## Multilevel Urban Tree Allometric equations

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## **Model Comparisons**

Short descriptions of the models tested and the brms sytax are in table ??

Note, I removed the scaling of the parameters (multiplying and dividing by 100) in the formula for clarity. In the code they are scaled so that the parameters are on the same order of magnitude and HMC sampling is improved.

Model	Description	brms formula syntax
1	No varying parameters	$DBH \sim b0 + b1 * (1 - exp(-b2 * AGE^{b3}))$
		$b0 \sim 1$
		$b1 \sim 1$
		$b2 \sim 1$
		$b3 \sim 1$
2	Parameters vary by city	DBH $\sim$ b0 + b1 * (1 - exp(-b2 * AGE <sup>b3</sup> ))
		$b0 \sim (1 \mid City)$
		$b1 \sim (1 \mid City)$
		$b2 \sim (1 \mid City)$
		$b3 \sim (1 \mid City)$
3	Parameters vary by genus and species	DBH $\sim b0 + b1 * (1 - exp(-b2 * AGE^{b3}))$
	Species is nested in genus	b0 $\sim$ (1   Genus / Species)
		b1 $\sim$ (1   Genus / Species)
		b2 $\sim$ (1   Genus / Species)
		b3 $\sim$ (1   Genus / Species)
4	Asymptote $(\beta_1)$ varies by climate	DBH $\sim$ b0 + b1 * (1 - exp(-b2 * AGE <sup>b3</sup> ))
		$b0 \sim 1$
		b 1 $\sim$ gdd * precip
		$b2 \sim 1$
		$b3 \sim 1$
5	Growth rate $(\beta_3)$ varies by climate	DBH $\sim$ b0 + b1 * (1 - exp(-b2 * AGE $^{b3}))$
		$b0 \sim 1$
		$b1 \sim 1$
		$b2 \sim 1$
		b 3 $\sim$ gdd * precip
6	Parameters vary by city, genus, and species.	DBH $\sim$ b0 + b1 * (1 - exp(-b2 * AGE $^{b3}))$
	Growth rate varies by climate.	b0 $\sim$ (1   City) + (1   Genus/Species)
		b1 $\sim$ (1   City) + (1   Genus/Species)
		b2 $\sim$ (1   City) + (1   Genus/Species)
		b3 ~ precip * gdd + (1   City) + (1   Genus/Species)
7	Parameters vary by city, genus, and species	DBH $\sim$ b0 + b1 * (1 - exp(-b2 * AGE $^{b3}))$
	(but asympote does not vary by city).	b0 $\sim$ (1   City) + (1   Genus/Species)
	Growth rate varies by climate.	b1 $\sim$ (1   Genus/Species)
		b2 $\sim$ (1   City) + (1   Genus/Species)
		b3 $\sim$ precip * gdd + (1   City) + (1   Genus/Species)

Table 1: elpd loo = expected log pointwise predictive density Model elpd diff  $elpd_{\mathrm{loo}}$ elpd loo se elpd loo -18845.41 Best 0.00 -18845.41 95.85 6 -18976.38 -18976.38 93.66 -130.973 -18989.24 -143.83-18989.2494.112 -19764.48 -919.06 88.69 -19764.48-20180.41 -1334.99 -20180.41 82.75-20195.21 -1349.80-20195.21 82.60 Worst 1 -20513.12 -1667.70 -20513.12 81.57