

Using the SRSim Software for Spatial and Rule-Based Modeling of Combinatorially Complex Biochemical Reaction Systems

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Abstract. The simulator software SRSim is presented here. It is constructed from the molecular dynamics simulator LAMMPS and a set of extensions for modeling rule-based reaction systems. The aim of this software is coping with reaction networks that are combinatorially complex as well as spatially inhomogeneous. On the one hand, there is a combinatorial explosion of necessary species and reactions that occurs when complex biomolecules are allowed to interact, e.g. by polymerization or phosphorylation processes. On the other hand, diffusion over longer distances in the cell as well as the geometric structures of sophisticated macromolecules can further influence the dynamic behavior of a system. Addressing the mentioned demands, the SRSim simulation system features a stochastic, particle based, spatial simulation of Brownian Dynamics in three dimensions of a rule-based reaction system.

Rule-based Modeling in Space

Biological systems exhibit a high number of possible combinations between interacting proteins, frequently leading to huge molecules of interconnected protein compounds. Examples are the complexes assembled for RNA or DNA transcriptases, ATP synthases [26], mitotic checkpoint networks [18] or the death inducing signaling complex (DISC) [41]. Next to the resulting complex graphs of interacting proteins, there are post-translational modification to proteins, e.g. from phosphorylations. Basically, each modification pattern defines a new chemical species with its unique chemical behavior. Exemplary, this would result in a number of 2^{27} different species for the tumor suppressor protein p53 which comprises 27 phosphorylation sites [2]. Such a high number of species poses problems for the simulation with (partial) differential equations and stochastic algorithms. But it also becomes very hard to analyze and understand the “mechanics” of such a complex model. A possible remedy for stochastic simulations is discussed here [35].

Another possible solution to the problem of combinatorial explosion is proposed by the **domain-oriented approach** and rule-based modeling [27, 15, 16,

8,12]. In this scenario, **elementary molecules** consist of a set of **components** or domains which can be modified or bound to the components of other molecules. Components, sites, binding sites and domains are used synonymously in this article. The resulting complex species, formed from a connection of elementary molecules, are called **molecule graphs**.

Instead of using reactions between explicit species now, the reactions are replaced by implicit reaction rules, which are applicable to a certain subset of all possible complex molecular species. This subset is defined through an equivalence class given by a molecule graph pattern. Any complex molecule graph that contains the graph pattern as an isomorphic sub-pattern is included in the equivalence class. A pattern might for example be described as demonstrated in Figure 1.

There is a lot of software available for rule-based modeling, as for example Stochsim [27], BioNetGen [5], BIOCHAM [10], Molculizer [23] or Pathway Logic Assistant [39] or Cellucitate. Nonetheless spatial aspects are mostly neglected in these approaches (except for Stochsim).

Spatial Aspects

Spatiotemporal heterogeneities in reaction systems are generally considered to be of high importance for many systems [3, 25, 19, 38]. This led to a variety of spatial simulation techniques, starting from deterministic, population-based, partial differential equations [28] towards stochastic simulation of single particles in discrete or continuous 3d space [40, 9, 21]. See [22, 38] for an overview on spatial simulation systems.

Similar to and partially based on the approaches [4, 34, 43, 20, 11, 37], we are using individual agents for each elementary molecule in the simulation. Synonymously with the agents, we are using the terms particles and elementary molecules here. The spatial simulation is carried out as an extension to the molecular dynamics simulator LAMMPS [31]. Each particle is represented by its position, its velocity, its species and the state of its components. The particles diffuse through the reactor and can push away other molecules if they come too close. When two molecules approach one another, a bimolecular reaction can happen between them, if they are fitting to a reaction pattern specified in the reaction rules and if the geometric constraints are met. If a reaction binds two elementary molecules together, bond forces are applied and their diffusion through the reactor is coupled, forming a complex molecule graph. Monomolecular reactions can be used to spontaneously break bonds in molecule graphs or to modify the component states of a molecule. More conventional reactions can also be used to completely exchange one molecule for another.

