oqcg

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1 Imports

Need to have jate.py in your folder

```
In [1]: %run jate.py #will import everything
```

2 Next chapter

2.1 memory clear (uses regex, so be careful)

```
In [2]: %reset_selective -f var1, var2 # replace var1, var2 with your defined ones
```

2.2 Building parts

2.2.1 Building the things to be calculated only once

Parameters

 $omega_1$: float

 $frequency\ corresponding\ to\ half\ of\ the\ difference\ between$

energy levels of the qubit

 H_0 : Qobj

Bare Hamiltonian

 H_1 : Qobj

Interaction Hamiltonian

 T_s : Qobj

Unitary to be implemented in the Hilbert space

```
Lin
       : Qobj
          Linbladian operators
        : int
d
          Dimension of the matrix. Defaults to 2
        : float
gamma
          Damping constant of the Linbladian
Returns
_____
ih0
        : Qobj
          I \circ H_{0}
ih1
        : Qobj
          I \setminus Otimes H_{1}
h0ci
        : Qobj
          $H_{0}^{*}\otimes I $
h1ci
        : Qobj
          $H_{1}^{*}\otimes I $
T
        : Qobj
          Target unitary transformed to the Liouville space
linbladian : Qobj
             The full lindbladian term as it appears on transformation to
             the Liouville space.
11 11 11
I = identity(d)
L I = tensor(I, I)
ih0 = tensor(I, H_0)
ih1 = tensor(I, H_1)
h0ci = tensor(H_0.conj(), I)
h1ci = tensor(H_1.conj(), I)
x_k = ih1 - h1ci
term1 = tensor(Lin.trans(), Lin)
term2 = tensor(I, ((Lin.dag())*(Lin)))
term3 = tensor(((Lin.trans())*(Lin.conj())), I)
lindbladian = 1j*(gamma)*(term1 - 0.5*(term2 + term3))
T = tensor(T_s.trans(), T_s) \# Transforming $T_{s}$ to liouville space
return ih0, ih1, h0ci, h1ci, x_k, lindbladian, T, L_I
```

```
In [4]: omega_1 = 0.5
           H_0 = omega_1*sigmaz()
           H_1 = sigmay()
           T_s = sigmax()
           Lin = sigmaz()
           gamma = 0.1 # check for default value
           ih0, ih1, h0ci, h1ci, x_k, lindbladian, T, L_I = maker(omega_1,
                                                                                 H_0, H_1, T_s,
                                                                                 Lin, d=2, gamma=gamma)
In [5]: gamma
Out[5]: 0.1
In [6]: L_I
    Out [6]:
    Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = True

\left(\begin{array}{ccccc}
1.0 & 0.0 & 0.0 & 0.0 \\
0.0 & 1.0 & 0.0 & 0.0 \\
0.0 & 0.0 & 1.0 & 0.0 \\
0.0 & 0.0 & 0.0 & 1.0
\end{array}\right)

2.2.2 Building A(t)
In [7]: def A(xi):
                r"""making $A(t)$"""
                A = ih0 - h0ci + xi*(ih1 - h1ci) + lindbladian
                return A
In [8]: A(0.5)
    Out[8]:
    Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
                        \begin{pmatrix} 0.0 & -0.500j & -0.500j & 0.0\\ 0.500j & (-1.0 - 0.200j) & 0.0 & -0.500j\\ 0.500j & 0.0 & (1.0 - 0.200j) & -0.500j\\ 0.0 & 0.500j & 0.500j & 0.0 \end{pmatrix}
2.2.3 Building L(t) and the Identity in the Liouville space
In [9]: def L(xi, dt):
                r"""Making $L(t) from $A(t)$"""
                L = (-1j*A(xi)*dt).expm()
                return L
In [10]: L(0.5, 0.001)
```

```
Out[10]:
```

Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False

```
 \begin{pmatrix} 1.000 & (-4.999 \times 10^{-04} - 2.500 \times 10^{-07}j) & (-4.999 \times 10^{-04} + 2.500 \times 10^{-07}j) \\ (4.999 \times 10^{-04} + 2.500 \times 10^{-07}j) & (1.000 + 9.998 \times 10^{-04}j) & -2.500 \times 10^{-07} \\ (4.999 \times 10^{-04} - 2.500 \times 10^{-07}j) & -2.500 \times 10^{-07}j) & (1.000 - 9.998 \times 10^{-04}j) \\ 2.500 \times 10^{-07} & (4.999 \times 10^{-04} + 2.500 \times 10^{-07}j) & (4.999 \times 10^{-04} - 2.500 \times 10^{-07}j) \end{pmatrix}
```

2.3 Major functions

2.3.1 Major functions 1

```
In [11]: # building the function to optimize (optimizee)
         def L_vec(xi_vec, dt):
             r"""Building the vector of differential $L(t)$"""
             L_vec = [L(xi, dt) for xi in xi_vec]
             return L_vec
In [12]: def fidelity_calc(A, B):
             r"""Making a generalised fidelity function"""
             first_part = (A - B).dag()
             second_part = (A - B)
             f_int = (first_part* second_part)
             f = f_int.tr()
             return f
In [13]: def L_full_maker(xi_vec, dt):
             r"""Building the L(t) for the total time t
             xi_vec_size = xi_vec.size # finding the size of xi
             L_full = L_I # Identity for the for loop of L
             L_v = L_vec(xi_vec, dt) # calling L_vec
             for i in range(xi_vec_size): # generating L_full
                 L_full = L_full*L_v[xi_vec_size - 1 - i]
             return L full
In [14]: def F(xi_vec, dt):
             r"""Using the fidelity metric to find out the closeness between $T$
             and L(t)"""
             L_full = L_full_maker(xi_vec, dt)
             F = real(-fidelity_calc(T, L_full))
             return F
2.3.2 Testing major functions 1
In [15]: fidelity_calc(sigmax(), sigmay())
Out[15]: 4.0
In [16]: fidelity_calc(sigmay(), sigmay())
```

```
Out[16]: 0.0
In [17]: xi_vec_test = array([1.0, 2.0])
         xi_vec_test
Out[17]: array([1., 2.])
In [18]: xi_vec_test.size
Out[18]: 2
In [19]: w_vec = [xi**2 for xi in xi_vec_test]
         w_vec
Out[19]: [1.0, 4.0]
In [20]: \# F(xi\_vec, dt)
         F(xi_vec_test, 0.001)
Out[20]: -7.998400634493138
In [21]: L_v = L_{vec}(xi_{vec}_{test}, 0.001)
In [22]: L v
Out[22]: [Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
          Qobj data =
          [[ 9.99999000e-01+0.00000000e+00j -9.99899173e-04-4.99933130e-07j
           -9.99899173e-04+4.99933130e-07j 9.99932920e-07+0.00000000e+00j]
           [ 9.99899173e-04+4.99933130e-07j 9.99798520e-01+9.99799187e-04j
           -9.99866260e-07+0.00000000e+00j -9.99899173e-04-4.99933130e-07j]
           [ 9.99899173e-04-4.99933130e-07j -9.99866260e-07+0.00000000e+00j
             9.99798520e-01-9.99799187e-04j -9.99899173e-04+4.99933130e-07j]
           [ 9.99932920e-07+0.00000000e+00j 9.99899173e-04+4.99933130e-07j
             9.99899173e-04-4.99933130e-07j 9.99999000e-01+0.00000000e+00j]],
          Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
          Qobj data =
          [[ 9.99996000e-01+0.00000000e+00j -1.99979435e-03-9.99865260e-07j
            -1.99979435e-03+9.99865260e-07j 3.99972768e-06+0.00000000e+00j]
           [ 1.99979435e-03+9.99865260e-07j 9.99795521e-01+9.99797187e-04j
           -3.99946104e-06+0.00000000e+00j -1.99979435e-03-9.99865260e-07j]
           [ 1.99979435e-03-9.99865260e-07j -3.99946104e-06+0.00000000e+00j
             9.99795521e-01-9.99797187e-04j -1.99979435e-03+9.99865260e-07j]
           [ 3.99972768e-06+0.00000000e+00j 1.99979435e-03+9.99865260e-07j
             1.99979435e-03-9.99865260e-07j 9.99996000e-01+0.00000000e+00j]]]
```

