

# Python 3 for scientific computing

Lecture 2, 31.1.2018

A first practical look at Python 3

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# Meta

## Last week

- Overview
  - What Python is: a general high-level programming solution, open source, ...
  - Why for numerics, why now; how Python compares to MATLAB
  - Language versions: current Python 3 vs. legacy Python 2
- Scientific Python is the bazaar to MATLAB's one-stop shop
- Python in the context of programming languages in general
  - Imperative, somewhat functional, interpreted, object-oriented, duck-typed, ...

# Meta

## Course schedule

(confidence = 0.949999999999999956)

- Week 1: Introduction and overview.
- **Week 2: A first practical look into Python 3.** Basics by example.
- Week 3: A second practical look into Python 3. Language features by example.  
Structuring programs in Python.
- Week 4: Overview of scientific Python: NumPy, SciPy, Matplotlib, SymPy.
- Week 5: Basics of NumPy, SciPy, Matplotlib, SymPy, by example.
- Week 6: More NumPy, SciPy, Matplotlib, SymPy. An overview of smaller scientific libraries for specific tasks. Behaviour of floating point numbers.
- Week 7: Parallel computing, in general and in Python. MPI, OpenMPI, mpi4py.
- Week 8: Fundamentals of software engineering: version control (local and social), effective use of comments, testing, static code analysis.
- Week 9: High-performance computing in Python via Cython and OpenMP.
- Week 10: The new paradigm: a gentle introduction to functional programming (FP).
- Week 11: Beyond Python: expressive power, lambda calculus, the Lisp family, and Racket (a modern Lisp).
- **Exercises will be posted after most lectures, starting week 3.**
  - The topics of weeks 1 and 2 are included in the exercises of week 3.
  - One week to solve. Each week starting from week 4, solutions to the previous week's exercises will be discussed.

# Meta

## General information

- Lecture slides (PDF), uploaded after each lecture:  
[https://github.com/Technologicat/python-3-scicomp-intro/tree/master/lecture\\_slides](https://github.com/Technologicat/python-3-scicomp-intro/tree/master/lecture_slides)
- Information on the **final assignment**:
  - A small software project in Python. A simple numerical solver is fine.
  - Individual work. Can be started after week  $\approx 6$ . Deadline **31.5**.
  - Topic can be freely chosen.
    - Everyone can suggest their own topic. *Is there something that would be useful in your own studies or research?*
  - Default topic, if none suggested:
    - Linear (or bilinear) finite element solver, heat equation, unit square, zero Dirichlet boundary conditions.
    - Use only NumPy, SciPy, Matplotlib et al.; ready-made FEM packages (e.g. SfePy or FeniCS) not allowed.
    - Keep it as simple as possible, this is intended as a small project (and the focus is not on how to make a generic FEM framework).
    - A summary of the required mathematics will be provided.

# Getting to know Python (1 of 2)

## (This set of slides)

- Python's documentation
- Basic control flow (loops, conditionals) ← From this point on we will have actual code
- Containers
  - Basic operations on lists and strings
  - String formatting
  - Slicing (indexing operation)
  - tuple (immutable list)
  - zip (interleaving iterables)
  - Tuple unpacking (destructuring bind and its friends)
  - set, dict
  - List comprehension  $B = [f(x) \text{ for } x \text{ in } A \text{ if } g(x)]$
- Functions
  - Defining; returning values
  - Argument passing (by position, by name)
  - Argument default values
  - Docstrings (where all the *help* comes from)
  - Functions as first-class objects; **lambda** (anonymous func.)
- Getting started with Spyder IDE (for exercises)

[ ] ( )  
{ }

%0.3g

"a" 'a'  
"""a"""

# Getting to know Python (2 of 2)

## (The next set of slides)

- Modules: defining, loading (**import**)
- The **with** statement (ensuring open files are eventually closed)
- Advanced control flow: *exceptions* (**try**, **except**, **finally**)
- Python and Unicode
- Language features, a closer look by example
  - Names and values (Python's "variables")
    - Special value **None**, keyword **is**; **global** and **nonlocal**
  - Paradigms: *imperative* vs. *functional* programming
  - Lexical scoping (contrast dynamic scoping)
  - Type system: strong typing, duck typing
  - Call-by-sharing (argument passing model)
- How to structure Python programs
  - Script (just a sequence of statements or expressions)
  - Procedural program
    - Conditional execution of the main program  
(allows dual use as main program and library)
  - Object-oriented program
    - Basics of object-oriented programming (OOP)  
(or, how to get rid of global variables in your solvers!)
    - Inheritance (single and multiple)

# Python's documentation

- In Python, almost everything is documented
- *help(foo)* to access documentation of object *foo* – such as a function, object instance, or object type.
  - Often contains technical details not easily found by searching the internet ...because if it's in *help*, no need to ask.
- Introspection tools useful to find candidates for *help*:
  - *dir*, *vars* (built-in functions)
  - Standard library module *inspect*, esp. its function *getmembers*
- IPython (incl. Spyder IDE, Jupyter Notebook):
  - *foo?* – *description*
  - *foo??* – source code (if applicable)
- ...

# • ... Python's documentation

- Spyder IDE – *help*, with rich text rendering (NumpyDoc format)
  - Click the object to get help on (to place the text cursor), press *Ctrl+I*
  - If the *Help* pane is not visible, *View ▷ Panes ▷ Help*
  - Depends on static code analysis to determine the type of the object instance under the text cursor – often works, but not always
- Internet!
  - For example, the Python 3 standard library reference:  
<https://docs.python.org/3/library/index.html>
  - Project websites (for libraries), e.g. in case of NumPy:  
<https://docs.scipy.org/doc/numpy/>
  - Search engines
    - E.g. googling for “python 3 inspect” is likely the fastest way to find this:  
<https://docs.python.org/3/library/inspect.html>
    - A useful complement for *help*. Other search results useful when the official documentation is unnecessarily cryptic.
    - See esp. any helpful questions/answers at StackOverflow.
    - Sometimes “python 3” better as a search term than just “python”, because of the still ongoing Python 2 to Python 3 transition.



