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Propagation-based fault detection and discrimination method and the optimization of sensor deployment

Abstract

A model (137) is created of a system (110) to be monitored (805). Operating states of the monitored system, including steady and transient states, are identified. Faults are injected into the model and the model is used to simulate each of the identified operating states (810). Results of each simulation are analyzed and used to develop one or more propagation-based fault detection and discrimination strategies (147) that can be used to identify faults in each of the identified operating states (815). The strategies may further be used to select an optimal set of sensors (155) to assist with fault detection.

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Background/Summary

CROSS-REFERENCE TO RELATED APPLICATIONS (1) This application is a U.S. National Stage application filed under 35 U.S.C. § 371 of PCT/US2022/015464 filed Feb. 7, 2022, which claims the benefit of priority to U.S. Provisional Application No. 63/171,699 filed Apr. 7, 2021, each of which is hereby incorporated herein by reference in their entirety.

BACKGROUND

(1) Sensor selection for sensor deployment strategy optimization is critical in designing a high-performance monitoring system for fault detection and isolation. Generally, fault detection and isolation uses the features of system behaviors (signal responses) in the monitored system under nominal and faulty states. At the system design stage, due to the lack of operating data, qualitative or quantitative models are employed for generating the system's behavioral features. However, to cover a wide range of different types of faults and obtain the system behaviors under these faulty states, a large number of simulations based on numerical models (e.g., computational fluid dynamics) are required, which may generate an overwhelming amount of data.

(2) It is with respect to these and other considerations that the various aspects and embodiments of the present disclosure are presented.

SUMMARY

(3) A model is created of a system to be monitored. Operating states of the monitored system, including steady and transient states, are identified. Faults are injected into the model and the model is used to simulate each of the identified operating states. Results of each simulation are analyzed and used to develop one or more propagation-based fault detection and discrimination

strategies that can be used to identify faults in each of the identified operating states. The strategies may further be used to select an optimal set of sensors to assist with fault detection.

(4) In an embodiment, a method is provided. The method includes: generating a model of a system by a computing device; simulating the system using the model in each operating state of a plurality of operating states by the computing device; and based on the simulations, generating a propagation-based fault detection and discrimination (“PFDD”) strategy for each operating state by the computing device.

(5) Embodiments may include some or all of the following features. The method may further include: determining a current operating state of the plurality of operating states of the system; and detecting and discriminating one or more faults in the system using the PFDD strategy generated for the current operating state. Generating the model may include generating a quantitative model and an algebraic model. The quantitative model may be generated using differential equations. The algebraic model is generated from the quantitative model using discretization methods. Simulating the system using the model in each operating state of a plurality of operating states may include repeatedly simulating the system using the generated algebraic model for a plurality of iterations. A different fault may be introduced into the simulation at each iteration of the plurality of iterations. The plurality of operating states may include steady states and transient states, and generating the PFDD strategy for a transient state may include: generating a plurality of fault feature matrices based on the simulation of the transient state for each of a plurality of faults; determining a plurality of unique subcases for each fault based on the fault feature matrices; defining one or more D-classes for each unique subcase of the plurality of unique subcases; generating a reduced fault feature matrix from the defined one or more D-Classes for each unique subcase of the plurality of unique subcases; generating one or more diagnosis strategies matrices based on the reduced fault feature matrix; and determining the PFDD strategy for the transient state based on the one or more diagnosis strategies matrices. Generating the PFDD strategy for a steady state may include: generating a plurality of fault feature matrices based on the simulation of the steady state for each of a plurality of faults; defining one or more D-classes for each pair of faults of the plurality of faults; generating one or more D-class feature matrices from the defined one or more D-classes; generating one or more diagnosis strategies matrices based on the one or more D-class feature matrices; and determining the PFDD strategy for the steady state based on the one or more diagnosis strategies matrices. Simulating the system using the model in an operating state of the plurality of operating states may include: determining a plurality of faults associated with the system; and for each fault of the plurality of faults, injecting the fault into the model and simulating the system using the model with the injected fault for the operating state. The method may further include: determining one or more propagation features related to each fault of the plurality of faults based on the simulations; and generating the PFDD strategy for each operating state based on the determined one or more propagation features. Generating a PFDD strategy for an operating state may include: generating one or more fault feature matrices for the operating state; generating one or more D-class feature matrices based on the one or more fault feature matrices; generating one or more diagnosis strategy matrices based on the one or more D-class feature matrices; and generating the PFDD strategy for the operating state based on the one or more diagnosis strategy matrices.

(6) In an embodiment, a method is provided. The method may include: generating a model of a system by a computing device, wherein the model includes a plurality of variables; simulating the system using the model in each operating state of a plurality of operating states by the computing device; and based on the simulations, selecting an optimal subset of the plurality of variables.

(7) Embodiments may include some or all of the following features. Simulating the system using the model in an operating state of the plurality of operating states may include: determining a plurality of faults associated with the system; and for each fault of the plurality of faults, injecting the fault into the model and simulating the system using the model with the injected fault for the operating state; and generating one or more fault feature matrices for the operating state. The

method may further include selecting the optimal subset of the plurality of variables using the one or more fault feature matrices. The method may further include selecting the optimal subset of the plurality of variables using the one or more fault feature matrices using a genetic algorithm. The method may further include selecting one or more sensors based on the optimal subset of the plurality of variables. The method may further include monitoring one or more signals of the system using the selected one or more sensors.

(8) In an embodiment, a first system is provided. The first system includes at least one computing device; and a computer readable medium storing computer executable instructions that when executed by the at least one computing device cause the at least one computing device to: generate a model of a second system; simulate the second system using the model in each operating state of a plurality of operating states; and based on the simulations, generate a PFDD strategy for each operating state.

(9) Embodiments may include some or all of the following features. The first system may further include computer executable instructions that when executed by the at least one computing device cause the at least one computing device to: determine a current operating state of the plurality of operating states of the second system; and detect and discriminate one or more faults in the second system using the PFDD strategy generated for the current operating state.

(10) This summary is provided to introduce a selection of concepts in a simplified form that are further described below in the detailed description. This summary is not intended to identify key features or essential features of the claimed subject matter, nor is it intended to be used to limit the scope of the claimed subject matter.

Description

BRIEF DESCRIPTION OF THE DRAWINGS

(1) The foregoing summary, as well as the following detailed description of illustrative embodiments, is better understood when read in conjunction with the appended drawings. For the purpose of illustrating the embodiments, there is shown in the drawings example constructions of the embodiments; however, the embodiments are not limited to the specific methods and instrumentalities disclosed. In the drawings:

(2) FIG. 1 is an illustration of an environment for creating propagation-based fault detection and discrimination (“PFDD”) strategies and for selecting sensors for a monitored system;

(3) FIG. 2 is an illustration of an example Integrated System Failure Analysis (“ISFA”) model;

(4) FIG. 3 is an illustration of a discrimination class (“D-class”) derivation mode matrix generated from a deviation mode matrix;

(5) FIG. 4 is an illustration of the generation of the diagnosis strategy matrices including a deviation strategy matrix, a variation strategy matrix, and a time order strategy matrix;

(6) FIG. 5 is an illustration of an example PFDD strategy;

(7) FIG. 6 is an illustration of example feature matrices;

(8) FIG. 7 is an illustration of an example method for generating one or diagnosis strategy matrices;

(9) FIG. 8 is an illustration of an example method for generating one or more PFDD strategies;

(10) FIG. 9 is an illustration of an example method for selecting one or more sensors to monitor a system for faults; and

(11) FIG. 10 shows an exemplary computing environment in which example embodiments and aspects may be implemented.

DETAILED DESCRIPTION

(12) This description provides examples not intended to limit the scope of the appended claims. The figures generally indicate the features of the examples, where it is understood and appreciated that like reference numerals are used to refer to like elements. Reference in the specification to

“one embodiment” or “an embodiment” or “an example embodiment” means that a particular feature, structure, or characteristic described is included in at least one embodiment described herein and does not imply that the feature, structure, or characteristic is present in all embodiments described herein.

(13) FIG. 1 is an illustration of an environment **100** for creating propagation-based fault detection and discrimination (“PFDD”) strategies and for selecting sensors for a monitored system. As shown, the monitored system **110** includes one or more components **111**. The one or more components **111** may receive and/or generate one or more signals **113**. The signals **113** may include both input signals **113** and output signals **113**. In addition, while not shown, each component **111** may receive signals **113** from, and may provide signals **113** to, other components **111** of the system **110**. Example systems include industrial systems such as power generation systems. Example signals **113** include signals **113** related to materials (e.g., water), energy, heat, electricity, and fuel. Other types of signals **113** may be supported.

(14) In order to monitor the system **110** and to determine if the system **110** is in a nominal state (i.e., acting or performing as planned) or if the system is in a faulty state (i.e., not acting or performing as planned), the environment **100** may use one or more sensors **155**. Each sensor **155** may be capable of measuring one or more signals **113** generated by the components **111** of the system **110**. Example of sensors **155** include temperature sensors, pressure sensors, electrical sensors, and optical sensors. Other types of sensors **155** may be supported.

(15) While sensors **155** are an effective way to monitor systems **110**, determining the optimal sensors **155** and sensor locations, to perform the monitoring is an ongoing problem. The use of sensors **155** can be expensive in both monitoring and collecting the data generated by the sensors **155**, as well as the cost of the sensors **155** themselves.

