

# CYK Algorithm HW #2

Creating grammars:

$$1. L = \{a^n b^n \mid n \geq 0\}$$

$$L = \{\epsilon, ab, aabb, aaabbb \dots\}$$

$$G = (V, \Sigma, R, S)$$

$$= (\{S\}, \{a, b\}, R, S) \text{ where}$$

$$R = \{S \rightarrow aSb \mid \epsilon\}$$

$$2. L = \{a^i b^j c^k \mid i = j \text{ or } j = k\}$$

$$G = \{\{SA BC\}, \{a, b, c\}, R, S\} \text{ where}$$

$$R = S \rightarrow AB \mid BC$$

$$A \rightarrow aA \mid a$$

$$B \rightarrow bBc \mid bc$$

$$C \rightarrow cCc \mid c$$

$$3. L = \{x_1 \# x_2 \# \dots \# x_k \mid k \geq 1, \text{ each } x_i \in \{a, b\}^*\}$$

and for some  $i$  and  $j$ ,  $x_i = x_j$

$$R = S \rightarrow X \mid X \# S$$

$$X \rightarrow A \mid B \mid A X \mid B X$$

$$A \rightarrow a \mid aa$$

$$B \rightarrow b \mid bb$$

4. The rules of the grammar are already listed:

$$S \rightarrow TT \mid U$$

$$T \rightarrow OT \mid T01 \mid \#$$

$$U \rightarrow OOOO \mid \#$$

## CFG to CNF

1.  $S \rightarrow aSb \mid \epsilon$

$S_0 \rightarrow S$

$S \rightarrow aSb \mid \epsilon$

$S_0 \rightarrow S \mid \epsilon$

$S \rightarrow aSb \mid ab$

$S_0 \rightarrow aSb \mid ab \mid \epsilon$

$S \rightarrow aSb \mid ab$

$S_0 \rightarrow aSb \mid ab \mid \epsilon$

$S \rightarrow aZ_1 \mid ab$

$Z_1 \rightarrow Sb$

$S_0 \rightarrow ab \mid aZ_1 \mid \epsilon$

$S \rightarrow ab \mid aZ_1$

$Z_1 \rightarrow Sb$

Note: ending all  
CNF in single  
terminal symbols  
makes it easier  
for our program  
to read

A  $\rightarrow CD \mid CG \mid \epsilon$

S  $\rightarrow CD \mid CB$

B  $\rightarrow SD$

C  $\rightarrow a$

D  $\rightarrow b$

2.

$$\begin{aligned} S &\rightarrow AB \mid BC \\ A &\rightarrow aA \mid a \\ B &\rightarrow bBc \mid bc \\ C &\rightarrow cC \mid c \end{aligned}$$

$$\begin{aligned} S_0 &\rightarrow AB \mid BC \\ S &\rightarrow AB \mid BC \\ A &\rightarrow aA \mid a \\ B &\rightarrow bC \mid bD \\ C &\rightarrow cC \mid c \\ D &\rightarrow BC \end{aligned}$$

$$\begin{aligned} S_0 &\rightarrow S \\ S &\rightarrow AB \mid BC \\ A &\rightarrow aA \mid a \\ B &\rightarrow bBc \mid bc \\ C &\rightarrow cC \mid c \end{aligned}$$

$$\begin{aligned} S_0 &\rightarrow AB \mid BC \\ S &\rightarrow AB \mid BC \\ A &\rightarrow xA \mid x \\ B &\rightarrow yz \mid yD \\ C &\rightarrow zC \mid z \\ D &\rightarrow Bz \\ X &\rightarrow a \\ Y &\rightarrow b \\ Z &\rightarrow c \end{aligned}$$

$$\begin{aligned} S_0 &\rightarrow S \\ S &\rightarrow AB \mid BC \\ A &\rightarrow aA \mid a \\ B &\rightarrow bBc \mid bc \\ C &\rightarrow cC \mid c \end{aligned}$$

$$\begin{aligned} S_0 &\rightarrow AB \mid BC \\ S &\rightarrow AB \mid BC \\ A &\rightarrow aA \mid a \\ B &\rightarrow bBc \mid bc \\ C &\rightarrow cC \mid c \end{aligned}$$

