that have been previously added and later deleted. Note that information about files leak if the second search query is issued after the files are added but before they are deleted. In [18], Zuo *et al.* formulated a stronger level of backward privacy named Type-I⁻ for single keyword queries. To deal with range queries, we map a range query to several keywords. For our range queries, to update a value, we need to update every keyword, which contains this value. Hence the update leaks the number of keywords corresponding to the value, which is the number of levels of the binary tree $\ell+1$. This type of backward privacy is called Type-R.

Type-R: Given a time interval between two calls issued for a range query q. Then it leaks the files that currently match q, and the total number of updates and the time of each update for each w, where w ∈ BRC. The update of a leaf (value v) leaks the number of keywords corresponding to the value.

To define Type-R formally, we need to introduce Time. For a range query q, $\mathrm{Time}(q)$ lists the timestamp t of all updates corresponding to each w, where $w \in \mathrm{BRC}$. Formally, for a sequence of update queries Q'

$$Time(q) = \{t : (t, op, (w, bs))\}_{w \in BRC}$$

Definition 3. A \mathcal{L} -adaptively-secure DSSE scheme is Type-R backward-private iff the search and update leakage function \mathcal{L}^{Search} , \mathcal{L}^{Update} can be written as

$$\mathcal{L}^{Update}(op,v,bs) = \mathcal{L}'(op,\ell+1),$$
 $\mathcal{L}^{Search}(q) = \mathcal{L}''(\operatorname{sp}(q),\operatorname{rp}(q),\operatorname{Time}(q)),$

where \mathcal{L}' and \mathcal{L}'' are stateless, $\ell+1$ is the number of levels of the full binary tree BT.

5 FORWARD AND BACKWARD PRIVATE DSSE FOR RANGE QUERIES

Now, we are ready to give our forward and backward private DSSE for range queries. We call it FBDSSE-RQ and it is defined by Algorithm 2. Our DSSE is based on the framework of [18], a simple symmetric encryption with homomorphic addition $\Pi = (\text{Setup}, \text{Enc}, \text{Dec}, \text{Add})$, and a keyed PRF F_K with key K. The scheme is defined by the following algorithm and two protocols:

- (EDB, $\sigma = (n, d, K, \mathbf{CT})) \leftarrow \mathbf{Setup}(1^{\lambda})$: The algorithm is run by a client. It takes the security parameter λ as input. Then it chooses a secret key K and an integer n, where $n = 2^y$ and y is the maximum number of files that this scheme can support. Moreover, it sets the range query boundary d, two empty maps EDB and \mathbf{CT} , where $R = \{0, \ldots, d-1\}$ is set of values for our range queries and the two maps are used to store the encrypted database as well as the current search token ST_c and the current counter c (the number of updates) for each keyword $w \in \mathbf{W}$, respectively. Finally, it outputs encrypted database EDB and the state $\sigma = (n, d, K, \mathbf{CT})$. The client keeps (d, K, \mathbf{CT}) secret.
- $(\sigma', \mathtt{EDB'}) \leftarrow \mathbf{Update}(v, bs, \sigma; \mathtt{EDB})$: The protocol runs between a client and a server. The client inputs a value v ($v \in R$), a state σ and a bit string bs.³ The client updates each keyword $w \in PT$. For each keyword w, he/she encrypts the bit string bs by using the simple symmetric encryption with homomorphic addition to get the encrypted bit string e. To save the client storage, the one time key sk_c is generated by a hash function $H_3(K'_w, c)$, where c is the counter. Then he/ she chooses a random search token and use a hash function to get the update token. He/She also uses another hash function to mask the previous search token. After that, the client sends the update token, eand the masked previous search token C to the server and update CT to get a new state σ' . Finally, the server outputs an updated encrypted database EDB'.
- bs ← Search(q, σ; EDB): The protocol runs between a client and a server. The client inputs a range query q and a state σ, and the server inputs EDB. First, the client gets BRC. For each keyword w ∈ BRC, he/she gets the search token corresponding to the keyword w from CT and generates the Kw. Then he/she sends them to the server. The server retrieves all the encrypted bit strings e corresponding to w. To reduce the communication overhead, the server adds them together by using the homomorphic addition (Add) of the simple symmetric encryption to get the final result Sume and sends it to the client. Finally, the client decrypts it and