(16) Accordingly, to determine the amount and placement of sensors **155** needed to monitor a system **110**, the environment **100** includes the sensor optimizer **120**. The sensor optimizer **120** may select one or more sensors **155** using what is referred to herein as a PFDD method. As shown, the sensor optimizer **120** includes several components including, but not limited to, a model engine **130**, a PFDD engine **140**, and a sensor engine **150**. The sensor optimizer **120**, and some or all of the components **130**, **140**, and **150** may be implemented together or separately using one or more general purpose computing devices such as the computing device **1000** illustrated with respect to FIG. 10.

(17) The model engine **130** may generate one or more models that describe the operation of the monitored system **110**. The model engine **130** may generate two types of models, one or more system models **135** and one or more ISFA models **137**. A system model **135** of a monitored system **110** may be a complex model that is generated by the model engine **130** using the laws of physics and knowledge about the operation of the one or more components **111** of the system **110**. For example, the model engine **130** may use existing materials that describe the components **111** of the system including manuals, schematics, and diagrams. These materials may have been created as part of the creation of the system **110**. Depending on the embodiment, the system model **135** may be a quantitative model. Other types of models may be used.

(18) The model engine **130** may generate the ISFA model **137** from the system model **135**. The ISFA model **137** may be an algebraic model and may include a variable for each signal **113** and may include linear piecewise approximations representing the changes in the signals **113** of the system **110** under both transient and steady operational states. Depending on the embodiment, the model engine **130** may generate the ISFA model **137** from the system model **135** by running or simulating the model **135** under both transient and operational states. The model engine **130** may record the values of the signals **113** generated by the system model **135** over time and may use the recorded values to generate the ISFA model **137**. In some embodiments, the model engine **130** may discretize the system model **135** to create the ISFA model **137**. Suitable discretization methods include the Euler method and the Runge-Kutta method. Other discretization methods may be used.

(19) The PFDD engine **140** may use the ISFA model **137** to infer trends of signal changes (i.e., increases or decreases) in different system states. In some embodiments, the signal engine **140** may simulate the system **110** using the ISFA models **137** and may use ISFA to deduce signal changes transferred among the various component **111** of the system **110** during the simulation. Based on the signal changes, trends of signal deviations (e.g., higher or lower than normal) and variations (e.g., increase or decrease) under different fault states can be generated. These trends may be used to determine one or more PFDD strategies **175**.

(20) The sensor engine **150** may select a set of sensors **155** that can detect and identify most types of faults in the system **110**. In some embodiments, the sensor engine **150** may use an optimization algorithm that chooses the set of sensors **155** that satisfy minimum deployment costs (e.g., the minimum number of sensors **155**). In some embodiments, a genetic optimization algorithm is used. Other optimization algorithms may be used. The sensors **155** may be selected based in part on the PFDD strategies **147**.

(21) The model engine **130** may create the ISFA model **137** using an iterative process where first an accurate system model **135** is created of the system **110**. The system model **135** is used to create the ISFA model **137**, and the ISFA model **137** is then evaluated and adjusted as necessary.

(22) In some embodiments, the ISFA model **137** may be generated using an ISFA technique. ISFA is an integrated tool for system modeling and fault analysis. ISFA constructs the ISFA model **137** based on the physical rules among system **110** components **111** and the logic among system functions. ISFA performs the failure analysis of hardware and software systems during the design stages of that system **110**.

(23) The ISFA model **137** consists of two parts: a component model and a function model. The component model defines the components **111** in a system **110** and depicts their connections. The function model defines the functions of the components **111** and the system **110**.

(24) For each component **111**, ISFA uses behavioral rules (“BR”) derived from qualitative physics to define components' behaviors in the normal and faulty conditions qualitatively. A functional failure logic (“FFL”) may be defined for each function to infer the state of that function based on the states of components and infer the state of system functions. The simulation of an ISFA model **137** is a discrete-time simulation integrated with an automatic reasoning capability. When a fault is injected into a component **111** of the ISFA model **137**, the behavioral rules of the component **111** are executed. Based on the links between components **111**, the behavioral rules of the related components are executed in sequence. Concurrently, the functional states of the components **111** and the system **110** (e.g., operational, degraded, or lost) are assessed by the FFLs. The propagation path of the fault, the set of components **111** affected by the fault, and the abnormal behaviors of the affected components **111** are attained through the simulation process. The qualitative values of system variables in the fault condition are analyzed and compared with those in the normal condition.

(25) The outputs of the simulation of the ISFA model **137** are the effects of faults through the components **111** of the system **110**. The PFDD engine **140** (described further below) utilizes these outputs to generate one or more fault features **145**. In some embodiments, the fault features **145** may be two lists of vectors. The first list of vectors is a list of deviation index vectors. A deviation index is the direction of the deviation of a variable at a time point in the simulation process of a fault. For example, if a tank is leaking, its water level is decreasing. There is a negative deviation of the water level from its expected value. The deviation index for the water level is “negative”. A deviation index vector lists the deviation index of the variable at all time points during a simulation of the system **110**. The fault features **145** includes deviation index vectors of all system variables of the ISFA model **137**.

(26) The second list of vectors in the fault features **145** is a list of variation index vectors. A variation index is the trend of the variation of a variable at a time point in the simulation process. A variation index vector lists the variation index of the variable at all time points. The second output

lists the variation index vectors of all system variables.

(27) An ISFA model **137** can be simulated by the PFDD engine **140** in both steady states and transient states. When simulating the ISFA model **137**, the PFDD engine **140** may inject a fault into the simulation. The injected fault may reveal the propagation features of related to the injected fault. These propagation features may be used to detect and discriminate system faults by the PFDD engine **140**, and to ultimately select sensors **155** by the sensor engine **150**.

(28) In some embodiments, the variables of a system **110** are the measurable quantities that characterize the state of a system (e.g., the pressure of a vessel, and the temperature of the water in a tank). These variables may correspond to the signals **113** of the components **111**.

(29) In the ISFA model **137**, the complete set of variables identified in the system **110** is denoted as CV. CV consists of the set of observable variables V and the set of unobservable variables U. Assume that sensors **155** have been placed to monitor a set of observable variables which are $\{v_{\text{sub}.1}, v_{\text{sub}.2}, v_{\text{sub}.i} \dots, v_{\text{sub}.m}\}$. The m variables are called observed variables. The observations of the m variables are used to detect and discriminate faults. The m variables are denoted in a vector $\{\vec{v}\} = [v_{\text{sub}.1}, v_{\text{sub}.2}, \dots v_{\text{sub}.i} \dots, v_{\text{sub}.m}]$ where $i \in [1, m]$.

(30) A system fault or fault may be defined as the failure of one or multiple system components **111** at the same time. Assume that the system **110** is subjected to n potential faults which are $\{f_{\text{sub}.1}, f_{\text{sub}.2}, \dots f_{\text{sub}.j} \dots, f_{\text{sub}.n}\}$. In the ISFA model **137** model, the system **110** is simulated in the fault $f_{\text{sub}.j}$ condition if a fault $f_{\text{sub}.j}$ is injected into the system **110**. The system **110** is in normal condition if there is no fault injected. In order to simplify the expression, the fact that no fault is in the system **110** may be generalized as a special “fault” $f_{\text{sub}.0}$. The fault $f_{\text{sub}.0}$ condition is equivalent to the normal condition. The potential faults $\{f_{\text{sub}.1}, f_{\text{sub}.2}, \dots f_{\text{sub}.j} \dots, f_{\text{sub}.n}\}$ and the generalized fault $f_{\text{sub}.0}$ can be denoted in a fault vector $\{\vec{f}\} = [f_{\text{sub}.0}, f_{\text{sub}.1}, \dots f_{\text{sub}.j} \dots, f_{\text{sub}.n}]$ where $j \in [0, n]$.

(31) The PFDD engine **140** may identify the operating states of the system **110**. The system **110** has steady states and transient states. A steady state is a state where system variables do not change over time. In a transient state, at least one variable changes over time. If the system **110** is in a steady state, the system behaviors in a fault condition do not depend on the time at which the fault is injected. If the system **110** is in a transient state, the system may behave differently when a fault occurs at a different time of the transient state.

(32) The PFDD engine **140** may simulate the system **110** in each operating state using the ISFA model **137** for each fault condition. In each simulation, the PFDD engine **140** assesses the qualitative value of each system **110** variable at a series of discrete time points. The time points at which the model is simulated as a time vector $\{\vec{t}\} = [t_{\text{sub}.1}, t_{\text{sub}.2}, \dots t_{\text{sub}.q} \dots, t_{\text{sub}.p}]$ where $q \in [1, p]$. If the model **137** is simulated with the fault $f_{\text{sub}.j}$ condition, the qualitative value of a variable $v_{\text{sub}.i}$ at a time point $t_{\text{sub}.q}$ is represented as $v_{\text{sub}.j.\text{sup}.i}(t_{\text{sub}.q})$. Each simulation outputs a list of deviation index vectors and a list of variation vectors (i.e., the fault features **145**) which are defined below.

(33) The deviation of a variable is the difference between its value in a fault condition and its value in the normal condition. Since the ISFA model **137** simulates the system **110** qualitatively, the deviation of a variable in a fault condition is represented using a deviation index.

