

The Simplex Method

Q1] Niki holds two part time, Job I & Job II, she never wants to work more than a total of 12 hr a week. She has determined that for every hour she works at Job I, she needs 2 hr of preparations time, and for every hour she work at Job II, she need 1 hr of preparation time, and she cannot spend more than 16 hr for preparation. If she makes \$40 an hour at Job I, and \$30 an hour at Job II, how many hour should she work per week at each Job to maximize her income?

Solution:-

Let

$x_1$  = The number of hours per week Niki will work at Job I

$x_2$  = The number of hours per week Niki will work at Job II

Maximize

$$Z = 40x_1 + 30x_2$$

Subject to

$$x_1 + x_2 \leq 12$$

$$2x_1 + x_2 \leq 16$$

$$x_1 \geq 0; x_2 \geq 0$$



Let us take  $x_3$  and  $x_4$  as Slack Variable

$$\text{Max } z = 40x_1 + 30x_2 + 0x_3 + 0x_4$$

$$x_1 + x_2 + x_3 + 0x_4 = 12$$

$$2x_1 + x_2 + 0x_3 + x_4 = 16$$

$$\begin{bmatrix} 1 & 1 & 1 & 0 \\ 2 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 12 \\ 16 \end{bmatrix}$$

Basic Variable	$C_B$	$C_j$ $x_B$	40 $x_1$	30 $x_2$	0 $x_3$	0 $x_4$	Min Ratio
$x_3$	0	12	1	1	1	0	12
$x_4$	0	16	2	1	0	1	8 ←
		$\Delta_j$	-40	-30	0	0	

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$$R_2 \rightarrow R_2 \div 2$$

$$R_1 \rightarrow R_1 - R_2$$

Basic Variable	$C_B$	$C_j$ $x_B$	40 $x_1$	30 $x_2$	0 $x_3$	Min Ratio
$x_3$	0	4	0	$\frac{1}{2}$	1	8 ←
$x_1$	40	8	1	$\frac{1}{2}$	0	16
		$\Delta_j$	0	-10	0	

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$$R_1 \rightarrow 2R_1$$

$$R_2 \rightarrow R_2 - \frac{1}{2}R_1$$



Basic		$C_j$	40	30	
Variable	CB	XB	$x_1$	$x_2$	Min Ratio
$x_2$	30	8	0	1	
$x_1$	40	4	1	0	
		$\Delta_j$	0	0	

$$x_2 = 8$$

$$x_1 = 4$$

$$Z = 40x_1 + 30x_2$$

$$= 40(4) + 30(8)$$

$$= 400$$

The Final solution say that if Niki work 4 hours at Job I and 8 hours at Job II she will maximize her income to \$400