



1. Backpatching



```

superLoop:
    if B = 0 goto labelL2
    ; B is true; start checking L1's items
    if L1[0] = 0 goto next
    if L1[1] = 0 goto next
    ...
    if L1[n] = 0 goto next
    goto doAction
labelL2:
    if L2[0] = 0 goto next
    if L2[1] = 0 goto next
    ...
    if L2[n] = 0 goto next
doAction:
    S1
    goto superLoop
next:
....

```

1.2. **Suggest IR except that the B after the super-loop will only be calculated once.** Note that we were not required to use backpatching so we can fairly easily duplicate the code of S1 to avoid re-calculation of where to jump at the end of S1.

Also note that it wasn't required to give an optimized solution so there's no problem duplicating the code of S1.

```

superLoop:
    if B = 0 goto labelL2
labelL1:
    if L1[0] = 0 goto next
    if L1[1] = 0 goto next
    ...
    if L1[n] = 0 goto next
    S1
    goto labelL1
labelL2:
    if L2[0] = 0 goto next
    if L2[1] = 0 goto next
    ...
    if L2[n] = 0 goto next
    S1
    goto labelL2
next:
....

```

1.3. **Write translation scheme using the backpatching method for the IR you suggested from section 1.1.** Note we used two different markers *ML* for label and *MG* for goto.

production	semantic action
$S \rightarrow \text{super-loop } ML1 \ B \ @ \ L1$	$MG1 \ @ \ ML2 \ L2 \ ML3 \ S1 \ MG2$ $S.next = \text{freshLabel}();$ $\text{backpatch}(L1.falseList, S.next);$ $\text{backpatch}(L2.falseList, S.next);$ $\text{backpatch}(B.falseList, ML2.label);$ $\text{backpatch}(MG1.gotoList, ML3.label);$ $\text{backpatch}(MG2.gotoList, ML1.label);$ $\text{emit}(S.next ':');$
$L \rightarrow L1 \ B$	$L.falseList = L1.falseList ++ B.falseList;$
$L \rightarrow B$	$L.falseList = B.falseList;$
$B \rightarrow id$	$B.falseList = [\text{nextInstr}]; \text{emit}('if'id.name == '0''goto _');$
$B \rightarrow 0$	$B.falseList = [\text{nextInstr}]; \text{emit}('goto _');$
$B \rightarrow 1$	$B.falseList = [];$ //We expect later that B will have falseList// Const
$MG \rightarrow \varepsilon$	$MG.gotoList = [\text{nextInstr}];$ $\text{emit}('goto _');$
$ML \rightarrow \varepsilon$	$ML.label = \text{freshLabel}();$ $\text{emit}(ML.label ':');$

2. Parsing

2.1. **Is the grammar $LR(0)$?** No. Because when we have L in the stack, and the next token is $[$, we get shift-reduce conflict (shift $[$ to progress towards $L[num]$ or reduce L to E).



2.2. **Is the grammar $LR(1)$?** Yes. The table is



Action						Go To			
	[]	num	,	\$	S	E	L	EL
0	s3						1	2	
1					acc				
2	s4				r1				
3		r4	s6						5
4			s7						
5		s8							
6				s9					
7		s10							
8	r3				r3				
9		r4	s6						11
10					r2				
11		r5							

2.3. Parse `[] [num]` and present the stack states in the process.

#	Stack State
1	0
2	0 [3
3	0 [3 EL
4	0 [3 EL 5
5	0 [3 EL 5] 8
6	0 L
7	0 L 2
8	0 L 2 [4
9	0 L 2 [4 num 7
10	0 L 2 [4 num 7] 10
11	0 E
12	0 E 1
13	accepted




2.4. Parse `[num,num] [num]` and present the stack states in the process.

#	Stack State
1	0
2	0 [3
3	0 [3 num 6
4	0 [3 num 6 , 9
5	0 [3 num 6 , 9 num 6
6	error



3. DFA

3.1. Define the lattice for the domain Seth suggests, what are the elements and what is the relation \sqsubseteq and what is \sqcup . Each node in the lattice will be a binary string in the length of the amount of ascii characters. 

In that case, the relation $x \sqsubseteq y \equiv ((x \& y) = x)$ and $x \sqcup y \equiv x \mid y$.

In if you need $x \sqcap y \equiv x \& y$.

3.2. Define the abstract semantic of the syntax. Let y, x, z strings. 

Let n_y, n_x, n_z the current node (domain) which represents y, x, z respectively.

Let nn the node (domain) of the result.

$$T_{const} [?] \equiv [nn := \{x \mid x \text{ is a letter in } const\}]$$

$$T_{y+x} [n_y, n_x] \equiv [nn := n_y \sqcup n_x]$$

Regarding $*$:

for $n \leq 0$: $T_{y*0} [?] \equiv [nn := 00 \dots 00]$

For $n > 0$: $T_{y*0} [n_y] \equiv [nn := n_y]$

Regarding *replace*:

For $len(x) < 1$: $T_{y.replace(x,z)} [n_y, n_x, n_z] \equiv [nn := n_y \sqcup n_z]$

For $len(x) < 1$

For $len(x) < 1$

For n_x


Assume t and T are the matching lower/upper case of each other.

$$T_{y.upper()} [n_y] \equiv [nn := \{T \mid t \in n_y\}]$$

$$T_{y.lower()} [n_y] \equiv [nn := \{t \mid T \in n_y\}]$$

$$T_{y=x} [n_x] \equiv [n_y := n_x]$$

3.3. Present the analysis on `foo`. Draw the *CFG*.

3.4. Is using Seth's idea we can prove the assert at line 7. No. Since the domain only track which letters **may** appear in the string but it doesn't mean that the letter **must** appear in the string. Meaning that we know that the assert **might** be true but it isn't promised. 

3.5. Mat's idea is to track the letters that must appear in the string. The relation $x \sqsubseteq y \equiv ((x \mid y) = x)$ and $x \sqcup y \equiv x \& y$. 

In if you need $x \sqcap y \equiv x \mid y$.

3.6. Ohh well. Why isn't the lecture/tutorial show any example of doing something like that :-)



3.7. Not so well. Here's a meme

