ASSIGNMENT 5

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probability that two of these boxes contain exactly 2 and 3 balls is:

b) $\frac{945}{2^{10}}$

a) $-\frac{3}{8}$ b) $\frac{3}{4}$ c) $\frac{3}{2}$

2) If 10 different balls have to be placed in 4 distinct boxes at random, then the

3) If $x = 2\sin\theta - \sin 2\theta$ and $y = 2\cos\theta - \cos 2\theta$, $\theta \in [0, 2\pi]$, then $\frac{d^2y}{dx^2}$ at $\theta = \pi$ is:

c) $\frac{945}{2^{11}}$

d) $\frac{965}{2^{11}}$

d) $-\frac{3}{4}$

1) If $A = [x \in \mathbb{R} : |x| < 2]$ and $B = [x \in \mathbb{R} : |x - 2| \ge 3]$, then:

a) $\frac{965}{2^{10}}$

4) Let f and g be differentiable functions on \mathbb{R} , such that $f \circ g$ is the identity function. If for some $a,b \in \mathbb{R}$, $g'(a) = 5$ and $g(a) = b$, then $f'(b)$ is equal to:			
a) $\frac{2}{5}$	b) 5	c) 1	d) $\frac{1}{5}$
5) In the expansion of $\left(\frac{x}{\cos\theta} + \frac{1}{x\sin\theta}\right)^{16}$ if I_1 is the least value of the term independent of x when $\theta \in \left[\frac{\pi}{8}, \frac{\pi}{4}\right]$ and I_2 is the least value of the term independent of x when $\theta \in \left[\frac{\pi}{16}, \frac{\pi}{8}\right]$, then the ratio $I_2: I_1$ is equal to:			
a) 16:1	b) 8:1	c) 1:8	d) 1:16
 α, which is also equation, then α a) 24 b) 25 c) 26 d) 28 7) Let a function 	o a root of the equal a^2+b^2 is equal to: $f:[0,5] o \mathbb{R}$ be	ation $x^2 - 2bx - 10 =$ e continuous, $f(1) =$	$5=0$ has a repeated root $=0$. If β is the root of this $=3$ and F be defined as:
			the function F , the point
a) a point of local maxima			
b) a point of local maxima.			

- c) a point of local minima.
- d) not a critical point.
- 8) Let [t] denote the greatest integer $\leq t$ and $\lim_{x\to 0} x\left[\frac{4}{x}\right] = A$. Then the function, $f(x) = [x^2] \sin \pi x$ is discontinuous when x is equal to:
 - a) $\sqrt{(A+1)}$
 - b) \sqrt{A}

 - c) $\sqrt{(A+5)}$ d) $\sqrt{(A+21)}$
- 9) Let a-2b+c=1. If $f(x)=\begin{vmatrix} x+a & x+2 & x+1 \\ x+b & x+3 & x+2 \\ x+c & x+4 & x+3 \end{vmatrix}$, then
 - a) f(-50) = 501
 - b) f(-50) = -1
 - c) f(50) = 1
 - d) f(-50) = -501
- 10) Given: $f(x) = \begin{cases} x, & 0 \le x < \frac{1}{2} \\ \frac{1}{2}, & x = \frac{1}{2} \\ 1 x, & \frac{1}{2} < x \le 1 \end{cases}$ and $g(x) = \left(x \frac{1}{2}\right)^2, x \in \mathbb{R}$. Then the area

the lines 2x = 1 to $2x = \sqrt{3}$ is:

- a) $\frac{\sqrt{3}}{4} \frac{1}{3}$ b) $\frac{1}{3} + \frac{\sqrt{3}}{4}$ c) $\frac{1}{2} + \frac{\sqrt{3}}{4}$ d) $\frac{1}{2} \frac{\sqrt{3}}{4}$

- 11) The length of the minor axis (along y-axis) of an ellipse of the standard form is $\frac{1}{\sqrt{3}}$. If this ellipse touches the line x + 6y = 8, then its eccentricity is:
 - a) $\frac{1}{2} \left(\frac{\sqrt{5}}{3} \right)$ b) $\frac{1}{2} \sqrt{\frac{11}{3}}$ c) $\sqrt{\frac{5}{6}}$
- 12) If z is a complex number satisfying |Re(z)| + |Im(z)| = 4, then |z| cannot be:
 - a) $\sqrt{7}$
 - b) $\sqrt{\frac{17}{2}}$
 - c) $\sqrt{10}$
 - d) $\sqrt{8}$
- 13) If $x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta$ and $y = \sum_{n=0}^{\infty} \cos^{2n} \theta$ where $0 < \theta < \frac{\pi}{4}$, then:
 - a) y(1+x)=1
 - b) x(1-y) = 1
 - c) y(1-x)=1

d)
$$x(1+y) = 1$$