The inclusion of spatial aspects in the rule-based reaction systems results in an expressive simulation system for moderately sized systems. Up to 100000 simulated particles can still be run on a desktop system for about 10^6 timesteps in some hours of computing time. Though SRSim was designed for the simulation of biological systems, also designing and planning chemical computing experiments might be a good application. We simulated for example the formation of

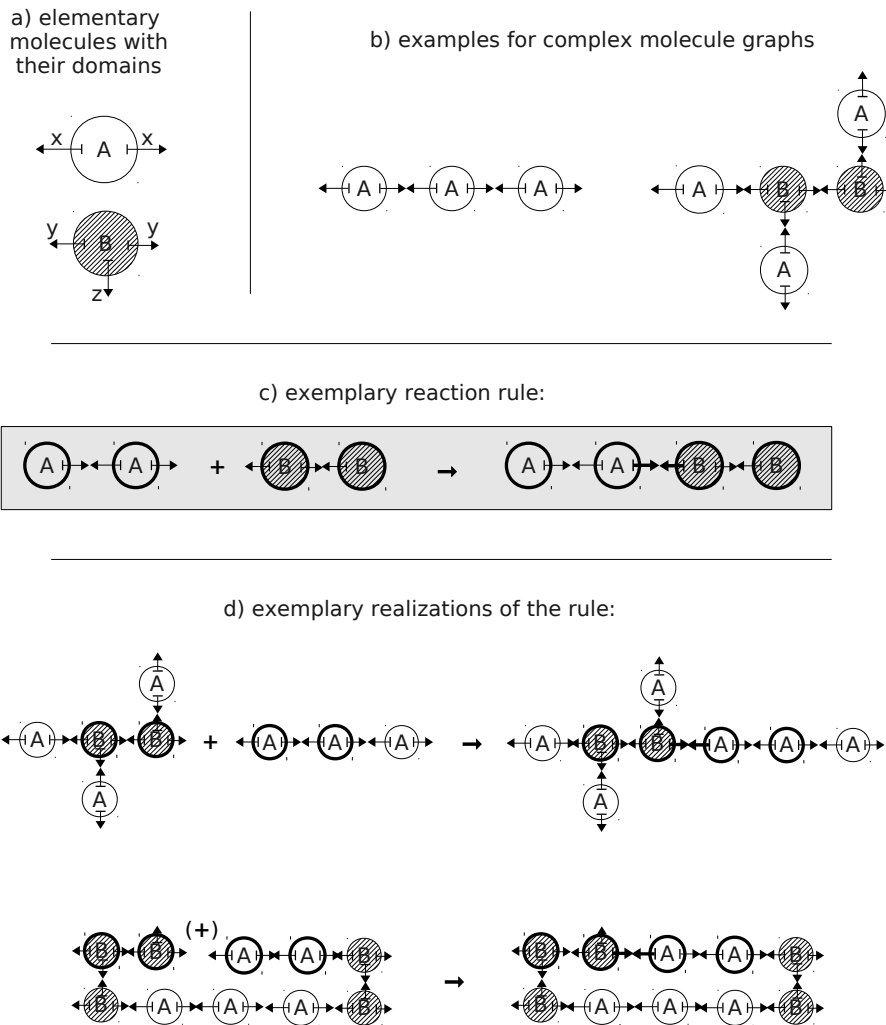


Fig. 1. Exemplary rule-based system, taken from [13]. Two elementary molecule types (A, B) with their sub domains (or **components**) are displayed (a). Each component can be bound to another component or be modified, e.g. denoting a phosphorylation or a conformational change. Site names need not be unique and hence a wide spectrum of possibilities for the system's specification is offered. Multiple elementary molecules can be connected at their components to form complex **molecule graphs** (b). Reaction rules, as the **binding reaction** (c), are specified by using patterns graphs (or **reactant patterns**) A reactant pattern fits to a molecule graph, if it is contained as a subgraph in the molecule graph. Note that some components are missing in the reactant pattern's definition, which are then ignored in the matching process. Panel (d) shows two different instances of the reaction rule. In the upper realization, two independent molecule graphs are connected. For the lower example on the other hand, both of the rules' reactant patterns are found in a single connected molecule graph.

