#### **SVD Plots**

#### **Importing Libraries**

```
In [46]: from keras import backend as K
         from keras import regularizers
         import numpy as np
         from gensim download import pickle rw
         from keras.layers import Dense
         from keras.models import Sequential
         import matplotlib.pyplot as plt
         import plotly.plotly as py
         import pandas as pd
         from sklearn.decomposition import PCA
         from sklearn.preprocessing import StandardScaler
         from sklearn.preprocessing import MinMaxScaler
         import numpy.linalg
         from numpy.linalg import det
         from numpy.linalg import inv
         import sympy as sympy
         from sympy import Matrix
         from plotly import version
         from plotly.offline import download plotlyjs, init notebook mode, plot, iplot
```

#### **Defining Functions**

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In [15]: **def** make dict(vocab, vectors): """Make dictionary of vocab and vectors""" return {vocab[i]: vectors[i] for i in range(len(vocab))} def vocab train test(embedding, lg1, lg2, lg1 vocab): """Create training and test vocabularies""" if embedding == 'zeroshot': with open('../data/zeroshot/transmat/data/' + 'OPUS en it europarl train 5K.txt') as f: vocab train = [( .split(' ')[0], .split(' ')[1]) for in f.read().split('\n')[:-1]] with open('../data/zeroshot/transmat/data/' + 'OPUS en it europarl test.txt') as f: vocab\_test = [(\_.split(' ')[0], \_.split(' ')[1]) for in f.read().split('\n')[:-1]] elif embedding in ['fasttext random', 'fasttext top']: embedding, split = embedding.split(' ') lg1\_lg2, lg2\_lg1 = pickle\_rw((lg1 + '\_' + lg2, 0), (lg2 + ' ' + lg1, 0), write=**False**) # T = Translation, R = Reverse (translated and then translated back) # Create vocab from 2D translations vocab 2D = []for lq1 word in lq1 vocab: # Translate 1q1 word if lq1 word in lq1 lq2: lg1 word T = lg1 lg2[lg1 word]# Check if translated word (or lowercase) is in 1g2 1g1 if lg1 word T in lg2 lg1.keys(): lg1 word R = lg2 lg1[lg1 word T]elif lg1 word T.lower() in lg2 lg1.keys(): lg1 word T = lg1 word T.lower() lg1 word R = lg2 lg1[lg1 word T]else: lq1 word R = None # Check if lq1 word and lq1 word R are equal (lowercase) if lq1 word R: if lq1 word.lower() == lq1 word R.lower(): vocab 2D.append((lq1 word, lq1 word T))

```
print('length of '+ lq1+'-'+ lq2+ ' vocab: '+str(len(vocab 2D)))
        #Create Train/Test vocab
        if split == 'random':
            sample = np.random.choice(len(vocab_2D), 6500, replace=False)
            vocab_train = np.asarray(vocab_2D)[sample[:5000]].tolist()
            vocab_test = np.asarray(vocab_2D)[sample[5000:]].tolist()
        elif split == 'top':
            sample = np.random.choice(range(6500), 6500, replace=False)
            vocab_train = np.asarray(vocab_2D)[:5000, :].tolist()
            vocab_test = np.asarray(vocab_2D)[:1500, :].tolist()
        else:
            pass
        # if split == 'random':
              sample = np.random.choice(len(vocab 2D), 900, replace=False)
              vocab train = np.asarray(vocab 2D)[sample[:700]].tolist()
              vocab test = np.asarray(vocab 2D)[sample[700:]].tolist()
        # elif split == 'top':
              sample = np.random.choice(range(900), 900, replace=False)
              vocab train = np.asarray(vocab 2D)[:700, :].tolist()
              vocab test = np.asarray(vocab 2D)[:200, :].tolist()
        # else:
              pass
   return vocab_train, vocab_test
def vectors train test(vocab train, vocab test):
    """Create training and test vectors"""
   X train, y train = zip(*[(lg1_dict[lg1_word], lg2_dict[lg2_word])
                             for lg1_word, lg2_word in vocab_train])
   X test, y test = zip(*[(lg1_dict[lg1_word], lg2_dict[lg2_word])
                           for lg1_word, lg2_word in vocab test])
   return map(np.asarray, (X train, X test, y train, y test))
def translation matrix(X train, y train):
    """Fit translation matrix T"""
   model = Sequential()
   model.add(Dense(300, use bias=False, input shape=(X train.shape[1],),kernel regularizer=regularizers
   model.compile(loss='mse', optimizer='adam')
```

```
history = model.fit(X_train, y_train, batch_size=128, epochs=20,
                        verbose=False)
    T = model.get_weights()[0]
    T = np.matrix(T)
   M = np.multiply(np.matrix(T), 100)
   T_norm, T_normed = normalize(M)
    D = np.linalg.det(M)
    I = inv(T)
    #Fr norm = np.linalq.det(np.subtract(np.matmul(M,M.getH()),np.matmul(M.getH(),M)))
    Fr_norm = np.linalg.det(np.matrix(np.subtract(np.matmul(T,T.getH()),np.matmul(T.getH(),T))))
    #print(T normed)
    #print(T normed.getH())
    #print(np.around(np.matmul(T normed,T normed.getH())))
    #print(np.around(np.matmul(T normed.getH(),T normed)))
    print ("Determinant:"+str(D))
    #print ("Fr norm:"+str(Fr norm))
    if np.array_equal(np.around(np.matmul(T_normed,T_normed.getH())), np.around(np.matmul(T_normed.getH()))
        tf = "True"
    else:
        tf = "False"
    return model, history, T, D, tf, I, M
def translation accuracy(X test, y test):
    """Get predicted matrix 'yhat' using 'T' and find translation accuracy"""
    # yhat
   yhat = X.dot(T)
   count = 0
    for i in range(len(y test)):
        if yhat[i,:].all() == y test[i,:].all():
```

```
count = count + 1
    accuracy = count/len(y_test)*100
   return accuracy
def svd(T):
   """Perform SVD on the translation matrix 'T' """
   U, s, Vh = numpy.linalg.svd(T, full matrices=False)
   return U, s, Vh
def T svd EDA(s):
   """Perform SVD on the translation matrix 'T' """
   plt.hist(s, bins='auto', range = (0,1), normed = 1)
   plt.show()
def normalize(matrix):
    """Normalize the rows of a matrix"""
   matrix_norm = np.linalg.norm(matrix, axis=1)
   matrix_normed = matrix / np.repeat(matrix_norm, matrix.shape[1]). \
        reshape(matrix.shape)
   return matrix norm, matrix normed
def translation_results(X, y, vocab, M, lg2_vectors, lg2_vocab):
   """X, y, vocab - The training or test data that you want results for
   T - The translation matrix
   lg2_vectors, lg2_vocab - Foreign language used to find the nearest neighbor
    # Data Prep on Inputs
   X_word, y_word = zip(*vocab)
   X_norm, X_normed = normalize(X)
   y_norm, y_normed = normalize(y)
   lg2_vectors_norm, lg2_vectors_normed = normalize(lg2_vectors)
    # yhat
   yhat = X.dot(M)
   yhat norm, yhat normed = normalize(yhat)
    \#X norm = normalize(X)
```

```
# Nearest Neighbors
      neg cosine = -yhat normed.dot(lg2 vectors normed.T)
#
      ranked neighbor indices = np.argsort(neg cosine, axis=1)
#
      # Nearest Neighbor
#
      nearest neighbor indices = ranked neighbor indices[:, 0]
#
      yhat neighbor = lg2 vectors[nearest neighbor indices, :]
#
      yhat neighbor norm, yhat neighbor normed = normalize(yhat neighbor)
#
      yhat neighbor word = np.asarray(lg2 vocab)[nearest neighbor indices]
#
      # Results DF
#
      cols = ['X norm', 'y norm', 'yhat norm', 'yhat neighbor norm',
              'X word', 'y word', 'yhat neighbor word']
#
#
     results df = pd.DataFrame({'X norm': X norm,
#
                                  'y norm': y norm,
#
                                  'yhat norm': yhat norm,
#
                                  'yhat neighbor norm': yhat neighbor norm,
#
                                  'X word': X word,
#
                                  'y word': y word,
#
                                  'yhat neighbor word': yhat neighbor word,})
#
      results df = results df[cols]
#
      results df['neighbor correct'] = results df.y word == \
#
          results df.yhat neighbor word
    return yhat_norm
def T norm EDA(results df):
    """Plot result norms side-by-side"""
    test_size = results_df.shape[0]
    test_accuracy = round(results_df.neighbor_correct.mean(), 2)
    print('Test Accuracy: '+str(test_accuracy)+'\n')
    plot_data = ['X norm', 'y norm', 'yhat_norm', 'yhat_neighbor_norm']
    # f, ax = plt.subplots(len(plot data), sharex=True, sharey=True,
                           figsize=(10, 10))
    # for i, d in enumerate(plot data):
          ax[i].hist(results df[d], bins=100)
          ax[i].axis('off')
          title = '{}: mean={}, std={}'.format(d, round(results df[d].mean(), 2), round(results df[d].st
          ax[i].set title(title)
```

```
# f.subplots adjust(hspace=0.7)
   # plt.savefig('../images/' + lq1 + ' ' + lq2 + ' ' + embedding +
                  ' T norm.png')
    # plt.close('all')
   return
def T pca EDA(T):
    """PCA on matrix T"""
   T_ss = StandardScaler().fit_transform(T)
   pca = PCA().fit(T_ss)
   n = pca.n components_
    # plt.figure(figsize=(10, 6))
   # plt.xlim((0, n))
   # plt.ylim((0, 1))
   # plt.plot(range(n + 1), [0] + np.cumsum(pca.explained variance ratio ).
               tolist())
    # plt.plot(range(n + 1), np.asarray(range(n + 1)) / n)
    # plt.xlabel('Number of Eigenvectors')
   # plt.ylabel('Explained Variance')
   # plt.savefig('../images/' + lg1 + '_' + lg2 + '_' + embedding +
                  ' T isotropy.png')
    # plt.close('all')
    isotropy = (1 - sum(np.cumsum(pca.explained_variance_ratio_) * 1 / n)) / .5
   return isotropy
def T report results (embedding, 1g1, 1g2, 1g1 vectors, 1g2 vectors,
                     X train, X test, D, results df, isotropy):
   md = '## ' + lg1.title() + ' to ' + lg2.title() + ' ' + \
        embedding.title() + ' \n'
   md += '- ' + lg1.title() + ' Vocabulary Size = ' + \
        '{:,.0f}'.format(lg1_vectors.shape[0]) + ' \n'
   md += '- ' + lg1.title() + ' Embedding Length = ' + \
        '{:,.0f}'.format(lg1 vectors.shape[1]) + ' \n'
   md += '- ' + lg2.title() + ' Vocabulary Size = ' + \
        '{:,.0f}'.format(lg2 vectors.shape[0]) + '\n'
   md += '- ' + lg2.title() + ' Embedding Length = ' + \
        '{:,.0f}'.format(lg2 vectors.shape[1]) + ' \n'
   md += '- Train Size = ' + '{:,.0f}'.format(X train.shape[0]) + ' \n'
   md += '- Test Size = ' + '{:,.0f}'.format(X test.shape[0]) + ' \n'
```

```
md += '- Determinant = ' + '{:,.0f}'.format(D) + ' \n'
md += '- <b>Test Accuracy = ' + \
    '{:,.1%}'.format(results_df.neighbor_correct.mean()) + '</b> \n\n'
md += '#### Test L2 Norms \n'
md += '- X_norm: L2 norms for ' + lg1.title() + ' test vectors \n'
md += '- y_norm: L2 norms for ' + lg2.title() + ' test vectors \n'
md += '- yhat_norm: L2 norms for X.dot(T) test vectors ' + \
    '(T = translation matrix) \n'
md += '- yhat neighbor norm: L2 norms for nearest neighbor' + \
    'to X.dot(T) in y test vectors \n'
md += '![](../images/' + lg1 + '_' + lg2 + '_' + embedding + \
    '_T_norm.png) \n\n'
md += '#### Translation Matrix Isotropy \n'
md += '- Isotropy = ' + '{:,.1%}'.format(isotropy) + ' \n'
md += '![](../images/' + lg1 + '_' + lg2 + '_' + embedding + \
    ' T isotropy.png) \n\n'
return md
```