^{3.} Note that, we can update many file identifiers through one update query by using bit string representation bs.

outputs the final bit string bs which can be used to retrieve the matching files. Note that, in order to save the server storage, for every search, the server can remove all entries corresponding to w and store the final result Sum_e corresponding to the current search token ST_c to the EDB. Moreover, the client does not need to re-encrypt the final result bs which makes our scheme more efficient than the one in [17].

Algorithm 2. FBDSSE-RQ

```
Setup(1^{\lambda})
Client:
 1: K \stackrel{\$}{\leftarrow} \{0,1\}^{\lambda}, n \leftarrow \text{Setup}(1^{\lambda})
 2: CT, EDB ← empty map
 3: Set the range boundary d.
 4: return (EDB, \sigma = (n, d, K, \mathbf{CT}))
Update(v, bs, \sigma; EDB) > 0 \le v < d
Client:
 1: BT \leftarrow TGen(d)
 2: PT \leftarrow TPath(v, BT)
 3: for w \in PT do
     K_w||K_w' \leftarrow F_K(w), (ST_c, c) \leftarrow \mathbf{CT}[w]
      if (ST_c, c) = \perp then
       c \leftarrow -1, ST_c \leftarrow \{0, 1\}^{\lambda}
6:
7:
     end if
8:
     ST_{c+1} \leftarrow \{0,1\}^{\lambda}
      \mathbf{CT}[w] \leftarrow (ST_{c+1}, c+1)
9:
10:
      UT_{c+1} \leftarrow H_1(K_w, ST_{c+1})
11:
      C_{ST_c} \leftarrow H_2(K_w, ST_{c+1}) \oplus ST_c
12:
       sk_{c+1} \leftarrow H_3(K'_w, c+1)
       e_{c+1} \leftarrow \operatorname{Enc}(sk_{c+1}, bs, n)
       Send (UT_{c+1}, (e_{c+1}, C_{ST_c})) to the server.
15: end for
Server:
16: Upon receiving (UT_{c+1}, (e_{c+1}, C_{ST_c}))
17: Set EDB[UT_{c+1}] \leftarrow (e_{c+1}, C_{ST_c})
Search(q, \sigma, \text{EDB}) \rhd q = [a, b], where 0 \le a < b < d.
Client:
1: BT \leftarrow TGen(d)
2: BRC \leftarrow TGetCover(q, BT)
3: for w \in BRC do
4: K_w||K_w' \leftarrow F_K(w), (ST_c, c) \leftarrow \mathbf{CT}[w]
5:
     if (ST_c, c) = \perp then
6.
        return \perp
7:
     end if
8: end for
9: Send \{(K_w, ST_c, c)\}_{w \in BRC} to the server.
Server:
10: Sum \leftarrow 0
11: for each (K_w, ST_c, c) do
12:
       Sum_e \leftarrow 0
       for i = c to 0 do
13:
14:
          UT_i \leftarrow H_1(K_w, ST_i)
15:
          (e_i, C_{ST_{i-1}}) \leftarrow \mathtt{EDB}[UT_i]
16:
          Sum_e \leftarrow Add(Sum_e, e_i, n)
17:
          Remove EDB[UT_i]
18:
          if C_{ST_{i-1}} = \perp then
19:
            Break
20:
21:
          ST_{i-1} \leftarrow H_2(K_w, ST_i) \oplus C_{ST_{i-1}}
22:
        end for
23:
        EDB[UT_c] \leftarrow (Sum_e, \perp)
24:
        Sum \leftarrow Add(Sum, Sum_e, n)
```

```
25: end for
26: Send Sum to the client.

Client:
27: Sum_{sk} \leftarrow 0
28: for w \in BRC do
29: for i = c to 0 do
30: sk_i \leftarrow H_3(K'_w, i)
31: Sum_{sk} \leftarrow Sum_{sk} + sk_i \bmod n
32: end for
33: end for
34: bs \leftarrow Dec(Sum_{sk}, Sum, n)
35: return bs
```

6 SECURITY ANALYSIS

In this section, we give the security proof of our proposed scheme.

