

ASSIGNMENT-02

STATISTICAL INFERENCE IN BIOENGINEERING

BM23MTECH11006
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Q1):-

```
import numpy as np
import pandas as pd
from scipy import stats
```

```
import numpy as np
import statsmodels.stats.api as sms
# Effect size
effect_size = 2
# Significance level (alpha)
alpha = 0.05
# Desired power
power = 0.95
```

a)

```
# Calculate the minimum sample size
n=sms.tt_ind_solve_power(effect_size=effect_size, nobs1=None, alpha=alpha, power=power,
ratio=1.0, alternative='two-sided')
print("Minimum sample size:", n)
Minimum sample size: 7.60895791594358
```

b)

```
alpha_new = 0.01
# Calculate the sample size for the new alpha
n_new = sms.tt_ind_solve_power(effect_size=effect_size, nobs1=None, alpha=alpha_new,
power=power, ratio=1.0, alternative='two-sided')
print("Sample size for alpha = 0.01:", n_new)
Sample size for alpha = 0.01: 10.710971202419103
```

c)

```
power_new = 0.99
# Calculate the sample size for the new power
n_power = sms.tt_ind_solve_power(effect_size=effect_size, nobs1=None, alpha=alpha,
power=power_new, ratio=1.0, alternative='two-sided')
print("Sample size for power = 0.99:", n_power)
Sample size for power = 0.99: 10.267583224566895
```

d)

n = 5

Calculate the smallest detectable difference

```
detectable_difference = sms.tt_ind_solve_power(effect_size=None, nobs1=n, alpha=alpha,
power=power_new, ratio=1.0, alternative='two-sided')
```

```
print("Smallest difference,  $|\mu_c - \mu_d|$  =", detectable_difference*10)
```

Smallest difference, $|\mu_c - \mu_d|$ = 31.22095933284507

2

e)

desired_difference = 2

Calculate the probability of detecting the desired difference

```
power_for_desired_difference = sms.tt_ind_solve_power(effect_size=desired_difference, nobs1=n,
alpha=alpha, power=None, ratio=1.0, alternative='two-sided')
```

```
print("Probability of detecting a difference =", power_for_desired_difference)
```

Probability of detecting a difference = 0.790542363607261

3

Q2):-

a)

desired_difference = 2

n_new=3

Calculate the probability of detecting the desired difference

```
power_for_desired_difference = sms.tt_ind_solve_power(effect_size=desired_difference,
nobs1=n_new, alpha=alpha, power=None, ratio=1.0, alternative='two-sided')
```

```
print("n=3 then Power value =", power_for_desired_difference)
```

n=3 then Power value = 0.46264080923120443

5

b)

```
without_delivery=np.array([138,155,121])
```

```
with_delivery=np.array([121,142,131])
```

Set the significance level

alpha = 0.05

```
print(stats.ttest_ind(without_delivery, with_delivery, equal_var=True))
```

Perform the two-sample t-test

```
t_stat, p_value = stats.ttest_ind(without_delivery, with_delivery)
```

why?

Check if the p-value is less than the significance level

if p_value < alpha:

```
print(f"The P value = {p_value} <  $\alpha$  = 0.05. So Null hypotheses rejected.\nThe delivery mechanism works in this experiment.")
```

else:

```
print(f"The P value = {p_value} >  $\alpha$  = 0.05. So Null hypotheses can not be rejected.\nThe delivery mechanism not works in this experiment.")
```

```
Ttest_indResult(statistic=0.5778319966569868, pvalue=0.5943464395237137)
```

The P value = 0.5943464395237137 > α = 0.05. **So Null hypotheses can not be rejected.**

The delivery mechanism not works in this experiment.

✓ 8

Q3):-

a)

```
#Calcium concentration in seawater  $\mu_o$   
#The average value of the sample of calcium concentration in animals  $\mu_a$   
#Null hypotheses  $H_0: \mu_o = \mu_a$   
#Alternative hypotheses  $H_a: \mu_o \neq \mu_a$ 
```

2

b)

```
data=np.array([28, 27, 29, 29, 30, 30, 31, 30, 33, 27, 30, 32,31])  
population_mean = 32  
print(stats.ttest_1samp(data,population_mean))  
t_stat, p_value = stats.ttest_1samp(data, population_mean)  
if p_value < 0.05:  
    print(f"The P value is ={p_value} < 0.05. So  $H_0$  can be rejected.")  
else:  
    print(f"The P value is ={p_value} > 0.05. So  $H_0$  can not be rejected.")  
TtestResult(statistic=-4.501673049096729, pvalue=0.0007245394934862643, df=12)  
The P value is =0.0007245394934862643 < 0.05. So  $H_0$  can be rejected.
```