2.3.3 Major Functions 2

```
In [23]: def L_comma_k_maker(xi_vec, k, dt):
               r"""Making of the derivative of full L(t) at time t_{k}"""
               N = xi vec.size
               # Determining the size of xi, and thus the time_steps indirectly.
              L v = L vec(xi vec, dt)# Making of the full L(t)$
               inner_part = L_I # Beginner for the for loop
               for i in range(N):
                   if i == (N - 1 - k):
                        # The step at which X_{k}(t) has to be inserted
                        inner_part = inner_part*x_k*L_v[k - 1]
                   else:
                        # Usual multiplications of $L_{k}$
                        inner_part = inner_part*L_v[N - 1 - i]
               l comma k = inner part
               return l_comma_k
In [24]: \# L_{comma_k_maker(xi_vec, k, dt)}
          L comma k maker(xi vec test, 2, 0.001)
   Out [24]:
   Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
                                (-0.003 - 3.499 \times 10^{-06}i)
                                                                   (-0.003 + 3.499 \times 10^{-06}i)
            1.000
   \begin{array}{l} (0.003 + 2.499 \times 10^{-06}j) & (1.000 + 0.002j) \\ (0.003 - 2.499 \times 10^{-06}j) & (-8.998 \times 10^{-06} - 2.999 \times 10^{-09}j) \end{array}
                                                               (-8.998 \times 10^{-06} + 2.999 \times 10^{-09}i)
                                                                                                  (-0.003 - 2)
                                                                        (1.000 - 0.002i)
                                 (0.003 + 3.499 \times 10^{-06}i)
                                                                    (0.003 - 3.499 \times 10^{-06}i)
In [25]: def updater(xi_vec, dt, epsilon):
               r"""Implementing the GRAPE update step"""
               xi_vec_size = xi_vec.size # finding the size of xi
              L_full = L_full_maker(xi_vec, dt)
               di = []
               for k in range(xi_vec_size):
                   # Building the thing to be added to the old function
                   L_comma_k = L_comma_k_maker(xi_vec, k, dt)
                   differentiated = T - L comma k
                   plain = T - L_full
                   c = -differentiated.dag()*plain
                   d = -plain.dag()*differentiated
                   inside = c.tr() + d.tr()
                   di.append(epsilon*inside)
               diff = array(di)
               xi new vec = xi vec + diff
               return diff, xi_new_vec
```

