Honours Degree of Bachelor of Science in Artificial Intelligence

Batch 21 - Level 2 (Semester 2)

CM 2320 - Mathematical Methods

Tutorial 6

1. Find the following:

a)
$$e^{-2t} * e^{-t}$$

b)
$$t^2 * e^{-3t}$$

2. Find f * g when

a)
$$f = 1, g = t$$

b)
$$f = t^2, g = t$$

c)
$$f = e^t, g = t$$

d)
$$f = \sin(t), g = t$$

In each case verify that $\mathcal{L}\left\{f\right\}\mathcal{L}\left\{g\right\} = \mathcal{L}\left\{f * g\right\}$.

3. If $F(s) = \frac{1}{s-1}$, $G(s) = \frac{1}{s}$ and $H(s) = \frac{1}{2s+3}$, use the convolution theorem to find the inverse Laplace transforms of following:

a)
$$F(s)G(s)$$

b)
$$F(s)H(s)$$

c)
$$G(s)H(s)$$

$$\textbf{4.} \ \ \text{Use the convolution theorem to determine the inverse Laplace transforms of following:}$$

a)
$$\frac{1}{s^2(s+1)}$$

b)
$$\frac{1}{(s+3)(s-2)}$$

c)
$$\frac{1}{(s^2+1)^2}$$