#### Main Function (with SVD stats)

In [36]: **if** name == ' main ': # Manually set list of translations (embedding, 1q1, 1q2) translations = [#('fasttext random', 'en', 'ru'), ('fasttext top', 'en', 'en'), ('fasttext top', 'en', 'ru'), #('fasttext random', 'en', 'de'), ('fasttext top', 'en', 'de'), #('fasttext random', 'en', 'es'), ('fasttext top', 'en', 'es'), #('fasttext random', 'en', 'zh-CN'), ('fasttext top', 'en', 'zh-CN'), #('fasttext random', 'ru', 'en'), ('fasttext top', 'ru', 'en'), #('fasttext random', 'ru', 'es'), ('fasttext top', 'ru', 'ru'), ('fasttext top', 'ru', 'de'), ('fasttext\_top', 'ru', 'es'), #('fasttext random', 'ru', 'zh-CN'), ('fasttext top', 'ru', 'zh-CN'), #('fasttext random', 'ru', 'de'), #('fasttext random', 'de', 'en'), ('fasttext top', 'de', 'en'), #('fasttext random', 'de', 'es'), ('fasttext top', 'de', 'ru'), #('fasttext random', 'de', 'ru'), ('fasttext\_top', 'de', 'de'), ('fasttext top', 'de', 'es'), #('fasttext random', 'de', 'zh-CN'), ('fasttext top', 'de', 'zh-CN'), #('fasttext random', 'es', 'en'), ('fasttext top', 'es', 'en'), #('fasttext random', 'es', 'de'), ('fasttext top', 'es', 'ru'),

```
('fasttext_top', 'es', 'de'),
                #('fasttext random', 'es', 'ru'),
                ('fasttext_top', 'es', 'es'),
                #('fasttext random', 'es', 'zh-CN'),
                ('fasttext_top', 'es', 'zh-CN'),
                #('fasttext random', 'zh-CN', 'en'),
                ('fasttext_top', 'zh-CN', 'en'),
                #('fasttext random', 'zh-CN', 'es'),
                ('fasttext_top', 'zh-CN', 'ru'),
                ('fasttext_top', 'zh-CN', 'de'),
                ('fasttext_top', 'zh-CN', 'es'),
                #('fasttext random', 'zh-CN', 'ru'),
                ('fasttext_top', 'zh-CN', 'zh-CN'),
                #('fasttext random', 'zh-CN', 'de'),
s_min_en=[]
s_max_en=[]
s_mean_en=[]
s_median_en=[]
s_std_en=[]
s1_min_en=[]
s1_max_en=[]
s1_mean_en=[]
s1_median_en=[]
s1_std_en=[]
s min es=[]
s_max_es=[]
s mean es=[]
s median es=[]
s_std_es=[]
```

```
s1_min_es=[]
s1_max_es=[]
s1_mean_es=[]
s1_median_es=[]
s1_std_es=[]
s_min_ru=[]
s_max_ru=[]
s_mean_ru=[]
s_median_ru=[]
s_std_ru=[]
s1_min_ru=[]
s1_max_ru=[]
s1_mean_ru=[]
s1_median_ru=[]
s1_std_ru=[]
s_min_de=[]
s_max_de=[]
s_mean_de=[]
s_median_de=[]
s_std_de=[]
s1_min_de=[]
s1_max_de=[]
s1_mean_de=[]
s1_median_de=[]
s1_std_de=[]
s_min_zh=[]
s_max_zh=[]
s_mean_zh=[]
s_median_zh=[]
s_std_zh=[]
s1_min_zh=[]
s1_max_zh=[]
```

```
s1_mean_zh=[]
s1_median_zh=[]
s1_std_zh=[]
md = ''
for translation in translations:
    embedding, lg1, lg2 = translation
    # Vocab/Vectors/Dicts
    lg1_vocab, lg1_vectors, lg2_vocab, lg2_vectors = \
        pickle_rw((lg1 + '_' + embedding.split('_')[0] + '_vocab', 0),
                  (lg1 + '_' + embedding.split('_')[0] + '_vectors', 0),
                  (lg2 + '_' + embedding.split('_')[0] + '_vocab', 0),
                  (lg2 + '_' + embedding.split('_')[0] + '_vectors', 0),
                  write=False)
    lg1_dict = make_dict(lg1_vocab, lg1_vectors)
    lg2 dict = make_dict(lg2_vocab, lg2_vectors)
    print('Translation: '+lg1+'->'+lg2+'\n')
    # Train/Test Vocab/Vectors
    vocab_train, vocab_test = vocab_train_test(embedding, lg1, lg2, lg1_vocab)
    X_train, X_test, y_train, y_test = vectors_train_test(vocab_train,
                                                           vocab_test)
    # Fit tranlation matrix to training data
    model, history, T, D, tf,I, M = translation_matrix(X_train, y_train)
    print('biggest element:'+str(np.max(T))+'\n')
    U,s,Vh = svd(T)
    #scaler = MinMaxScaler()
    #scaler.fit(s)
    \#s = scaler.transform(s)
    s1 = np.log10(s)
    print("min: "+str(min(s))+"\n")
    print("max: "+str(max(s))+"\n")
```

```
print("mean: "+str(np.mean(s))+"\n")
print("median: "+str(np.median(s))+"\n")
print("std: "+str(np.std(s))+"\n")
print("min: "+str(min(s1))+"\n")
print("max: "+str(max(s1))+"\n")
print("mean: "+str(np.mean(s1))+"\n")
print("median: "+str(np.median(s1))+"\n")
print("std: "+str(np.std(s1))+"\n")
if lg1 == 'en':
    s_min_en.append(min(s))
    s_max_en.append(max(s))
    s_mean_en.append(np.mean(s))
    s_median_en.append(np.median(s))
    s_std_en.append(np.std(s))
    s1_min_en.append(min(s1))
    s1_max_en.append(max(s1))
    s1_mean_en.append(np.mean(s1))
    s1_median_en.append(np.median(s1))
    s1_std_en.append(np.std(s1))
if lq1 == 'es':
    s_min_es.append(min(s))
    s_max_es.append(max(s))
    s_mean_es.append(np.mean(s))
    s_median_es.append(np.median(s))
    s_std_es.append(np.std(s))
    s1_min_es.append(min(s1))
    s1_max_es.append(max(s1))
    s1_mean_es.append(np.mean(s1))
```

```
s1_median_es.append(np.median(s1))
    s1_std_es.append(np.std(s1))
if lq1 == 'ru':
    s_min_ru.append(min(s))
    s_max_ru.append(max(s))
    s_mean_ru.append(np.mean(s))
    s_median_ru.append(np.median(s))
    s_std_ru.append(np.std(s))
    s1_min_ru.append(min(s1))
    s1_max_ru.append(max(s1))
    s1_mean_ru.append(np.mean(s1))
    s1_median_ru.append(np.median(s1))
    s1_std_ru.append(np.std(s1))
if lg1 == 'de':
    s_min_de.append(min(s))
    s_max_de.append(max(s))
    s_mean_de.append(np.mean(s))
    s_median_de.append(np.median(s))
    s_std_de.append(np.std(s))
    s1_min_de.append(min(s1))
    s1 max de.append(max(s1))
    s1_mean_de.append(np.mean(s1))
    s1_median_de.append(np.median(s1))
    s1_std_de.append(np.std(s1))
if lq1 == 'zh-CN':
    s_min_zh.append(min(s))
    s_max_zh.append(max(s))
    s_mean_zh.append(np.mean(s))
    s median zh.append(np.median(s))
    s_std_zh.append(np.std(s))
    s1_min_zh.append(min(s1))
    s1_max_zh.append(max(s1))
    s1_mean_zh.append(np.mean(s1))
    s1_median_zh.append(np.median(s1))
```

```
s1_std_zh.append(np.std(s1))
#
          #print(s)
          plt.hist(s,bins='auto')#bins=50,normed='True',range = (0.0,0.2))
#
          #plt.plot(s)
          plt.show()
max: 0.625777
mean: 0.0208729
median: 0.0114701
std: 0.0446892
min: -3.99049
max: -0.203581
mean: -1.9647
median: -1.94044
std: 0.491782
```

## **Heatmaps of SVD Statistics**

```
In [53]:
              s_min = []
              s_min.append(s min en)
             s_min.append(s_min_ru)
             s_min.append(s_min_de)
              s_min.append(s min es)
              s_min.append(s_min_zh)
              s_max = []
             s_max.append(s_max_en)
             s_max.append(s_max_ru)
             s_max.append(s_max_de)
             s_max.append(s_max_es)
             s_max.append(s_max_zh)
              s_mean = []
             s_mean.append(s_mean_en)
             s_mean.append(s_mean_ru)
             s_mean.append(s_mean_de)
             s_mean.append(s_mean_es)
             s_mean.append(s_mean_zh)
             s_median = []
              s_median.append(s_median_en)
              s_median.append(s_median_ru)
              s_median.append(s_median_de)
             s_median.append(s_median_es)
             s_median.append(s_median_zh)
             s_std = []
              s_std.append(s std en)
              s_std.append(s_std_ru)
             s_std.append(s_std_de)
              s_std.append(s std_es)
             s_std.append(s_std_zh)
              s1_min = []
             s1_min.append(s1 min_en)
              s1_min.append(s1_min_ru)
              s1_min.append(s1_min_de)
              s1 min.append(s1 min es)
             s1_min.append(s1_min_zh)
             s1_max = []
             s1_max.append(s1_max_en)
             s1_max.append(s1_max_ru)
             s1_max.append(s1_max_de)
             s1_max.append(s1_max_es)
```

```
s1 max.append(s1 max zh)
s1_mean = []
s1_mean.append(s1_mean_en)
s1_mean.append(s1_mean_ru)
s1_mean.append(s1 mean_de)
s1_mean.append(s1 mean_es)
s1_mean.append(s1_mean_zh)
s1_median = []
s1_median.append(s1_median_en)
s1_median.append(s1_median_ru)
s1_median.append(s1_median_de)
s1_median.append(s1_median_es)
s1_median.append(s1_median_zh)
s1_std = []
s1_std.append(s1_std_en)
s1_std.append(s1_std_ru)
s1_std.append(s1_std_de)
s1_std.append(s1_std_es)
s1_std.append(s1_std_zh)
init_notebook_mode(connected=True)
trace = go.Heatmap(z=s min,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s_min',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s_min')
trace = go.Heatmap(z=s max,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s max',
```

