

# ASSIGNMENT 6

EE24BTECH11034 - K Teja Vardhan

## I. JEE PYQ JAN 20, SHIFT 1

- 1) Let  $y = mx + c$ ,  $m > 0$  be the focal chord of  $y^2 = -64x$  which is tangent to  $(x + 10)^2 + y^2 = 4$ . Then the value of  $4\sqrt{2}(m + c)$  is equal to
  - a) 16
  - b) 24
  - c) 34
  - d) 40
- 2) A continuous differentiable function  $f(x)$  is increasing in  $(-\infty, \frac{3}{2})$  and decreasing in  $(\frac{3}{2}, \infty)$ . Then  $x = \frac{3}{2}$  is
  - a) a point of local maxima
  - b) a point of local minima
  - c) a point of inflection
  - d) None of these
- 3) If  $z$  and  $w$  are complex numbers such that  $|z\omega| = 1$ ,  $\arg(z) - \arg(w) = \frac{3\pi}{2}$ , then find  $\arg\left(\frac{1-2z\omega}{1+3z\omega}\right)$ 
  - a)  $\frac{\pi}{4}$
  - b)  $-\frac{\pi}{4}$
  - c)  $\frac{3\pi}{4}$
  - d)  $-\frac{3\pi}{4}$
- 4) If an invertible function  $f(x)$  is defined as  $f(x) = 3x - 2$ , and  $g(x)$  is also an invertible function such that  $f^{-1}(g^{-1}(x)) = x - 2$ , then  $g(x)$  is
  - a)  $\frac{x-8}{3}$
  - b)  $\frac{x+8}{3}$
  - c)  $\frac{x-3}{8}$
  - d)  $\frac{x+3}{8}$
- 5) The probability of selecting integers  $a \in [-5, 30]$ , such that  $x^2 + 2(a + 4)x - 5a + 64 > 0$  for all  $x \in \mathbb{R}$  is:
  - a)  $\frac{1}{2}$
  - b)  $\frac{1}{3}$
  - c)  $\frac{1}{4}$
  - d)  $\frac{1}{5}$
- 6) If  $\int_0^a e^{x-[x]} dx = 10e - 9$ , then the value of  $a$  is
  - a)  $9 + \ln 2$
  - b)  $10 + \ln 2$
  - c) 10
  - d) 9
- 7) If the shortest distance between the lines
 
$$\mathbf{r}_1 = \alpha \hat{i} + 2\hat{j} + 2\hat{k} + \lambda (\hat{i} - 2\hat{j} + 2\hat{k})$$
 ,  $\lambda \in \mathbb{R}$ ,  $\alpha > 0$  and
 
$$\mathbf{r}_2 = -4\hat{i} - \hat{k} + \mu (3\hat{i} - 2\hat{j} - 2\hat{k})$$
 ,  $\mu \in \mathbb{R}$  is 9, then the value of  $\alpha$  is:

a) 2

b) 4

c) 6

d)  $\sqrt{6}$

8) Let  $a_{ij} = \begin{cases} 1, & i = j \\ -x, & |i - j| = 1 \\ 2x + 1, & \text{otherwise} \end{cases}$

,  $A = [a_{ij}]_{3 \times 3} = \det(A)$ . Then find the sum of local maximum and minimum values of  $f(x)$ .

a)  $\frac{20}{27}$

b)  $-\frac{20}{27}$

c)  $\frac{88}{27}$

d)  $-\frac{88}{27}$

9) Find the coefficient of  $a^3b^4c^5$  in  $(ab + bc + ca)^6$ .

a) 60

b) 45

c) 40

d) 90

10)  $x \left( \frac{dy}{dx} \right) \tan \left( \frac{y}{x} \right) = y \tan \left( \frac{y}{x} \right) + x$ ,  $y \left( \frac{1}{2} \right) = \frac{\pi}{6}$ . The area bounded by  $x = 0$ ,  $x = \frac{1}{\sqrt{2}}$ , and  $y = y(x)$  is:

a)  $\frac{\pi-1}{8}$

b)  $\frac{\pi-2}{16}$

c)  $\frac{\pi-3}{32}$

d)  $\frac{\pi-4}{64}$