Sierpinski triangles [13] following the work of Winfree et al. and Rothmund et al. [42, 33].

Though the SRSim simulation system cannot directly be used to simulate P-Systems [29, 30], there are some parallels to the membrane computing perspective. Similar to some P-System [24, 32] we are using a stochastic simulation approach that is based on individual particles in 3d space, though with limited support for the constitution of membranes. That is, if we want to setup an implicit diffusion barrier in our system “SRSim”, we can do this by adding forces to the reactor that confine certain molecules to defined subvolumes inside the reactor. Then, reactions can be used to transfer particles with specified rates through these pseudo-membranes. Nonetheless, that would be a rather awkward workaround to the „missing” membranes in the SRSim approach. On the other hand, similar to approaches like [11, 36], the dynamic creation, modification and destruction of membranes can be reduced to the underlying macromolecular interactions by simulating lipid molecules that build the membranes.

Another similarity might be that both approaches, the rule-based and the membrane-computing systems, use further constraints on the underlying non-deterministic reaction system. While in membrane computing, there are dynamic membranes to separate different molecules against interactions, there are the geometry and the complex molecule-graph structure in the SRSim approach that allows or even favours one kind of reactions and that inhibits other types. For the inner workings of biological cells, both types of processes might be equally important. Maybe there could even be seen a hierarchy of first controlling geometries of interacting particles on the level of macromolecules and then constraining these interactions through the relationship between the compartments. From the computational point of view, both types of systems offer a high combinatorial complexity, leading to computational capacities as shown for P-Systems [30, 36] and for self-assembly systems [1, 33, 7]. When intending to build computing systems from scratch, self-assembling macromolecules as well as structured membranes might both supply helpful building blocks.

Though that is not what we present in this paper, it might prove interesting to combine both types of constraints to a single system. This would also open the possibility to describe geometric relations not only between the particles, but also between the membranes. For the rule-based modelling community on the other hand, it would certainly be very handy to use the concept of dynamic membrane formation and decay. In the case of non-spatial simulation and static membranes, this was already done [14].

In the following sections, we try not to unfold the complete technical simulation process. Instead, the process of setting up and running a simple system will be demonstrated from installing the software to setting up and running the simulation. For the theory behind the spatial and rule-based simulation, please refer to [13].

Installing SRSim

Unfortunately the installation of SRSim is not yet fully automatized, so there are some uncomplicated steps to do. The following installation instructions are addressed to x86 linux users, who are assumed to have Gnu Make and a C++ compiler installed. No tests were carried out using different hard- or software platforms, but as long as the required libraries are present, no architecture specific code is used.

Required Software

In the first place, make sure that the following libraries are present on your system, namely **Xerces-C++**¹, which is required for XML parsing. The other dependency is the “Message Passing Interface”² (**MPI**), a parallel computing standard used by LAMMPS. There are different MPI implementations available.

It is recommended but not necessary to install the software “Visual Molecular Dynamics”³ (**VMD**) [17], which can be very helpful to visualize molecular trajectories calculated by SRSim.

Compiling SRSim

To build a SRSim executable, first the Rule System is compiled to a library that is later linked against the LAMMPS molecular dynamics simulator sources. After unpacking the SRSim distribution to a directory **X**, this should basically be done by invoking `make lmp_srsim` in the directory **X/source** of the SRSim distribution. This will create the library, build the tool `createGeo` and then compile LAMMPS with the additional modules necessary for SRSim.

If the MPI and Xerces libraries are not in the standard paths for include and library files, you have to modify the `-I` and `-L` paths in the makefiles **X/source/lammpsCompilation/Makefile** and **X/source/RuleSys/Makefile**.