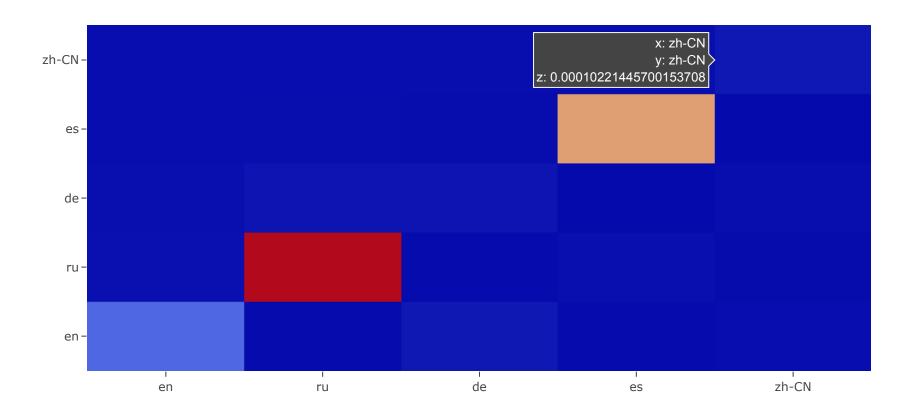
```
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s max')
trace = go.Heatmap(z=s_mean,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s_mean',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s_mean')
trace = go.Heatmap(z=s median,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s_median',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s_median')
trace = go.Heatmap(z=s_std,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
fig = go.Figure(data=data, layout=layout)
layout = go.Layout(
title='s std',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s_std')
trace = go.Heatmap(z=s1 min,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
```

```
layout = go.Layout(
title='s1 min',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s1_min')
trace = go.Heatmap(z=s1 max,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s_max',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s max')
trace = go.Heatmap(z=s1_mean,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s1_mean',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s1_mean')
trace = go.Heatmap(z=s1 median,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s1_median',
fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s1_median')
trace = go.Heatmap(z=s1 std,
               x=['en', 'ru', 'de', 'es', 'zh-CN'],
               y=['en', 'ru', 'de', 'es', 'zh-CN'])
data=[trace]
layout = go.Layout(
title='s1 std',
```

fig = go.Figure(data=data, layout=layout)
iplot(fig, filename='s1\_std')



