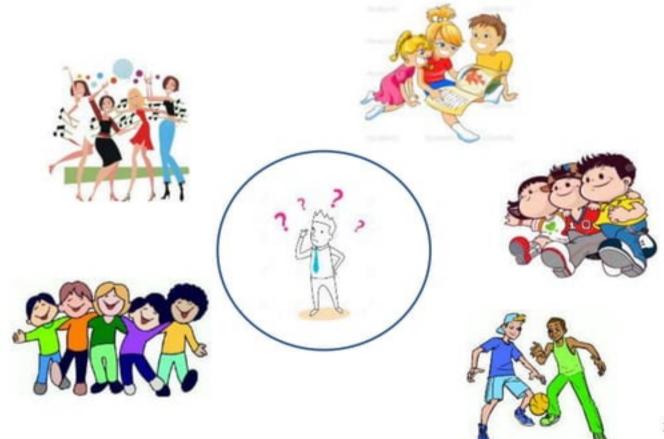
# **Algorithms: K Nearest Neighbors**

Tilani Gunawardena

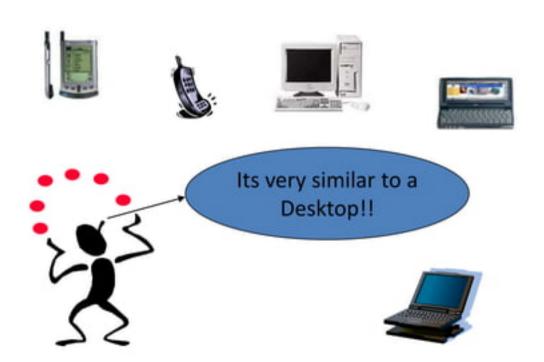
# **Algorithms: K Nearest Neighbors**

# Simple Analogy...

 Tell me about your friends(who your neighbors are) and I will tell you who you are.



# Instance-based Learning



### KNN – Different names

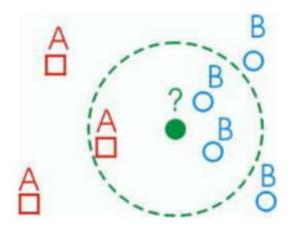
- K-Nearest Neighbors
- Memory-Based Reasoning
- Example-Based Reasoning
- Instance-Based Learning
- Lazy Learning

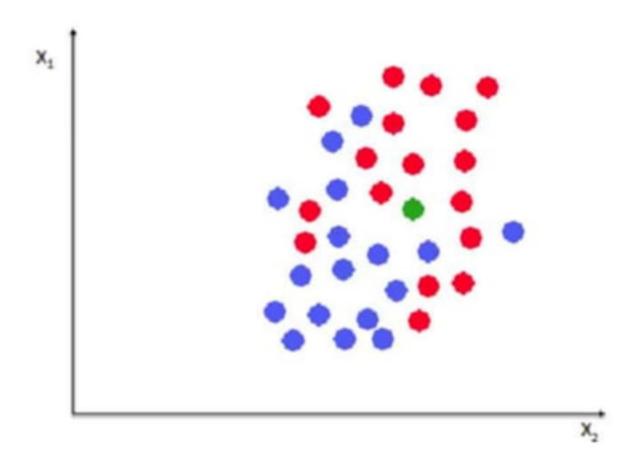
### What is KNN?

- A powerful classification algorithm used in pattern recognition.
- K nearest neighbors stores all available cases and classifies new cases based on a <u>similarity measure</u>(e.g <u>distance function</u>)
- One of the top data mining algorithms used today.
- A non-parametric lazy learning algorithm (An Instancebased Learning method).

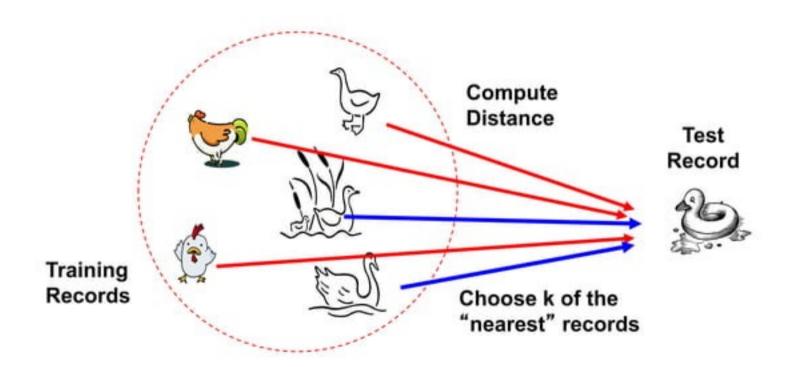
# KNN: Classification Approach

- An object (a new instance) is classified by a majority votes for its neighbor classes.
- The object is assigned to the most common class amongst its K nearest neighbors.(measured by a distant function)