Theorem 1 (Adaptive forward and Type-R backward privacy of FBDSSE-RQ). Let F be a secure PRF, $\Pi = (\text{Setup}, \text{Enc}, \text{Dec}, \text{Add})$ be a perfectly secure simple symmetric encryption with homomorphic addition, and H_1 , H_2 and H_3 be random oracles. We define $\mathcal{L}_{\text{FBDSSE-RQ}} = (\mathcal{L}_{\text{FBDSSE-RQ}}^{Search}, \mathcal{L}_{\text{FBDSSE-RQ}}^{Update})$, where $\mathcal{L}_{\text{FBDSSE-RQ}}^{Search}(q) = (\text{sp}(q), \text{rp}(q), \text{Time}(q))$ and $\mathcal{L}_{\text{FBDSSE-RQ}}^{Update}(op, v, bs) = \mathcal{L}(\ell+1)$. Then FBDSSE-RQ is $\mathcal{L}_{\text{FBDSSE-RQ}}$ -adaptively forward and Type-R backward private.

Proof. Similar to the proof from [18], we formulate a sequence of games from DSSEREAL to DSSEIDEAL. We show that every two consecutive games are indistinguishable. Finally, we simulate DSSEIDEAL with the leakage functions defined in *Theorem 1*.

Game G_0 . G_0 is exactly same as the real world game DSSEREAL AFBDSSE-RQ (λ). So we can write that

$$\Pr[\texttt{DSSEREAL}_{AFBDSSE-RQ}(\lambda) = 1] = \Pr[G_0 = 1].$$

Game G_1 . Instead of generation of a key for a keyword w using F, we chooses the key at random and with uniform probability. The key and the corresponding keyword are stored in the table Key. If a keyword has been queried, then the corresponding key is fetched from the table Key. Assuming that an adversary \mathcal{A} is able to distinguish between G_0 and G_1 , then we can build an adversary \mathcal{B}_1 to distinguish between F and a truly random function. More formally

$$\Pr[G_0 = 1] - \Pr[G_1 = 1] \le \mathbf{Adv}_{F,\mathcal{B}_1}^{\mathsf{prf}}(\lambda).$$

Game G_2 . The game is described in Algorithm 3. For the Update protocol, an update token UT is picked randomly and is stored in the table UT. When the Search protocol is called, the random tokens are generated by the random oracle H_1 such that $H_1(K_w, ST_c) = \mathrm{UT}[w,c]$. The value (K_w, ST_c) is stored in table H_1 for future queries. If an entry (K_w, ST_{c+1}) already in table H_1 , then we cannot obtain the requested equality $H_1(K_w, ST_{c+1}) = \mathrm{UT}[w,c+1]$ and the game aborts. Now, we show that the abortion possibility is negligible. As a search token is chosen randomly, the probability of a correct guess for search token ST_{c+1} by the adversary is $1/2^{\lambda}$. If $\mathcal A$ makes polynomial number $p(\lambda)$ of queries, then