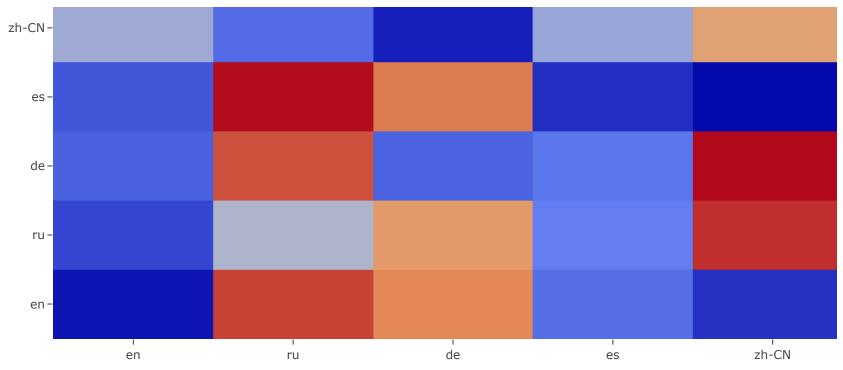
## s\_min



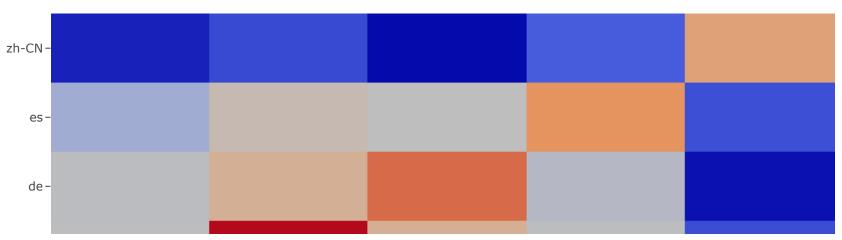
s\_max





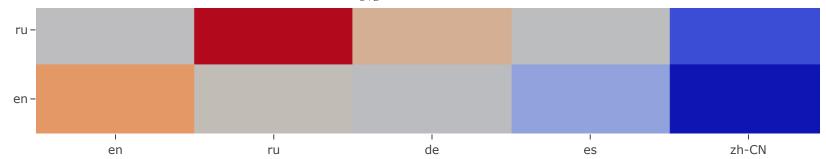


### s\_mean

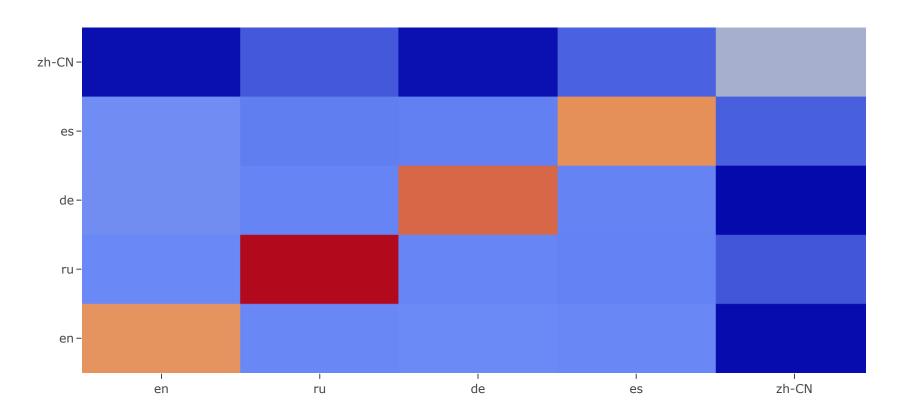




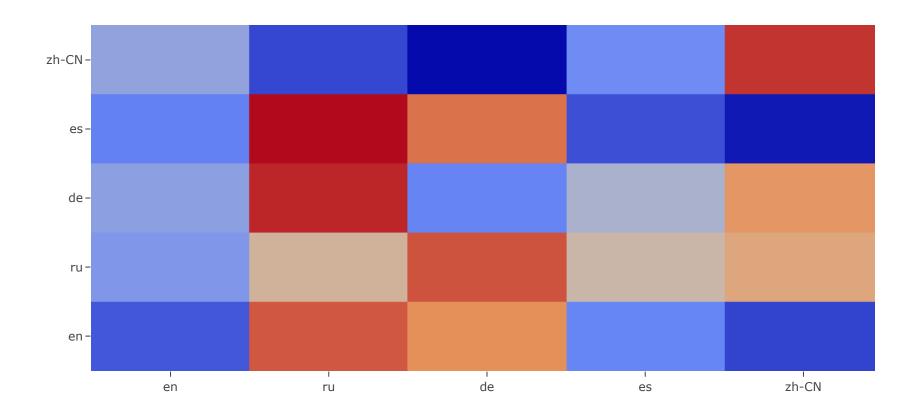




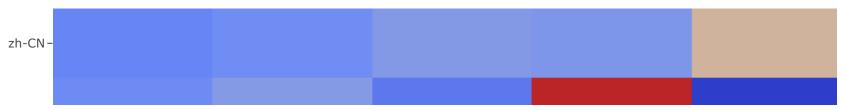
# s\_median



s\_std

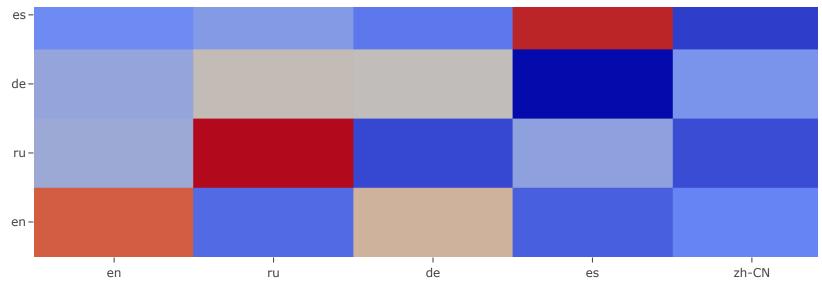


s1\_min

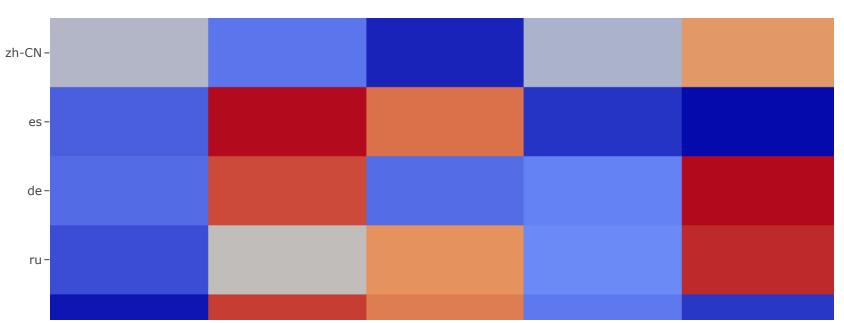








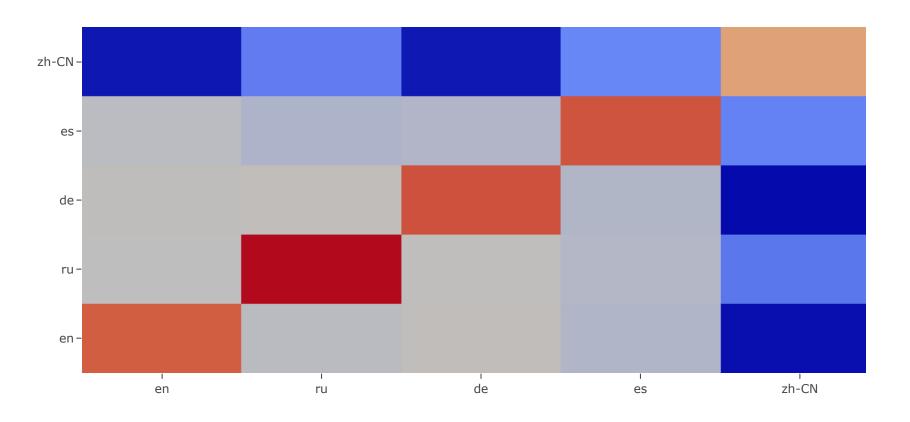
#### s\_max



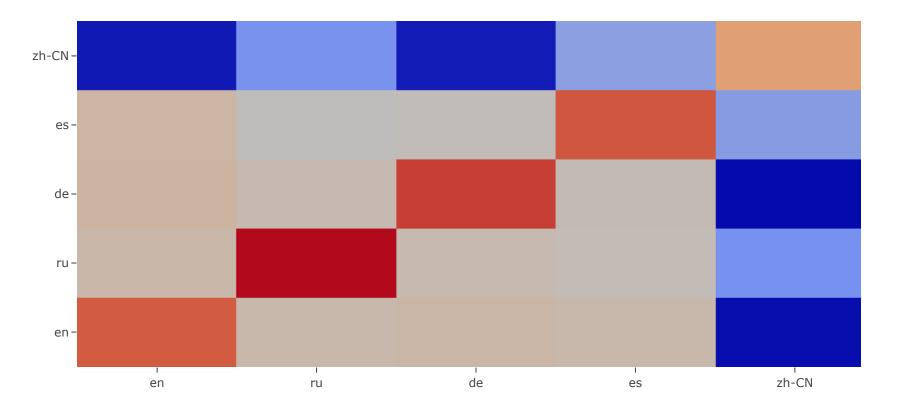




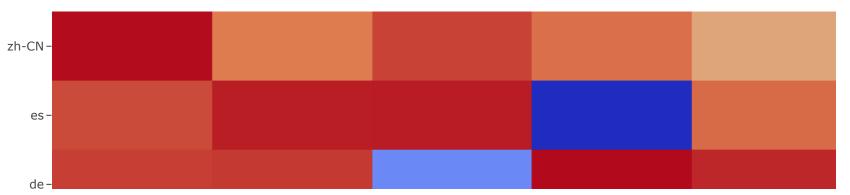
s1\_mean



s1\_median

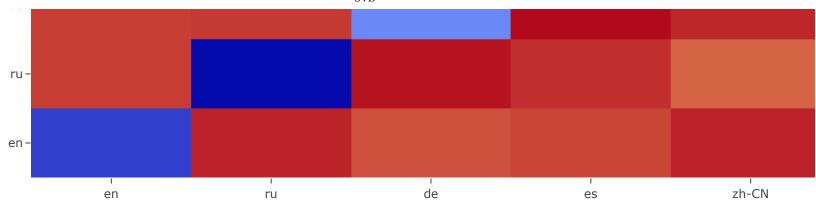


s1\_std









# **Inverted Matrices**

In [11]: **if** name == ' main ': # Manually set list of translations (embedding, 1q1, 1q2) translations = [#('fasttext random', 'en', 'ru'), ('fasttext\_top', 'en', 'ru'), #('fasttext random', 'en', 'de'), ('fasttext top', 'en', 'de'), #('fasttext random', 'en', 'es'), ('fasttext top', 'en', 'es'), #('fasttext random', 'en', 'zh-CN'), ('fasttext top', 'en', 'zh-CN'), #('fasttext random', 'de', 'en'), ('fasttext top', 'de', 'en'), #('fasttext random', 'de', 'es'), ('fasttext top', 'de', 'es'), #('fasttext random', 'de', 'ru'), ('fasttext top', 'de', 'ru'), #('fasttext random', 'de', 'zh-CN'), ('fasttext top', 'de', 'zh-CN'), #('fasttext random', 'ru', 'en'), ('fasttext top', 'ru', 'en'), #('fasttext random', 'ru', 'es'), ('fasttext top', 'ru', 'es'), #('fasttext random', 'ru', 'zh-CN'), ('fasttext top', 'ru', 'zh-CN'), #('fasttext random', 'ru', 'de'), ('fasttext top', 'ru', 'de'), #('fasttext random', 'zh-CN', 'en'), ('fasttext top', 'zh-CN', 'en'), #('fasttext random', 'zh-CN', 'es'), ('fasttext top', 'zh-CN', 'es'), #('fasttext random', 'zh-CN', 'ru'), ('fasttext top', 'zh-CN', 'ru'), #('fasttext random', 'zh-CN', 'de'), ('fasttext top', 'zh-CN', 'de'), #('fasttext random', 'es', 'en'), ('fasttext top', 'es', 'en'), #('fasttext random', 'es', 'de'), ('fasttext top', 'es', 'de'), #('fasttext random', 'es', 'ru'), ('fasttext top', 'es', 'ru'), #('fasttext random', 'es', 'zh-CN'), ('fasttext top', 'es', 'zh-CN')

```
md = ''
for translation in translations:
    embedding, lg1, lg2 = translation
    # Vocab/Vectors/Dicts
    lg1_vocab, lg1_vectors, lg2_vocab, lg2_vectors = \
        pickle rw((lg1 + '_' + embedding.split('_')[0] + '_vocab', 0),
                  (lg1 + '_' + embedding.split('_')[0] + '_vectors', 0),
                  (lg2 + ' ' + embedding.split('_')[0] + '_vocab', 0),
                  (lg2 + ' ' + embedding.split('_')[0] + '_vectors', 0),
                  write=False)
    lg1 dict = make dict(lg1 vocab, lg1 vectors)
    lg2_dict = make_dict(lg2_vocab, lg2_vectors)
    print('Translation: '+lg1+'->'+lg2+'\n')
    # Train/Test Vocab/Vectors
    vocab_train, vocab_test = vocab_train_test(embedding, lg1, lg2, lg1_vocab)