(34) The deviation index $\theta_{\text{sub}.j.\text{sup}.i}(t_{\text{sub}.q})$ represents the direction of the deviation of a variable $v_{\text{sub}.i}$ in the fault $f_{\text{sub}.j}$ condition at the time point $t_{\text{sub}.q}$. The deviation index $\theta_{\text{sub}.j.\text{sup}.i}(t_{\text{sub}.q})$ is defined in equation (1) where ε is a pre-defined threshold.

$$(35) \quad \theta_{\text{sub}.j.\text{sup}.i}(t_{\text{sub}.q}) = \begin{cases} 0, & \text{if } v_{\text{sub}.j.\text{sup}.i}(t_{\text{sub}.q}) \in [v_0^i(t_{\text{sub}.q}) - \varepsilon, v_0^i(t_{\text{sub}.q}) + \varepsilon] \\ 1, & \text{if } v_{\text{sub}.j.\text{sup}.i}(t_{\text{sub}.q}) \in (v_0^i(t_{\text{sub}.q}) + \varepsilon, +\infty) \\ 2, & \text{if } v_{\text{sub}.j.\text{sup}.i}(t_{\text{sub}.q}) \in (-\infty, v_0^i(t_{\text{sub}.q}) - \varepsilon) \end{cases} \quad (1)$$

- (36) The deviation index vector $\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}}$ consists of the deviation indexes of a variable $v_{\text{sub.i}}$ at all time-points in the fault $f_{\text{sub.j}}$ condition and can be denoted as $\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}} = [\theta_{\text{sub.j.sup.i}}(t_{\text{sub.1}}), \theta_{\text{sub.j.sup.i}}(t_{\text{sub.2}}), \dots, \theta_{\text{sub.j.sup.i}}(t_{\text{sub.q}}) \dots \theta_{\text{sub.j.sup.i}}(t_{\text{sub.p}})]$.
- (37) An example of deviation index vector for $v_{\text{sub.i}}$ is $[\theta, 0, 1, 1, 2, 2]$, which tells that the variable does not change at the first two points, then its values are higher than the expected value at the following two time points. The values of the variable $v_{\text{sub.i}}$ are below the expected values at the last two time points.
- (38) The deviation index vector of $v_{\text{sub.i}}$ in the normal condition (fault $f_{\text{sub.0}}$ condition) is $\{\text{right arrow over } (\theta)\}_{\text{sub.0.sup.i}} = [\theta_{\text{sub.0.sup.i}}(t_{\text{sub.1}}), \theta_{\text{sub.0.sup.i}}(t_{\text{sub.2}}), \dots, \theta_{\text{sub.0.sup.i}}(t_{\text{sub.q}}), \dots, \theta_{\text{sub.0.sup.i}}(t_{\text{sub.p}})]$ where $\theta_{\text{sub.0.sup.i}}(t_{\text{sub.q}}) = 0$ for all $q \in [1, p]$.
- (39) The variation of a variable at a time point is defined as the difference between its value at the current time point and that at the previous time point. The variation index is used to qualitatively represent the trend of the variation of a variable.
- (40) The variation index of $\delta_{\text{sub.j.sup.i}}(t_{\text{sub.q}})$ represents the trend of the variation of a variable $v_{\text{sub.i}}$ at the time point $t_{\text{sub.q}}$ in a fault $f_{\text{sub.1}}$ condition. The variation index $\delta_{\text{sub.j.sup.i}}(t_{\text{sub.q}})$ is defined by comparing $v_{\text{sub.j.sup.i}}(t_{\text{sub.q}})$ and $v_{\text{sub.j.sup.i}}(t_{\text{sub.q-1}})$ as equation (2) where ε is a pre-defined threshold and $v_{\text{sub.j.sup.i}}(t_{\text{sub.0}})$ is the initial value of the variable $v_{\text{sub.i}}$ in the fault $f_{\text{sub.1}}$ condition.

$$(41) \quad \delta_{\text{sub.j.sup.i}}(t_q) = \begin{cases} 0, & \text{if } v_j^i(t_q) \in [v_j^i(t_{q-1}) - \varepsilon, v_j^i(t_{q-1}) + \varepsilon] \\ 1, & \text{if } v_j^i(t_q) \in (v_j^i(t_{q-1}) + \varepsilon, +\infty) \\ 2, & \text{if } v_j^i(t_q) \in (-\infty, v_j^i(t_{q-1}) - \varepsilon) \end{cases} \quad (2)$$

- (42) The variation index vector $\{\text{right arrow over } (\delta)\}_{\text{sub.j.sup.i}}$ consists of the variation index of the variable $v_{\text{sub.i}}$ at all time points in a fault $f_{\text{sub.j}}$ condition, i.e., $\{\text{right arrow over } (\delta)\}_{\text{sub.j.sup.i}} = [\delta_{\text{sub.j.sup.i}}(t_{\text{sub.1}}), \delta_{\text{sub.j.sup.i}}(t_{\text{sub.2}}), \dots, \delta_{\text{sub.j.sup.i}}(t_{\text{sub.q}}) \dots \delta_{\text{sub.j.sup.i}}(t_{\text{sub.p}})]$.
- (43) Given an operating state, the PFDD engine **140** generates the deviation index vectors and variation index vectors for all variables in each fault condition as the fault features **145**. The PFDD engine **140** may use the fault features **145** to develop the PFDD strategies **147** for the system.
- (44) To ensure that the PFDD **147** strategies developed by the PFDD engine **140** are effective, the deviation and variation index vectors generated in each fault condition shall be accurate (i.e., consistent with experimental data or data generated by a high-order system model **135** which is time consuming for simulation). Given an ISFA model **137**, the accuracy of results obtained through its simulation is significantly impacted by the pre-defined threshold E .
- (45) The PFDD engine **140** may generate a plurality of PFDD strategies **147** for each operating state of the system **110**. The PFDD engine **140** may use a different method to generate the PFDD strategy **147** for an operating state depending on whether the operating state is a steady state or a transient state.
- (46) If the system **110** is in a steady state, the behaviors of the system **110** in a fault condition do not depend on the time at which the fault is injected. Assuming that a fault is injected at the time point $t_{\text{sub.1}}$ in the simulation process, in each fault condition, the deviation index vectors and variation index vectors can be generated by the PFDD engine **140** simulating the ISFA model **137**.
- (47) From those vectors of the fault features **145**, a set of features of system variables are extracted to characterize the process of propagation of the fault. The propagation features of system variables used herein include 1) the directions by which the system variables deviate from their expected values, 2) the trends with which the system variables vary over time, and 3) the order in which each variable is influenced during the propagation of a fault.
- (48) The fault features **145** of all system variables in all fault conditions are summarized using

three fault feature matrices **146** which are the deviation mode matrix, variation mode matrix, and time order matrix. The criteria by which a fault can be detected and discriminated in a steady state are formulated using those matrices. The PFDD strategy **147** in a steady state is then developed accordingly.

(49) The deviation mode matrix summarizes the directions by which the system variables deviate from their expected values in all fault conditions. The deviation mode matrix is constructed based on the deviation index vectors from the fault features **145**. The procedure used to construct the deviation mode matrix is described below.

(50) A deviation index vector $\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}}$ may contain a series of consecutive repetitive deviation indexes if the variable $v_{\text{sub.i}}$ has the same direction of deviation over a period of time for the fault $f_{\text{sub.j}}$ condition. For example, a deviation index vector $\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}} = [0, 0, 1, 1, 2, 2]$ which tells that the variable does not deviate from normal in the first two time points, deviates positively from normal in the next two time points and deviates negatively from normal in the last two time points. However, the time points do not represent the accurate time in a real system. The consecutive repetition of a deviation index does not provide more information than a single deviation index in terms of direction of deviation. To abstract the main deviation features of a deviation index vector, the deviation feature vector and derivation mode are defined.

(51) A deviation feature vector $\{\text{right arrow over } (d)\}_{\text{sub.j.sup.i}}$ abstracts the main deviation features of the variable $v_{\text{sub.i}}$ in the fault $f_{\text{sub.j}}$ condition by merging the consecutive repetitive deviation indexes in $\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}}$. Vector $\{\text{right arrow over } (d)\}_{\text{sub.j.sup.i}}$ can be generated from $\delta_{\text{sub.j.sup.i}}$ using a duplication removal function $F_{\text{sub.DR}}(\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}})$ as given in Equation (3) where $F_{\text{sub.DR}}(\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}})$ removes the elements in $\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}}$ whose value is equal to its left side neighbor. For example, the deviation feature vector $\{\text{right arrow over } (d)\}_{\text{sub.j.sup.i}}$ for the deviation index vector $\{\text{right arrow over } (\theta)\}_{\text{sub.j.sup.i}} = [\theta, 0, 1, 1, 2, 2]$ is $\{\text{right arrow over } (d)\}_{\text{sub.j.sup.i}} = [\theta, 1, 2]$.

$$\text{.fwdarw.}_j^i = F_{\text{DR}}(\text{.fwdarw.}_j^i) = [\text{.}_j^i(t_{q_1}), \text{.}_j^i(t_{q_2}), \text{.Math.}\theta_j^i(t_{q_x}), \text{.Math.}, \text{.}_j^i(t_{q_y})], x \in [1, y] \quad (3)$$

(53) Each deviation index vector generates a deviation feature vector. Since the length of different deviation feature vectors might be different, the deviation mode is defined to simplify and unify the representations of the deviation feature vectors.