# Basic control flow

## Loops, **for**

- Python supports **for** and **while** loops. Some examples of **for** loops:

```
for k in range(10): # integers 0, 1, ..., 9
    print(k**2)      # ** denotes exponentiation (like in Fortran)
```

```
A = [5, 17, 23, 42] # list, we will discuss them below
for x in A:         # loop directly over a container (here a list)
    print(x)
```

- *Note the consistent indentation.* The loop body **must** be indented.
  - This is how Python knows where the loop body ends in your source code.
- As usual, **continue** skips the rest of one iteration; **break** exits the loop.
- Recall Python's lexical scoping rules from lecture 1: the loop counter lives *in the scope containing the loop* (the loop does **not** introduce a new scope).
  - In other words: the loop counter remains visible after the loop finishes, and has the value it had when the loop finished.
  - Language feature, can be useful.

<https://eli.thegreenplace.net/2015/the-scope-of-index-variables-in-pythons-for-loops/>

# Basic control flow

## Loops, **for**

- Python's **for** loop always runs over an *iterable* (contrast C, Java).
- To iterate over integers, first consider if you really need to.
  - If you only need an index, iterate over the container itself instead.
  - If need to get corresponding elements from two or more sequences, **zip** them (will be discussed later in this lecture).
- If you really do need an integer, use the **range** built-in function, which – roughly speaking – gives an iterable view into the natural numbers.
  - See `help(range)` for more options (start, step).
- Range is *lazy*. No array; each number is produced on-demand.
  - This was changed in Python 3.0. In legacy codes (Python 2.x), one may see `xrange()`, which is essentially equivalent to the Python 3 `range()`.
- Technically speaking... `range()` creates a *range object*, which is Python's built-in way to represent ranges. It behaves mostly like a *generator*, except that one can iterate over it multiple times (each time starting from the beginning).

# Basic control flow

## Loops, **for/else**

- In Python, a **for** loop may have an **else** block:

```
for k in range(10):  
    m = k**2  
    if m > 100:  
        break  
    print(m)    # here  $m \leq 100$ ; no need for an else block (for the if)  
else:          # this else belongs to the for (indentation!)  
    print("All squares were  $\leq 100$ .")
```

- The **else** in a **for/else** means “if no **break** occurred”.
- Although the feature is known as **for/else**, mnemonic: (**for/**)**break/else**
- Keep in mind you can access the final value of the loop counter also in the else block (this makes **for/else** actually useful).

(But for searching a collection for an item, there is a more pythonic way, see below.)

# Basic control flow

## Loops, while

- Example of a **while** loop:

```
x = 0
while x**2 < 100:
    print(x)
    x = x + 1
```

- As usual, **continue** skips the rest of one iteration; **break** exits the loop.
- Be careful: when writing a **while**, all too easy to forget to update the counter.
  - The **for** loop does that for you, whereas the **while** loop expects you to do that yourself.
- The scope for the loop counter is the same as for the **for** loop, but here it is more explicit (since the counter is initialized manually).
- A **while** loop is not really meant to iterate over a collection; use **for** instead. It is appropriate when the decision on whether to keep looping must be made dynamically, i.e. *while* the loop is running: **while** do\_something(...):

# Basic control flow

## Conditionals, **if** statement

- Python has two forms of **if**. First, the statement form:

```
if 0 < x < 1:    # this works, and evaluates each term (at most) once
    print("hello, ε!")
elif x < 0:      # in Python, "else if" is spelled "elif"
    print("now that's too negative")
else:
    print("...")
```

- As usual, the conditions are tested in sequence until one is true, or the **else** block is reached. The corresponding body runs.
- In Python, most things that are not **None** or **False** are “truthy”. Details: <https://docs.python.org/3/library/stdtypes.html#truth-value-testing>
- **elif** and **else** parts are optional. There may be several **elif**s.
- Chained comparisons in Python: <https://docs.python.org/3/reference/expressions.html#comparisons>

# Basic control flow

## Conditionals, logical operators

- To create more complex conditions, use the logical operators **and**, **or**, **not** (and parenthesize where needed).
- The **and** and **or** operators evaluate one term at a time, from left to right.
- They *short-circuit*, i.e. stop as soon as the result becomes known. Hence:
  - **and** stops evaluation after the first falsey value.
  - **or** stops evaluation after the first truthy value.
- The return value from an expression involving **and** and/or **or** is the *actual value of the last term tested*, not a bool! (No implicit conversions.)
- For decision purposes (also in **if**, **while**), only truthiness matters.
- Examples:

a <b>or</b> b	# if a is truthy, return a; else return b
a <b>and</b> b	# if a is truthy, test and return b; else return a
a <b>or</b> b <b>or</b> c	# from the left, return the first one that is truthy, or finally c
a <b>and</b> b <b>and</b> c	# from the left, return the first one that is falsey, or finally c

# Basic control flow

## Conditionals, **if** expression

- Python also has an expression form of **if**, sometimes used in assignments:

```
x = some_expr if condition else other_expr
```

In this variant, `other_expr` is mandatory, because an expression **must** always return a value, and the **elif** part is not supported.

Similar to C's ternary operator `a?b:c`, but different ordering: `b if a else c`

History for the curious:

<https://docs.python.org/2.5/whatsnew/pep-308.html>

<https://www.python.org/dev/peps/pep-0308/> Conditional expressions (2.5+)

- Also sometimes seen: a conditional assignment using only logical operators:

```
x = some_expr or other_expr
```

This is useful if `some_expr` may be falsey, and in that case one wants to use `other_expr` (e.g. default value for an optional argument initialized to **None**).

Equivalent to:

```
x = some_expr if some_expr else other_expr
```

# Containers

## Basic operations on lists and strings

- Indexing uses square brackets: [ ]
- **Indices always start from 0**, also in NumPy (contrast Fortran, MATLAB)
- Negative indices allowed: **-1** is the last element, **-2** second to last, ...
- Accesses are bounds-checked (like in MATLAB; contrast C); any access past the end raises **IndexError**; silent memory corruption cannot occur
- A **list** is a sequence of arbitrary elements
- Lists are represented using square brackets, e.g. ['foo', 'bar', 'baz']
- A **string** is a sequence of characters (a character is a length-1 string)
- Python 3 strings support Unicode *transparently*, e.g. '∂²u/∂x²', '∃x', 'λ', ' あ '
- i.e. requiring no additional effort from the programmer
- The type name is *str*; e.g. str(**1**) → "**1**"
- String literals are quoted, as usual. Supported styles:
  - Single quote (apostrophe): 'a'
  - Double quote: "a"
  - Three double quotes: """a"""
    - This variant allows embedded newlines. Especially useful for docstrings.
  - Same meaning for 'a', "a" and """a""" (contrast \*nix shells, e.g. *bash*)



# Containers

## Basic operations on lists and strings

- Examples:

```
empty_list = [] # just square brackets [ ]
```

```
letters = ['a', 'b', 'c']
```

```
numbers = [1, 2, 3]
```

```
all = letters + numbers # for lists, + concatenates
```

```
numbers_thrice = 3 * numbers # for lists, * repeats
```

- Python lists are *heterogeneous*, i.e. elements can have different types:

```
stuff = ['cat', 42, True]
```

- Useful methods: append, extend, insert, pop, remove, sort, reverse
- Strings also support joining via str.join. This is invoked as a method on a str instance that represents the separator:

```
s = ', '.join(letters) # ⇒ 'a, b, c'
```

- Inverse operation: str.split

# Containers

## Basic operations on lists and strings

- **Escape sequences:**

"This string contains a quote \" and\na newline."    # \" ⇒ ", \n ⇒ newline

Full list:

[https://docs.python.org/3/reference/lexical\\_analysis.html#string-and-bytes-literals](https://docs.python.org/3/reference/lexical_analysis.html#string-and-bytes-literals)

General explanation:

[https://en.wikipedia.org/wiki/Escape\\_sequence#Programming\\_languages](https://en.wikipedia.org/wiki/Escape_sequence#Programming_languages)

- Specifically for quotes, can also use alternate styles (also `"""..."""`):

"I'm a string containing an apostrophe."

'The cat said "meow", so this string contains two double-quotes.'

- **Raw strings** disable escape sequences (Python-specific feature):

r"Here \n is just backslash and n."    # prefix r denotes a raw string

(Very convenient with LaTeX math in Matplotlib labels, and with regexes.)

# Containers

## String formatting

- A.k.a. *string literal interpolation*. Or in plain English, *insertion of values into a string at runtime, based on a template with placeholders*. Critically important for (human-language) localization; also makes code look clearer than concatenating pieces via `+`. Currently, three ways to do it:

- **Traditional**, also known as **C `sprintf`** style. In Python, `%` interpolates strings:

```
msg = "Hello %s, the result is %0.6g." % ("Fred", 17/23)
```

<https://docs.python.org/3/library/stdtypes.html#printf-style-string-formatting>

- Python 3.0 and later, **`str.format`**, invoked as a method of a `str` instance that is the template:

```
msg = "Hello {name:s}, the result is {result:0.6g}.".format(name='Fred', result=17/23)
```

<https://docs.python.org/3/library/string.html#formatspec>

- Python 3.6 and later, **`f-strings`**, i.e. *formatted string literals*. Can use Python expressions inline.

```
name = "Fred"
result = 17/23
msg = f"Hello {name:s}, the result is {result:0.6g}." # prefix f denotes a formatted string
```

[https://docs.python.org/3/reference/lexical\\_analysis.html#formatted-string-literals](https://docs.python.org/3/reference/lexical_analysis.html#formatted-string-literals)

- Examples in plain English: <https://pyformat.info/>

# Containers

## Slicing (indexing operation)

- Like MATLAB, Python supports *slicing*:

```
s = 'category'
s[:3]          # ⇒ 'cat'
```

- Full syntax: *start:stop:step*
  - **CAUTION:** First *stop*, then *step*, unlike MATLAB!
  - Slicing only allowed in indexing expressions
    - See `np.r_` if you absolutely must `0:101:10` in MATLAB style, but prefer `np.linspace(0,100,11)` for that.
  - All parts optional; *start* is inclusive; *stop* is one-past-end; default step is `+1`
  - For step `> 0`, default start is `0`, default end end-of-string
  - For step `< 0`, default start is `-1`, default end start-of-string
- Examples:

```
s[4:6]  # elements 4, 5 (counting from 0!)
s[1:]   # all elements, starting from element 1 (the second one)
s[:-1]  # all elements except the last one
s[1::2] # starting from element 1, every other element
```

# Containers

## Tuple (immutable list) vs. list

- **Lists** are *mutable*, i.e. elements may be added or removed:

```
letters = ['a', 'b', 'c']  
letters.append('d')      # add a new single element to the end  
letters.extend(['e', 'f']) # concatenate another list to this one, modify in-place  
print(len(letters))      # how many letters now?
```

- **Tuples** are *immutable*, i.e. once the tuple is created, elements cannot be added or removed. Useful because:
  - Immutable objects are often *hashable*, i.e. can be used as dictionary keys and be included into (mathematical) sets.
  - Language-enforced *guarantee* that there will be no modifications.

```
letters = ('a', 'b', 'c') # parentheses denote a tuple  
just_one = ('a',)        # one-element tuple (must use a trailing comma  
                          # to distinguish from parenthesized expression)  
the_empty_tuple = ()     # the empty tuple is a singleton (i.e. there is only one)
```

- However, keep in mind that the container type says nothing of whether each element itself is mutable or immutable.

# Containers

## zip (interleaving iterables)

- Useful for obtaining the corresponding elements from two iterables (e.g. lists or tuples) of the same length. Example:

```
T1 = (1, 2, 3)
```

```
T2 = ('a', 'b', 'c')
```

```
print(tuple(zip(T1,T2))) # ⇒ ((1, 'a'), (2, 'b'), (3, 'c'))
```

- Technical detail: we need the final tuple() because Python 3 treats some sequences lazily; often that is very useful. (The zipped sequence is generated on-demand rather than all-at-once; tuple() forces the generator.)
- Zipping is often used in loops:

```
for a,b in zip(T1,T2):
```

```
    print("Our values are %s and %s" % (a, b))
```

- Note the use of two counter variables, which step in sync; Python *unpacks* each element of the sequence given on the right-hand side of **in**.
- Mnemonic: think of a zipper, the physical object.

# Containers

## Tuple unpacking

- Regarding the loop with `zip()`, we mentioned *tuple unpacking*. Examples:

```
a,b,c = (0,1,2)           # ⇒ a = 0, b = 1, c = 2
a,b,*others = range(5)    # ⇒ a = 0, b = 1, others = [2, 3, 4]
*rest,last = range(5)     # ⇒ rest = [0, 1, 2, 3], last = 4
```

- The operation *de-structures* the tuple (or any sequence) on the right-hand side, and *binds* parts of it to names on the left-hand side. Hence *destructuring bind*.
- The star means “the rest”. In an assignment, there can be only one star, and up to Python 3.4, only on the LHS. Python 3.5+ allows some uses of a star on the RHS:

```
T1 = range(5)
T2 = [100, *T1, 200]  # ⇒ T2 = [100, 0, 1, 2, 3, 4, 200]
```

<https://www.python.org/dev/peps/pep-0448/> (Additional unpacking generalizations)

- <https://stackoverflow.com/questions/2238355/what-is-the-pythonic-way-to-unpack-tuples>  
<https://stackoverflow.com/questions/2921847/what-does-the-star-operator-mean>
- <https://www.python.org/dev/peps/pep-3132/> (tuple unpacking in Python 3.0+)
- See also lecture material, p. 36.

# Containers

## Unordered containers, **set**

- A Python **set** represents a mathematical set: an *unordered collection of unique elements*. Elements must be *hashable*, which implies immutable. Elements can have any type, and can be heterogeneous.

```
S = {'a', 'b', 'c', 'd'}  
S.add('e') # add an element to the set; if duplicate, discarded automatically  
S.remove('a')
```

```
empty_set = set() # no “the”, mutable. Syntax {} means empty dict instead (historical reasons).
```

- Other interesting methods: intersection, union, difference
- Searching a collection for an item, pythonic way. Use the **in** operator:

```
if 'b' in S: # for the opposite, use “not in”: if 'b' not in S:  
    print("Yes, 'b' is in S")  
else:  
    print("No, 'b' is not in S")
```

- **Sets** themselves are mutable, **frozensets** immutable (useful as dict keys).

```
F1 = frozenset(('a', 'b', 'c', 'd')) # make tuple, convert to frozenset  
F2 = frozenset(S) # convert a set to frozenset
```

- Note double parentheses for F1; the frozenset constructor wants just one iterable.



# Containers

## Unordered containers, **dict**

- A **dict** (*dictionary*, a.k.a. *associative array*, *map* (data structure)) is an *unordered collection of key-value pairs*. Keys must be *hashable*, which implies *immutable*. No restrictions on values. Keys and values can have any type, and can be heterogeneous.
- Dictionaries are a highly useful as small ad hoc data structures, since the keys can be human-readable strings.
- To read or write a **dict**, index it with the desired key.

```
D = {'a': 1, 'b': 2, 'c': 3}
```

```
D['a'] # ⇒ 1
```

```
D['d'] = 4
```

```
if 'b' in D: # search the keys for 'b'
```

```
    print("Yes, 'b' is in D, the corresponding value is %s" % (D['b']))
```

```
else:
```

```
    print("No, 'b' is not in D")
```

```
empty_dict = {} # no "the", because dict (just like set) is mutable.
```

# Containers

## Unordered containers, **dict**

- How to iterate over a **dict**:

```
for k in D:           # iterating over the dict itself iterates over the keys
    print(k, D[k])
```

```
for k in D.keys():    # same; old way, still sometimes seen in the wild
    print(k, D[k])
```

```
for v in D.values():  # values only, no access to corresponding keys
    print(v)           # because dict is one-way
```

```
for k,v in D.items(): # useful when you need both keys and values
    print(k, v)
```

- Read from a **dict**, with a default value if the key is not there:

```
D.get('some_nonexistent_key', 42)
```

(Indexing the dict with a nonexistent key instead raises **KeyError**.)

# Containers

## Unordered containers, **dict**

- Some final points on **dict**:
  - Keys are (operationally) a set, i.e. an *unordered* collection.
  - To display a sorted list of keys (e.g. for debugging), use

```
print(sorted(D.keys()))
```

**Sorted** is a built-in function in Python, which takes an iterable and returns a sorted copy. See also **reversed**.

- To update a dict using the contents of another, use `.update`:

```
D = {'a': 1, 'b': 2, 'c': 3}
E = {'d': 4, 'e': 5, 'f': 6, 'a': 100}
D.update(E)    # insert/overwrite into D, using data from E
```

Any new keys will be added, and existing keys will overwrite.

- If, at some point, you happen to need a dictionary that remembers the order the items were inserted into it, see the standard library module **collections**, and there **OrderedDict**.

# Containers

## List comprehension

- *List comprehension* is a syntax for building new sequences from existing sequences by filtering and mapping. In Python:

$B = [f(x) \text{ for } x \text{ in } A \text{ if } g(x)]$

says that:

- **for**  $x$  **in**  $A$ : Consider the elements  $x$  of the sequence  $A$ , in order.
  - **[filter step]** Accept those elements for which  $g(x)$  is truthy.
  - **[map step]** Pass each accepted  $x$  to the function  $f$ , and record its result.
  - Build the output sequence from these results.
  - Bind the output sequence to the name  $B$ .
- The notation used in Python borrows ideas from set-builder notation and the axiom schema of comprehension, from set theory in mathematics.  
[https://en.wikipedia.org/wiki/Set-builder\\_notation](https://en.wikipedia.org/wiki/Set-builder_notation)  
[https://en.wikipedia.org/wiki/Axiom\\_schema\\_of\\_specification#Unrestricted\\_comprehension](https://en.wikipedia.org/wiki/Axiom_schema_of_specification#Unrestricted_comprehension)

# Containers

## List comprehension

- The filter step (**if** ...) is optional. Similarly, the map step may also just pass through its input, as in `[x for x in range(10) if g(x)]`.
- Using round parentheses in place of square brackets makes instead a *generator expression*, which evaluates its output lazily (on-demand).
- Python has also **set comprehension** and **dict comprehension**. The syntax is similar to list comprehension, but with curly braces.

- **Set comprehension:**

```
evens = {x for x in range(10) if x % 2 == 0}  # for numbers, % is “modulo”
```

- **Dict comprehension:**

```
D = {x: x**2 for x in range(100)}  # map  $x \mapsto x^2$  for  $x \in [0, 100)$ 
```

Note the colon in the expression part, separating the key and value. This is the only syntactic difference between a set comprehension and a dict comprehension in Python.

# Functions

## defining; return values

- To define a function, use the keyword **def**:

```
def my_function(x):  
    return x**2
```

- Preferred naming convention is *all\_lowercase\_with\_underscores*. For mathematical functions just *f* or similar is fine.
- No distinction between functions and procedures (contrast Fortran).
  - Any function may (but does not have to) return a value.
  - If no **return** statement, the return value is the special value **None**.
  - The return value is not declared, and is not part of the function signature. Just “**return** some\_expr” if you want to return a value.
    - But if you really like statically typed languages, see:  
<https://www.python.org/dev/peps/pep-0484/> Type hints (3.5+)  
<http://mypy-lang.org/> Mypy, optional static type checker for Python
- The return value can be any Python object, including containers.
  - Output arguments needed very rarely (contrast Fortran).  
But if needed, can use mutable objects as arguments, for in-place output of e.g. large arrays.
- To return several objects at once, pack them into a container such as tuple:

```
def my_other_function(a, b):  
    return (2*a, 3*b**2)
```

# Functions

## Defining, anywhere

- Functions can be defined anywhere, also inside other functions. Arbitrarily deep nesting is allowed. In this example, we have just two levels for clarity:

```
def f(x):  
    def g(y):  
        return (2*y, 3*y)  
    return g(x)
```

- An inner function is inside the outer function's lexical scope, hence it can access also any names visible in the outer function:

```
def f(x):  
    def g(y):  
        print('a is {0:d}, x is {1:d}, y is {2:d}'.format(a, x, y))  
    a = 23  
    g(y=42) # the argument of g is always y; we're just being explicit
```

- **Note!** “a” does not yet have a value when Python reads the definition of g(y).
  - That's fine, because we are just defining “g” (not running it yet), and the name “a” is visible in the whole body of “f” (the lexical scope in which “a” is created).
- Only attempting to actually use “a” before setting a value will raise **NameError**.

# Functions

## Argument passing: named args

- Function arguments *can be passed by name* as well as by position. (This is one of Python's great strengths for improving readability.)

```
def f(a, b):  
    print('a = {}'.format(a))  
    print('b = {}'.format(b))
```

Here “a” and “b” are named.

```
f(a=2, b=3) # pass both “a” and “b” by name  
f(b=3, a=2) # when using names, ordering does not matter  
f(2, b=3)   # pass first argument by position, “b” by name  
f(2, 3)     # pass both by position
```

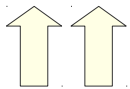
- Tuple unpacking, \*, is allowed in function calls. It passes by position:  
lst = (2, 3)  
f(\*lst) # unpack lst into positional arguments of “f”
- ...as well as is **dictionary unpacking**, \*\*. It passes by name:  
dic = {'a': 2, 'b': 3}  
f(\*\*dic) # keys must be arguments accepted by “f”, by name



# Functions

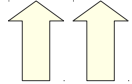
Terminology: *formal parameters, arguments*

```
def f(a, b):
```

... 

**Formal parameters:** placeholder names, to be filled at call time with...

```
f(2, 3)
```



**Arguments:** ...actual values (object instances)

```
x = 5
```

```
f(a=x, b=10)
```

This call to “f” sets the formal parameter “a” to the current value of “x” (*passes in* the object “x” currently points to in the caller's scope), and sets the formal parameter “b” to 10 (by internally creating a temporary object).

```
a = 3
```

```
f(a=a, b=10)
```

This call sets f's “a” to the current value of *the caller's* “a” (and “b” to 10).

# Functions

## Terminology: *shadowing/masking*

# names defined at the module's top-level scope

a = 1

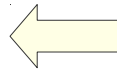
x = 2

**def** f(a, b):

print(a) # 3

print(b) # 5

print(x) # 2



The formal parameter “a” **shadows** (hides) the “a” defined in the top-level scope.

f(3, 5)

- In computer programming, **variable shadowing** occurs when a variable declared within a certain scope (decision block, method, or inner class) has the same name as a variable declared in an outer scope. At the level of identifiers (names, rather than variables), this is known as **name masking**. This outer variable is said to be **shadowed by** the inner variable, while the inner identifier is said to **mask** the outer identifier.

[https://en.wikipedia.org/wiki/Variable\\_shadowing](https://en.wikipedia.org/wiki/Variable_shadowing)

- Recall Python's **LEGB** rule for name lookup (lecture 1, slide 24).

# Functions

## Argument passing: collecting by \*, \*\*

- In the list of formal parameters, \* makes the function accept any number of positional arguments, collecting any extra ones into a list. In the function body, this list is bound to the name immediately following the \*:

```
def f(*args):  
    for x in args:  
        print(x)
```

```
f(2, 3, 5)
```

- Here “extra” means leftovers after positionally passed values have been assigned to all named parameters in the function definition. (Example on next slide.)
  - To keep this short, we will omit discussion of corner cases.
- Similarly, \*\* makes the function accept any named arguments, and collects into a dictionary any that do not match the name of any named parameter in the function definition. In the function body, this dictionary is bound to the name immediately following the \*\*:

```
def f(**kwargs):    # kwargs is a common abbreviation for “keyword arguments”  
    for k,v in kwargs:  
        print('{} → {}'.format(k, v))
```

```
f(a=2, b=3, c=5)
```

# Functions

## Argument passing: example

- The different argument passing styles may be mixed freely:

```
def f(a, b, *args, **kwargs):  
    print('a = {}'.format(a))  
    print('b = {}'.format(b))  
    for x in args:  
        print(x)  
    for k,v in kwargs:  
        print('{} → {}'.format(k, v))  
    if 'foo' in kwargs: # check for given dictionary key  
        print('foo given, its value is {}'.format(kwargs['foo']))
```

```
f(a=2, b=3, c=5) # a and b by name; no formal param c, so c into kwargs  
f(2, 3, c=5)     # first two by position, c into kwargs  
f(2, 3, 5)       # all by position; since f has just two named formal  
                 # parameters, the third positional arg goes into args
```

- The names “args” and “kwargs” are conventional; any name can be used.
  - Sometimes seen instead of “kwargs”: “kwds”, “kws”, “kw”

# Functions

## Argument passing: optional args

- Pythonic way to implement optional arguments:

```
def f(a, b, c=42):  # here c is optional; if not given, default to 42
    print('a = {}'.format(a))
    print('b = {}'.format(b))
    print('c = {}'.format(c))
```

```
f(2, 3)           # use default value for c
```

```
f(2, 3, 5)        # pass in a value also for c, overriding the default
```

```
f(2, 3, c=5)      # clearer style, especially if “f” supports more than one optional arg
```

- Another way, for rarely used optional arguments:

```
def f(a, b, **kwargs):
    c = kwargs['c'] if 'c' in kwargs else 42
    print('a = {}'.format(a))
    print('b = {}'.format(b))
    print('c = {}'.format(c))
```

- This way, rarely used optional args won't clutter the function signature in *help*
- On the other hand, must document manually so that users know what optional arguments exist. (No guarantees on which keys “f” reads from kwargs!)

# Functions

## Argument passing: *keyword-only* args

- Finally, Python 3 allows defining also *keyword-only arguments*:

```
def f(*, a, b):  
    print('a = {}'.format(a))  
    print('b = {}'.format(b))
```

- A lone star in the formal parameter list means that all the parameters that follow it *can be passed by name **only***:

```
f(a=2, b=3) # pass both "a" and "b" by name  
f(2, 3)     # TypeError, "f" takes no positional arguments
```

- Useful to improve readability, to protect against passing arguments by position for functions for which it could be confusing (e.g. if the arguments naturally form a set, instead of an ordered sequence).
- <https://www.python.org/dev/peps/pep-3102/> Keyword-only arguments (3.0+)

# Functions

## Argument default values

- To set default values for optional arguments, use the assignment notation (like in C++):

```
def f(a=42):
```

```
    ...
```

- If the exact value of the default is an implementation detail, use **None** to signify “not given”, and set the actual value inside the function body:

```
def f(a=None):
```

```
    a = a or 42
```

```
    ...
```

(Otherwise someone will eventually pass in 42 just to explicitly signify “yes, I thought about it, and I want to use the default here”).)

- This follows the programming principle of *information hiding*:
  - Protects the user from unimportant internal details.
  - Call sites do not need changes even if those details change later.

# Functions

## Documenting

- **Docstrings** (*documentation strings*) are where all the *help* comes from.
- In Python, it is just the first expression in a function body, if that first expression is a string:

```
def rectangle_area(a, b):  
    """Compute the area of a rectangle.
```

Parameters:

a: number  
    The width.  
b: number  
    The height.

Returns:

Number:  
    The area.  
**return** a\*b

- Note indentation. The start-quote is indented, but the following lines (inside the docstring) do not have to be. The three-double-quotes syntax is very useful here.
- Spyder's Help window supports pretty-rendering the format used here.
- Docstrings are easy to make. Highly useful when you return to your old code later.



# Functions

as first-class objects – as arguments

- In Python, functions are *first-class objects*. They can be:
  - passed in as arguments to other functions  
⇒ *higher-order functions*
  - returned from functions
  - saved to variables (names), stored in containers, ...

```
def f(a):  
    return a**2
```

```
def do_stuff(op, lst): # “op” short for “operation”  
    result = []  
    for x in lst:  
        result.append(op(x))  
    return result
```

This is an executable  
pseudocode sketch of the  
higher-order function  
commonly known as **map**.

(Try it, it works.)

It has nothing to do  
with the data structure  
also called **map**  
(dict, associative array).

```
L = range(10)  
K = do_stuff(op=f, lst=L)
```

(Except that both are instances of  
the mathematical idea of mapping.)

# Functions

## as first-class objects – as return values

- The *function factory* is a design pattern where we return a function instance. It can be used to parameterize operations that have a common template, such as:

```
def make_adder(inc):  
    def adder(x):  
        return x + inc  
    return adder
```

```
f = make_adder(inc=3)  # create function from template, bind to name "f"  
print(f(2))           # 5
```

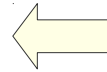
- This particular use of a function factory utilizes *lexical closures*.
  - Roughly, a *closure* is a function together with an *environment* that contains the values for its *free variables*. *Lexical* due to lexical scoping.
  - We will return to this in week 9, on functional programming.
  - [https://en.wikipedia.org/wiki/Closure\\_\(computer\\_programming\)](https://en.wikipedia.org/wiki/Closure_(computer_programming))
- In short, in each adder instance created here, “inc” is bound to the object the caller gave when calling make\_adder to create that particular instance – the created function instance “remembers” the value (object reference, to be exact).

# Functions

## as first-class objects – **lambda**

- Python supports creating short *anonymous functions*, using the keyword **lambda**. These are useful as throwaways for one-off tasks, saving the verbosity of a **def**:

```
lst = range(10)
result = tuple(map(lambda x: x**2, lst))
print(result)
```



Python provides **map**  
(the higher-order  
function) as a built-in.

...but for this particular application, prefer a list comprehension (more readable).

- The body must consist of a single expression only. No statements allowed.
  - Ways around: use a tuple as a container, and index to select the return value. Abuse the short-circuiting logical operators to conditionally sequence tasks.
    - But this is seriously frowned upon, for good reason: such approaches significantly harm readability.
  - Generally, the Python community prefers using **def** almost everywhere.
- Beware: since **lambda** is a keyword, “lambda” is not available as a variable name.
  - Many numerical Python programmers use “lamda” or “lam”. Can also use “λ” (U+3bb, GREEK SMALL LETTER LAMDA), but perhaps not recommended.  
[ftp://ftp.unicode.org/Public/UNIDATA/UnicodeData.txt](http://ftp.unicode.org/Public/UNIDATA/UnicodeData.txt)
- Python's **map** returns a lazy sequence, hence we call tuple() to force the result.
- Python's **lambda** x: ... is like MATLAB's @(x) ...

# Spyder IDE

## Getting started

- To start: *All programs* ▸ *Anaconda* ▸ *Spyder*
- May be named “Spyder3” for the Python 3 version

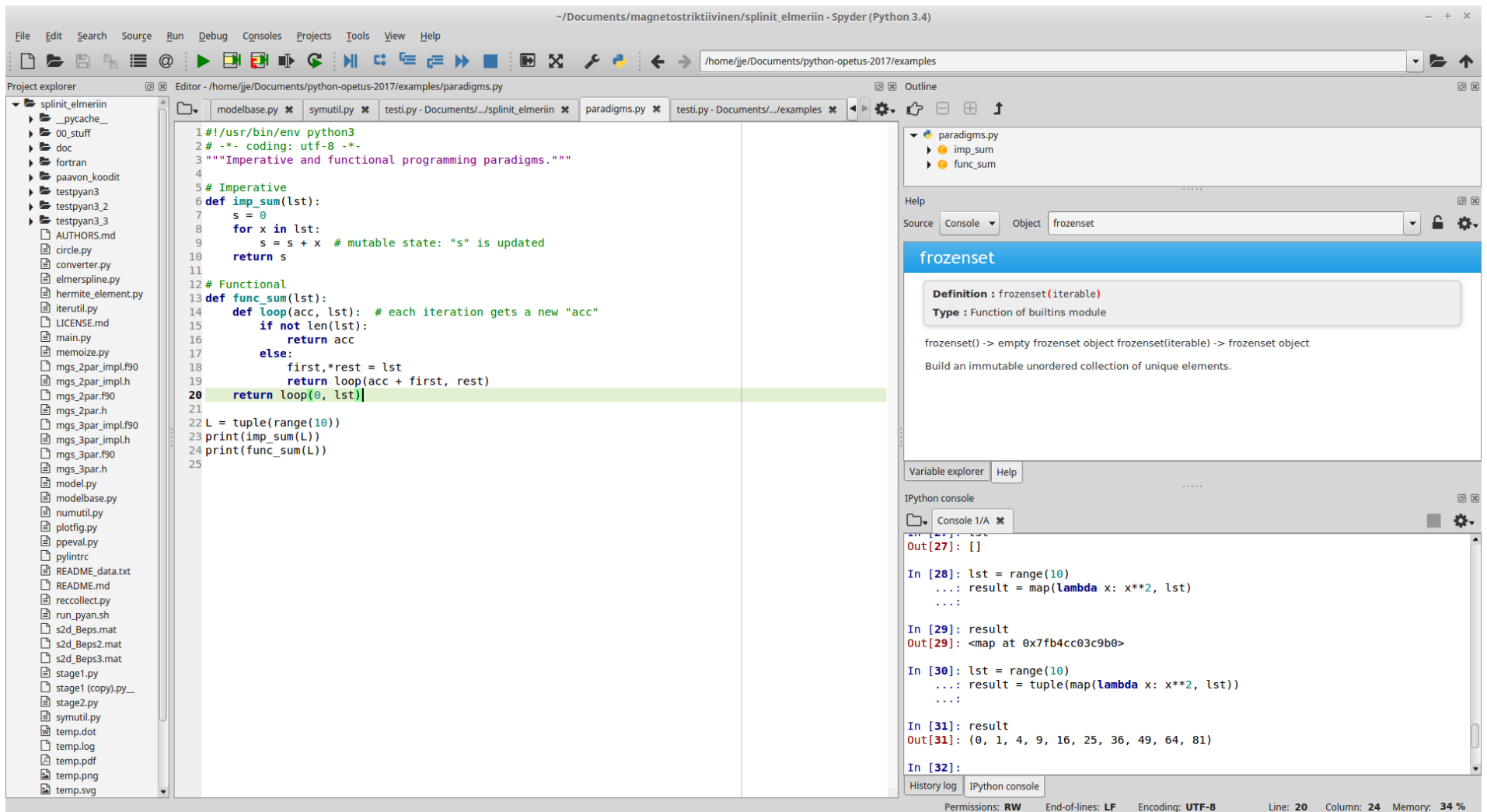


(If this appears, things are going well.)

# Spyder IDE

## GUI layout

- Once loading completes, Spyder looks approximately like this:



# Spyder IDE

## GUI layout

Run menu and button “▶”

Can also run by pressing F5.

The screenshot shows the Spyder IDE interface with several components highlighted by colored boxes and text annotations:

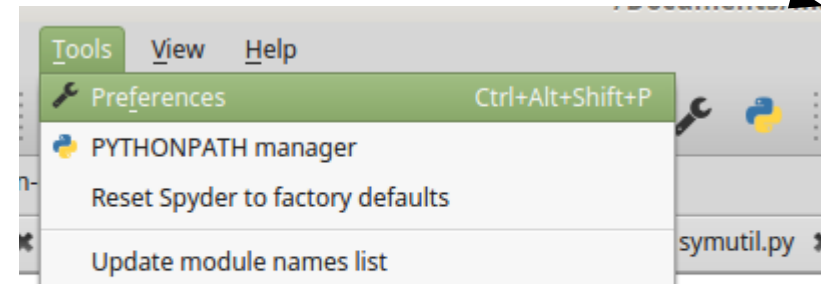
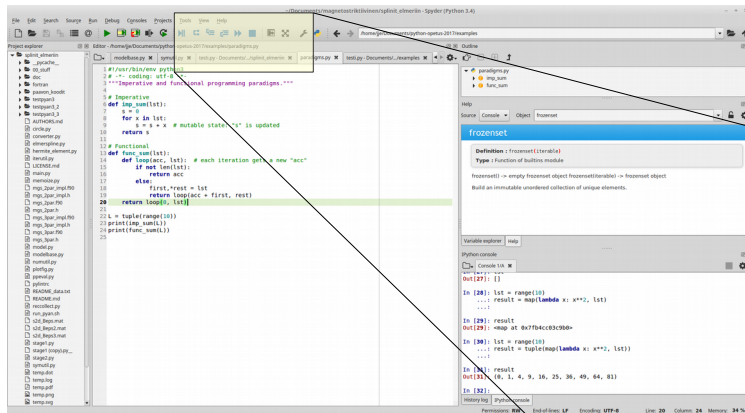
- Project explorer:** A blue box on the left highlights the 'Project explorer' panel, which shows a tree view of the project files. An annotation 'Files in your project folder' points to this panel. Below it, another annotation 'See the Projects menu' points to the 'Projects' menu item in the top toolbar.
- Code editor:** A large central area with a light yellow background contains the code editor. It displays a Python script named 'paradigms.py'. An annotation 'Code editor' points to this area. Below the editor, a list of features is provided:
  - The file currently active in the editor runs when you Run
  - For autocompletion, start typing and press Ctrl+Space
- Outline:** A panel on the right side shows the 'Outline' of the currently active file, listing the functions 'imp\_sum' and 'func\_sum'. An annotation 'Outline of the currently active file, for quick code navigation' points to this panel.
- Help, Variable explorer, et al.:** A panel on the right side shows the 'Help' section for the 'frozenset' object, including its definition and type. An annotation 'Help, Variable explorer, et al.' points to this panel.
- REPL (IPython):** A panel at the bottom right shows the IPython console with a series of commands and their outputs. An annotation 'REPL (IPython) For interactive work.' points to this panel.

The top toolbar contains various icons for file operations, editing, and running code. The 'Run' button (a green play icon) is specifically highlighted with a green circle and an arrow pointing to the 'Run menu and button “▶”' annotation.

# Spyder IDE

## Configuring

- For settings, see *Tools* ▸ *Preferences*:

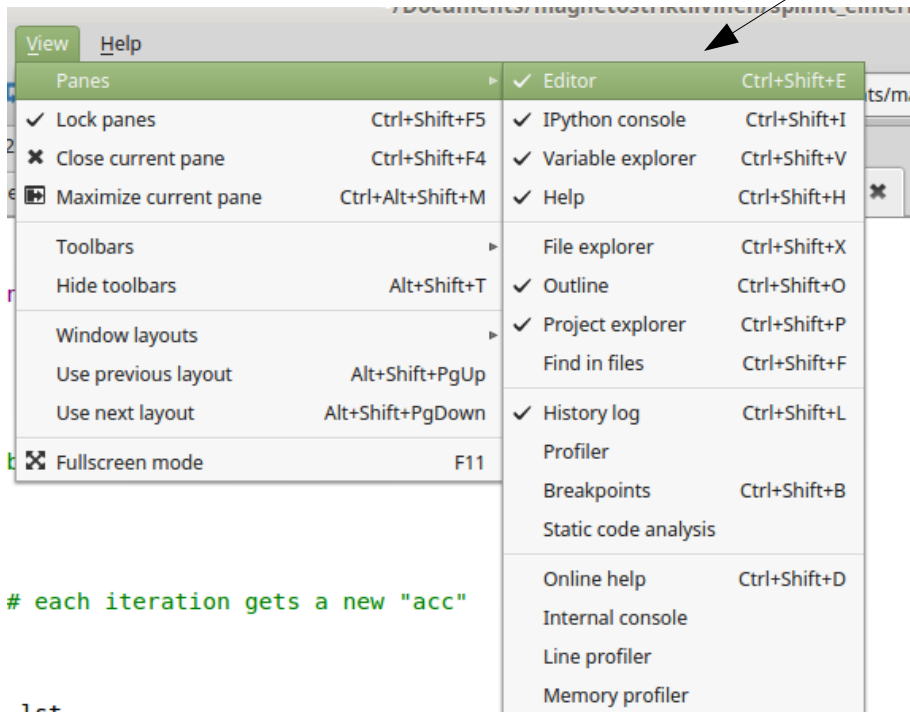


- One particularly useful option is whether figures open inline or in their own windows:  
*Tools* ▸ *Preferences* ▸ *IPython console* ▸ *Graphics* ▸ *Backend*
- Color setup for syntax highlighting:  
*Tools* ▸ *Preferences* ▸ *Syntax coloring* ▸ *Scheme*

# Spyder IDE

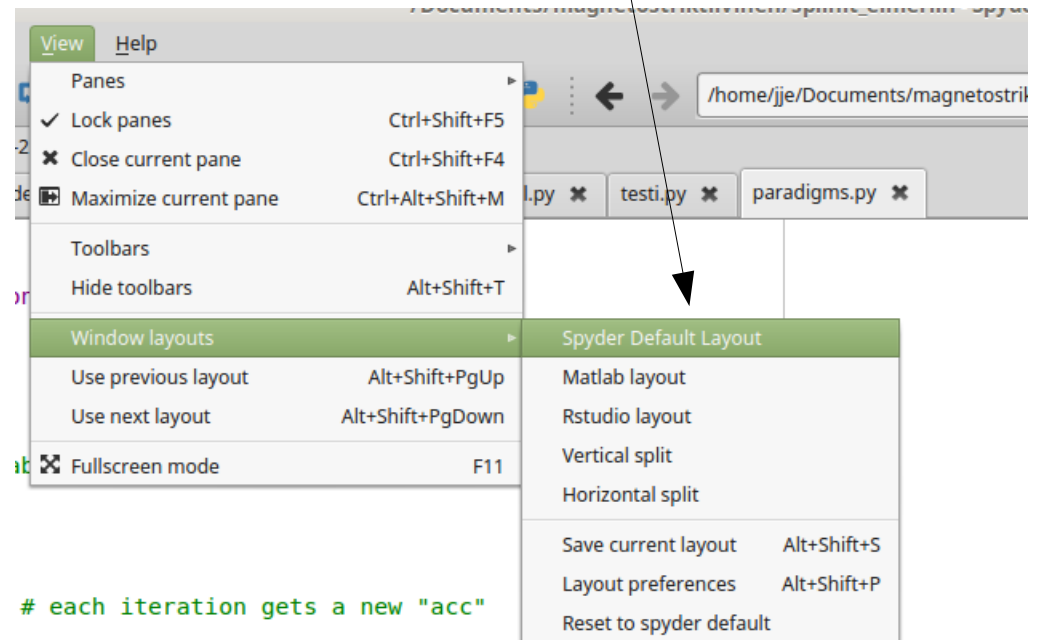
## Customizing the layout

- If you want to change the layout, see **View ▷ Panes** and **View ▷ Window layouts**



# each iteration gets a new "acc"

```
lst  
cc + first, rest)
```



# each iteration gets a new "acc"



*To be continued...*

`print('See you next week!')`

U+28, LEFT PARENTHESIS