    X_train, X_test, y_train, y_test = vectors_train_test(vocab_train,
                                                           vocab test)
    # Fit tranlation matrix to training data
    model, history, T, D, tf, I, M = translation_matrix(X_train, y_train)
    print('Inverse:'+str(I)+'\n')
```

```
Translation: en->ru

length of en-ru vocab: 6839

Determinant:6.68409e-20

Fr_norm:-0.0

Inverse:[[ 11.04030704 -58.05263901 -70.07519531 ..., 25.41628647 30.97108078 -40.67876816]
[ 91.81015015 155.81185913 63.31090164 ..., -51.2548027 -34.41306305 47.90806961]
[ 23.46608734 12.1979866 -52.79821777 ..., 23.93603897 -7.66915035 5.51542711]
```

```
[-95.40709686 -29.07827187 87.29953003 ..., 100.88738251 -16.7738266]
  153.37922668]
 [-147.87860107 -81.68314362 -44.3213768 ..., 173.213974
                                                             -59.09873962
   59.42921829
 [ 16.56924438 -103.65172577 -142.10444641 ..., -78.63152313
  117.04570007 -168.28567505]]
Translation: en->de
length of en-de vocab: 16693
Determinant:2.40427e-21
Fr norm:0.0
Inverse: [ 755.14819336 -133.340271 206.62522888 ..., 1882.01904297
  -709.5010376 -1083.3581543 1
 [ 242.50422668 -23.07047462
                                  5.77775288 ..., 960.47021484
  -322.10214233 -420.7321167
 [ -431.28991699 97.79253387
                                -95.18783569 ..., -1025.21264648
   330.7355957 584.13464355]
 ...,
                                 96.03134155 ..., -1551.60412598
 [ -422.92025757 46.88298035
   493.1998291 651.64038086]
                                 202.88879395 ..., 1523.80834961
 [ 611.00964355 -180.95664978
  -622.27716064 -950.3012085 ]
                                -96.83132935 ..., -761.62390137
 [ -259.61535645 10.06036949
   190.62011719 434.51565552]]
Translation: en->es
length of en-es vocab: 10422
Determinant:-1.16279e-23
Fr norm:0.0
Inverse: [ -98.68668365 -260.83862305 -587.78167725 ..., 379.01580811
   57.62456131 647.65167236]
 [ -93.85202026
                31.28058624 144.4175415 ..., -42.15445328
    3.08430982 -151.31071472
 [ 284.58007812 -404.34399414 -712.90319824 ..., 552.19470215
  -39.45856476 884.690063481
 [ 200.77197266 -179.4989624 -525.70465088 ..., 256.63024902
  -38.14390945 414.311248781
 [-100.97593689 -223.18373108 -465.73358154 ..., 310.7088623
                                                               63.51074219
   427.6505127 ]
```

```
[-123.85021973 -202.60536194 -432.22723389 ..., 316.81027222
    15.20920467 519.00701904
Translation: en->zh-CN
length of en-zh-CN vocab: 1460
Determinant:-0.0
Fr norm:-0.0
Inverse: [[ 279.08325195 -50.90645218 174.09918213 ..., 90.67852783
  -125.23526001 138.2858429 ]
 [ 282.04492188 -24.62430573 276.77432251 ..., 248.19404602
   -95.89566803 -59.2610321 ]