(54) A deviation mode is a positive integer used to represent a deviation feature vector. The deviation mode $D_{\text{sub.j.sup.i}}$ is used to represent the deviation feature vector $\{\text{right arrow over } (d)\}_{\text{sub.j.sup.i}}$. $D_{\text{sub.j.sup.i}}$ can be calculated using equation (4).

$$D_j^i = \text{.Math.}_{x=1}^y \text{.}_j^i(t_{q_x}) * 3^{y-x} \quad (4)$$

(56) Since $\theta_{\text{sub.j.sup.i}}(t_{\text{sub.qx}}) \in \{0, 1, 2\}$, $\{\text{right arrow over } (d)\}_{\text{sub.j.sup.i}}$ can be regarded as a ternary integer, equation (4) essentially calculates the decimal value of $\{\text{right arrow over } (d)\}_{\text{sub.j.sup.i}}$. The deviation mode has the following features: 1) the deviation modes of two different deviation feature vectors are different, 2) the deviation mode of the normal condition (i.e. $\{\text{right arrow over } (d)\}_{\text{sub.0.sup.i}} = [0]$) is $D_{\text{sub.0.sup.i}} = 0$, 3) given a deviation mode, the associated deviation feature vector can be generated by converting the decimal value of the deviation mode to the ternary value. Given the deviation mode of all variables in all fault conditions, a deviation mode matrix can be constructed by the PFDD engine **140**.

(57) The deviation mode of all variables in all fault conditions can be collected in a $(n+1) \times m$ deviation mode matrix D , where $D_{\text{sub.j.sup.i}}$ is the deviation mode of the variable $v_{\text{sub.i}}$ in the fault $f_{\text{sub.j}}$ condition, $n+1$ is the number of faults in $\{\text{right arrow over } (f)\}$ (including n faults and

the normal condition $f_{\text{sub}.0}$, m is the number of observed variables in $\{\text{right arrow over } (v)\}$. It should be noted that $D_{\text{sub}.0.\text{sup}.i}=0$ for all $i \in [1, m]$ since $f_{\text{sub}.0}$ is the normal condition.

(58) The variation mode matrix summarizes the trends with which the system **110** variables vary overtime in all fault conditions. The variation mode matrix may be constructed by the PFDD engine **140** based on the variation index vectors of the fault features **145**. The procedure followed to construct the variation mode matrix is described below.

(59) For each variation index vector, a variation feature vector is first generated to abstract the main variation features. A variation feature vector $\{\text{right arrow over } (c)\}_{\text{sub}.j.\text{sup}.i}$ abstracts the main variation features of the variable $v_{\text{sub}.i}$ in the fault $f_{\text{sub}.j}$ condition by merging consecutive repetitive deviation indexes in $\delta_{\text{sub}.j.\text{sup}.i}$, $\{\text{right arrow over } (c)\}_{\text{sub}.j.\text{sup}.i}$ can be defined using the duplication removal function as defined in equation (5).

$$(60) \quad \text{fwdarw.}^i_j C_j = F_{\text{DR}}(\text{fwdarw.}^i_j) = [\text{ }^i_j(t_{q_1}), \text{ }^i_j(t_{q_2}), \text{Math. }^i_j(t_{q_x}), \text{Math. }^i_j(t_{q_y})], x \in [1, y] \quad (5)$$

(61) The variation mode is then defined to simplify and unify the representations of the variation feature vectors. A variation mode $C_{\text{sub}.j.\text{sup}.i}$ is an integer used to represent the variation feature vector $\{\text{right arrow over } (c)\}_{\text{sub}.j.\text{sup}.i}$. $C_{\text{sub}.j.\text{sup}.i}$ can be calculated using the equation (6).

$$(62) \quad C_j^i = \text{Math.}_{x=1}^y \text{ }^i_j(t_{q_x}) * 3^{y-x} \quad (6)$$

(63) The variation mode has the following features: 1) the variation modes of two different variation feature vectors are different, 2) given a variation mode, the associated variation feature vector can be generated by converting the decimal value of the variation mode to the ternary value. Given the variation mode of all variables in all fault conditions, the variation mode matrix can be constructed.

(64) The variation mode of all variables in all fault conditions can be displayed in a $(n+1) \times m$ matrix C , where $C_{\text{sub}.j.\text{sup}.i}$ is the variation mode of the variable $v_{\text{sub}.i}$ in the fault $f_{\text{sub}.j}$ condition. Based on the definition of deviation mode and variation mode, a proposition **1** is defined that can be used later to define the criteria for fault detection and discrimination: If the variation mode of a variable $v_{\text{sub}.i}$ in the fault $f_{\text{sub}.j}$ condition is not equal to its variation mode in the normal condition, the deviation mode of $v_{\text{sub}.i}$ in the fault $f_{\text{sub}.j}$ condition is not zero (i.e., If $C_{\text{sub}.j.\text{sup}.i} \approx C_{\text{sub}.0.\text{sup}.i}$, then $D_{\text{sub}.j.\text{sup}.i} \approx 0$).

(65) When a fault $f_{\text{sub}.j}$ occurs in the system **110**, variables start to deviate in a particular sequence as the fault propagates. The chronological order in which the variables start to deviate during the process of propagation of the fault $f_{\text{sub}.j}$ can also be used to discriminate $f_{\text{sub}.j}$ from the other faults. The time order matrix is introduced further below.

(66) FIG. 2 is used as an illustrative example. In FIG. 2, two variables, i.e. $v_{\text{sub}.1}$ and $v_{\text{sub}.2}$, are defined in an ISFA model **137**. In the fault $f_{\text{sub}.j}$ condition, the deviation index vectors for the two variables are: $\{\text{right arrow over } (\theta)\}_{\text{sub}.j.\text{sup}.1}=[0, 0, 1, 1, 2, 2]$, $\{\text{right arrow over } (\theta)\}_{\text{sub}.j.\text{sup}.2}=[0, 2, 2, 2, 1, 1]$.

(67) To obtain the time order of the variables, the time point at which a variable starts to deviate from normal is first identified by the PFDD engine **140**. The deviation start time of a variable is defined below.

(68) The deviation start time $o_{\text{sub}.j.\text{sup}.i}$ is the index of the time point at which the variable $v_{\text{sub}.i}$ starts to deviate in the fault $f_{\text{sub}.j}$ condition. $o_{\text{sub}.j.\text{sup}.i}$ can be obtained based on the deviation index vector $\{\text{right arrow over } (\theta)\}_{\text{sub}.j.\text{sup}.i}$ as defined in equation (7).

$$(69) \quad o_j^i = \begin{cases} q & \text{if } t_q \text{ is the first time point at which } \text{ }^i_j(t_q) \neq 0 \\ +\infty & \text{if } \forall x \in [0, p] \text{ }^i_j(t_x) = 0 \end{cases} \quad (7)$$

(70) For the example ISFA model **137** of FIG. 2, the deviation start time of the two variables are

o.sub.j.sup.1=3 and o.sub.j.sup.2=2 since v.sub.1 and v.sub.2 start to deviate at the third time point and the second time point respectively.

(71) Given the deviation start time of all variables in a fault condition, the order in which all variables start to deviate can be obtained by the PFDD engine **140**. The time order of each variable is defined below.

(72) The time order of a variable v.sub.i in the fault f.sub.j condition is denoted as O.sub.j.sup.i where O.sub.j.sup.i-1 is the number of variables that start to deviate before v.sub.i starts to deviate. In the example of FIG. 2, the time order of variable v.sub.1 is O.sub.j.sup.1=2. The time order of variable v.sub.2 is O.sub.j.sup.2=1. The time order of a variable v.sub.i in the normal condition is O.sub.0.sup.i=0. Given the time order of all variables in all fault conditions, the time order matrix can be constructed.

(73) Time order matrix O is a (n+1)×m matrix, where O.sub.j.sup.i is the time order of variable v.sub.i in the fault f.sub.j condition. The following proposition 2 can be derived based on the definition of time order. If there exists a variable v.sub.i that has the feature O.sub.j.sub.1.sup.i≈O.sub.j.sub.2.sup.i, the faults f.sub.j.sub.1 and f.sub.j.sub.2 can be discriminated from each other. The criteria necessary and sufficient for a fault to be detected are given in the following proposition 3. A fault f.sub.j(j∈[1, n]) can be detected if and only if ∃i∈[1,m] such that D.sub.j.sup.i≈0.

(74) Faults can be discriminated using the fault feature matrices, i.e., D, C, and O. The following proposition 4 defines the criteria under which a fault can be discriminated.

(75) Two faults f.sub.j.sub.1 and f.sub.j.sub.2 (j.sub.1, j.sub.2∈[1, n]) can be discriminated from each other if and only if ∃i∈[1, m], O.sub.j.sub.1.sup.i≈O.sub.j.sub.2.sup.i or D.sub.j.sub.1.sup.i≈D.sub.j.sub.2.sup.i or C.sub.j.sub.1.sup.i≈C.sub.j.sub.2.sup.i.

(76) Based on proposition 4, two faults can be discriminated from each other as long as there is a variable whose deviation mode, variation mode, or time order is different in the two fault conditions. The following proposition 5 integrates the criteria under which a fault can be detected and discriminated. Detecting a fault is equivalent to discriminating a fault from the normal condition. (i.e., a fault f.sub.j can be detected if and only if it can be discriminated from f.sub.0).

(77) Based on proposition 5, detection and discrimination of a fault f.sub.j(j∈[1, n]) is equivalent to discriminating f.sub.j from all the other faults in {right arrow over (f)} (including f.sub.0). Since there may be faults that cannot be discriminated from each other, the discrimination classes of the faults are defined to classify the non-distinguishable faults.