#3.

$$S \rightarrow X \mid X \# S$$

$$X \rightarrow A \mid B \mid A X \mid B X$$

$$A \rightarrow a \mid a A$$

$$B \rightarrow b \mid b B$$

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$$S_0 \rightarrow S$$

$$S \rightarrow X \mid X \# S$$

$$X \rightarrow A \mid B \mid A X \mid B X$$

$$A \rightarrow a \mid a A$$

$$B \rightarrow b \mid b B$$

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$$S_0 \rightarrow X \# S \mid A X \mid B X \mid a \mid a A \mid b \mid b B$$

$$S \rightarrow X \# S \mid A X \mid B X \mid a \mid a A \mid b \mid b B$$

$$X \rightarrow A X \mid B X \mid a \mid a A \mid b \mid b B$$

$$A \rightarrow a \mid a A$$

$$B \rightarrow b \mid b B$$

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$$S_0 \rightarrow A X \mid B X \mid a \mid a A \mid b \mid b B \mid X C$$

$$S \rightarrow A X \mid B X \mid a \mid a A \mid b \mid b B \mid X C$$

$$X \rightarrow A X \mid B X \mid a \mid a A \mid b \mid b B$$

$$A \rightarrow a \mid a A$$

$$B \rightarrow b \mid b B$$

$$C \rightarrow \# S$$

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$$S_0 \rightarrow A X \mid B X \mid X C \mid D \mid D A \mid E \mid E B$$

$$S \rightarrow A X \mid B X \mid X C \mid D \mid D A \mid E \mid E B$$

$$X \rightarrow A X \mid B X \mid D \mid D A \mid E \mid E B$$

$$A \rightarrow D \mid D A$$

$$D \rightarrow q$$

$$B \rightarrow E \mid E B$$

$$E \rightarrow y$$

$$C \rightarrow F \mid S$$

$$F \rightarrow H$$

#4.  $S \rightarrow TT \cup$   
 $T \rightarrow OT \mid TO \mid \#$   
 $U \rightarrow OUOO \mid \#$

$S_0 \rightarrow S$   
 $S \rightarrow TT \cup$   
 $T \rightarrow OT \mid TO \mid \#$   
 $U \rightarrow OUOO \mid \#$

Note:

$S_0 \rightarrow TT \mid OUOO \mid \#$   
 $S \rightarrow TT \mid OUOO \mid \#$   
 $T \rightarrow OT \mid TO \mid \#$   
 $U \rightarrow OUOO \mid \#$

$a = O$   
 $b = \#$

inputs changed  
 to less error prone  
 symbols for the  
 program

$S_0 \rightarrow TT \mid DUOO \mid \#$   
 $S \rightarrow TT \mid DUOO \mid \#$   
 $T \rightarrow OT \mid TO \mid \#$   
 $U \rightarrow DUOO \mid \#$

$Y_1 \rightarrow OO$   
 $Z_1 \rightarrow UY_1$

$A \rightarrow TT \mid D \mid EC$
$S \rightarrow TT \mid D \mid EC$
$T \rightarrow ET \mid TE \mid D$
$U \rightarrow D \mid EC$
$B \rightarrow EE$
$C \rightarrow UB$
$D \rightarrow b$
$E \rightarrow a$

## Group 3 CFG Questions in CNF

$S_0 \rightarrow AB \mid BC$   
 $S \rightarrow AB \mid BC$   
 $A \rightarrow XA \mid a$   
 $B \rightarrow YZ \mid YD$   
 $C \rightarrow ZC \mid c$   
 $D \rightarrow BZ$   
 $X \rightarrow a$   
 $Y \rightarrow b$   
 $Z \rightarrow C$

## Group 3 CFG Questions in CNF

$S_0 \rightarrow AB \mid BC$   
 $S \rightarrow AB \mid BC$   
 $A \rightarrow XA \mid a$   
 $B \rightarrow YZ \mid YD$   
 $C \rightarrow ZC \mid c$   
 $D \rightarrow BZ$   
 $X \rightarrow a$   
 $Y \rightarrow b$   
 $Z \rightarrow C$