



LEARNING MACHINE LEARNING

2018-07-12

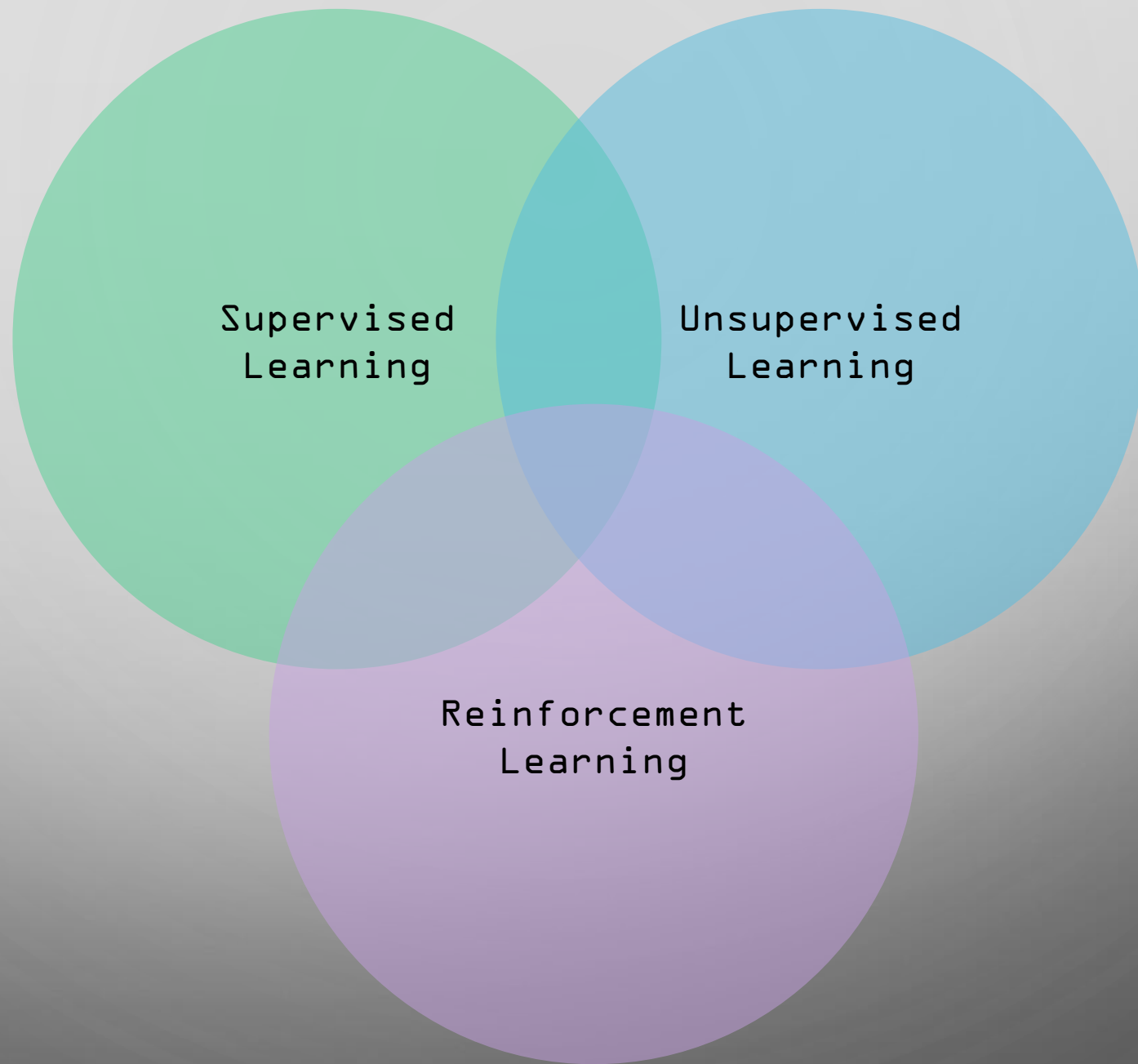
REVLR

TEAM S.C.P

CONTENTS

- review
- Binary classification Model
- sigmoid function
- softmax classification
- softmax classifier's cost function