After the successful compilation, two new executables, **X/source/lammpsCompilation/lmp_srsim** and **X/source/RuleSys/createGeo** can be found. You have to copy or link these files to a place in your system that is in your search path, as for example `/usr/local/bin` or `~/bin`. If you do not have a special directory for executables, you can just add the LAMMPS compilation directory directly to your search path by editing `~/.bashrc` and adding a line `export PATH=$PATH:X/source/lammpsCompilation:X/source/RuleSys`.

If the command `lmp_srsim` outputs the following line, you are done installing SRSim.

¹ download from <http://xerces.apache.org/xerces-c/> or use the system’s packet manager. Versions 2.7 and 2.8 seem to work fine.

² download for example MPICH from <http://www.mcs.anl.gov/research/projects/mpich2/> or use your system’s packet manager.

³ download from <http://www.ks.uiuc.edu/Research/vmd/>

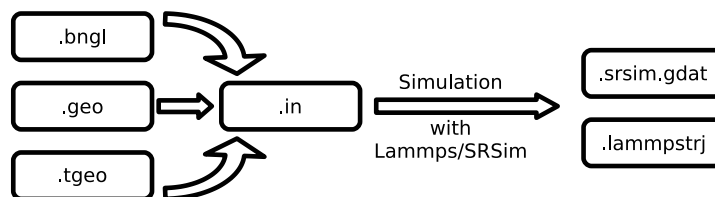


Fig. 2. Overview of the input / output file structure of SRSim.

LAMMPS (7 Jul 2009)

Here, the 7th July 2009 is the LAMMPS version, that SRSim was built upon.

Using the Software

The molecular dynamics simulator LAMMPS is a script-driven command line program. Since SRSim is no autonomous tool, but an extension to LAMMPS, it is started in the same way as the Molecular Dynamics simulator: `lmp_srsim < input_script.in`. The LAMMPS input script `*.in` is then referencing three other input files and two or more output files as illustrated in Figure 2. The referenced input files are the `*.bngl` file, specifying the used rule-based reaction system, the `*.geo` file for the molecular geometry definition and finally the `*.tgeo` file for the template geometry definition. The output files will usually be a `*.srsim.gdat` file containing the concentrations of the observed species and a `*.lammptstrj` file with all the molecular coordinates, which can be used to visualize and to analyze the simulation run in detail.

To observe the results, gnuplot and VMD can be used. Type `vmd output.lammptstrj` for instance, to see a graphic representation of the reaction volume. Though VMD (See Section 1) was rather designed to display all-atom systems, it can be customized neatly and various helper scripts can be found on the Internet.

An Exemplary System

Let us assume we try to build a simple simulation with two elementary molecules. Species A will be a polymerizing molecule that requires energy provided by a molecule B to further polymerize. To allow a linear polymerization for molecules of type A, two opposing components `a` and `c` are introduced. A third component `b` will be used as the binding site for the type B molecules. The type B particles will only be able to bind to type A molecules, so only one binding site `b` is necessary. Nonetheless, to demonstrate the concept of modifications, we will also add another component `e` to the type B particles. Component `e` will be existing in two different energetic levels `~triP` and `~diP`. See figures 3 and 4 for an idea of what the system's behavior should be like, when simulated.

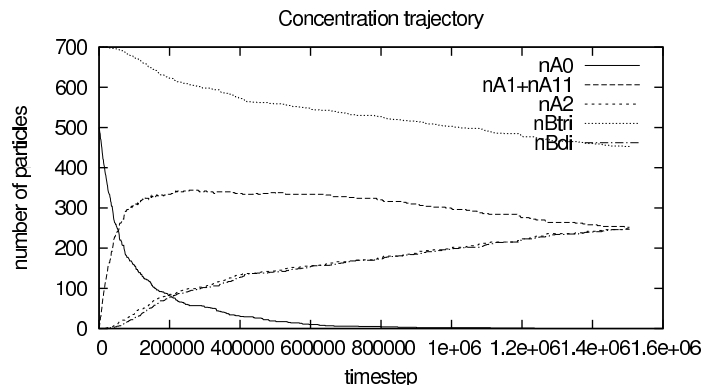


Fig. 3. Particle Quantity Trajectory. The displayed quantities will be defined and explained in the next Section about the rule system. The curve $nA1 + nA11$ denotes the number of particles “A” that have only either their site “a” or “c” bound. It can be observed, that this value increases rapidly in the beginning and falls down slowly then. This decrease is due to the larger complexes that are slowly forming in the later phase of the simulation.

