## **ASSIGNMENT 5**

1

[-2, -1]

d)  $\frac{965}{2^{11}}$ 

## EE24BTECH11034 - K Teja Vardhan

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2) If 10 different balls have to be placed in 4 distinct boxes at random, then the

3) If  $x = 2\sin\theta - \sin 2\theta$  and  $y = 2\cos\theta - \cos 2\theta$ ,  $\theta \in [0, 2\pi]$ , then  $\frac{d^2y}{dx^2}$  at  $\theta = \pi$  is:

c)  $\frac{945}{211}$ 

probability that two of these boxes contain exactly 2 and 3 balls is:

b)  $\frac{945}{2^{10}}$ 

a)  $\frac{965}{2^{10}}$ 

1) If  $A = [x \in \mathbb{R} : |x| < 2]$  and  $B = [x \in \mathbb{R} : |x - 2| \ge 3]$ , then:

a) A-B = [-1,2] [-2,5] [2,5] b)  $B-A = \mathbb{R} -$  c)  $A \cup B = \mathbb{R} -$  d)  $A \cap B$ 

a) $-\frac{3}{8}$	b) $\frac{3}{4}$	c) $\frac{3}{2}$	d) $-\frac{3}{4}$	
	be differentiable function $a,b\in\mathbb{R},\ g'(a)=5$ and		$f \circ g$ is the identity function $g(g)$ is equal to:	n.
a) $\frac{2}{5}$	b) 5	c) 1	d) $\frac{1}{5}$	
5) In the expansion of $\left(\frac{x}{\cos\theta} + \frac{1}{x\sin\theta}\right)^{16}$ if $I_1$ is the least value of the term independent of $x$ when $\frac{\pi}{8} \leq \theta \leq \frac{\pi}{4}$ and $I_2$ is the least value of the term independent of $x$ when $\frac{\pi}{16} \leq \theta \leq \frac{\pi}{8}$ , then the ratio $I_2: I_1$ is equal to:				
a) 16:1	b) 8:1	c) 1:8	d) 1:16	
$\alpha$ , which is			$+5 = 0$ has a repeated roo $= 0$ . If $\beta$ is the root of th	
			= 3 and $F$ be defined a or the function $F$ , the point	
<ul><li>a) a point of</li><li>b) a point of</li></ul>	f inflection. f local maxima.			

- c) a point of local minima.
- d) not a critical point.
- 8) Let [t] denote the greatest integer  $\leq t$  and  $\lim_{x\to 0} x\left[\frac{4}{x}\right] = A$ . Then the function,  $f(x) = [x^2] \sin \pi x$  is discontinuous when x is equal to:
  - a)  $\sqrt{(A+1)}$
  - b)  $\sqrt{A}$

  - c)  $\sqrt{(A+5)}$ d)  $\sqrt{(A+21)}$
- 9) Let a-2b+c=1. If  $f(x)=\begin{vmatrix} x+a & x+2 & x+1 \\ x+b & x+3 & x+2 \\ x+c & x+4 & x+3 \end{vmatrix}$ , then
  - a) f(-50) = 501
  - b) f(-50) = -1
  - c) f(50) = 1
  - d) f(-50) = -501
- 10) Given:  $f(x) = \begin{cases} x, & 0 \le x < \frac{1}{2} \\ \frac{1}{2}, & x = \frac{1}{2} \\ 1 x, & \frac{1}{2} < x \le 1 \end{cases}$  and  $g(x) = \left(x \frac{1}{2}\right)^2, x \in \mathbb{R}$ . Then the area

(in sq. units) of the region bounded by the curves y = f(x) and y = g(x) between the lines 2x = 1 to  $2x = \sqrt{3}$  is:

- a)  $\frac{\sqrt{3}}{4} \frac{1}{3}$ b)  $\frac{1}{3} + \frac{\sqrt{3}}{4}$ c)  $\frac{1}{2} + \frac{\sqrt{3}}{4}$ d)  $\frac{1}{2} \frac{\sqrt{3}}{4}$

- 11) The following system of linear equations 7x + 6y 2z = 0 3x + 4y + 2z = 0x - 2y - 6z = 0 has
  - a) infinitely many solutions, (x, y, z) satisfying y = 2z
  - b) infinitely many solutions (x, y, z) satisfying x = 2z
  - c) no solution
  - d) only the trivial solution
- 12) If  $p \to (p \land \neg q)$  is false, then the truth values of p and q are respectively:
  - a) *F*, *T*
- b) *T*, *F*
- c) *F*, *F*
- 13) The length of minor axis (along y-axis) of an ellipse of the standard form is  $\frac{4}{\sqrt{3}}$ . If this ellipse touches the line x + 6y = 8, then its eccentricity is:

  - b)  $\frac{1}{2}\sqrt{\frac{11}{3}}$  c)  $\sqrt{\frac{5}{6}}$

14) If z is a complex number satisfying |Re(z)| + |Im(z)| = 4, then |z| cannot be:

a) 
$$\sqrt{7}$$

b) 
$$\sqrt{\frac{2}{2}}$$
  
c)  $\sqrt{10}$ 

d) 
$$\sqrt{8}$$

15) If  $x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta$  and  $y = \sum_{n=0}^{\infty} \cos^{2n} \theta$  where  $0 < \theta < \frac{\pi}{4}$ , then:

a) 
$$y(1+x) = 1$$

b) 
$$x(1-y) = 1$$

c) 
$$y(1-x) = 1$$

d) 
$$x(1+y) = 1$$