 \begin{bmatrix} -3.75852799 & -152.42700195 & 65.89362335 & \dots, & 302.29708862 \end{bmatrix}
 -105.84304047 -232.65254211]
 [ 211.2144165 -100.81359863 124.05513 ..., 331.4234314 -124.95433044
 -216.73834229]
 [-125.23327637 \quad 128.56265259 \quad 89.98539734 \dots, \quad -53.60145569
    78.57273102 57.74006271
 103.99213409 30.01247787
Translation: de->en
length of de-en vocab: 16693
Determinant: -2.15217e-17
Fr norm:-0.0
Inverse: [ 1.84647417 -55.90779495 -43.97912598 ..., 39.81010818
   -39.84086227 -105.50863647]
 91.50335693 135.40769958 272.12155151 ..., 170.50970459
   -79.33867645 -129.798507691
 \begin{bmatrix} -1.02397203 & 67.86239624 & -5.41641092 \dots, & 94.55872345 \end{bmatrix}
 -108.43566895 -34.19537735]
 . . . ,
 [-55.88882065 -73.20679474 -167.59153748 ..., -99.45224762
    50.38871765 40.59305191
 \begin{bmatrix} 71.21019745 & 31.15022278 & 143.98403931 & \dots, & 29.07103348 \end{bmatrix}
   -51.79080582 -67.524017331
 \begin{bmatrix} 1.01958323 & -3.17144513 & -0.39861795 \dots, -27.27108765 & 64.1984024 \end{bmatrix}
    79.6170578 ]]
```

Translation: de->es

```
length of de-es vocab: 11456
Determinant:4.61531e-23
Fr norm:0.0
Inverse: [[-208.12774658 129.30685425 286.38415527 ..., 161.75546265
   -65.80812836 -153.169769291
 [ 47.54762268 -11.62705421
                                95.54808807 ..., 122.13251495
    95.22483063 -182.45480347]
 [ -68.93095398 29.17188644
                                10.01784801 ..., 80.02574921
   -23.01441765 -80.31826782]
 . . . ,
 [ -60.41200256 46.29036331
                                83.87097168 ..., -34.00827026
 -115.82743073 -35.87575531]
 [-335.98999023 66.93195343 189.75874329 ..., 24.15080833
 -275.91699219 87.48773193
 1.96587789 -25.36977577 105.56586456 ..., 206.55760193
    43.54348755 -296.44512939]]
Translation: de->ru
length of de-ru vocab: 5910
Determinant:-1.09467e-19
Fr norm:0.0
Inverse: [[-151.40771484 -30.88466072 77.30550385 ..., 38.58583069
   128.15287781 -20.5597744 1
 \begin{bmatrix} -38.43872452 & -37.58361816 & -96.61126709 \dots, & 37.91732788 \end{bmatrix}
   100.82440948 20.59609604
 [-176.77554321 23.42058182
                                27.32201767 ..., -75.23674011
   106.20679474 -273.70327759]
 [-194.94673157 -2.72268939 -151.26535034 ..., -133.86204529]
  145.88725281 -384.5640564 ]
 \begin{bmatrix} 70.48829651 & -24.49956322 & -85.98475647 & \dots, & -49.60044098 \end{bmatrix}
   -56.12587738 -85.30728912]
                 7.60398245 -20.77565765 ..., -214.16625977
 [-378.18856812
    72.85224152 -715.15490723]]
Translation: de->zh-CN
length of de-zh-CN vocab: 1820
Determinant:0.0
Fr norm:-0.0
Inverse:[[ 182.77256775 -12.98318291
                                             8.14419556 ..., -44.43376541
     78.37240601 -77.561012271
```