Definition of the Rule System

The rule-based reaction system is specified in the BioNetGen Language [16] (BNGL⁴). Basically it is not necessary to change a BNGL file to use it with SR-Sim. However, the commands `generate_network`, `simulate_ode`, `simulate_ssa` and `setConcentration` will be ignored. These commands’ semantics can be replaced by using the LAMMPS input script instead, as we will explain later.

To define the reaction system, we first add the “parameters” and “species” blocks which allow the definitions of rate constants and the molecule types to appear in the simulation. Note that a molecular species is defined by its name followed by its components in brackets, optionally followed by a modification state. The constants A0 and B0 denote the initial quantity of particles of this type.

example1.bngl - part 1 of 3

```
begin parameters
  k1      1.5e-2
  k2      1.5e-2
  k3      5e-5

  A0      500
  B0      700
end parameters
```

⁴ See the BioNetGen Documentation. A BioNetGen tutorial can be found online at <http://bionetgen.org/index.php/BioNetGen-Tutorial>.

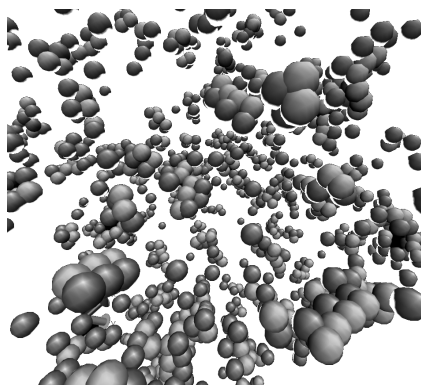


Fig. 4. A scene rendered from the reactor with VMD after 500000 timesteps. short multimerizations of two to four A-B dimers can be observed.

```
begin species
  A(a,b,c)          A0
  B(b,e~triP)       B0
end species
```

The next block defines which reactions are possible. A first rule is used to bind molecule A with a free b site to a molecule B with a free b site. The connections of two molecules via their components is expressed through the exclamation mark, followed by a common identifier, !1. Since we did not mention any of the sites a or c of molecule A, they can be in any state, free or bound to any other complex molecule. To allow the polymerization of the A molecules, we need to define the second reaction rule. It should state, that a molecule A with a free binding site a can bind to another molecule A' with a free binding site a'. But only when one of them has bound an energy supplying molecule B. The third rule states, that a high-energy molecule B drops down into a lower energy state ~diP, when the molecule A it belongs to has no free connection sites any more. Note that the binding symbol a!+ marks a site that is bound to any other molecule that is not explicitly named.

example1.bngl - part 2 of 3

```
begin reaction rules
  1 A(b) + B(b)          ->  A(b!1).B(b!1)          k1

  2 A(c) + A(a,b!1).B(b!1,e~triP)  ->  A(c!2).A(a!2,b!1).B(b!1,e~triP)  k2

  3 A(a!+,c!+,b!1).B(b!1,e~triP)  ->  A(a!+,c!+,b!1).B(b!1,e~diP)      k3
end reaction rules
```

For the analysis of the reaction system, a fourth, optional block can be defined, listing patterns whose quantities should be output in the simulation. This

might be for example the numbers of A molecules with no, one or two attached neighbors, or the numbers of B molecules in the high- or low energy state.

example1.bngl - part 3 of 3

```
begin observables
  Molecules    nA0    A(a,c)
  Molecules    nA1    A(a,c!+)
  Molecules    nA11   A(a!+,c)
  Molecules    nA2    A(a!+,c!+)
  Molecules    nBtri  B(e~triP)
  Molecules    nBdi   B(e~diP)
end observables
```