$$\Pr[G_1 = 1] - \Pr[G_2 = 1] < p(\lambda)/2^{\lambda}.$$

Algorithm 3. G_2 Setup(1 $^{\lambda}$)

```
Client:
 1: K \stackrel{\$}{\leftarrow} \{0,1\}^{\lambda}, n \leftarrow \text{Setup}(1^{\lambda})
 2: CT, EDB ← empty map
 3: Set the range boundary d.
 4: return (EDB, \sigma = (n, d, K, \mathbf{CT}))
Update(v, bs, \sigma; EDB) > 0 \le v < d
Client:
 1: BT \leftarrow TGen(d)
 2: PT \leftarrow TPath(v, BT)
 3: for w \in PT do
 4: K_w||K_w' \leftarrow \text{Key}(w)
 5: (ST_0, \ldots, ST_c, c) \leftarrow \mathbf{CT}[w]
6: if (ST_c, c) = \perp then
7:
     c \leftarrow -1, ST_c \leftarrow \{0,1\}^{\lambda}
8: end if
9: ST_{c+1} \leftarrow \{0,1\}^{\lambda}
10: \mathbf{CT}[w] \leftarrow (ST_0, \dots, ST_{c+1}, c+1)
11: UT_{c+1} \leftarrow \{0, 1\}
12: UT[w, c+1] \leftarrow UT_{c+1}
13: C_{ST_c} \leftarrow H_2(K_w, ST_{c+1}) \oplus ST_c
      sk_{c+1} \leftarrow H_3(K'_w, c+1)
15: e_{c+1} \leftarrow \operatorname{Enc}(sk_{c+1}, bs, n)
16: Send (UT_{c+1}, (e_{c+1}, C_{ST_c})) to the server.
17: end for
Server:
18: Upon receiving (UT_{c+1}, (e_{c+1}, C_{ST_c}))
19: Set EDB[UT_{c+1}] \leftarrow (e_{c+1}, C_{ST_c})
Search(q, \sigma, \text{EDB}) \rhd q = [a, b], where 0 \le a < b \le d - 1.
Client:
1: BT \leftarrow TGen(d)
2: BRC \leftarrow TGetCover(q, BT)
3: for w \in BRC do
4: K_w||K_w' \leftarrow \texttt{Key}(w)
5: (ST_0, \ldots, ST_c, c) \leftarrow \mathbf{CT}[w]
6: if (ST_c, c) = \perp then
7:
       return 丄
8: end if
9: for i = 0 to c do
          H_1(K_w, ST_i) \leftarrow \mathtt{UT}[w, i]
10:
11:
       end for
12: end for
13: Send \{(K_w, ST_c, c)\}_{w \in BRC} to the server.
Server:
14: Sum \leftarrow 0
15: for each (K_w, ST_c, c) do
16: Sum_e \leftarrow 0
       for i = c to 0 do
17:
         UT_i \leftarrow H_1(K_w, ST_i)
18:
19:
          (e_i, C_{ST_{i-1}}) \leftarrow \mathtt{EDB}[UT_i]
20:
          Sum_e \leftarrow Add(Sum_e, e_i, n)
21:
          Remove EDB[UT_i]
22:
          if C_{ST_{i-1}} = \perp then
23:
            Break
          end if
24:
          ST_{i-1} \leftarrow H_2(K_w, ST_i) \oplus C_{ST_{i-1}}
25:
26:
        end for
        \mathtt{EDB}[UT_c] \leftarrow (Sum_e, \bot)
27:
28: Sum \leftarrow Add(Sum, Sum_e, n)
29: end for
30: Send Sum to the client.
Client:
```

31: $Sum_{sk} \leftarrow 0$

```
32: for w \in BRC do

33: for i = c to 0 do

34: sk_i \leftarrow H_3(K'_w, i)

35: Sum_{sk} \leftarrow Sum_{sk} + sk_i \mod n

36: end for

37: end for

38: bs \leftarrow Dec(Sum_{sk}, Sum, n)

39: return bs
```

Game G_3 . We model the H_2 as a random oracle which is similar to H_1 in G_2 . So we can write

$$\Pr[G_2 = 1] - \Pr[G_3 = 1] \le p(\lambda)/2^{\lambda}.$$

Game G_4 . Again, we model the H_3 as a random oracle. If the adversary does not know the key K'_w , then the probability of guessing the right key is $1/2^{\lambda}$ (we set the length of K'_w to λ). Assuming that $\mathcal A$ makes polynomial number $p(\lambda)$ of queries, the probability is $p(\lambda)/2^{\lambda}$. So we have

