

Studio funzione

domenica 12 giugno 2022 21:48

1) $f(x) = \sqrt{1 + \ln x}$

$$1 + \ln x \geq 0 \rightarrow \ln x \geq -1 \rightarrow x \geq e^{-1} \rightarrow x \geq \frac{1}{e}$$

$$\ln x > 0 \rightarrow x > 0$$

$$\frac{1}{e} > 0$$

$$\rightarrow \left[\frac{1}{e}, +\infty \right)$$

2) $f(x) = x^3 - 3x$

$$I = (-1, +1)$$

$$f'(x) = 3x^2 - 3$$

$$3x^2 - 3 > 0 \rightarrow 3x^2 > 3 \rightarrow x^2 > 1 \rightarrow x > \pm 1$$

$$+++(-1)----(+1)++++$$

La funzione è decrescente

3) $f(x) = \begin{cases} \cos x^2 + a \rightarrow x \leq 0 \\ \frac{\ln(1+x)}{x + e^x} \rightarrow x > 0 \end{cases}$

$$\lim_{x \rightarrow 0^+} \frac{\ln 1}{0 + 1} = \frac{0}{1} = 0$$

$$\cos x + a = 0$$

$$\cos(0) = 1$$

$$1 + a = 0 \rightarrow a = -1$$

4) $f(x) = e^{-x^2}$

$$f'(x) = -2xe^{-x^2}$$

$$-2xe^{-x^2} > 0$$

$$-\frac{2x}{e^{x^2}} > 0$$

$$-2x > 0 \rightarrow x < 0$$

$$-e^{x^2} < 0 \rightarrow \text{mai}$$

$$++++++(0)-----$$

0 è massimo assoluto

5) $\lim_{n \rightarrow +\infty} (n^2 - n^3 + 3e^{-n} + \cos n^2) \sim \lim_{x \rightarrow +\infty} -n^3 + 3e^{-n} = -\infty + 0 = -\infty$

6) $\lim_{n \rightarrow +\infty} \frac{\ln(2 + n^3) - 5\sqrt{n^2 - n} + 2^{-n^4 + 5n}}{5n + 3 \ln n - n \ln n} \sim \frac{2^{-n^4}}{n \ln n} \rightarrow \text{converge}$
Ricorda: $-n^4 = -1 * (n^4)$

7) $\lim_{x \rightarrow +\infty} n^2 \sin \frac{1}{n + n^2} \sim n^2 * \frac{1}{n + n^2} = n^2 * \frac{1}{n(n+1)} = \frac{n}{n+1} = \frac{n}{n * \left(1 + \frac{1}{n}\right)} = \frac{1}{1 + \frac{1}{n}} = 1$

8) $\lim_{x \rightarrow +\infty} (\ln n - \sqrt{n} + 3e^{-n} + \sin n^2)$

$$\sim \ln n - \sqrt{n} + 0$$

$$\ln n - \frac{1}{n^2} \sim -n = -\infty$$

9) $\lim_{x \rightarrow +\infty} \frac{n^2 + e^{-n} + \ln n}{\ln(1 + n) + n^3 - 1} \sim \frac{n^2}{n^3} = \frac{1}{n} = 0$