Molecule and Template Geometry Files

Now that the reaction system is defined, we have to specify the geometry for the elementary molecules A and B that we want to use in the ***.geo** geometry file. For each species, the mass and radius as well as the attributes for each component have to be defined. The orientations of the particles' binding sites are expressed as spherical coordinates through the angles phi, theta and a distance from the particles center. Phi can be imagined as the geographic longitude, while theta is similar to the geographic latitude. In contrast to geographic coordinates, **theta=0** specifies one pole, **90°** is the equatorial plane and **180°** is the other pole. For each elementary molecule type, a **molecule** section has to be defined. Within this, each site that is mentioned in the reaction system has to be represented by a **site** tag inside the molecule definition.

A general section in the beginning of the geometry file lists general property values for the simulation and values that should be used by default for all the particles. To specify certain values more individually, property tags can be included in the molecule and site blocks as well. See Table 1 for a list of property names and where they can be used.

A final section **DihedralAngles** can be used in the geometry definition to specify dihedral angles for certain bonds.

example1.geo - part 1 of 3

```
<?xml version="1.0"?>
<molecule-geometry-definition>
  <version value="1.01"/>

  <GeneralProperties>
    <property name="GPT_Devi_Dist" value="0.2"/>
    <property name="GPT_Devi_Angle" value="40"/>
    <property name="GPT_Mol_Mass" value="50"/>
    <property name="GPT_Mol_Rad" value="1"/>
    <property name="GPT_Site_Dist" value="1"/>

    <property name="GPT_Force_Repulsion" value="1.5"/>
```

Property Name	glob	mol	site	function
GPT_Site_Theta	p	p	rp	spheric site coordinates
GPT_Site_Phi	p	p	rp	“
GPT_Site_Dist	p	p	rp	“
GPT_Site_Dihedral	p	-	-	not yet used
GPT_Mol_Mass	p	rp	-	molecular mass
GPT_Mol_Rad	p	rp	-	molecular radius
GPT_Devi_Dist	p	p	rp	max distance deviation for bond formation
GPT_Devi_Angle	p	p	rp	max angular deviation for bond formation
GPT_Diffusion	p	p	-	not yet used
GPT_Refractory	p	p	-	not yet used
GPT_Force_Repulsion	rp	-	-	factor for repulsive forces
GPT_Force_Bond	rp	-	-	factor for bond forces
GPT_Force_Angle	rp	-	-	factor for angular forces
GPT_Force_Dihedral	rp	-	-	factor for dihedral angles
GPT_Temperature	rp	-	-	not yet used
GPT_Option_Dihedrals	rp	-	-	use dihedrals 0/1
GPT_Option_Impropers	rp	-	-	not yet used
GPT_Option_Rigid	rp	-	-	use rigid bodies 0/1

Table 1. Overview of the options that can be specified in the geometry file. The columns “glob” to “site” indicate, whether an option is (r)equired or (p)ossible on the (glob)al, the per-(mol)ecule, or the per-(site) level, respectively. Values that are defined in a more specialized context, e.g. for a special site overwrite the values that were specified in the more global context.

```

        <property name="GPT_Force_Bond"           value="1.5"/>
        <property name="GPT_Force_Angle"         value="1.5"/>
        <property name="GPT_Force_Dihedral"      value="1.5"/>
        <property name="GPT_Temperature"         value="300"/>

        <property name="GPT_Option_Dihedrals"    value="1"/>
        <property name="GPT_Option_Improper"     value="0"/>
        <property name="GPT_Option_Rigid"        value="0"/>
    </GeneralProperties>

    <molecule name="A">
        <site name="a"  phi="0"  theta="0"  dist="1" />
        <site name="c"  phi="0"  theta="180" dist="1" />
        <site name="b"  phi="0"  theta="90"  dist="1">
            <property name="GPT_Devi_Angle" value="30"/>
        </site>
    </molecule>

    <molecule name="B">
        <property name="GPT_Mol_Mass" value="30"/>
        <site name="b"  phi="0"  theta="0"  dist="1" />
        <site name="e"  phi="0"  theta="180" dist="1" />
    </molecule>

    <DihedralAngles>
        <dihedral around="A(b,a!1).A(c!1,b)" angle="10" />
    </DihedralAngles>

</molecule-geometry-definition>