✓

5

c)

```
#Calcium concentration in seawater  $\mu_o$   
# The average value of the sample of calcium concentration in animals  $\mu_a$   
# Null hypotheses  $H_0: \mu_o > \mu_a$   
# Alternative hypotheses  $H_a: \mu_o < \mu_a$ 
```

X

```
print(stats.ttest_1samp(data, population_mean, alternative='greater'))  
t_stat, p_value = stats.ttest_1samp(data, population_mean, alternative='greater')  
if p_value < 0.05:  
    print(f"The P value is ={p_value} < 0.05. So  $H_0$  can be rejected. The species maintains a coelomic  
calcium level greater than that of their environment.")  
else:  
    print(f"The P value is ={p_value} > 0.05. So  $H_0$  cannot be rejected. The species maintains a  
coelomic calcium level less than that of their environment")  
TtestResult(statistic=-4.501673049096729, pvalue=0.9996377302532569, df=12)  
The P value is =0.9996377302532569 > 0.05. So  $H_0$  cannot be rejected. The species maintains a  
coelomic calcium level less than that of their environment
```

2

X

Q4):-

```
male=np.array([220.1,218.6,229.6,228.8,222.0,224.1,226.5])
```

```
female=np.array([223.4,221.5,230.2,224.3,223.8,230.8])
```

a)

The average value of the sample of Serum cholesterol concentrations in male μ_m

The average value of the sample of Serum cholesterol concentrations in female μ_f

Null hypotheses $H_0: \mu_m = \mu_f$

Alternative hypotheses $H_a: \mu_m \neq \mu_f$

2

b)

#Shapiro Test for checking Normality

```
print("shapiro male results:",stats.shapiro(male))
```

```
print("shapiro female results:",stats.shapiro(female))
```

```
_,p_value_male=stats.shapiro(male)
```

```
_,p_value_female=stats.shapiro(female)
```

```
if p_value_male > 0.05 and p_value_female > 0.05:
```

```
    print("Both male and female data appear to be normally distributed.")
```

```
else:
```

```
    print("At least one of the datasets does not appear to be normally distributed.")
```

```
print("By the Shpiro-Wilk normality test the P-value > Alpha. So Null hypotheses can not be rejected  
and the data was normally distributed.")
```

```
shapiro male results: ShapiroResult(statistic=0.9439237117767334, pvalue=0.6742751598358154)
```

```
shapiro female results: ShapiroResult(statistic=0.841784656047821, pvalue=0.13486963510513306)
```

Both male and female data appear to be normally distributed.

By the Shpiro-Wilk normality test the P-value > Alpha. So Null hypotheses can not be rejected and the data was normally distributed.

5

c)

This experiment has two independent data set groups: male & female

The data are normally distributed.

The aim was to compare the two distinct sample means.

Two sample t-test was suitable for the above conditions.

✓ 5

d)

```
print(stats.ttest_ind(male,female))
```

```
t_stat, p_value = stats.ttest_ind(male, female)
```

```
if p_value < 0.05:
```

```
    print("Reject the null hypothesis. There is evidence that male and female turtles have different  
mean serum cholesterol concentrations.")
```

```
else:
```

```
    print(f"the P-value={p_value} > Alpha (0.05). There is no strong evidence to reject the null  
hypotheses. So, the mean of both mele and female serum cholesterol concentrations are same.")
```

```
Ttest_indResult(statistic=-0.6268108404512706, pvalue=0.543572996867541)
```

the P-value=0.543572996867541 > Alpha (0.05). There is no strong evidence to reject the null hypotheses. So, the mean of both mele and female serum cholesterol concentrations are same.

4

Q5):-

```
exam_after_coffee=np.array([72,64,81,90,73,54,87])
```

```
exam_after_tea=np.array([75,64,79,85,82,90,90])
```

a)

""" The same group of students gave the two sets of exams in the two different situations. The two

situations involved consuming tea or coffee before the exam. The given data looks suitable for a paired

sample t-test. """

Shapiro Test for checking Normality

```
print(stats.shapiro(exam_after_coffee))
```

```
print(stats.shapiro(exam_after_tea))
```

```
_p_value_coffee=stats.shapiro(exam_after_coffee)
```

```
_p_value_tea=stats.shapiro(exam_after_tea)
```

```
if p_value_coffee > 0.05 and p_value_tea > 0.05:
```

```
    print("Both exam_after_coffee and exam after tea data appear to be normally distributed.")
```

```
else:
```

```
    print("At least one of the datasets does not appear to be normally distributed.")
```

```
print("By the Shpiro-Wilk normality test the P-value > Alpha. So Null hypotheses can not be rejected and the data was normally distributed.")
```

```
ShapiroResult(statistic=0.9621812105178833, pvalue=0.8372160792350769)
```

```
ShapiroResult(statistic=0.918850302696228, pvalue=0.46051329374313354)
```

Both exam_after_coffee and exam after tea data appear to be normally distributed.