### Distance Measure



### Distance measure for Continuous Variables

#### Distance functions

Euclidean 
$$\sqrt{\sum_{i=1}^{k} (x_{i} - y_{i})^{2}}$$

Manhattan 
$$\sum_{i=1}^{k} |x_i - y_i|$$

Minkowski 
$$\left(\sum_{i=1}^{k} (|x_i - y_i|)^q\right)^{1/q}$$

# Distance Between Neighbors

Calculate the distance between new example
 (E) and all examples in the training set.

- Euclidean distance between two examples.
  - $-X = [x_1, x_2, x_3, ..., x_n]$
  - $-Y = [y_1, y_2, y_3, ..., y_n]$

– The Euclidean distance between X and Y is defined as:

 $D(X,Y) = \sqrt{\sum_{i=1}^{n} (x_i - y_i)^2}$ 

### K-Nearest Neighbor Algorithm

- All the instances correspond to points in an n-dimensional feature space.
- Each instance is represented with a set of numerical attributes.
- Each of the training data consists of a set of vectors and a class label associated with each vector.
- Classification is done by comparing feature vectors of different K nearest points.
- Select the K-nearest examples to E in the training set.
- Assign E to the most common class among its K-nearest neighbors.

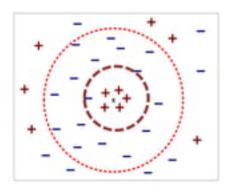
# 3-KNN: Example(1)

Customer	Age	Income	No. credit cards	Class
George	35	35K	3	No
Rachel	22	50K	2	Yes
Steve	63	200K	1	No
Tom	59	170K	1	No
Anne	25	40K	4	Yes
John	37	50K	2	YES

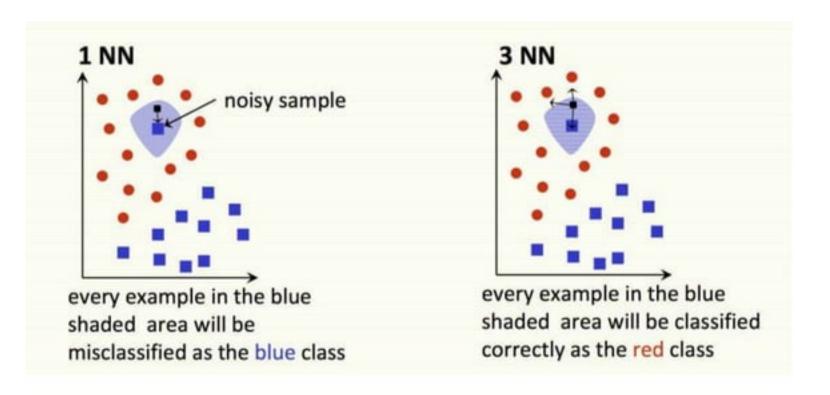
Distance from John				
sqrt [(35-37) <sup>2</sup> +(35-50) <sup>2</sup> +(3- 2) <sup>2</sup> ]=15.16				
sqrt [(22-37) <sup>2</sup> +(50-50) <sup>2</sup> +(2- 2) <sup>2</sup> ]=15				
sqrt [(63-37) <sup>2</sup> +(200-50) <sup>2</sup> +(1- 2) <sup>2</sup> ]=152.23				
sqrt [(59-37) <sup>2</sup> +(170-50) <sup>2</sup> +(1- 2) <sup>2</sup> ]=122				
sqrt [(25-37) <sup>2</sup> +(40-50) <sup>2</sup> +(4- 2) <sup>2</sup> ]=15.74				

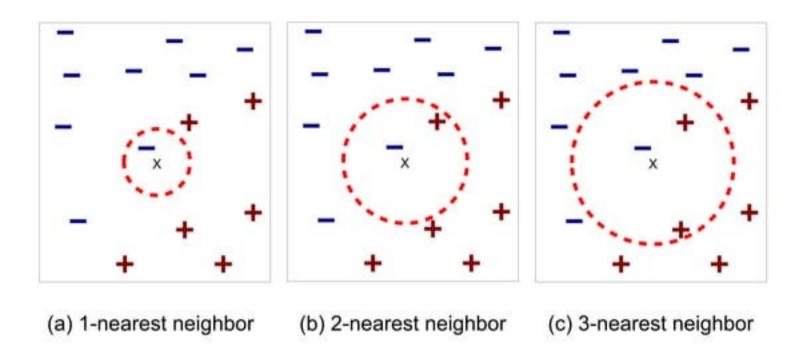
### How to choose K?