http://localhost:8888/notebooks/SVD.ipynb#

```
[ 80.42079163 -243.8031311
                                -268.67929077 ...,
                                                     112.42276764
    37.31299591 -114.50111389
 780.19976807 -752.38586426 -606.61517334 ..., -107.82647705
    144.76489258 -893.77630615]
 . . . ,
 [ -113.08462524 269.40768433
                                 195.55578613 ...,
                                                     -34.58014297
  -143.97172546 110.33963776]
 [ 214.31100464 -313.65765381
                                 -16.46645927 ...,
                                                     -42.66078186
    139.57568359 -233.36196899]
 [ 653.07806396 -1090.84179688 -776.70593262 ...,
                                                     27.33714294
    350.93087769 -820.984375 ]]
Translation: ru->en
length of ru-en vocab: 6839
Determinant:-1.14019e-20
Fr norm:0.0
Inverse: [[-234.50318909 22.7103157 468.10519409 ..., -142.00621033
   224.19677734 -438.632965091
 [ 44.44205093 -110.10383606 -214.72457886 ...,
                                                  56.50108719
 -131.72332764 84.38804626]
 [ 288.88677979 -277.25476074 -490.5708313 ..., 175.72525024
 -196.50019836 467.42556763]
 . . . ,
 [-241.14767456 \ 226.14082336 \ 325.89718628 \dots, -45.59486771
   226.55795288 -221.37988281]
 [ -8.15202427 145.6502533
                               33.30801773 ..., -147.27935791
   -15.43331718 -206.29437256]
 [-225.9641571 \quad 250.87538147 \quad 396.88607788 \dots, -133.33071899
   170.97853088 -433.68011475]]
Translation: ru->es
length of ru-es vocab: 5870
Determinant:1.06374e-22
Fr norm:-0.0
Inverse: [[-138.00456238 -6.45686722 71.60140991 ..., -36.70297241
    58.82127762 154.655838011
 [ 49.72098923 -52.75326538 104.88195801 ..., 20.12860298
   -74.70955658 40.26996613]
                               98.62489319 ..., 85.64072418
 [ -2.66938472 -147.09407043
    23.54691696 125.169189451
 . . . ,
```

```
[-118.95442963 13.25885868
                            91.0585022 ..., -67.21045685
   62.11876678 115.23573303]
 [ -36.5912056
               65.4972229
                            -3.35349679 ..., -29.58674812
                                                        53.3549614
  113.96194458]
 [-71.00119781 - 125.49362183 \ 112.67459106 \dots, \ 49.41052246
   34.73974228 -78.90220642]]
Translation: ru->zh-CN
length of ru-zh-CN vocab: 1266
Determinant:0.0
Fr norm:-0.0
Inverse: [ 123.87176514 101.6381073 194.61276245 ..., -42.12559891
   96.63561249 138.75669861
[-744.82489014 -704.24475098 -446.41647339 ..., -491.5687561 -63.25275421
  222.485656741
 119.09024811 102.5777359 ]
 . . . ,
 [ 195.69140625 27.52499962
                            45.47441101 ..., 102.32037354
    3.24064541 -41.37684631]
32.16794586
                6.01663494]
 [ 108.89143372 119.61774445 169.33660889 ..., 119.6232605
                                                         44.22268295
   93.17635345]]
Translation: ru->de
length of ru-de vocab: 5910
Determinant:-1.0791e-19
Fr norm:0.0
Inverse: [ 231.7795105 -53.77041626 35.14373016 ..., 41.9601593 -18.7463932
  138.1625824 ]
[-185.92315674 - 348.37637329 - 128.53903198 ..., -3.67792106
  113.00837708 -41.82150269
                            52.89003372 ..., 130.93800354
 [ 274.20281982 89.54084778
 -106.85772705 159.0308075 ]
 . . . ,
 [ 195.22572327 -163.60261536
                            73.5228653 ..., -102.59391785
  -55.86291504 83.46475983]
[ 13.79369545 -42.29308701
                            -1.58617067 ···, 57.35632324
  -16.52289391 40.294601441
 70.41092682 278.4899292 115.18925476 ..., 110.06312561
```

-41.55050659 37.66139984]]

```
Translation: zh-CN->en
length of zh-CN-en vocab: 1460
Determinant:-0.0
Fr norm:0.0
Inverse: [ 750.95532227 -2677.73120117 -2790.56835938 ..., -500.21502686
   6477.76611328 -906.92370605]
 [ -856.35272217 2233.87646484 2544.17041016 ...,
                                                   560.26184082
 -5371.02587891 496.52096558]
 [-1010.84552002 2835.54589844 2717.16064453 ...,
                                                   713.1763916
 -6876.35498047 718.14050293
 . . . ,
 [ -357.97131348 629.50219727
                                654.39550781 ...,
                                                   254.75791931
 -1516.64099121 115.86322784]
 [ 610.44421387 -1544.09875488 -1381.81567383 ..., -359.84481812
   3450.50390625 -447.62716675]
 [-1167.98925781 2801.60986328 2767.17675781 ..., 756.30444336
 -6591.30371094 868.70123291]]
Translation: zh-CN->es
length of zh-CN-es vocab: 1164
Determinant:-0.0
Fr norm:0.0
Inverse: [ 17.54487991 23.9071846 -69.86971283 ..., 89.22011566
   67.72798157 108.96387482]
 \begin{bmatrix} -19.26591682 & -58.13566971 & -63.12947464 \dots, & 12.89937305 & 102.1413269 \end{bmatrix}
   64.83384705]
 53.17620087 -105.45384216 -46.82474899 ..., 29.39961052
  285.44174194 51.69458771]
 [ -97.70675659 -172.0501709
                              11.54387856 ..., -69.68674469
  -87.34493256 -99.78017426]
 83.51582336
  427.69055176 193.971878051
 [ -33.97097397 -28.83506012
                              35.82284927 ..., 70.83348083
   -68.67223358 97.35033417]]
```