SUPERVISED LEARNING MODEL

Logistic
(regression)
Classification

Binary
Classification

Multi-label
Classification




Play time(x1) Deck power(x2)	
10	5
9	5
3	2
2	4
11	1

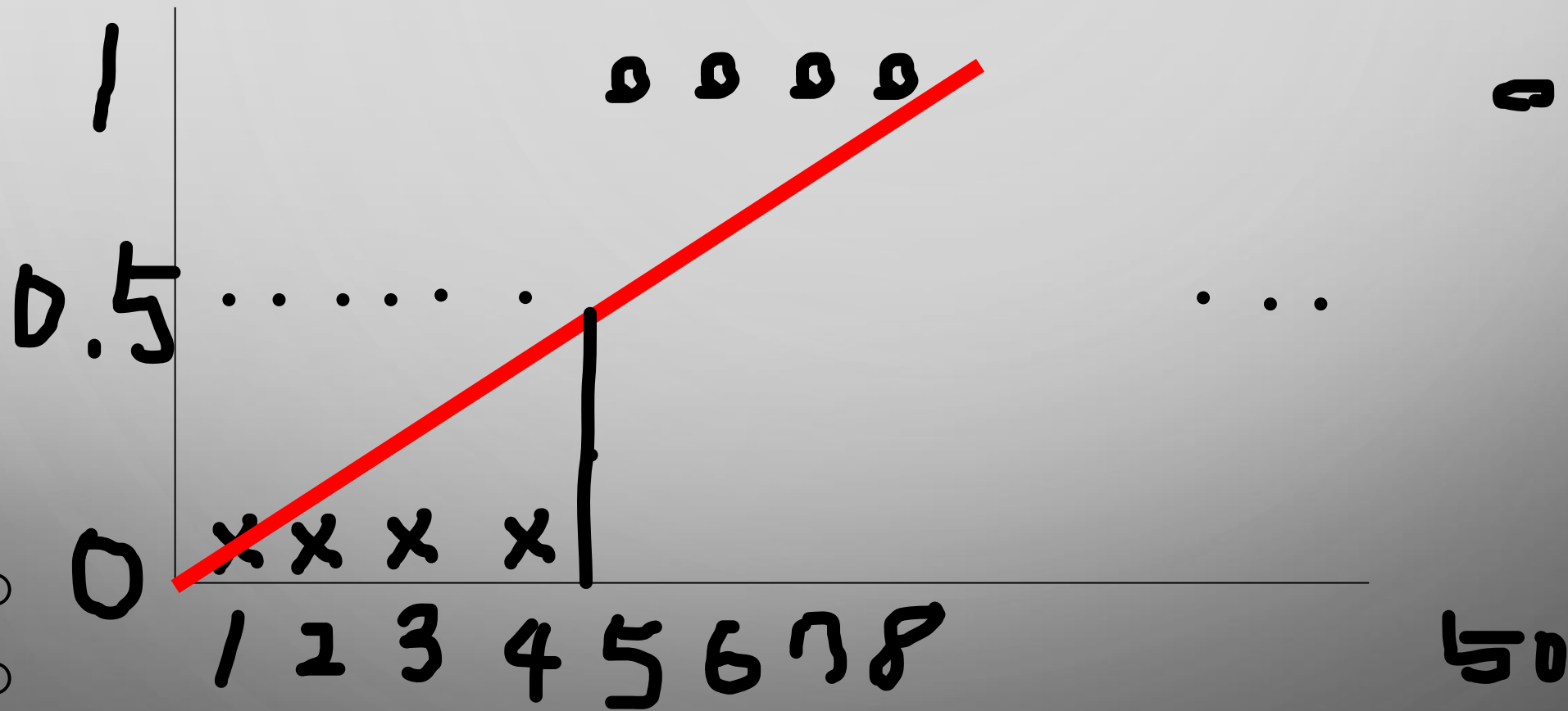
Wins(y1)
42
38
7
8
2

Legend(y2)
1
0
0
0
0

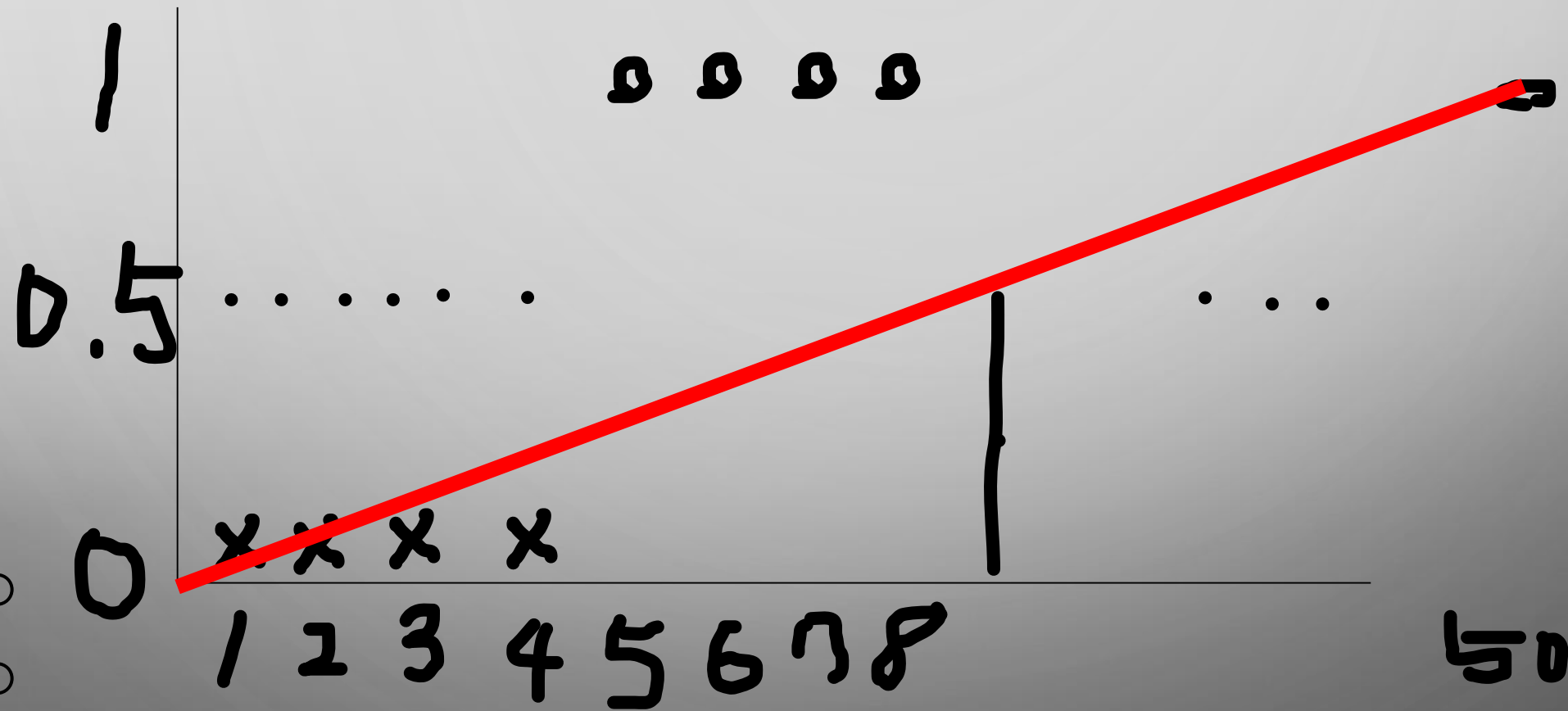
Grade(y3)
0
2
18
14
25



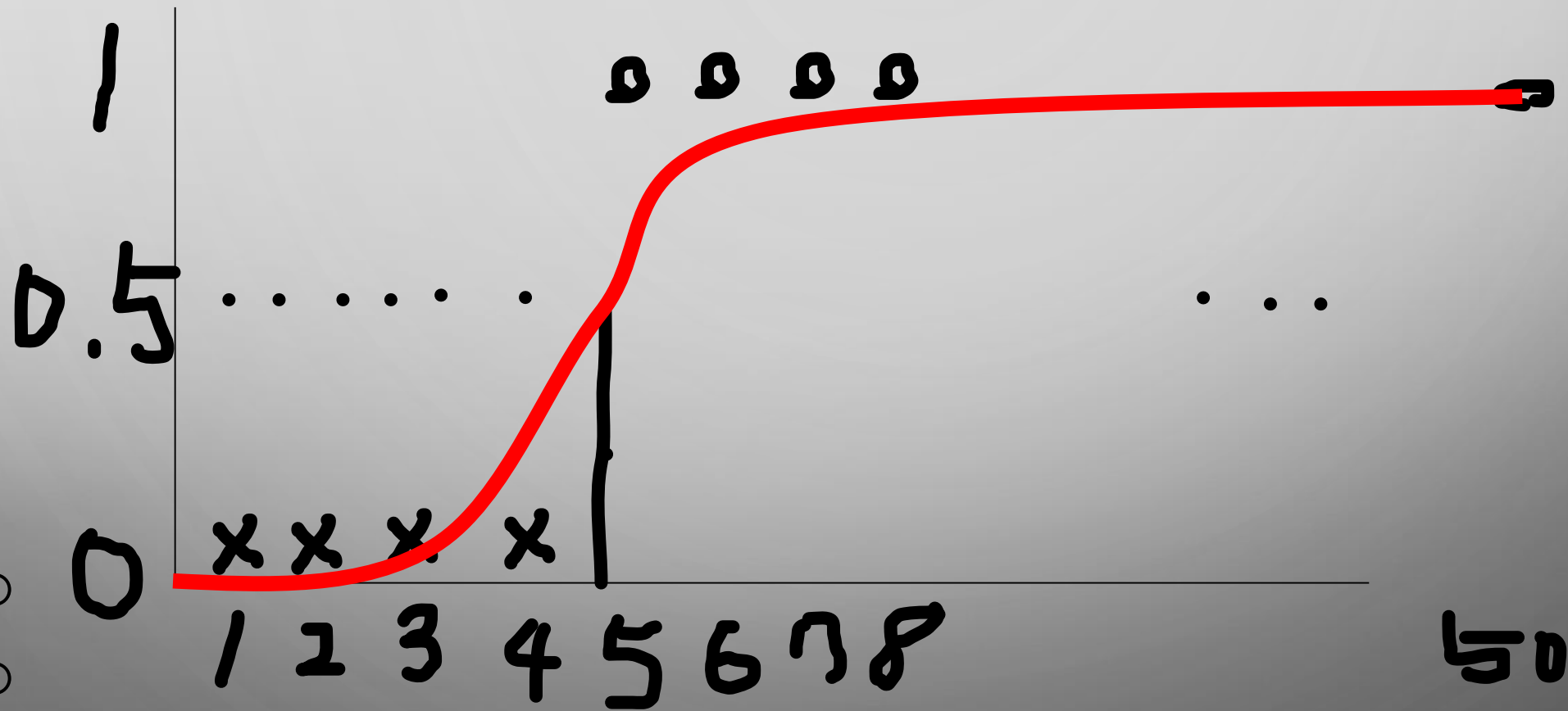
BINARY CLASSIFICATION MODEL

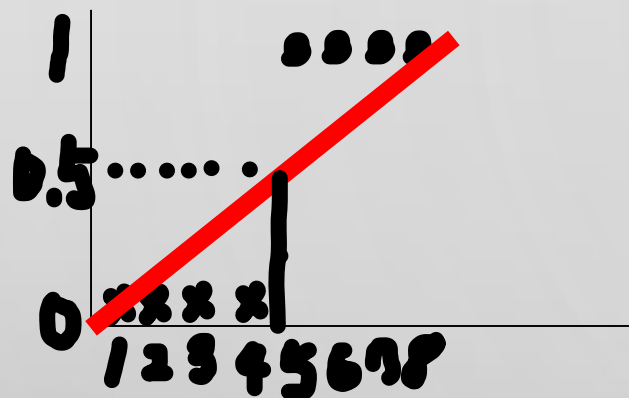


BINARY CLASSIFICATION MODEL



BINARY CLASSIFICATION MODEL





$$H(x) = Wx + b$$

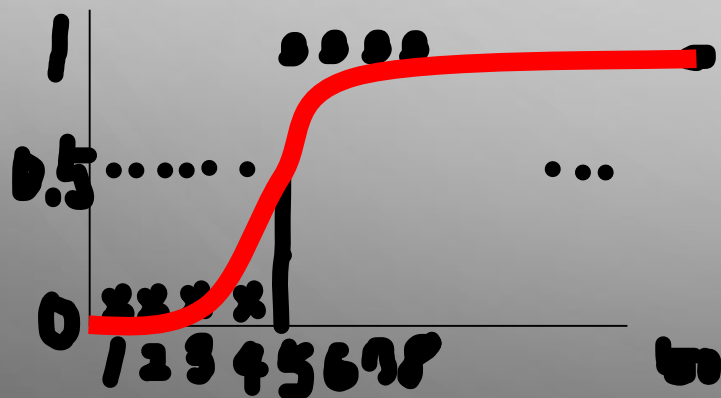
$$H(x) = \frac{1}{10}x \quad (W = \frac{1}{10}, b = 0)$$

$$H(x)_{50} = 5 \quad (5 \gg 1)$$

$$0 < H(x) < 1 \quad ???$$

$$\text{cost}(W, b) = \frac{1}{m} \sum_{i=1}^m (H(x_i) - y_i)^2$$

Sigmoid Function



$$g(z) = \frac{1}{(1 + e^z)}$$

$$H(X) = \frac{1}{1 + e^{W^t X}}$$

COST FUNCTION

$$\text{cost}(W, b) = \frac{1}{m} \sum_{i=1}^m (H(x_i) - y_i)^2$$

$$H(x) = Wx + b$$

$$H(X) = \frac{1}{1 + e^{W^t X}}$$



COST FUNCTION

$$H(X) = \frac{1}{1 + e^{W^t X}}$$



$$\text{cost}(W) = \frac{1}{m} \sum_{i=1}^m c(H(x_i), y_i)$$

$$c(H(x_i), y_i) = \begin{cases} -\log(H(x)) & : y = 1 \\ -\log(1 - H(x)) & : y = 0 \end{cases}$$

$$\text{cost}(W) = -\frac{1}{m} \sum_{i=1}^m \{y \log(H(x)) + (1 - y) \log(1 - H(x))\}$$

$$\therefore W \leftarrow W - \alpha \frac{\partial}{\partial W} \text{cost}(W, b)$$

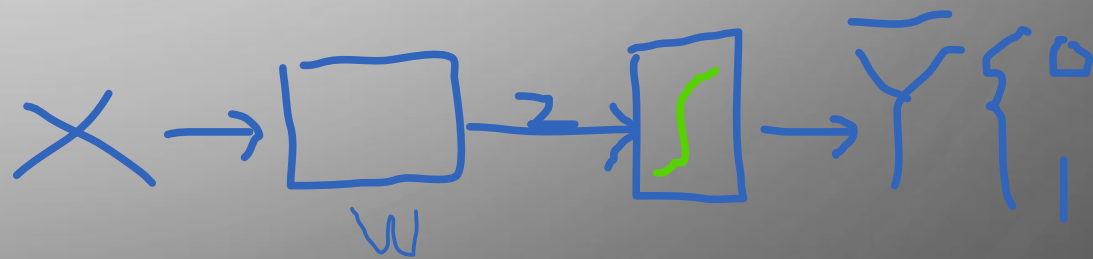
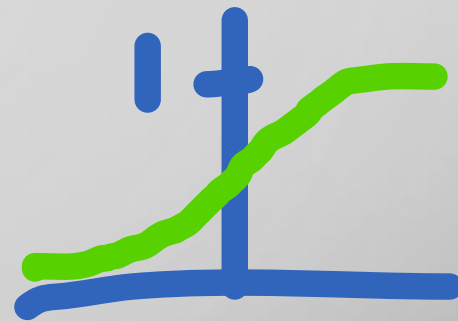
SOFTMAX CLASSIFICATION

$$H_L(x) = Wx$$

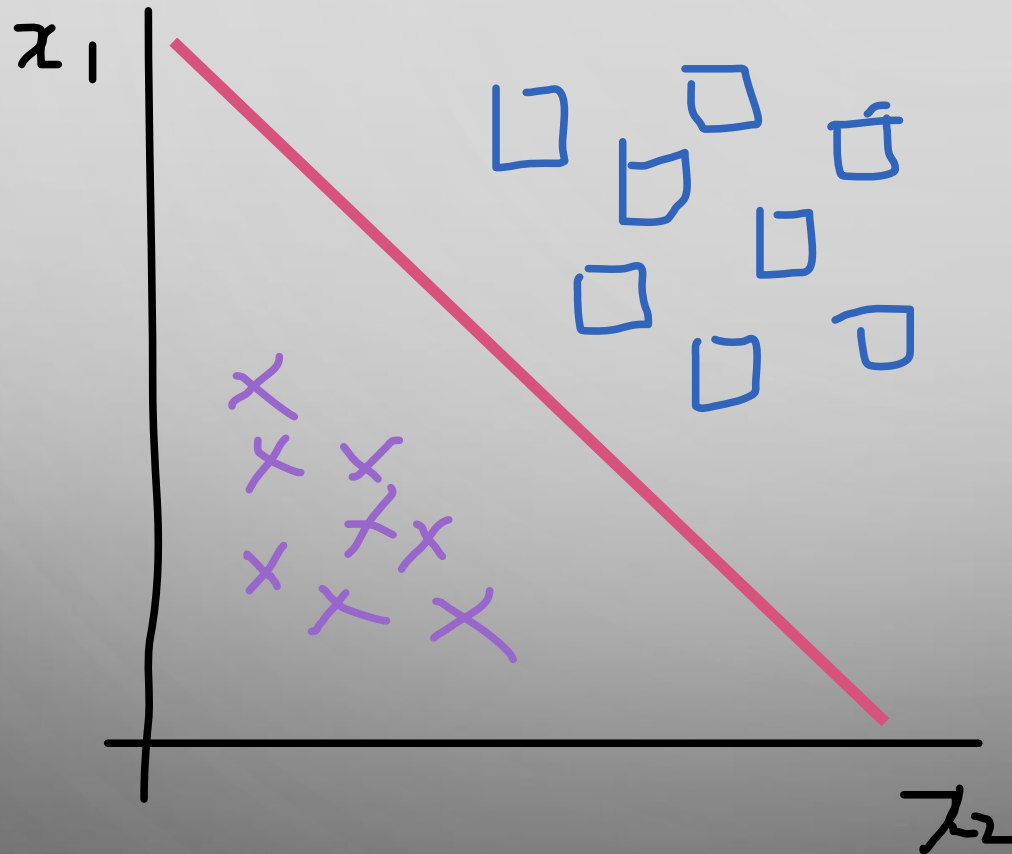
$$z = H_L(x), \quad g(z)$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$H_P(x) = g(H_L(x))$$



SOFTMAX CLASSIFICATION

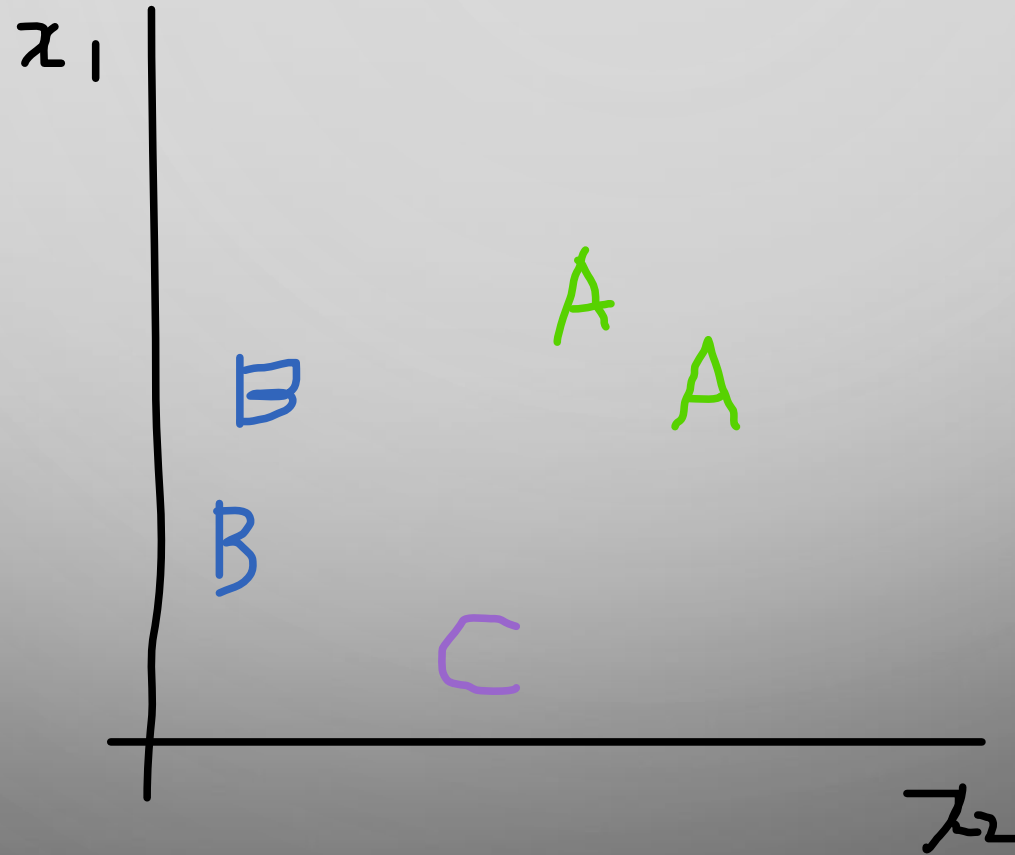


$$g(z) = \frac{1}{1 + e^{-z}}$$

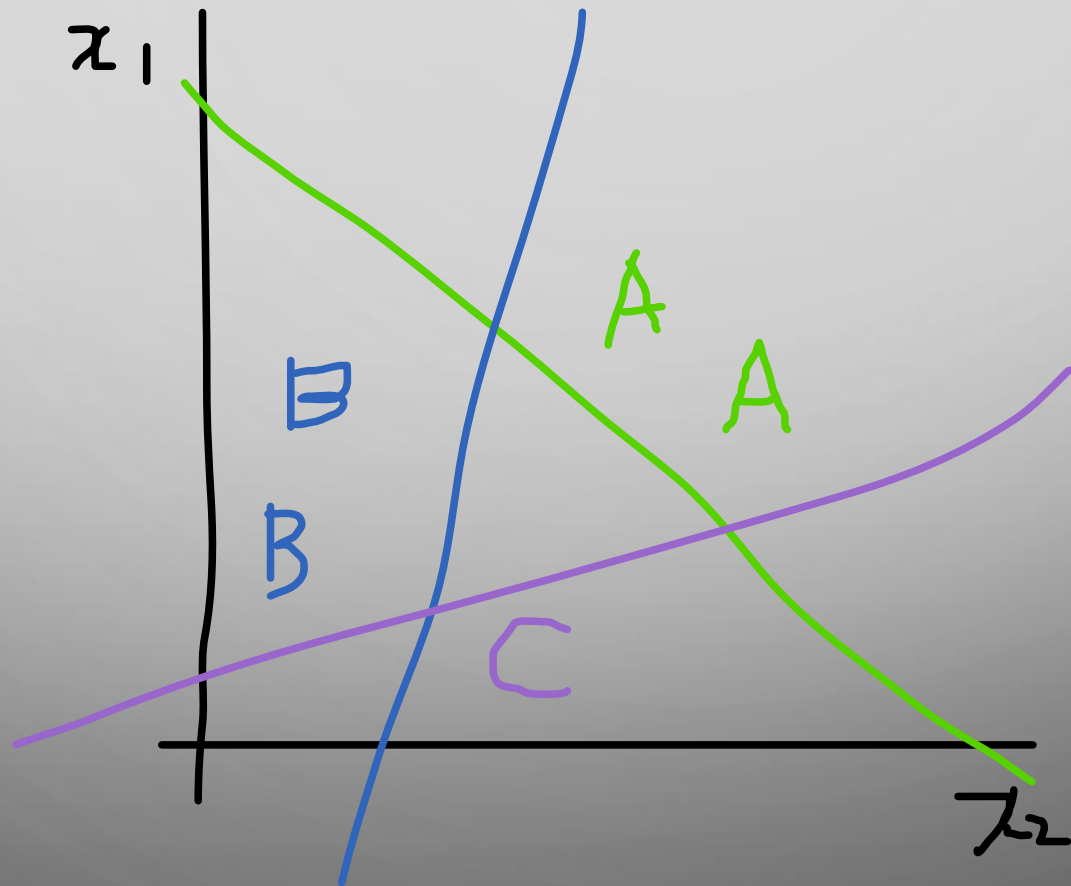
$$H_R(x) = g(H_L(x))$$

$$x \rightarrow \boxed{w} \rightarrow \boxed{g} \rightarrow \bar{Y} \{0, 1\}$$

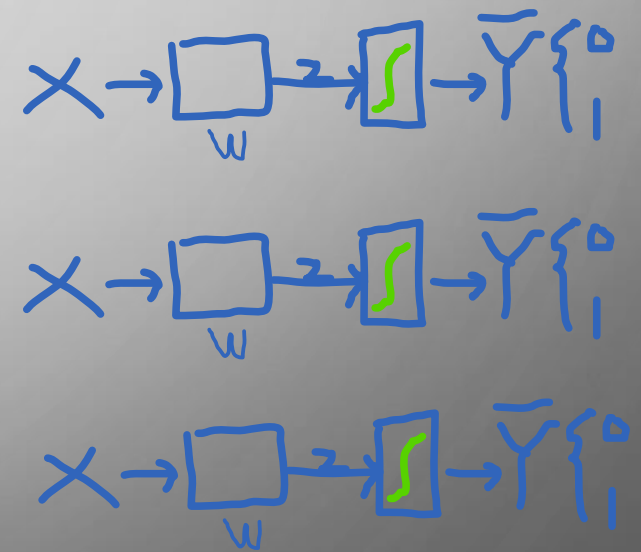
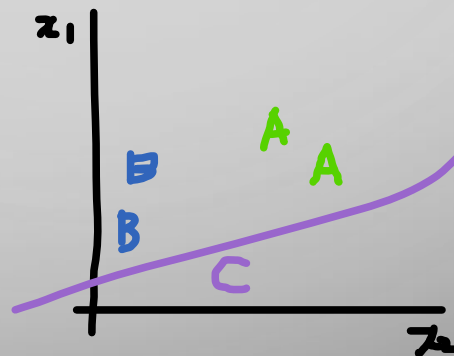
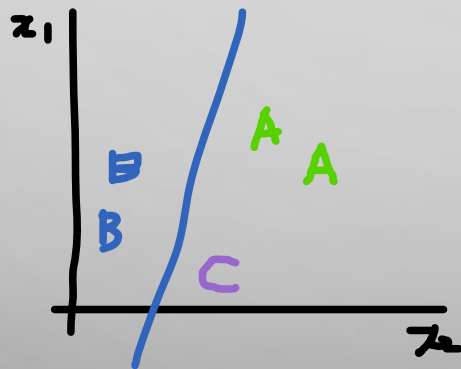
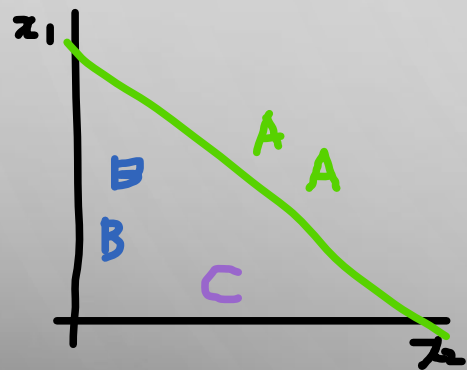
MULTINOMIAL CLASSIFICATION