$$\Pr[G_3 = 1] - \Pr[G_4 = 1] \le p(\lambda)/2^{\lambda}.$$

Algorithm 4. Simulator $\mathcal{S} \mathcal{S}$.**Setup**(1^{λ})

```
1: n \leftarrow \text{Setup}(1^{\lambda})
 2: Set the range boundary d.
 3: CT, EDB \leftarrow empty map
  4: return (EDB, CT, n, d)
S.Update(\ell + 1)
Client:
 1: for 0 to \ell do
  2: UT[t] \leftarrow \{0,1\}^{\lambda}
 3: C[t] \leftarrow \{0,1\}^{\lambda}
 4: \operatorname{sk}[t] \leftarrow \{0,1\}^{\lambda}
 5: e[t] \leftarrow Enc(sk[t], 0s, n)
6: Send (UT[t], (e[t], C[t])) to the server.
7: t \leftarrow t + 1
8: end for
S.Search(sp(q), rp(q), Time(q))
Client:
1: \hat{q} \leftarrow \min \operatorname{sp}(q)
2: \hat{\mathsf{BRC}} \leftarrow \hat{q}
3: for w \in BRC do
4: K_w||K_w' \leftarrow \texttt{Key}(w)
5: (ST_c, c) \leftarrow \mathbf{CT}[w]
6: Parse rp(\hat{q}) as bs.
7: Parse Time(w) as (t_0, \ldots, t_c), where Time(w) \in Time(\hat{q}).
8: if (ST_c, c) = \perp then
9:
        return ⊥
10: end if
11:
        for i = c to 0 do
12:
          ST_{i-1} \leftarrow \{0,1\}^{\lambda}
13:
          Program H_1(K_w, ST_i) \leftarrow \mathtt{UT}[t_i]
          Program H_2(K_w, ST_i) \leftarrow C[t_i] \oplus ST_{i-1}
14:
          if i = c and w is the last keyword in BRC then
15:
16:
             Program H_3(K'_w, i) \leftarrow \operatorname{sk}[t_i] - bs
17:
             Program H_3(K'_w, i) \leftarrow \text{sk}[t_i]
18:
19:
           end if
        end for
21: end for
22: Send \{(K_w, ST_c, c)\}_{w \in \hat{\mathsf{BRC}}} to the server.
```

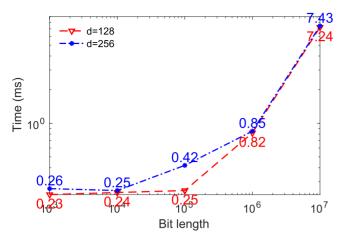


Fig. 3. The update time of ${\tt FBDSSE-RQ}$ for different bit lengths and the parameter d

Game G_5 . We replace the bit string bs by the string of all zeros (its length is y). If the adversary \mathcal{A} is able to distinguish between G_5 and G_4 , then we can build a reduction \mathcal{B}_2 to break the perfect security of the simple symmetric encryption with homomorphic addition Π . So we have

$$\Pr[G_4 = 1] - \Pr[G_5 = 1] \le \mathbf{Adv}_{\Pi, \mathcal{B}_2}^{\mathsf{PS}}(\lambda).$$

Simulator Now we can replace the searched range query q with $\operatorname{sp}(q)$ in G_5 to simulate the ideal world in Algorithm 4, it uses the first timestamp $\hat{q} \leftarrow \min \operatorname{sp}(q)$ for the range query q. We ignore a part of Algorithm 3 which does not influence the view of the adversary.

We are ready to show that G_5 and Simulator are indistinguishable. For Update, it is obvious since we choose new random strings for each update in G_5 . For Search, the simulator starts from the current search token ST_c and choose a random string for previous search token. Then it embeds it to the ciphertext C through H_2 . Moreover, S embeds the \overline{bs} to the ST_c of the last keyword in BRC and all 0s to the remaining search tokens through H_3 . Finally, we map the pairs (w,i) to the global update count t. Then we can map the values in the table UT, C and C0 and C1 are the pair C2 and C3 are the pair C3 and C4. Hence

$$\Pr[G_5 = 1] = \Pr[\texttt{DSSEIDEAL}_{A,S^{\texttt{FBDSSE-RQ}}}(\lambda) = 1].$$