Translation: zh-CN->ru

```
length of zh-CN-ru vocab: 1266
Determinant:-0.0
Fr norm:-0.0
-2.2412765 1
81.02592468 48.94137955 -144.85075378 ..., -4.63170481
  -69.93479919 10.257637021
 \begin{bmatrix} 61.70194244 & -108.61361694 & -82.55732727 & \dots, & -18.13778687 \end{bmatrix}
   68.86730194 25.89509964]
 . . . ,
 39.08507919 -40.19970322 -63.80712128 ..., 24.37394714
   10.56565571 -40.56039429]
[ -98.20683289 39.0988884 -53.12154007 ..., 48.00292587
  -98.26872253 -1.27546012]
[ 12.94785118 -89.91964722 41.29096603 ..., 84.5228653
                                                         60.32333374
  -83.64056396]]
Translation: zh-CN->de
length of zh-CN-de vocab: 1820
Determinant:-0.0
Fr norm:-0.0
Inverse: [[-167.89735413 -169.32441711 262.71853638 ..., -49.06270218
 -218.04176331 -502.0098877 ]
[-211.6706543 -78.65090179 313.97622681 ..., 24.95234871
 -260.29180908 -415.22360229]
[-234.07113647 	 170.86058044 	 -28.66379738 	 ..., 	 49.25692368
  -20.01120186 285.25259399]
526.26983643 551.908569341
[ 923.55871582 -237.44372559 -63.26832199 ..., -316.19677734
  187.92474365 53.57709885]
 54.23075104 -414.93478394 291.21899414 ..., -158.23045349
 -240.38543701 -549.38092041]]
Translation: es->en
length of es-en vocab: 10422
Determinant:-8.86887e-23
Fr norm:0.0
Inverse: [ 3.66905022e+01 5.63451538e+01 -4.43629608e+01 ..., 1.47553272e+01
  -2.23721695e+01 1.92639114e+021
```

```
[ -2.38301963e-01 -8.82871704e+01
                                   1.55858719e+02 ..., 6.18005409e+01
   6.82027817e+01 -8.13018112e+01]
 [-9.10500641e+01 5.23132744e+01 -4.51392250e+01 ..., 3.51174103e+02
  -7.27205811e+01 -9.86932297e+01]
 [ 2.95722256e+01 -2.66521339e+01
                                    1.52041245e+02 ..., -9.97995734e-01
   5.86561394e+01 1.26562370e+02]
 \begin{bmatrix} -2.66694126e+01 & 1.24087509e+02 & -1.58618713e+02 & \dots, & 1.02118347e+02 \end{bmatrix}
   1.51513977e+02 -4.62004089e+02]
 [ 3.96808014e+01 2.40333366e+01
                                  3.03186607e+01 ..., -7.37969131e+01
   1.03059483e+01 2.31150391e+02]]
Translation: es->de
length of es-de vocab: 11456
Determinant:-1.67781e-22
Fr norm:-0.0
Inverse:[[-211.0153656 -109.92762756 -235.15696716 ..., -462.22366333
 -298.97665405 -98.863082891
 [ 50.72947311 31.43056297
                               7.85100508 ..., 32.22510147
   61.28936005 -22.80888176]
 189.72543335 96.867210391
 . . . ,
 [-216.62428284 -85.879776 -237.69984436 ..., -293.89746094 -273.0133667
 -253.99163818]
 [-192.18464661 -32.1150589 -150.17906189 ..., -291.48083496]
 -243.19403076 -141.9500885 ]
 [ 84.87358093 -22.03468704 134.11616516 ..., 305.0322876 173.19493103
   64.18505859]]
Translation: es->ru
length of es-ru vocab: 5870
Determinant:3.42516e-22
Fr norm:-0.0
Inverse: [[ -36.88964081 -38.66049194 171.79954529 ..., -23.12669563
  -56.12367249
                  6.872184281
53.82025909 212.07670593 -42.72406769 ..., -787.01470947
  112.25466919 61.76227188
 [ -6.68660975 177.28474426
                              32.79327393 ..., -769.54364014
  125.00292969
               -8.67141724]
 . . . ,
```

```
[ 38.5022583
                150.08508301 -30.97211075 ..., -298.6656189 152.74972534
   -61.62663651]
 [ 51.41888809
                211.19586182 -60.89271164 ..., -822.25720215
   239.45413208 -25.49222755]
 19.69354248 128.50161743 -26.33551598 ..., -596.45941162
    98.39897156
                11.74662304]]
Translation: es->zh-CN
length of es-zh-CN vocab: 1164
Determinant:-0.0
Fr norm:-0.0
Inverse: [ 1.54408991e-01 -7.29956970e+01 -5.20634460e+01 ..., -1.46622116e+02
   -1.52809097e+02 -3.85142250e+01]
 7.74740076e+00 3.60843201e+01 -7.10157700e+01 ..., -4.23915291e+01
  -9.08426361e+01 3.14684830e+01]
 \begin{bmatrix} 1.35625973e+01 & -5.47755051e+01 & -1.08091764e+01 \dots, & -7.55519513e-03 \end{bmatrix}
   -1.25363716e+02 2.30807434e+02]
 . . . ,
 [ 1.06153564e+02 -2.54409866e+02
                                      1.49036392e+02 ..., -4.00590363e+01
  -2.20805008e+02
                   1.89460587e+02]
 [ 2.15465317e+02 -2.01847336e+02
                                      9.14659595e+00 ..., -8.39445953e+01
   -2.12597778e+02 1.59251205e+02]
 [ -4.10690651e+01
                   3.38989067e+01
                                      4.17062912e+01 ..., 8.21285019e+01
   -1.81661606e+02
                    2.83516327e+02]]
```

#### **Sanity Check on Determinants**

In [19]: **if** name == ' main ': # Manually set list of translations (embedding, 1q1, 1q2) translations = [#('fasttext random', 'en', 'ru'), ('fasttext\_top', 'en', 'ru'), #('fasttext random', 'en', 'de'), ('fasttext top', 'en', 'de'), #('fasttext random', 'en', 'es'), ('fasttext top', 'en', 'es'), #('fasttext random', 'en', 'zh-CN'), ('fasttext top', 'en', 'zh-CN'), #('fasttext random', 'de', 'en'), ('fasttext top', 'de', 'en'), #('fasttext random', 'de', 'es'), ('fasttext top', 'de', 'es'), #('fasttext random', 'de', 'ru'), ('fasttext top', 'de', 'ru'), #('fasttext random', 'de', 'zh-CN'), ('fasttext top', 'de', 'zh-CN'), #('fasttext random', 'ru', 'en'), ('fasttext top', 'ru', 'en'), #('fasttext random', 'ru', 'es'), ('fasttext top', 'ru', 'es'), #('fasttext random', 'ru', 'zh-CN'), ('fasttext top', 'ru', 'zh-CN'), #('fasttext random', 'ru', 'de'), ('fasttext top', 'ru', 'de'), #('fasttext random', 'zh-CN', 'en'), ('fasttext top', 'zh-CN', 'en'), #('fasttext random', 'zh-CN', 'es'), ('fasttext top', 'zh-CN', 'es'), #('fasttext random', 'zh-CN', 'ru'), ('fasttext top', 'zh-CN', 'ru'), #('fasttext random', 'zh-CN', 'de'), ('fasttext top', 'zh-CN', 'de'), #('fasttext random', 'es', 'en'), ('fasttext top', 'es', 'en'), #('fasttext random', 'es', 'de'), ('fasttext top', 'es', 'de'), #('fasttext random', 'es', 'ru'), ('fasttext top', 'es', 'ru'), #('fasttext random', 'es', 'zh-CN'), ('fasttext top', 'es', 'zh-CN')

```
md = ''
for translation in translations:
    embedding, lg1, lg2 = translation
    # Vocab/Vectors/Dicts
    lg1_vocab, lg1_vectors, lg2_vocab, lg2_vectors = \
        pickle rw((lg1 + '_' + embedding.split('_')[0] + '_vocab', 0),
                  (lg1 + '_' + embedding.split('_')[0] + '_vectors', 0),
                  (lg2 + '_' + embedding.split('_')[0] + '_vocab', 0),
                  (lg2 + '_' + embedding.split('_')[0] + '_vectors', 0),
                  write=False)
    lg1_dict = make_dict(lg1_vocab, lg1_vectors)
    lg2 dict = make_dict(lg2_vocab, lg2_vectors)
    print('Translation: '+lg1+'->'+lg2+'\n')
    # Train/Test Vocab/Vectors
    vocab_train, vocab_test = vocab_train_test(embedding, lg1, lg2, lg1_vocab)
    X_train, X_test, y_train, y_test = vectors_train_test(vocab_train,
                                                           vocab test)
    # Fit tranlation matrix to training data
    model, history, T, D, tf, I, M = translation_matrix(X_train, y_train)
    y_norm = translation_results(X_test, y_test, vocab_test, T,
                                    lg2 vectors, lg2 vocab)
    #print('Volume of X matrix: '+ np.prod(X norm)+'\n')
    print(y_norm)
    print(T)
    print('Volume of yhat matrix: '+ str(np.prod(y norm))+'\n')
```

Translation: en->ru

length of en-ru vocab: 6839

```
Determinant:2.03775e-19
[ 0.67061174  0.6873163
                           0.85272115 ..., 1.20578921 1.40582168
  0.93844253]
[[ 4.34536341e-04 -1.01042946e-03
                                       1.29217806e-04 ...,
                                                              2.51814048e-03
    2.25269631e-03 -3.78022756e-041
                     1.11204310e-04
                                       3.61257058e-04 ...,
 [ -2.70378281e-04
                                                              1.47847389e-03
    2.56023044e-03
                     3.06686998e-04]
 [-7.82030053e-04 -2.08674697e-03 -3.18972440e-03 ...,
                                                              1.43284816e-03
    8.56383296e-04 -5.04361931e-04]
 . . . ,
 [ 3.68732936e-03
                     1.84817414e-03
                                       2.45620660e-03 ...,
                                                              4.04990744e-03
   -1.71988842e-03
                    -2.58150208e-03]
                     5.78932850e-05
 9.60162492e-04
                                       2.89971940e-03 ...,
                                                              8.86483584e-04
   -2.09363061e-03 -8.01478338e-04]
 \begin{bmatrix} -3.22616356e-03 & -2.79117911e-03 & -1.80032675e-03 \dots, & 1.22218125e-03 \end{bmatrix}
    1 762212000 02
                     7 650/65100 0/11
```

In [ ]: