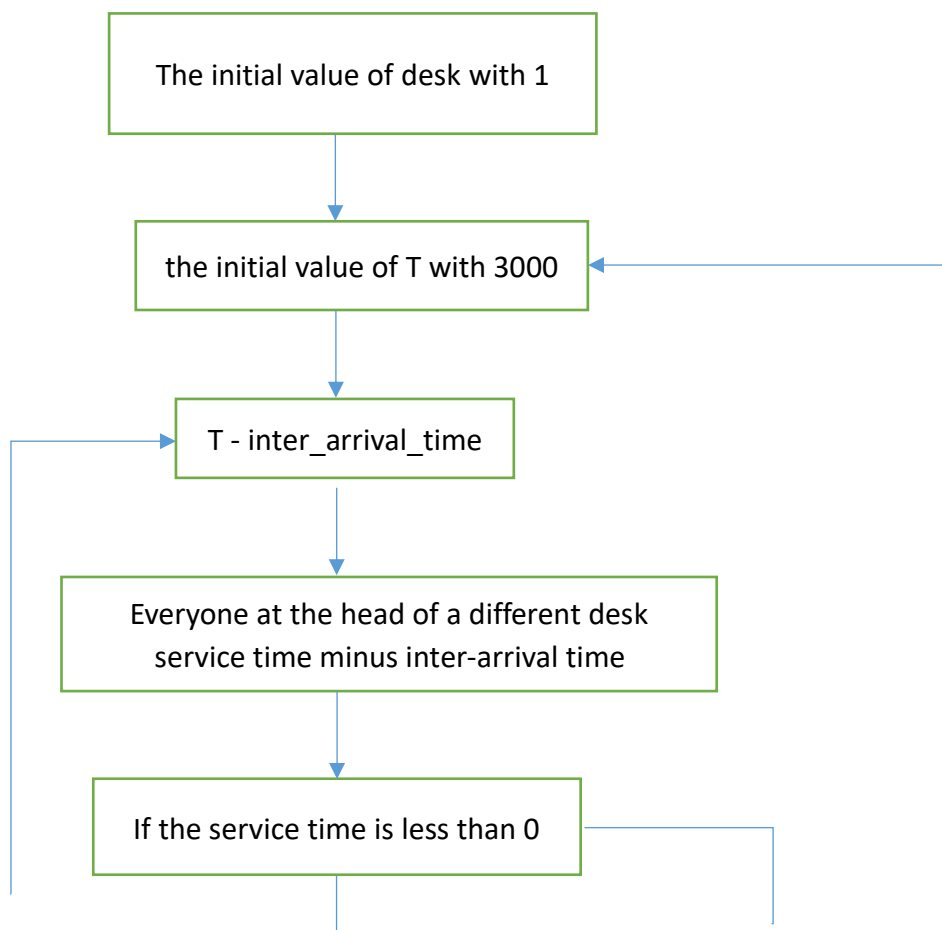
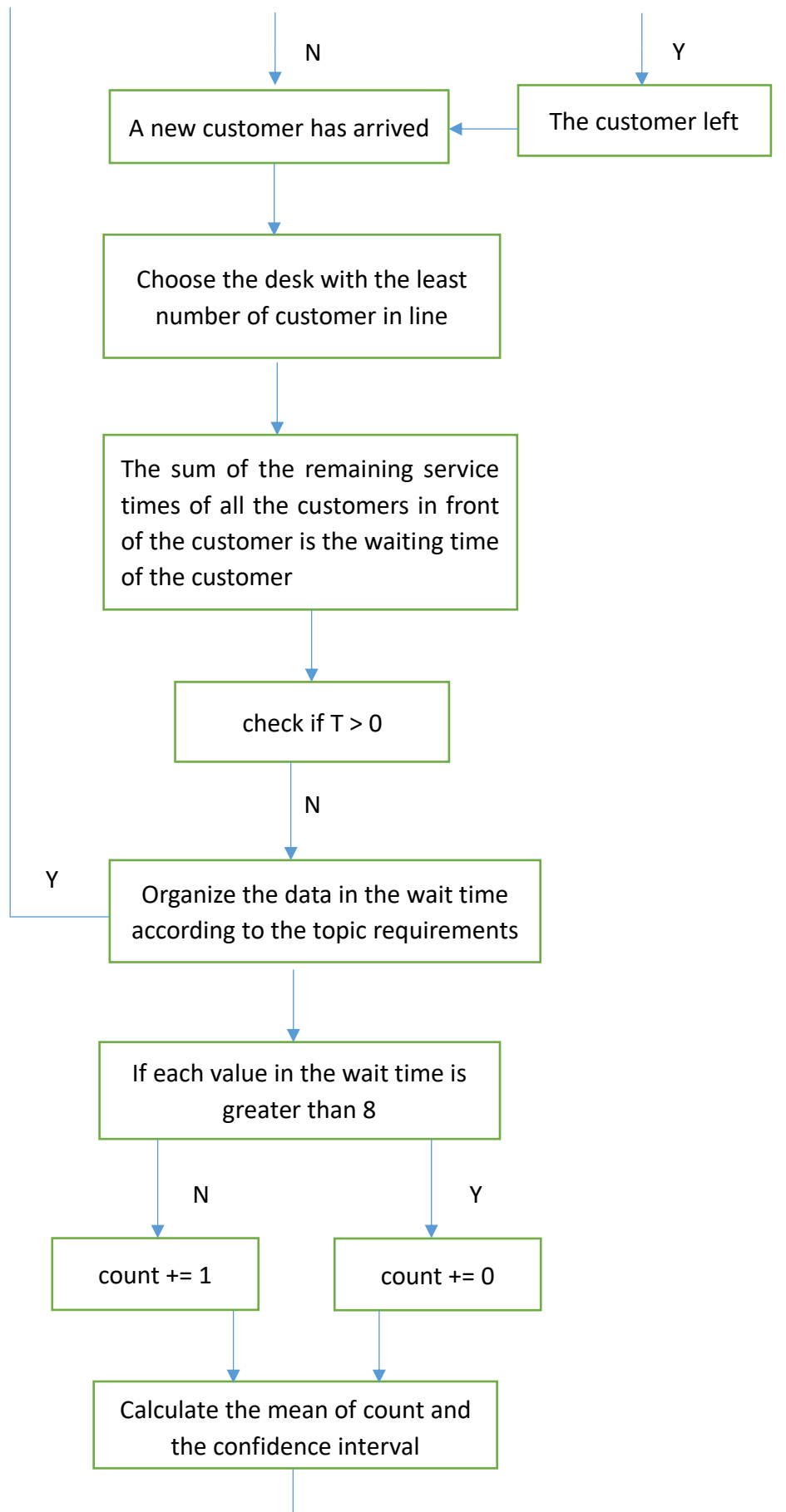


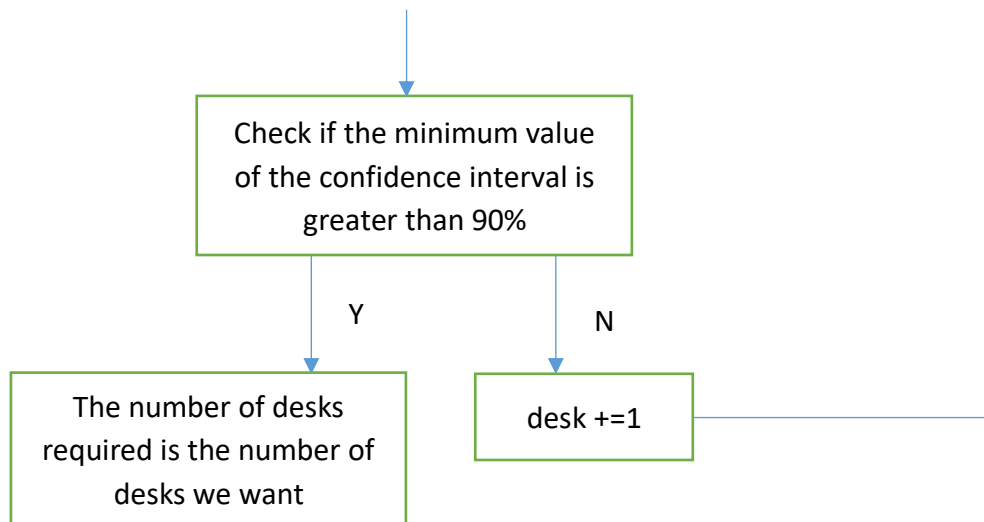
(a)

The meaning of the question is: When we were asked to figure out how many desks there were, less than 10% of us kept customers waiting for more than eight minutes. Each customer has two data, one is "inter-arrival time", which means the time interval with the previous customer's arrival; The other is "service time", which means the amount of time the customer spends at the desk. Customers will choose to wait at the desk with the least number of people in line. The customer's waiting time is the time required after the customer inter-arrival time and before the service time. The data in the waiting time is sorted out according to the topic requirements, and then the proportion of customer waiting time less than 8 minutes is calculated, and the confidence interval is calculated. When the minimum value of the confidence interval is greater than 90%, the number of desks required is the number of desks we want.

(b)



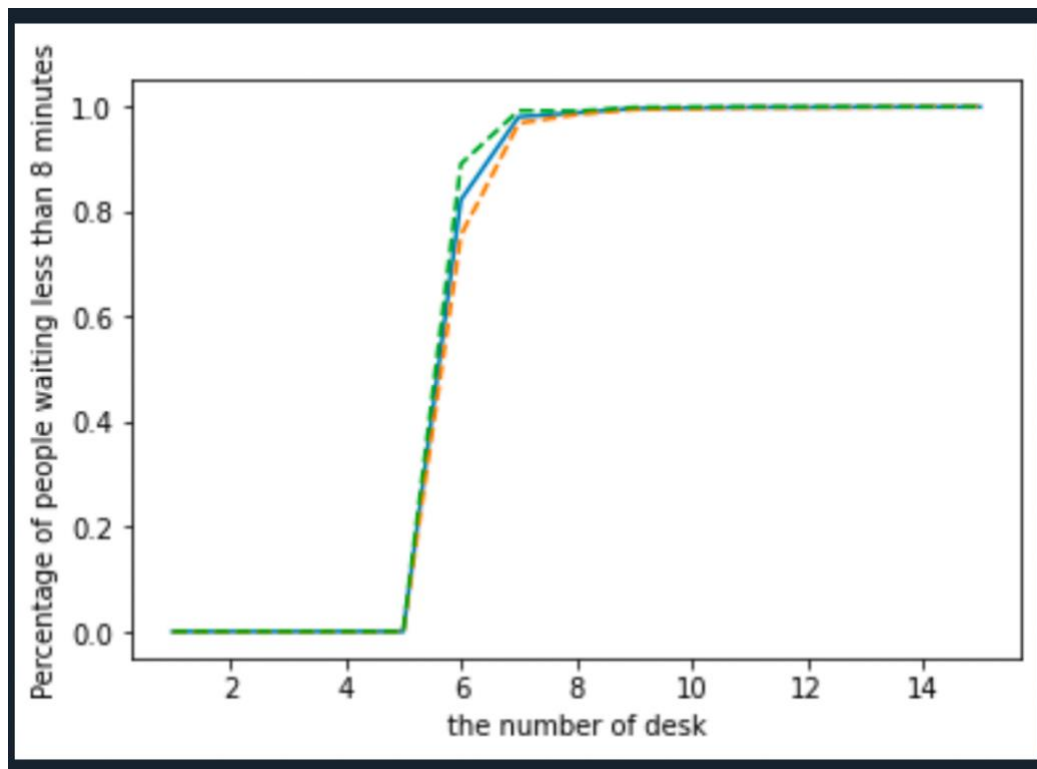




Below is the parameter I need and what it means.

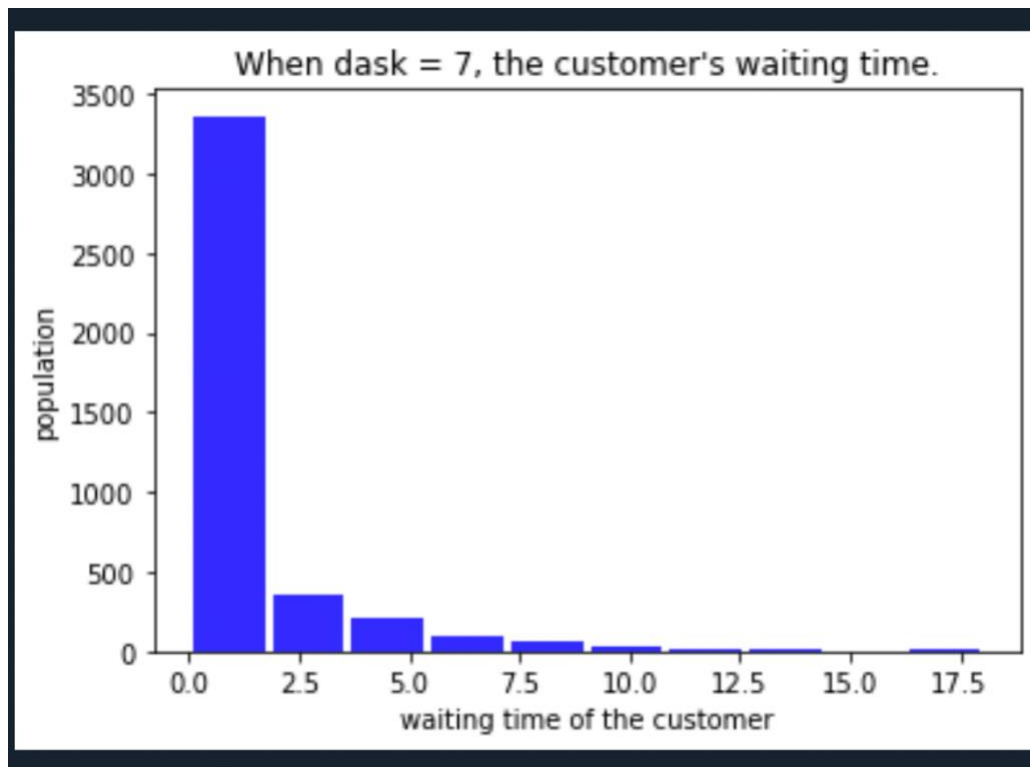
Parameter	Type	Mean
N	int	In the known that using N = 50 batches to estimate the probability
min_desk	int	The minimum number of desks that satisfy the topic condition, and the initial value with -1
wait	list	As many desks as there are, store as many sub-lists in this list. Each sub-list stores the waiting time for each customer with a corresponding number of desks.
result	list	There are three sub-lists in this list. The first sub-list stores the percentage of the number of customers meeting the conditions of the question under a different number of desks. The second sub-list stores the minimum value of the confidence interval for this percentage for a different number of desks; The third sub-list stores the maximum value of the confidence interval of this percentage for the number of desks.
desks	list	There are as many sub-lists as there are desks, and each sub-list stores the service time of the customer of the corresponding desk.
count	list	Under the current number of tables, "0" is stored if the customer has waited more than 8 minutes, and "1" is stored if the customer has waited less than 8 minutes.
count_N	list	Estimated probability of 'count' based on using N = 50 batches.
T	int	In the known that T = 3000 units of time.

(c)



Desk	Probability	95%CI
1	0.0%	(0.0%, 0.0%)
2	0.0%	(0.0%, 0.0%)
3	0.0%	(0.0%, 0.0%)
4	0.0%	(0.0%, 0.0%)
5	0.0%	(0.0%, 0.0%)
6	82.314%	(75.482%, 89.147%)
7	98.075%	(96.867%, 99.284%)
8	98.860%	(98.535%, 99.185%)
9	99.679%	(99.470%, 99.887)
10	99.795%	(99.632%, 100.0%)
11	99.926%	(99.845%, 100.0%)
12	99.923%	(99.838%, 100.0%)
13	99.967%	(99.905%, 100.0%)
14	100.0%	(100.0%, 100.0%)
15	100.0%	(100.0%, 100.0%)

As can be seen from the graph, when the number of desks is no more than 5, the waiting time of customers is more than 8 minutes. But when the number of desks exceeded 5, the proportion of customers waiting less than 8 minutes increased significantly. When the number of desks is more than 8, most customers wait less than 8 minutes.



Waitin g time	(0.0~ 1.8)	(1.8~ 3.6)	(3.6~ 5.4)	(5.4~ 7.2)	(7.2~ 9.0)	(9.0~ 10.8)	(10.8~ 12.6)	(12.6~ 14.4)	(14.4~ 16.2)	(16. 2~)
Propo rtion of the popul ation	81.1 65%	8.65 6%	4.86 0%	2.44 2%	1.49 9%	0.629 %	0.266 %	0.290 %	0.048 %	0.14 5%

As can be seen from the above figure, when the number of desks is 7, the waiting time of most customers is less than 3.6 minutes, and few customers who wait more than 8 minutes are left behind.

The minimum number of desks is 7.  
The mean of the percentage that meets the requirement = 0.9807592988264636  
The CI of the percentage that meets the requirement = ( 0.9686747876163044 , 0.9928438100366228 )

(d)

From the above analysis, we calculate that when desk=7, is the minimum number of desks that meet the topic condition. We calculate that when desk is 7, the mean of customer waiting time is 0.9898m, and its confidence interval is (0.9241m, 1.0554m).

```
the mean of customer waiting time = 0.9898329074899873
the CI of customer waiting time = ( 0.9241743610864085 , 1.055491453893566 )
```

(e)

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
```

```
df = pd.read_csv('data.csv')
```

```
np.random.seed(len(df))
```

```
N = 50
```

```
min_desk = -1
```

```
wait = []
```

```
result = [[],[],[]]
```

```
for desk in range(1, 16):
```

```
    desks = []
```

```
    count = []
```

```
    count_N = []
```

```
    T = 3000
```

```
    wait.append([])
```

```
    for i in range(desk):
```

```
        desks.append([])
```

```
    while T >= 0:
```

```
        row = np.random.randint(len(df))
```

```
        T -= df.loc[row].values[0]
```

#Check whether the remaining service time of the first customer on each desk is negative. If so, delete his time and add the negative time to the service time of the next customer.

```
    for i in range(desk):
```

```
        if desks[i]:
```

```
            desks[i][0] -= df.loc[row].values[0]
```

```
            while desks[i][0] <= 0:
```

```
                if desks[i][1:]:
```

```
                    desks[i][1] += desks[i][0]
```

```

        desks[i] = desks[i][1:]
    elif not desks[i][1:]:
        desks[i] = desks[i][1:]
        break

    #Find the desk with the smallest queue.
    #To be clear, I'm not looking for No. of desk with the smallest queue here,
    but I'm setting No. of desk with the smallest queue to be 0.
    for i in range(len(desks)):
        least = i
        for k in range(i + 1, len(desks)):
            if len(desks[k]) < len(desks[least]):
                least = k
        desks[least], desks[i] = desks[i], desks[least]

    #Obtain the wait time of the customer
    desks[0].append(df.loc[row].values[1])
    wait[desk - 1].append(sum(desks[0][:-1]))

#Discard the first 30% of the samples
index = (len(wait[desk - 1]) * 3) // 10
wait[desk - 1] = wait[desk - 1][index:]

#Gets the number of customers whose wait time is less than 8 minutes
for i in range(len(wait[desk - 1])):
    if wait[desk - 1][i] > 8:
        count.append(0)
    elif wait[desk - 1][i] <= 8:
        count.append(1)

#Using N = 50 batches to estimate the probability
for i in range(N):

count_N.append(np.mean(count[(0+i*len(count)//50):(len(count)//50)*(i+1)]))

#The percentage of the number of customers meeting the conditions
result[0].append(np.mean(count_N))

#The minimum value of the confidence interval for this percentage
result[1].append(np.mean(count_N) - 1.96 * np.std(count_N) / len(count_N) **
0.5)

```

```

#The maximum value of the confidence interval of this percentage
result[2].append(np.mean(count_N) + 1.96 * np.std(count_N) / len(count_N) **
0.5)

```

```

#Find out the minimum number of desks that meet the topic condition

```

```

if min_desk == -1:
    if result[1][desk-1] > 0.9:
        min_desk = desk

```

```

print('The minimum number of desks is {}'.format(min_desk))
print('The mean of the percentage that meets the requirement = ',result[0][min_desk - 1])
print('The CI of the percentage that meets the requirement = (' ,result[1][min_desk - 1], ' ',result[2][min_desk - 1],')')

```

```

plt.plot(range(1,16), result[0])
plt.plot(range(1,16), result[1], linestyle='--')
plt.plot(range(1,16), result[2], linestyle='--')
plt.xlabel('the number of desk')
plt.ylabel('Percentage of people waiting less than 8 minutes')
plt.show()

```

```

fig = plt.figure()
ax = fig.add_subplot(111)
ax.hist(wait[min_desk-1],color='blue',alpha=0.8,rwidth=0.9)
plt.xlabel('waiting time of the customer')
plt.ylabel('population')
plt.title(u"When dask = 7, the customer's waiting time.")
plt.show()

```

```

print('the mean of customer waiting time = ',np.mean(wait[min_desk-1]))
print('the CI of customer waiting time = (' ,np.mean(wait[min_desk-1])-
1.96*np.std(wait[min_desk-1])/len(wait[min_desk-1])**0.5,
',',np.mean(wait[min_desk-1])+1.96*np.std(wait[min_desk-1])/len(wait[min_desk-
1])**0.5,')')

```