```

When complex molecule graphs are initially added to the simulation, the relative positions of the constituting elementary molecules have to be known. So they are specified manually or calculated in advance by an independent simulation step using the tool `createGeo` and stored in the template geometry `*.tgeo` files. In our case, this file looks very simple, since we are not adding complex molecules. More complex template definitions can be found in the other examples distributed with SRSim.

example1.tgeo

```

<?xml version="1.0"?>
<template-geometry-definition>

    <template id="0" name="A(a,b,c)">
<mol id="0" x= "0" y="0" z= "0" />
    </template>

    <template id="1" name="B(b,e~triP)">
<mol id="0" x= "0" y="0" z= "0" />

```

</template>

</template-geometry-definition>

The LAMMPS Input Script

The LAMMPS input script is parsed line by line, each of which holds one command modifying the simulation system. Comments can be added using the # sign. Note that the order of the commands is important since the input script is parsed from top to bottom. There is a large number of possible commands that can be used to customize the simulation, so please refer to the LAMMPS documentation⁵ for further details on the original LAMMPS commands. These commands can for example be used to define custom force terms or to create simulation outputs in different formats.

example1.in

```
##
# Phase 1 - setup reactor
##

dimension      3
boundary        f f f      # use fixed boundary conditions
units           real        # timescale: fs,  distances: Angstrom
newton          on

atom_style       srsim example1.bngl example1.geo example1.tgeo 11111
#####          cmd         .bngl          .geo          .tgeo      random_seed

lattice         none
region Nucleus block -40 40 -40 40 -40 40 units box
#####          dimensions of the reaction volume

create_box      100         Nucleus
#              n_atom_types Region_name

start_state_srsim coeffs
start_state_srsim atoms
# set initial values e.g. bond forces etc.
# and add molecules to the simulation

neighbor        5.0 bin
#              size of neighbor-grouping bins

##
# Phase 2 - setup forces
```

⁵ The LAMMPS documentation comes together with LAMMPS' sources and can be accessed online at <http://lammps.sandia.gov/doc/Manual.html>.

```

##

fix 1 all langevin 300 300 160.0 12345
# parameters: Temp Temp Gamma^-1 random_seed

fix 2 all nve
fix 3 all wall/reflect xlo xhi ylo yhi zlo zhi

fix 4 all srsim 1 45678 1.0 1.0 1.0 1.0 1.0 50
# fix srsim syntax: fix id group srsim | nEvery randomSeed
# preFactBindR preFactBreakR preFactExchangeR
# preFactModifyR_1 preFactModifyR_2 refractoryTime

##
# Phase 3 - run
##

# Dumps:
thermo 5000 # write thermodynamics information every 5k timesteps
timestep 1 # one timestep = 1 fs

dump 1 all atom 1000 example1.lammpstrj
##### trajectory output
dump_modify 1 scale yes
dump 2 all srsim 1000 example1.srsim.gdat
##### concentrations output

# first run phase for 500k ts
run 500000

# second run phase with higher time-resolution
dump_modify 1 every 10
run 5000

```

In the first phase, some basic parameters have to be set, as for example the units to be used, the size of the reaction volume, the maximum number of molecular species and the initial configuration of the simulation system. Note that the command `atom_style` uses a special atom style, specially designed for SRSim, which is followed by the names of the other input files and the random seed.