(78) A D-class in a steady state is a set of faults in {right arrow over (f)} that cannot be discriminated from each other. The number of D-classes in the steady state can be denoted as η. In a steady state, all faults that cannot be discriminated from each other are placed in one D-class. A fault f.sub.j in the D-class that contains f.sub.0 is not detectable. The number of D-classes of a system in a steady state is determined by the system's capability of detecting and discriminating faults in the steady state.

(79) The measure equivalence level of a system is defined below and used to quantify the capability of PFDD engine **140** in detecting and discriminating faults. The equivalence level of a system in a steady state is the number of faults that are not detectable or discriminable. It is defined as e=n+1-η where n+1 is the number of faults in {right arrow over (f)}, and η is the number of D-classes.

(80) Based on the criteria of detecting and discriminating a fault, the PFDD engine **140** may generate a PFDD strategy **147** in three steps. In a first step, the PFDD engine **140** may generate the D-class feature matrices based on fault feature matrices. In a second step, the PFDD engine **140** may generate the diagnosis strategy matrices based on the D-class feature matrices. Finally, in a third step the PFDD engine **140** may determine the PFDD strategy **147** using the diagnosis strategy matrices.

(81) With regards to the first step of generating the D-class feature matrices, proposition 4 specifies

that any two faults $f_{\text{sub.j.sub.1}}$ and $f_{\text{sub.j.sub.2}}$ ($j_{\text{sub.1}}, j_{\text{sub.2}} \in [1, n]$) in the same D-class satisfy the property that $\forall i \in [1, m], O_{\text{sub.j1.sub.1}}^{\text{sup.i}} = O_{\text{sub.j.sub.2.sub.1}}^{\text{sup.i}}, D_{\text{sub.j.sub.1.sub.1}}^{\text{sup.i}} = D_{\text{sub.j2.sub.1}}^{\text{sup.i}}$ and $C_{\text{sub.j.sub.1.sub.1}}^{\text{sup.i}} = C_{\text{sub.j2.sub.1}}^{\text{sup.i}}$ i.e. the rows of $f_{\text{sub.j.sub.1}}$ and $f_{\text{sub.j.sub.2}}$ in the fault feature matrices are equivalent. The dimension of the fault feature matrices can be reduced by merging the faults in the same D-class. The outputted matrices are called D-class feature matrices including the D-class deviation mode matrix, D-class variation mode matrix, and D-class time order matrix.

(82) FIG. 3 is an illustration of a D-class derivation mode matrix **310** generated from a deviation mode matrix **305**. Given the deviation mode matrix **305** on the left, the $D_{\text{class.sub.j}}$ consists of the faults $f_{\text{sub.a.sub.j.sub.1}}, f_{\text{sub.a.sub.j.sub.2}}, \dots, f_{\text{sub.a.sub.j.sub.}\eta_{\text{sub.j}}}$, where $\eta_{\text{sub.j}}$ is the number faults in $D_{\text{class.sub.j}}$. Then, the deviation mode of a variable $v_{\text{sub.i}}$ in any fault condition of $D_{\text{class.sub.j}}$ is $D_{\text{sub.a.sub.j.sub.1}}^{\text{sup.i}}$ since $D_{\text{sub.a.sub.j.sub.1}}^{\text{sup.i}} = D_{\text{sub.a.sub.j.sub.2}}^{\text{sup.i}} = \dots = D_{\text{sub.a.sub.j.sub.}\eta_{\text{sub.j}}}^{\text{sup.i}}$. The rows of the faults $f_{\text{sub.a.sub.j.sub.1}}, f_{\text{sub.a.sub.j.sub.2}}, \dots, f_{\text{sub.a.sub.j.sub.}\eta_{\text{sub.j}}}$ in the deviation mode matrix **305** are merged in the D-class deviation mode matrix **310**. In a D-class deviation mode matrix, each row represents a D-class, and each column is a variable. The D-class variation mode matrix and D-class time order matrix can be obtained following the same approach.

(83) With regards to the second step of generating the diagnosis strategy matrices, a deviation/variation mode is a compressed representation of a deviation/variation feature vector. Introducing the deviation modes and variation modes can reduce the amount of computation required to determine D-classes. However, the deviation modes and variation modes in the D-class feature matrices cannot be used directly for fault diagnosis in operation.

(84) In the second step, the PFDD engine **140** may generate the diagnosis strategy matrices by converting the deviation modes and variation modes in the D-class feature matrices back to the corresponding deviation feature vectors and variation feature vectors based on equation (4) and equation (6). The generated diagnosis strategy matrices can be used directly by the PFDD engine **140** for PFDD strategy **147** generation.

(85) FIG. 4 is an illustration of the generation of the diagnosis strategy matrices including a deviation strategy matrix **410**, a variation strategy matrix **420**, and a time order strategy matrix **430**. As shown, the deviation strategy matrix **410** is generated from a D-class deviation mode matrix **405**, the variation strategy matrix **420** is generated from a D-class variation mode matrix **415**, and the time order strategy matrix **430** is generated from a D-class time order matrix **425**.

(86) In the third step, the PFDD engine **140** may generate the PFDD strategy **147** for the steady operational state from the diagnosis strategy matrices. The deviation index vectors and variation index vectors of system variables can be obtained in real-time using the sampled signals and the predicted values of each variable. Once a deviation is observed, the deviation feature vector, variation feature vector, and time order of the variables under the current operational state can be calculated and compared with each row of the diagnosis strategy matrices.

(87) The deviation feature vector, variation feature vector, and time order of a variable $v_{\text{sub.i}}$ may be defined under the current operational state as $\{\tilde{\text{over}}(\{\text{right arrow over (d)}\})\}^{\text{sup.i}}, \{\tilde{\text{over}}(\{\text{right arrow over (c)}\})\}^{\text{sup.i}}$, and $\tilde{O}^{\text{sup.i}}$. In the deviation strategy matrix, if $\{\tilde{\text{over}}(\{\text{right arrow over (d)}\})\}^{\text{sup.i}}$ does not match the pre-defined deviation feature vector $\{\text{right arrow over (d)}\}^{\text{sub.a.sub.j.sub.1.sub.1}}^{\text{sup.i}}$, $D_{\text{class.sub.j}}$ can be eliminated from the diagnosis. $D_{\text{class.sub.j}}$ can also be eliminated from the diagnosis if $\{\tilde{\text{over}}(\{\text{right arrow over (c)}\})\}^{\text{sup.i}}$ does not match $\{\text{right arrow over (c)}\}^{\text{sub.a.sub.j.sub.1.sub.1}}^{\text{sup.i}}$ in the variation strategy matrix or $\tilde{O}^{\text{sup.i}}$ is not equal to $\tilde{O}^{\text{sub.a.sub.j.sub.1.sub.1}}^{\text{sup.i}}$ in the time order strategy matrix. The features $\{\tilde{\text{over}}(\{\text{right arrow over (d)}\})\}^{\text{sup.i}}, \{\tilde{\text{over}}(\{\text{right arrow over (c)}\})\}^{\text{sup.i}}$, and $\tilde{O}^{\text{sup.i}}$ of all observed variables are updated as time proceeds. Only one D-class will remain. The PFDD engine **140** may then determine that the system **110** suffers a fault in that D-class.

(88) FIG. 5 is an illustration of an example PFDD strategy **147**. As shown, the strategy includes

several diagnosis strategy matrices including a deviation strategy matrix **505**, a variation strategy matrix **510**, and a time order strategy matrix **515**. The system **110** corresponding to FIG. 5 has one observed variable v.sub.1 and is subjected to three faults f.sub.1, f.sub.2, and f.sub.3. In FIG. 5, the D-class **0** includes only f.sub.0 (i.e. the normal condition), D-class **1** consists of f.sub.1, D-class **2** consists of f.sub.2, and D-class **3** consists of f.sub.3.

(89) Assuming that the system corresponding to FIG. 5 samples the signals of v.sub.1 every second, in the first 3 seconds, no abnormality is observed. At the fourth second, a negative deviation and variation of v.sub.1 is observed. The deviation index vector and variation index vector observed are $[0, 0, 0, 2]$ and $[0, 0, 0, 2]$. The deviation feature vector, variation feature vector, and time order of the variable v.sub.1 under the current condition are $\{\tilde{\overrightarrow{d}}\}^{sup.1}=[0,2]$, $\{\tilde{\overrightarrow{d}}\}^{sup.1}=[0,2]$, and $\tilde{O}^{sup.1}=1$. By comparing $\{\tilde{\overrightarrow{d}}\}^{sup.1}$, $\{\tilde{\overrightarrow{c}}\}^{sup.1}$, and $\tilde{O}^{sup.1}$ to each row of the matrices in FIG. 5, D-class **0** is first excluded from the diagnosis since $\{\tilde{\overrightarrow{d}}\}^{sup.1}=[0,2]$ will not match the pre-defined deviation feature vector $\{\overrightarrow{d}\}^{sub.1}=[0]$ and $\{\tilde{\overrightarrow{c}}\}^{sup.1}=[0,2]$ will not match $\{\overrightarrow{c}\}^{sub.1}=[0]$. D-class **1** and D-class **2** are excluded for the same reason. Therefore, the system must be suffering from a fault in D-class **3**. Since there is only one fault in D-class **3**, the system **110** may be diagnosed with in a fault f.sub.3 condition.

(90) Overall, the PFDD strategy **147** for a steady state condition can be generated as follows. 1. Construct the ISFA model **137** for the steady state condition. 2. Simulate the ISFA model **137** with each fault injected into the model **137**. 3. Generate the fault features matrices from the results of the stimulation. 4. Define the D-classes of the system faults based on proposition **4** and proposition **5** by examining the discriminability of each pair of faults. 5. Derive the D-class feature matrices from the D-classes. 6. Derive the diagnosis strategy matrices from the D-class feature matrices. 7. Determine the PFDD strategy **147** from the D-class feature matrices.

(91) The PFDD engine **140** may further generate a PFDD strategy **147** when the system **110** is in a transient state. The ISFA model **137** allows simulation in a transient state. The time points at which the ISFA model **137** is simulated may be denoted as a time vector $\{\overrightarrow{t}\}=[t.sub.1, t.sub.2, \dots, t.sub.q, \dots, t.sub.p, \dots, t.sub.p]$. The transient state starts at t.sub.1 and ends at t.sub.p, if no fault is injected. The model **137** operates in a steady state after the time point t.sub.p.

(92) A fault f.sub.j can be injected by the PFDD engine **140** at a time point t.sub.q ($q \in [1, p']$) in the transient state. The results of the simulation provide the features of system **110** variables when the fault f.sub.j occurs at t.sub.q. In a transient state, the features of system **110** variables after injecting f.sub.j depend on the time at which f.sub.j is injected. The results of simulation may vary if the fault f.sub.j is injected at a different time point. Hence, the fault f.sub.j may be injected into the model **137** at a series of time points of the transient state to uncover the possible behaviors of the system **110** when the fault occurs in the transient state. The subcases of a fault condition are defined below to represent the specific cases in which the fault is injected at different time points.

(93) The system **110** is simulated by the PFDD engine **140** in the subcase .sup.jf.sub.q (of the fault f.sub.j condition) if a fault f.sub.j is injected at the time point t.sub.q in a transient state. When f.sub.j is injected at the time points $[t.sub.q1, t.sub.q2, \dots, t.sub.qk, \dots, t.sub.qs]$ in the transient state where $k \in [1, s]$, s is the number of subcases of the fault f.sub.j condition. The system **110** is simulated in the following subcases: $[.sup.jf.sub.q1, .sup.jf.sub.q2, \dots, .sup.jf.sub.qk, \dots, .sup.jf.sub.qs]$.

(94) The results of simulation are generated in each subcase of each fault condition. The fault feature matrices can be constructed accordingly. The fault feature matrices in a transient state are defined below.

(95) The outputs of simulating the ISFA model **137** in a subcase .sup.jf.sub.qk ($k \in [1, s]$ and $j \in [1, n]$) can be used to derive the deviation modes, variation modes, and time orders of all variables for

the subcase .sup.jf.sub.qk following the same steps as described previously with respect to the steady or non-transient operational state.

(96) The deviation mode matrix can be constructed by the PFDD engine **140** given the deviation mode of the variables in each subcase of each fault condition. The deviation mode matrix in a transient state is defined below and illustrated in FIG. **6** as the deviation mode matrix **605**.

(97) A deviation mode matrix in a transient state is also denoted as D. It describes the deviation modes of all variables in all subcases of all fault conditions. D is a $((n+1).Math.s) \times m$ matrix where $n+1$ is the number of faults in $\{\text{right arrow over (f)}\}$, s is the number subcases of each fault and m is the number of variables. In the deviation mode matrix **605** displayed of FIG. **6** an element $D.\text{sub.k}+j.Math.s.\text{sup.i}$ represents the deviation mode of the variable $v.\text{sub.i}$ in the subcase .sup.jf.sub.qk.

(98) The variation mode matrix and time order matrix can be constructed by the PFDD engine **140** using the variation mode and time order of the variables in each subcase of each fault condition. The variation mode matrix and the time order matrix are defined below and are illustrated in FIG. **6** as the variation mode matrix **610** and the time order matrix **615**.

(99) In a transient state, the variation mode matrix C is also a $((n+1).Math.s) \times m$ matrix. $C.\text{sub.k}+j.Math.s.\text{sup.i}$ is the variation mode of the variable $v.\text{sub.i}$ in the subcase .sup.jf.sub.qk. The time order matrix O is a $((n+1).Math.s) \times m$ matrix where $O.\text{sub.k}+j.Math.s.\text{sup.i}$ is the time order of the variable $v.\text{sub.i}$ in the subcase .sup.jf.sub.qk.

(100) Detection of a fault in a transient state is detecting the subcases of the fault conditions. Given the fault feature matrices, the criteria used to detect a subcase of a fault condition in a transient state can be defined. A subcase .sup.jf.sub.qk is detectable if and only if $\exists i \in [1, m]$ such that $D.\text{sub.k}+j.Math.s.\text{sup.i} \approx 0$. It should be noted that a fault $f.\text{sub.j}$ could be detectable in some subcases and not detectable in the other subcases.

(101) Discrimination of a fault in a transient state is to discriminate a subcase of the fault condition from the subcases of the other fault conditions. The criteria used to discriminate two subcases in a transient state are given as: Two subcases .sup.j1f.sub.qk.sub.1 and .sup.j2f.sub.qk.sub.2 can be discriminated from each other if and only if $\exists i \in [1, m]$,

$O.\text{sub.k.sub.1.sub.}+j.\text{sub.1.sub.}.Math.s.\text{sup.i} \approx O.\text{sub.k.sub.2.sub.}+j.\text{sub.2.sub.}.Math.s.\text{sup.i}$ or $D.\text{sub.k.sub.1.sub.}+j.\text{sub.1.sub.}.Math.s.\text{sup.i} \approx D.\text{sub.k.sub.2.sub.}+j.\text{sub.2.sub.}.Math.s.\text{sup.i}$ or $C.\text{sub.k.sub.1.sub.}+j.\text{sub.1.sub.}.Math.s.\text{sup.i} \approx C.\text{sub.k.sub.2.sub.}+j.\text{sub.2.sub.}.Math.s.\text{sup.i}$.

(102) Since the goal is to discriminate faults, the PFDD engine **140** only need to discriminate the subcases of different fault conditions. If two subcases of a fault $f.\text{sub.j}$ condition cannot be discriminated from each other, one subcase is considered to be redundant. Consider the subcases of a fault $f.\text{sub.j}$ condition (i.e., $\{\text{sup.jf.sub.q1}, \text{sup.jf.sub.q2} \dots, \text{sup.jf.sub.qk}, \dots, \text{sup.jf.sub.qs}\}$). A unique subcase set of the fault condition can be generated by removing the redundant subcases.

(103) The unique subcase set of a fault $f.\text{sub.j}$ is denoted as

$$(104) U_j = \{j_{f_{q_{k_1}^j}}, j_{f_{q_{k_2}^j}}, \text{Math.}, j_{f_{q_{k_x}^j}}, \text{Math.}, j_{f_{q_{k_y}^j}}, \text{Math.}, j_{f_{q_{k_z}^j}}\}$$

where 1) $z.\text{sub.j}$ is the number of elements in $U.\text{sub.j}$; 2) $\forall x, y \in [1, z.\text{sub.j}]$ and

$$(105) x \neq y, j_{f_{q_{k_x}^j}}$$

can be discriminated from

$$(106) 0j_{f_{q_{k_y}^j}}.$$

Each element in $U.\text{sub.j}$ is called a unique subcase of $f.\text{sub.j}$. The unique subcase

$$(107) j_{f_{q_{k_x}^j}}$$

is simplified as .sup.ju.sub.x in the following sections. The unique subcase set $U.\text{sub.j}$ is then $\{\text{sup.ju.sub.1}, \text{sup.ju.sub.2}, \dots, \text{sup.ju.sub.x}, \dots, \text{sup.ju.sub.z.sub.j}\}$.

(108) It should be noted that $f.\text{sub.0}$ has only one unique subcase which can be denoted as

.sup.0u.sub.1.

(109) Based on the proposition 5, detection and discrimination of a unique subcase is equivalent to discriminating the unique subcase from all the other unique subcases (including .sup.0u.sub.1). Since there can be unique subcases that cannot be discriminated from each other, D-classes in a transient state are defined.

(110) In a transient state, a D-class is a set of unique subcases that are not discriminable from each other. All unique subcases that cannot be discriminated from each other are placed in one D-class. The number of D-classes of a system is denoted as rl which indicates the system's capability in detecting and discriminating faults in the transient state. The equivalence level of a system in a transient state is defined below and can be used to assess the system's capability of detecting and discriminating faults in a transient state.

(111) The equivalence level of a system in a transient is the degree to which the system cannot detect and discriminate the unique subcases of fault conditions. The equivalence level is denoted as $e = \sum_{j=1}^{nz} z_{sub.j} - \eta$, where $z_{sub.j}$ is the number of unique subcases of a fault $f_{sub.j}$ condition, η is the number of D-classes in the transient state.

(112) Based on the criteria established to detect and discriminate a unique subcase, generating the diagnosis strategy matrices is described below. The method used is illustrated in FIG. 7 as an example.

(113) At step 1, the subcases that are not in a unique subcase set are removed from the fault feature matrices to reduce the dimension of the matrices. The deviation mode matrix **701** contains $(n+1) \cdot \text{Math.s}$ rows. Each row is corresponding to a subcase of a fault. It may be assumed that there are $z_{sub.j}$ unique subcases in the fault $f_{sub.j}$ condition. This step 1 generates a unique subcase deviation mode matrix **703** with $\sum_{j=0}^{nz} z_{sub.j}$ rows. Each row of the matrix **703** may be a unique subcase of a fault.