- If K is too small it is sensitive to noise points.
- Larger K works well. But too large K may include majority points from other classes.



Rule of thumb is K < sqrt(n), n is number of examples.</li>





K-nearest neighbors of a record x are data points that have the k smallest distance to x

### KNN Feature Weighting

 Scale each feature by its importance for classification

$$D(a,b) = \sqrt{\sum_{k} w_{k} (a_{k} - b_{k})^{2}}$$

- Can use our prior knowledge about which features are more important
- Can learn the weights w<sub>k</sub> using cross-validation (to be covered later)

#### Feature Normalization

- Distance between neighbors could be dominated by some attributes with relatively large numbers.
  - e.g., income of customers in our previous example.

$$a_i = \frac{v_i - \min v_i}{\max v_i - \min v_i}$$

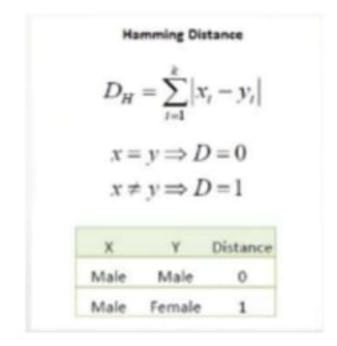
- Arises when two features are in different scales.
- Important to normalize those features.
  - Mapping values to numbers between 0-1.

# Nominal/Categorical Data

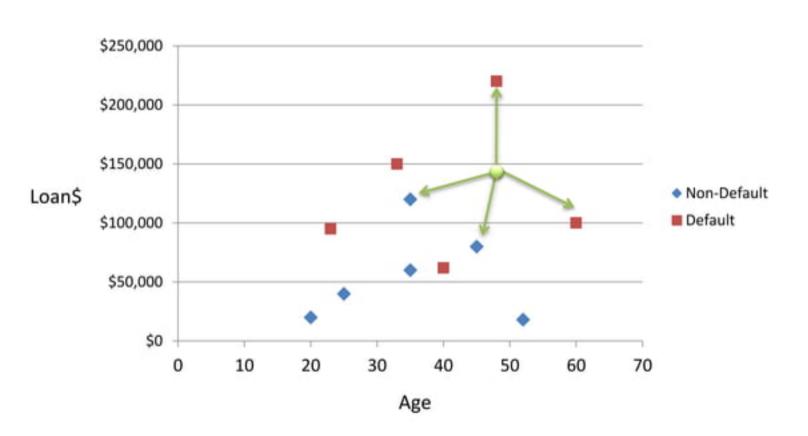
Distance works naturally with numerical attributes.

Binary value categorical data attributes can be regarded as 1

or 0.



### KNN Classification



### KNN Classification — Distance

Age	Loan	Default	Distance
25	\$40,000	N	102000
35	\$60,000	N	82000
45	\$80,000	N	62000
20	\$20,000	N	122000
35	\$120,000	N	22000
52	\$18,000	N	124000
23	\$95,000	Υ	47000
40	\$62,000	Υ	80000
60	\$100,000	Υ	42000
48	\$220,000	Υ	78000
33	\$150,000	Υ <table-cell-columns></table-cell-columns>	8000
		<u>↓</u>	
48	\$142,000	?	

 $D = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ 

### KNN Classification — Standardized Distance

Age	Loan	Default	Distance
0.125	0.11	N	0.7652
0.375	0.21	N	0.5200
0.625	0.31	_ N ←	0.3160
0	0.01	N	0.9245
0.375	0.50	N	0.3428
0.8	0.00	N	0.6220
0.075	0.38	Υ	0.6669
0.5	0.22	Y	0.4437
1	0.41	Y	0.3650
0.7	1.00	Y	0.3861
0.325	0.65	Υ	0.3771
0.7	0.61	<b>-</b> ?	

Standardized Variable
$$X_{s} = \frac{X - Min}{Max - Min}$$

#### Strengths of KNN

- Very simple and intuitive.
- Can be applied to the data from any distribution.
- Good classification if the number of samples is large enough.

#### Weaknesses of KNN

- Takes more time to classify a new example.
  - need to calculate and compare distance from new example to all other examples.
- Choosing k may be tricky.
- Need large number of samples for accuracy.