

Week 6:

1a) Bubble sort:

$n \leftarrow \text{array.length}$

do

swapped  $\leftarrow$  false

for  $i \leftarrow 1$  to  $n-1$  (inclusive)

if array[i-1] ~~>~~ array[i] then array[i] then:

temp = array[i-1]

array[i-1] = array[i]

array[i] = temp

swapped  $\leftarrow$  true

endif

endfor  $n = n-1$

while (swapped == false).

b) Best case is when they are array is sorted, meaning there are  $n$  comparisons:  $\Theta(n)$ .

Worst case is when array is not sorted and so, there are  $n$  comparison for  $n$  possible positions, hence  $O(n^2)$ .

Average case is if half the elements need to be swapped, so;  $O\left(\frac{n(n-1)}{2} \cdot \frac{1}{2}\right) = O(n^2)$



c) Insertion sort is stable, as elements are in order & will not be swapped.

Bubble sort is

Stable because if they are ordered, they will not be swapped.

Heap sort is unstable as even if elements <sup>are</sup> in order, they might be swapped.

Merge sort is stable when we use  $Left \leq Right$ .

d) Insertion sort is adaptive as best case  $O(n)$ .

Bubble sort is adaptive as best case  $O(n)$

Merge & Heap Sort are not adaptive as both worst best is  $O(n \log n)$ .

2.

a) & b) in Heap q2.cpp.

c) As seen in graph time.png, Bottomup takes less time, but they have same complexity.