2015-PH-14-26

1

EE24BTECH11034 - K Teja Vardhan

- 1) Let \vec{L} and \vec{p} be the angular and linear momentum operators, respectively, for a particle. The commutator $[L_z, p_y]$ gives
 - a) $-i\hbar p_x$
 - b) 0
 - c) $i\hbar p_x$
 - d) $i\hbar p_u$
- 2) The decay $\mu^+ \to e^+ + \gamma$ is forbidden, because it violates
 - a) momentum and lepton number conservations
 - b) baryon and lepton number conservations
 - c) angular momentum conservation
 - d) lepton number conservation
- 3) An operator for a spin- $\frac{1}{2}$ particle is given by $\hat{A} = \lambda \vec{\sigma} \cdot \vec{B}$, where $\vec{B} = \frac{B}{\sqrt{2}}\hat{x} + i\frac{B}{\sqrt{2}}\hat{y}$, $\vec{\sigma}$ denotes Pauli matrices and λ is a constant. The eigenvalues of \hat{A} are
 - a) $\pm \lambda B \sqrt{2}$
 - b) $\pm \lambda B$
 - c) $0, \lambda B$
 - d) $0, -\lambda B$
- 4) In an inertial frame S, two events A and B take place at $(ct_A = 0, \vec{r}_A = 0)$ and $(ct_B = 0, \vec{r}_B = 2\hat{y})$, respectively. The times at which these events take place in a frame S' moving with a velocity 0.6cy with respect to S are given by
 - a) $ct'_A = 0; ct'_B = -3/2$
 - b) $ct'_{A} = 0; ct'_{B} = 0$
 - c) $ct_A^{''} = 0; ct_B^{'} = 3/2$
 - d) $ct'_A = 0; ct'_B = 1/2$
- 5) Given that the magnetic flux through the closed loop PQRSP is Φ . If $\int_P^R \vec{A} \cdot \vec{dl} = \phi_1$ along PQR, the value of $\int_P^R \vec{A} \cdot \vec{dl}$ along PSR is
 - a) $\Phi \phi_1$
 - b) $\phi_1 \Phi$
 - c) $-\phi_1$
 - d) ϕ_1
- 6) If $f\left(x\right)=e^{-x^{2}}$ and $g\left(x\right)=|x|e^{-x^{2}},$ then
 - a) f and g are differentiable everywhere
 - b) f is differentiable everywhere but g is not
 - c) g is differentiable everywhere but f is not
 - d) g is discontinuous at x = 0
- 7) In Bose-Einstein condensates, the particles

- a) have strong interparticle attraction
- b) condense in real space
- c) have overlapping wavefunctions
- d) have large and positive chemical potential
- 8) Consider a system of N non-interacting spin- $\frac{1}{2}$ particles, each having a magnetic moment μ , is in a magnetic field $\vec{B} = B\hat{z}$. If \vec{E} is the total energy of the system, the number of accessible microstates Ω is given by

a)
$$\Omega = \frac{N!}{\frac{1}{2} \left(N - \frac{E}{\mu B} \right)! \frac{1}{2} \left(N + \frac{E}{\mu B} \right)!}$$
b)
$$\Omega = \frac{\left(N - \frac{E}{\mu B} \right)!}{\left(N + \frac{E}{\mu B} \right)!}$$
c)
$$\Omega = \frac{1}{2} \left(N - \frac{E}{\mu B} \right)! \frac{1}{2} \left(N + \frac{E}{\mu B} \right)!}$$
d)
$$\Omega = \frac{N!}{\left(N + \frac{E}{\mu B} \right)!}$$

c)
$$\Omega = \frac{1}{2} \left(N - \frac{E}{\mu B} \right) ! \frac{1}{2} \left(N + \frac{E}{\mu B} \right)$$

d)
$$\Omega = \frac{N!}{\left(N + \frac{E}{\mu B}\right)!}$$

- 9) For a black body radiation in a cavity, photons are created and annihilated freely as a result of emission and absorption by the walls of the cavity. This is because
 - a) the chemical potential of the photons is zero
 - b) photons obey Pauli exclusion principle
 - c) photons are spin-1 particles
 - d) the entropy of the photons is very large
- 10) Consider w = f(z) = u(x, y) + iv(x, y) to be an analytic function in a domain D. Which one of the following options is NOT correct?
 - a) u(x,y) satisfies Laplace equation in D
 - b) v(x,y) satisfies Laplace equation in D
 - c) $\int_{z_1}^{z_2} f(z) dz$ is dependent on the choice of the contour between z_1 and z_2 in D
 - d) f(z) can be Taylor expanded in D
- 11) The value of $\int_0^3 t^3 \delta(3t-6) dt$ is
- 12) Which one of the following DOES NOT represent an exclusive OR operation for inputs A and B?
 - a) $(A + \bar{B}) \bar{A}B$
 - b) $\bar{A}B + \bar{B}A$
 - c) $(A+B)(\bar{A}+\bar{B})$
 - d) $(A+B)\bar{A}B$
- 13) Consider a complex function $f(z) = \frac{1}{z(z+\frac{1}{z})\cos(z\pi)}$. Which one of the following statements is correct?
 - a) f(z) has simple poles at z=0 and $z=-\frac{1}{2}$
 - b) f(z) has a second order pole at $z=-\frac{1}{2}$
 - c) f(z) has infinite number of second order poles
 - d) f(z) has all simple poles