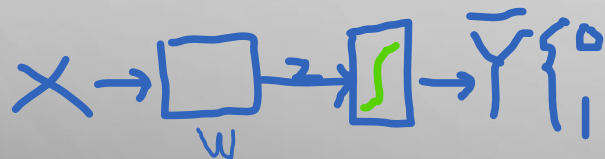
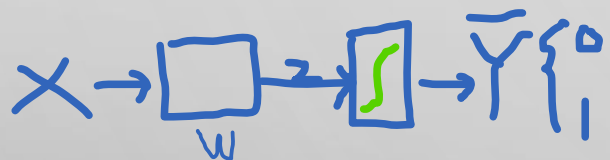
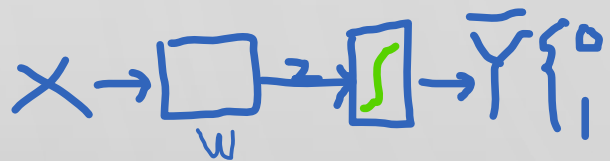


MULTINORMAL CLASSIFICATION



MULTINOMIAL CLASSIFICATION





$$[w_1, w_2, w_3] \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = [w_1 x_1 + w_2 x_2 + w_3 x_3]$$

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$$[w_1, w_2, w_3] \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = [w_1 x_1 + w_2 x_2 + w_3 x_3]$$

$$\begin{bmatrix} w_1 & w_2 & w_3 \\ w_1 & w_2 & w_3 \\ w_1 & w_2 & w_3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \end{bmatrix} = \begin{bmatrix} \overline{y_A} \\ \overline{y_B} \\ \overline{y_C} \end{bmatrix}$$

$$\begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \\ w_{31} & w_{32} & w_{33} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \end{bmatrix} = \begin{bmatrix} y_A \\ y_B \\ y_C \end{bmatrix}$$

a

b

c

2.0
1.0
0.1

$$x \begin{bmatrix} 2.0 \\ 1.0 \\ 0.1 \end{bmatrix} \xrightarrow{s(y)}$$

0.7

0.2

0.1

→

1

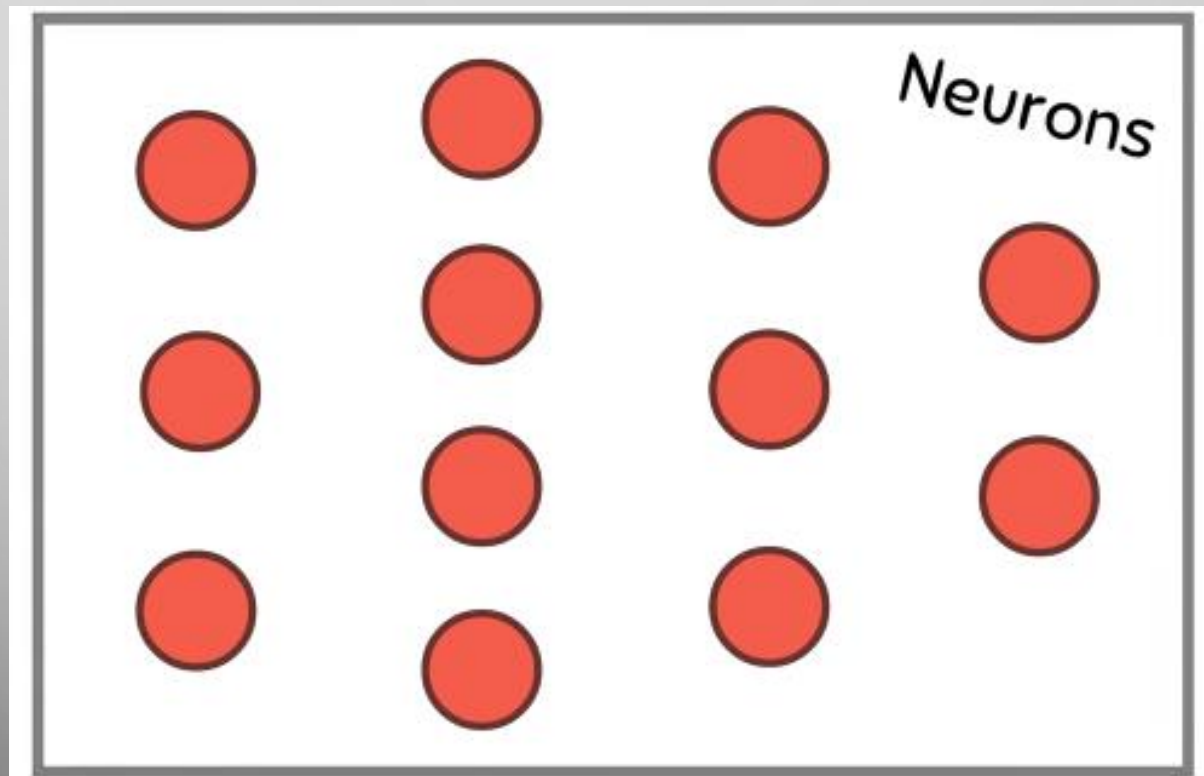
0

0

a

c

NURAL NETWORK



NURAL NETWORK