Finally

$$\begin{split} \Pr[\texttt{DSSEREAL}_{\mathcal{A}^{\texttt{FBDSSE-RQ}}}(\lambda) &= 1] - \Pr[\texttt{DSSEIDEAL}_{\mathcal{A},\mathcal{S}^{\texttt{FBDSSE-RQ}}}(\lambda) \\ &= 1] \leq \mathbf{Adv}^{\texttt{prf}}_{F,\mathcal{B}_1}(\lambda) + \mathbf{Adv}^{\texttt{PS}}_{\Pi,\mathcal{B}_2}(\lambda) + 3p(\lambda)/2^{\lambda}, \end{split}$$

which completes the proof.

7 EXPERIMENTAL ANALYSIS

In this section, we evaluate the performance of our schemes using a testbed of one workstation. This machine plays the roles of the client and server. The hardware and software of this machine are as follows: Mac Book Pro, Intel Core i7 CPU @ 2.8 GHz RAM 16 GB, Java Programming Language, and macOS 10.13.2. Note that we use the bitmap index to denote file identifiers. We use the "BigInteger" with different bit

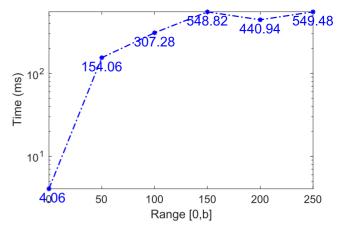


Fig. 4. The search time of FBDSSE-RQ for different ranges (d=256, bit length is 10^7).

lengths to denote the bitmap index with different sizes, which act as the database with different numbers of files. The relation between the *i*th bit and the actual file is out of our scope. The update time includes the client token generation time and server update time. The search time includes the token generation time, the server search time and the client decryption time. Note that the result depends on the maximum number of files supported by the system (the bit length) only.

Fig. 3 shows the update time of our scheme for different bit lengths and the parameter d. The bit length refers to y, which is equal to the maximum number of files supported by the system. The parameter d refers to the boundary of our range query. We update one time for each value. We get the total update time for all values and divide it by the number of values, so we get the average update time for each value. As the bit length increases, the update time grows (see Fig. 3). There is an exception when the bit length jumps from 10^3 to 10^4 (see the line for d=256). This is due to the fact that modulo addition does not contribute too much when the bit string is smaller than 10^4 . We also observe that the average update time for d=256 is larger than the time for d=128. This is because, when d=256, the binary tree has more levels, which means it needs more updates than the one for d=128.

We evaluate the search time of our scheme for different ranges ([0,0], [0,50], [0,100], [0,150], [0,200], [0,250]), where d=256 and bit length is 10^7 . The results are given in Fig. 4. It can be seen that in general, a larger range requires a larger search time. However, this is not always true. The search time depends on the number of keywords in BRC of a range. The search time for the range [0,150] is larger than the search time for the range [0,200] because the number of keywords in BRC for the range [0,150]. In addition, with the increase of the bit length, the search time increases.

Theoretically, the bit string can be of an arbitrary length, but a larger n (e.g., $\ell=2^{23}$) significantly increases the time needed for modulo additions. To mitigate this problem, we can divide a large bit string into several shorter ones as in the multi-block setting [18]. We refer readers to [18] for details.

8 CONCLUSION

In this paper, we propose a forward and backward private DSSE for range queries (named FBDSSE-RQ), which requires only one roundtrip. In other words, for every search, it does

not require re-encryption of the matching files, which makes our scheme more efficient. Moreover, we refine the construction of the binary tree from [15]. Names of nodes are derived from their leaf nodes, rather than from the order of node insertion [15]. In addition, we define a new backward privacy notion for our range queries called Type-R. For our range query, to update a file with value v, it leaks the number of keywords that have been updated due to the binary tree data structure. From the security and experimental analyses, we can see that our proposed scheme achieves claimed security goals and is efficient.

ACKNOWLEDGMENTS

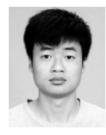
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