(114) At step 2, the unique subcases that are in the same D-class can be further merged to generate the D-class time order matrix, D-class deviation mode matrix, and D-class variation mode matrix. Consider that $D_class_{sub.j}$ consists of $\eta_{sub.j}$ unique subcases, i.e.

$\{ \text{sup.a.sub.1.sub.ju.sub.b.sub.j.sub.1}, \text{sup.aj.sub.2u.sub.b.sub.j.sub.2}, \dots, \text{sup.a.sub.j.sub.nju.sub.b.sub.j.sub.nj} \}$. The generated D-class deviation mode matrix **705** is illustrated in FIG. 7.

(115) At step 3, the diagnosis strategy matrices which can be used to generate the PFDD strategy **147** are generated. The diagnosis strategy matrices include the deviation strategy matrix, variation strategy matrix and time order strategy matrix. The deviation strategy matrix and variation strategy matrix can be generated by converting the deviation modes and variation modes of the D-class deviation mode matrix and D-class variation mode matrix into the related deviation feature vectors and variation feature vectors. The D-class deviation feature matrix **707** obtained from step 3 is illustrated in FIG. 7.

(116) Generating the PFDD strategy **147** in a transient state is similar to how the PFDD strategy **147** in a steady state is generated. In a transient state, the deviation index vector and variation index vector under the current condition of the system **110** can be obtained in real-time by the PFDD engine **140** using the sampled signals and the predicted values of each observed variable. Once a deviation of a variable is observed, the deviation feature vector, variation feature vector, and time order of the variables under the current condition can be calculated and compared with each row of the diagnosis strategy matrices.

(117) The deviation feature vector, variation feature vector, and time order of a variable $v_{sub.i}$ under the current condition are $\{\tilde{\overrightarrow{d}}\}^{sup.i}$, $\{\tilde{\overrightarrow{c}}\}^{sup.i}$, and $\tilde{O}^{sup.i}$. $D_class_{sub.j}$ can be eliminated from the diagnosis if d does not match the pre-defined deviation feature vector $\{\overrightarrow{d}\}_{sub.a.sub.j.sub.1}^{sup.i}$, does not match $\{\overrightarrow{c}\}_{sub.a.sub.j.sub.1}^{sup.i}$, or $\tilde{O}^{sup.i}$ is not equal to $O_{sub.a.sub.j.sub.1}^{sup.i}$. The features of each variable (i.e. $\{\tilde{\overrightarrow{d}}\}$

(d)}ⁱ, { $\tilde{\text{right arrow over (c)}}$ }ⁱ, and $\tilde{\text{O}}$ ⁱ are updated as time proceeds. Only one D-class will remain. The fault in the system **110** can be discriminated by relating the subcases in that D-class to the associated faults.

(118) Overall, the PFDD strategy **147** for a transient state condition can be generated as follows. 1. Construct the ISFA model **137** of the system **110** in the transient state. 2. Inject faults and simulate the model **137** in each subcase of the transient state. 3. Generate the fault feature matrices **146** (i.e., time order matrix, deviation mode matrix, and variation mode matrix) based on the results of simulation. 4. Determine the unique subcases for each fault. 5. Define the D-classes of the unique subcases of the faults. 6. Generate the reduced fault feature matrices. 7. Generate the diagnosis strategy matrices. 8. Determine the PFDD strategy **147** in the transient state.

(119) The sensor engine **150** may select an optimal set of sensors **155** by selecting an optimal subset of variables from the system **110** to monitor. The selected sensors **155** may then be placed at locations in the system **110** where the corresponding signals **113** to the variables may be best monitored.

(120) An optimal subset of variables shall satisfy two goals of sensor deployment. The primary goal is to maximize the system capability for fault detection and discrimination. The secondary goal is to minimize the cost of sensor **155** deployment. As defined before, the equivalence level can be used to measure the system's capability for fault detection and discrimination. The system's capability can be maximized by selecting a set of variables that minimize the system equivalent level.

(121) The cost of sensor deployment is directly related to the number of variables selected. For purposes of illustration, it is assumed that the costs of all sensors **155** are equal. The variable selection rate is defined below and used to assess the cost of sensor deployment for the set of variables selected.

(122) The variable selection rate is defined as the proportion of variables selected in all observable variables and denoted as γ (see equation (8)).

$$(123) \quad \gamma = \frac{\text{number of variables selected}}{\text{total number of variables}} \quad (8)$$

(124) An optimal subset of variables shall be selected using two criteria: 1) first minimize the system equivalent level, 2) then minimize the variable selection rate. A measure quality index is defined below to quantify the degree to which the variables selected satisfy the two criteria.

(125) Given a subset of variables, the quality index λ of the subset is defined as the sum of system equivalence level $e_{\text{sub.sys}}$ and the variable selection rate (i.e., $\lambda = e_{\text{sub.sys}} + \gamma$). An optimal subset of variables is a subset of variables whose quality index is minimized.

(126) Given a system **110**, the set of observable variables is defined as V . The power set of V can be defined as $P_{\text{sub}.V}$. Each element in $P_{\text{sub}.V}$ is a subset of V . $P_{\text{sub}.V}$ consists of all subsets of variables that can be generated from V . The cardinality of set V is the number of observable variables and can be denoted as $\text{card}(V)$. The cardinality of the set $P_{\text{sub}.V}$ is the number subsets that can be obtained from V and can be denoted as $\text{card}(P_{\text{sub}.V})$. Since each observable variable in V is either selected or not selected in a subset, the cardinality of $P_{\text{sub}.V}$ can be obtained as using equation 9 where $C_{\text{sub}. \text{card}(V)}^i$ is the number of combinations obtained when choosing i elements from $\text{card}(V)$ elements.

$$(127) \quad \text{card}(P_V) = \sum_{i=0}^{\text{card}(V)} C_{\text{card}(V)}^i = 2^{\text{card}(V)} \quad (9)$$

(128) The strategy of selecting an optimal subset of variables is to search for an element in $P_{\text{sub}.V}$ whose quality index is lower than or equal to all the other elements of $P_{\text{sub}.V}$.

(129) The sensor engine **150** may select the optimal set of variables and may select the sensors **155** corresponding to the signals **113** that are associated with the variables. The total number of steady states and transient states of a system is 1. The states can be denoted in a state set $S = \{S_{\text{sub}.1}, S_{\text{sub}.2}, \dots, S_{\text{sub}.k}, \dots, S_{\text{sub}.l}\}$ where $k \in [1, l]$. A state $S_{\text{sub}.k}$ can be a steady state or a

transient state.

(130) Given the ISFA model **137** of the system, the sensor engine **150** may use the ISFA model **137** to simulate each state of the system. As described above, each simulation for a state results in deviation index vectors and variation index vectors for each observable variable in the ISFA model **137**. The sensor engine **150** may select the optimal variables for the set of optimal variables based on the deviation index vectors and variation index vectors. Depending on the embodiment, the optimal variables may be selected using one or both of a brute force algorithm or a genetic algorithm. Other types of algorithms may be used.

(131) FIG. **8** is an illustration of an example method **800** for generating one or more PFDD strategies **147**. The method **800** may be implemented by the sensor optimizer **120**.

(132) At **805**, a model is generated. The model **137** may be an ISFA model **137** and may be generated by the model engine **130** from an existing system model **135** of a system **110**. Depending on the embodiment, the model engine **130** may generate an ISFA model **137** for each operating state of the system **110**.

(133) At **810**, the system is simulated using the model in each operating state. The system **110** may be simulated by the PFDD engine **140** using the ISFA model **137** for each state by injecting faults of a plurality of faults into the ISA model **137**. As part of simulating the system **110**, the PFDD engine **140** may determine one or more propagation features related to each of the faults.

(134) At **815**, PFDD strategies are generated for each operating state. The PFDD strategies **147** may be generated by the PFDD engine **140** from the propagation features related to each of the faults. In some embodiments, the propagation features may be one or more feature matrices **146**.

(135) FIG. **9** is an illustration of an example method for selecting one or more sensors **155** to monitor a system **110** for faults. The method **900** may be implemented by the sensor optimizer **120**.

(136) At **905**, a model is generated. The model **137** may be an ISFA model **137** and may be generated by the model engine **130** from an existing system model **135** of a system **110**. Depending on the embodiment, the model engine **130** may generate an ISFA model **137** for each operating state of the system **110**. The model **137** may include a plurality of variables and each variable may correspond to a signal **113** of the system **110**.

(137) At **910**, the system is simulated using the model in each operating state. The system **110** may be simulated by the PFDD engine **140** using the ISFA model **137** for each state by injecting faults of a plurality of faults into the ISA model **137**. As part of simulating the system **110**, the PFDD engine **140** may generate one or more feature matrices **146** related to each of the faults and operating state.

(138) At **915**, an optimal set of variables is selected. The optimal set of variables may be selected by the sensor engine **150** from the one or more feature matrices **146**. Depending on the embodiment, the sensor engine **150** may use a genetic algorithm to select the variables.

(139) At **920**, sensors are selected based on the optimal set of variables. The sensors **155** may be selected by the sensor engine **155**. Depending on the embodiment, the sensor engine **155** may select a sensor **155** for each variable in the set of optimal variables.

(140) At **925**, the system is monitored using the selected sensors. The system **110** may be monitored by placing each sensor **155** at a location in the system **110** where it can monitor the signal **133** associated with the variable corresponding to the sensor **155**.