In the second phase, different “fixes” are selected to be applied to the simulation. These are computations which influence each molecule’s data, for example their positions, velocities or binding states. The most basic fix, called `nve`, is the calculation applied to move each particle according to Newton’s equations of motion in dependency of the applied forces. The fix `langevin` adds implicit solvent effects, resulting in Brownian movement of the particles. The second last parameter to the fix `langevin` is called damping factor (γ^{-1}). It depends directly on the diffusion coefficient D and the temperature T by $\gamma^{-1} = \frac{D}{k_B T}$,

where k_B is the Boltzmann constant. Since fixed boundary conditions were chosen before, molecules moving out of the reaction volume would be lost, so the fix `wall/reflect` is applied. The last fix, `srsim` is the part of SRSim that checks for molecular collisions, analyzes which rules are applicable and finally executes them.

In the last phase, the types of output and the length of the simulation runs will be defined. The dump type `srsim` creates a plain text file in the same format as BioNetGen, to allow an easy comparison of the computed trajectories. Note that the intervals between two successive output data writes can be changed using the command `dump_modify`. If new molecules are to be added to the running simulation, the command `runmodif_srsim addMols` can be used, given the specified molecule-graph type was already listed in the reaction system definition.

The Tool “createGeo”

To simplify the creation of `.geo` and `.tgeo` files, the tool `createGeo` was added to the SRSim programs. It is used in the following syntax:

```
createGeo input.bngl input.geo input.tgeo
```

If either the `.geo` or the `.tgeo` file is not existing, it will be created. Molecule geometries are created with initial values of 1.0 for all distances and predefined angles for up to 6 sites. Template geometries are calculated by running short MD simulations to relax all bond distances and angles.

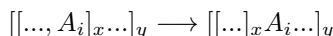
Concluding Remarks

In this manual, we have shown for a very simple system how to setup the SRSim simulation system. Not every possibility for configuration was mentioned, though. This is mostly due to the vast amount of options offered by the LAMMPS scripting language. Most of the molecular dynamics simulator’s capabilities can still be used with SRSim, offering a great potential to describe a system’s peculiarities. Another reason is, that SRSim is still under development and some features are still changing or are not yet fully tested. There are other examples in the SRSim package which might convey more ideas on what is possible with the simulation system.

Features that are missing at the moment are reactions that can change the states of three or more components instantaneously. So at this stage of the development, it is not possible to have a binding reaction, that also changes the modification state of a component at the same time. Nonetheless a wide range of reaction systems can be expressed under these constraints and more features will be included in future releases of the software. Another aspect that is not covered by this paper on the SRSim software, is the analysis of the results. Though special systems will probably require customized methods for the analysis, a first idea of what happens in the reactor can mostly be obtained through molecular dynamics visualization tools. VMD [17] for example comes with an import filter

for LAMMPS trajectories. It is also possible to extend VMD with python and tcl scripts for more specialized purposes.

SRSim can be interpreted as a P-System without explicit membranes. Reactions are constrained by spatial configurations and geometries instead of explicit membranes. So far, membranes can only be defined as static force fields or can emerge (e.g. like lipid layers formations [36]), which is computationally extremely demanding. Thus, we suggest to use explicit membranes like it is done in P-Systems, enriched by geometric information. In this approach, geometric properties like a form (e.g. sphere), a location, a size and a velocity are added to a membrane, so that it can have an effect on and can be affected by spatial heterogeneities. For example, a reaction to make a molecule of species A leave a membrane x



might require an appropriate particle A_i to be situated close to the membrane, before it can exit. Other constraints follow easily, e.g. mean transition times from one membrane into another compartment that is situated some distance away. Similar ideas were implemented in demonstrating software by Damien Pous⁶ following the concepts of “mobile ambients” [6].

SRSim as well as LAMMPS are released under the GPL, so the sources can freely be downloaded⁷ and modified. Especially the Rule System that handles the rule-based reaction system is independent from the molecular dynamics simulator and could be plugged into a different spatial or non-spatial realization of a rule-based simulation system.

Acknowledgements

The research was supported by the NEUNEU project (248992) sponsored by the European Community within FP7-ICT-2009-4 ICT-4-8.3 - FET Proactive 3: Bio-chemistry-based Information Technology (CHEM-IT) program.

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⁷ www.biosystemsanalysis.de

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