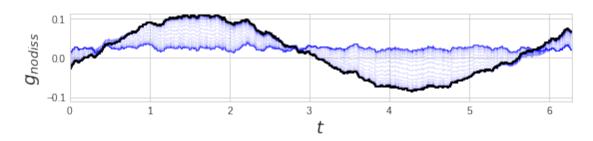
8.999

(-0.003 + 2)

```
In [26]: # updater(xi_vec, dt, epsilon)
          updater(xi_vec_test, 0.001, 0.001)
Out[26]: (array([-0.008+0.j, -0.008+0.j]), array([0.992+0.j, 1.992+0.j]))
2.4 Qutip grape for closed system
In [27]: import time
In [28]: total_time_evo = 2*pi # total time allowed for evolution
In [29]: times = linspace(0, total_time_evo, 500)
In [30]: # vector of times at which discretization
          # is carried out
In [31]: U = T_s
   Out[31]:
   Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True
                                         \left(\begin{array}{cc} 0.0 & 1.0 \\ 1.0 & 0.0 \end{array}\right)
In [32]: R = 500
In [33]: H_{ops} = [H_{1}]
          H_ops
Out[33]: [Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True
           Qobj data =
           [[0.+0.j \ 0.-1.j]
             [0.+1.j 0.+0.j]]
In [34]: H_labels = [r'$g_{no diss}]']
          H_labels
Out[34]: ['$g_{no diss}$']
In [35]: HO = H_O
          НО
   Out [35]:
   Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True
                                      \begin{pmatrix} 0.500 & 0.0 \\ 0.0 & -0.500 \end{pmatrix}
In [36]: c_ops = []
```

```
In [37]: from qutip.control.grape import plot_grape_control_fields, _overlap
         from qutip.control.grape import grape_unitary_adaptive, cy_grape_unitary
In [38]: from scipy.interpolate import interp1d
         from qutip.ui.progressbar import TextProgressBar, EnhancedTextProgressBar
In [39]: u0 = array([rand(len(times)) * 2 * pi * 0.05 for _ in range(len(H_ops))])
In [40]: from numpy import convolve
         u0 = [convolve(ones(10)/10, u0[idx,:], mode='same') for idx in range(len(H_ops))]
In [41]: u_limits = None \#[0, 1 * 2 * pi]
         alpha = None
In [42]: result = cy_grape_unitary(U, H0, H_ops, R, times, u_start=u0, u_limits=u_limits,
                                   eps=2*np.pi*1, alpha=alpha, phase_sensitive=False,
                                   progress_bar=TextProgressBar())
10.0%. Run time: 35.21s. Est. time left: 00:00:05:16
20.0%. Run time: 68.84s. Est. time left: 00:00:04:35
30.0%. Run time: 102.50s. Est. time left: 00:00:03:59
40.0%. Run time: 135.89s. Est. time left: 00:00:03:23
50.0%. Run time: 169.45s. Est. time left: 00:00:02:49
60.0%. Run time: 202.93s. Est. time left: 00:00:02:15
70.0%. Run time: 236.24s. Est. time left: 00:00:01:41
80.0%. Run time: 269.57s. Est. time left: 00:00:01:07
90.0%. Run time: 302.86s. Est. time left: 00:00:00:33
Total run time: 335.83s
```

Plot of optimized control field without dissipation



In [44]: U

Out [44]:

Quantum object:
$$dims = [[2], [2]]$$
, $shape = (2, 2)$, $type = oper$, $isherm = True$

$$\left(\begin{array}{cc} 0.0 & 1.0 \\ 1.0 & 0.0 \end{array}\right)$$

In [45]: result.U_f

Out[45]:

Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = False

$$\left(\begin{array}{ccc}
-9.937 \times 10^{-17} & 1.000j \\
1.0j & 9.631 \times 10^{-17}
\end{array}\right)$$

2.5 Analysis of result of qutip grape for closed system

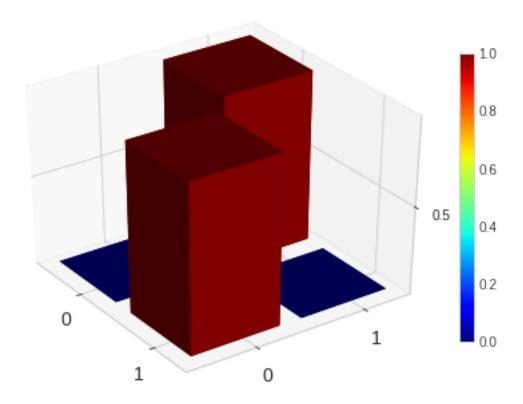
In [46]: result.U_f/result.U_f[0,0]

Out[46]:

Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = False

$$\left(\begin{array}{cc} 1.0 & (-1.828 \times 10^{+15} - 3.440 \times 10^{+14} j) \\ (-1.828 \times 10^{+15} - 3.440 \times 10^{+14} j) & (0.880 + 0.348 j) \end{array}\right)$$

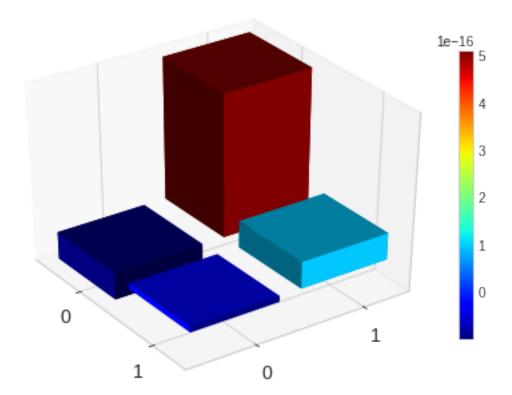
In [47]: matrix_histogram(U)