By the Shpiro-Wilk normality test the P-value > Alpha. So Null hypotheses can not be rejected and the data was normally distributed.

Levene Test for checking Variance

```
stats.levene(exam_after_coffee,exam_after_tea)
```

```
LeveneResult(statistic=0.7067307692307687, pvalue=0.4169679986979009)
```

b)

""" The paired observations should be independent of each other.

• The variance of the pairs was approximately equal, and the data were considered normally distributed. """

c)

""" The average value of the sample of exam after coffee μ_c

The average value of the sample of exam after tea μ_t

Null hypotheses $H_0: (\mu_c - \mu_t) = 0$

Alternative hypotheses $H_a: (\mu_c - \mu_t) \neq 0$ """

```
print(stats.ttest_rel(exam_after_coffee, exam_after_tea))
```

```
t_stat, p_value = stats.ttest_rel(exam_after_coffee, exam_after_tea)
```

```
if p_value < 0.05:
```

```
    print("Reject the null hypothesis. There is evidence that coffee and tea have different effects on exam performance.")
```

```
else:
```

```
    print(f"The P-value={p_value} > Alpha (0.05). Null hypotheses cannot be rejected. There is no significant difference between the means of the students' exams after the coffee and after the tea.")
```

```
TtestResult(statistic=-1.2025868531803559, pvalue=0.27443586794212094, df=6)
```

The P-value=0.27443586794212094 > Alpha (0.05). Null hypotheses cannot be rejected. There is no significant difference between the means of the students' exams after the coffee and after the tea.

Q6):-

```
import pandas as pd
from scipy import stats
BME=pd.DataFrame([78.49, 58.25, 76.33, 75.39, 73.00, 83.62, 67.81, 72.84, 82.02, 77.64, 71.44,
61.54, 66.20, 47.35, 82.45, 81.11,
72.84, 77.09, 69.41, 76.14, 72.05, 78.43, 59.73, 71.60, 82.22])
NonBME=pd.DataFrame([82.81, 78.36, 71.43, 55.71, 85.42, 26.17, 59.20, 62.38, 57.35, 70.45, 66.53,
74.57, 77.74, 73.85, 83.07,
83.66, 84.64, 85.65, 77.77, 69.47, 80.22, 74.72, 77.79])
```

a)

BME.describe()

count	25.000000
mean	72.599600
std	8.729939
min	47.350000
25%	69.410000
50%	73.000000
75%	78.430000
max	83.620000

BME.var()

76.211837

NonBME.describe()

count	23.000000
mean	72.128696
std	13.487674
min	26.170000
25%	68.000000
50%	74.720000
75%	81.515000
max	85.650000

NonBME.var()

181.917348

2

appropriate?

b)

checking for which group is better performed

```
if int(BME.mean()>NonBME.mean()):  
    print("BME performed Better")  
else:  
    print("Non BME group Performed Better")
```

BME performed Better

why mean?

2

c)

""Mean meaks of BME Students μ_{BME}

The mean of Non-BME Students $\mu_{Non-BME}$

Null hypotheses $H_0: \mu_{BME} = \mu_{Non-BME}$

Alternative hypotheses $H_a: \mu_{BME} \neq \mu_{Non-BME}$ ""

```
print(stats.ttest_ind(BME, NonBME))
```

```
t_stat, p_value = stats.ttest_ind(BME, NonBME)
```

```
t_stat, p_value
```

```
Ttest_indResult(statistic=array([0.14475831]), pvalue=array([0.8855341]))  
(array([0.14475831]), array([0.8855341]))
```

why t-test?

10

```
if p_value < 0.05:
```

```
    print(" Conclusion: Reject the null hypothesis. Having a BME background may help in scoring  
    higher marks.")
```

```
else:
```

```
    print(f"The P-value {p_value} > Alpha (0.05). The null hypotheses were true. The BME background  
    did not provide any help in scoring higher marks in BM5033. ")
```

The P-value [0.8855341] > Alpha (0.05). The null hypotheses were true. The BME background did not provide any help in scoring higher marks in BM5033.