(141) FIG. **10** shows an exemplary computing environment in which example embodiments and aspects may be implemented. The computing device environment is only one example of a suitable computing environment and is not intended to suggest any limitation as to the scope of use or functionality.

(142) Numerous other general purpose or special purpose computing devices environments or configurations may be used. Examples of well-known computing devices, environments, and/or configurations that may be suitable for use include, but are not limited to, personal computers, server computers, handheld or laptop devices, multiprocessor systems, microprocessor-based

systems, network personal computers (PCs), minicomputers, mainframe computers, embedded systems, distributed computing environments that include any of the above systems or devices, and the like.

(143) Computer-executable instructions, such as program modules, being executed by a computer may be used. Generally, program modules include routines, programs, objects, components, data structures, etc. that perform particular tasks or implement particular abstract data types. Distributed computing environments may be used where tasks are performed by remote processing devices that are linked through a communications network or other data transmission medium. In a distributed computing environment, program modules and other data may be located in both local and remote computer storage media including memory storage devices.

(144) With reference to FIG. 10, an exemplary system for implementing aspects described herein includes a computing device, such as computing device **1000**. In its most basic configuration, computing device **1000** typically includes at least one processing unit **1002** and memory **1004**. Depending on the exact configuration and type of computing device, memory **1004** may be volatile (such as random access memory (RAM)), non-volatile (such as read-only memory (ROM), flash memory, etc.), or some combination of the two. This most basic configuration is illustrated in FIG. 10 by dashed line **1006**.

(145) Computing device **1000** may have additional features/functionality. For example, computing device **1000** may include additional storage (removable and/or non-removable) including, but not limited to, magnetic or optical disks or tape. Such additional storage is illustrated in FIG. 10 by removable storage **1008** and non-removable storage **1010**.

(146) Computing device **1000** typically includes a variety of computer readable media. Computer readable media can be any available media that can be accessed by the device **1000** and includes both volatile and non-volatile media, removable and non-removable media.

(147) Computer storage media include volatile and non-volatile, and removable and non-removable media implemented in any method or technology for storage of information such as computer readable instructions, data structures, program modules or other data. Memory **1004**, removable storage **1008**, and non-removable storage **1010** are all examples of computer storage media. Computer storage media include, but are not limited to, RAM, ROM, electrically erasable program read-only memory (EEPROM), flash memory or other memory technology, CD-ROM, digital versatile disks (DVD) or other optical storage, magnetic cassettes, magnetic tape, magnetic disk storage or other magnetic storage devices, or any other medium which can be used to store the desired information and which can be accessed by computing device **1000**. Any such computer storage media may be part of computing device **1000**.

(148) Computing device **1000** may contain communication connection(s) **1012** that allow the device to communicate with other devices. Computing device **1000** may also have input device(s) **1014** such as a keyboard, mouse, pen, voice input device, touch input device, etc. Output device(s) **1016** such as a display, speakers, printer, etc. may also be included. All these devices are well known in the art and need not be discussed at length here.

(149) It should be understood that the various techniques described herein may be implemented in connection with hardware components or software components or, where appropriate, with a combination of both. Illustrative types of hardware components that can be used include Field-programmable Gate Arrays (FPGAs), Application-specific Integrated Circuits (ASICs), Application-specific Standard Products (ASSPs), System-on-a-chip systems (SOCs), Complex Programmable Logic Devices (CPLDs), etc. The methods and apparatus of the presently disclosed subject matter, or certain aspects or portions thereof, may take the form of program code (i.e., instructions) embodied in tangible media, such as floppy diskettes, CD-ROMs, hard drives, or any other machine-readable storage medium where, when the program code is loaded into and executed by a machine, such as a computer, the machine becomes an apparatus for practicing the presently disclosed subject matter.

(150) Although exemplary implementations may refer to utilizing aspects of the presently disclosed subject matter in the context of one or more stand-alone computer systems, the subject matter is not so limited, but rather may be implemented in connection with any computing environment, such as a network or distributed computing environment. Still further, aspects of the presently disclosed subject matter may be implemented in or across a plurality of processing chips or devices, and storage may similarly be effected across a plurality of devices. Such devices might include personal computers, network servers, and handheld devices, for example.

(151) Although the subject matter has been described in language specific to structural features and/or methodological acts, it is to be understood that the subject matter defined in the appended claims is not necessarily limited to the specific features or acts described above. Rather, the specific features and acts described above are disclosed as example forms of implementing the claims.

Claims

1. A method comprising: generating a model of a system by a computing device; simulating the system using the model in each operating state of a plurality of operating states by the computing device; and based on the simulations, generating a propagation-based fault detection and discrimination (“PFDD”) strategy for each operating state by the computing device to infer trends of signal changes in different operating states for a simulated fault condition at discrete time periods by deriving a deviation index indicative of a deviation of a variable in the fault condition at a time point and a deviation index vector that consists of deviation indexes of the variable at all time points in the simulated fault condition.
2. The method of claim 1, further comprising: determining a current operating state of the plurality of operating states of the system; and detecting and discriminating one or more faults in the system using the PFDD strategy generated for the current operating state.
3. The method of claim 1, wherein generating the model comprises generating a quantitative model and an algebraic model.
4. The method of claim 3, wherein the quantitative model is generated using differential equations.
5. The method of claim 3, wherein the algebraic model is generated from the quantitative model using discretization methods.
6. The method of claim 3, wherein simulating the system using the model in each operating state of a plurality of operating states comprises repeatedly simulating the system using the generated algebraic model for a plurality of iterations.
7. The method of claim 6, wherein a different fault is introduced into the simulation at each iteration of the plurality of iterations.
8. The method of claim 1, wherein the plurality of operating states comprises steady states and transient states, and generating the PFDD strategy for a transient state comprises: generating a plurality of fault feature matrices based on the simulation of the transient state for each of a plurality of faults; determining a plurality of unique subcases for each fault based on the fault feature matrices; defining one or more D-classes for each unique subcase of the plurality of unique subcases; generating a reduced fault feature matrix from the defined one or more D-Classes for each unique subcase of the plurality of unique subcases; generating one or more diagnosis strategies matrices based on the reduced fault feature matrix; and determining the PFDD strategy for the transient state based on the one or more diagnosis strategies matrices.
9. The method of claim 8, wherein generating the PFDD strategy for a steady state comprises: generating a plurality of fault feature matrices based on the simulation of the steady state for each of a plurality of faults; defining one or more D-classes for each pair of faults of the plurality of faults; generating one or more D-class feature matrices from the defined one or more D-classes; generating one or more diagnosis strategies matrices based on the one or more D-class feature matrices; and determining the PFDD strategy for the steady state based on the one or more

diagnosis strategies matrices.

10. The method of claim 1, wherein simulating the system using the model in an operating state of the plurality of operating states comprises: determining a plurality of faults associated with the system; and for each fault of the plurality of faults, injecting the fault into the model and simulating the system using the model with the injected fault for the operating state.

11. The method of claim 10, further comprising: determining one or more propagation features related to each fault of the plurality of faults based on the simulations; and generating the PFDD strategy for each operating state based on the determined one or more propagation features.

12. The method of claim 1, wherein generating a PFDD strategy for an operating state comprises: generating one or more fault feature matrices for the operating state; generating one or more D-class feature matrices based on the one or more fault feature matrices; generating one or more diagnosis strategy matrices based on the one or more D-class feature matrices; and generating the PFDD strategy for the operating state based on the one or more diagnosis strategy matrices.

13. A method comprising: generating a model of a system by a computing device, wherein the model includes a plurality of variables; simulating the system using the model in each operating state of a plurality of operating states by the computing device to infer trends of signal changes in different operating states for a simulated fault condition at discrete time periods by deriving a deviation index indicative of a deviation of a variable in the fault condition at a time point and a deviation index vector that consists of deviation indexes of the variable at all time points in the simulated fault condition; and based on the simulations, selecting an optimal subset of the plurality of variables.

14. The method of claim 13, wherein simulating the system using the model in an operating state of the plurality of operating states comprises: determining a plurality of faults associated with the system; and for each fault of the plurality of faults, injecting the fault into the model and simulating the system using the model with the injected fault for the operating state; and generating one or more fault feature matrices for the operating state.

15. The method of claim 14, further comprising selecting the optimal subset of the plurality of variables using the one or more fault feature matrices.

16. The method of claim 15, further comprising selecting the optimal subset of the plurality of variables using the one or more fault feature matrices using a genetic algorithm.

17. The method of claim 13, further comprising selecting one or more sensors based on the optimal subset of the plurality of variables.

18. The method of claim 17, further comprising monitoring one or more signals of the system using the selected one or more sensors.

19. A first system comprising: at least one computing device; and a computer readable medium storing computer executable instructions that when executed by the at least one computing device cause the at least one computing device to: generate a model of a second system; simulate the second system using the model in each operating state of a plurality of operating states; and based on the simulations, generate a propagation-based fault detection and discrimination ("PFDD") strategy for each operating state to infer trends of signal changes in different operating states for a simulated fault condition at discrete time periods by deriving a deviation index indicative of a deviation of a variable in the fault condition at a time point and a deviation index vector that consists of deviation indexes of the variable at all time points in the simulated fault condition.

20. The first system of claim 19, further comprising computer executable instructions that when executed by the at least one computing device cause the at least one computing device to: determine a current operating state of the plurality of operating states of the second system; and detect and discriminate one or more faults in the second system using the PFDD strategy generated for the current operating state.