In [48]: matrix_histogram(result.U_f)

Out[48]: (<Figure size 432x288 with 2 Axes>,

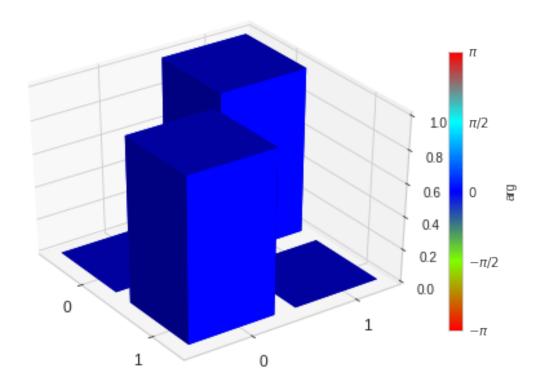
<mpl_toolkits.mplot3d.axes3d.Axes3D at 0x7fefd043c240>)



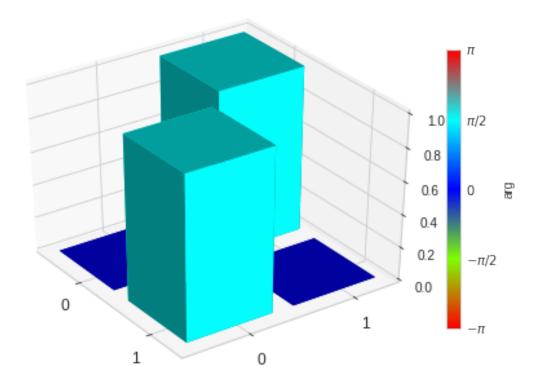
In [49]: matrix_histogram_complex(U)

Out[49]: (<Figure size 432x288 with 2 Axes>,

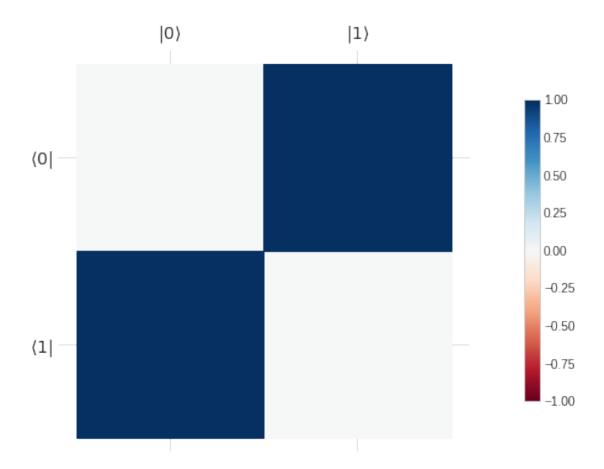
<mpl_toolkits.mplot3d.axes3d.Axes3D at 0x7fefd03a70b8>)



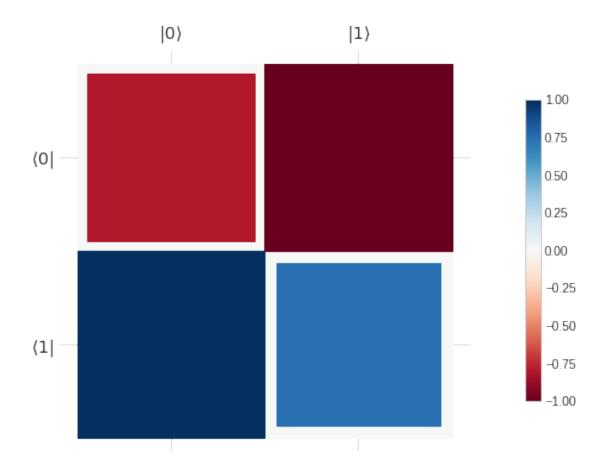
In [50]: matrix_histogram_complex(result.U_f)



In [51]: hinton(U)



In [52]: hinton(result.U_f)



```
In [53]: updater(result.u[-1, 0, :], (2*pi)/500, epsilon=((0.1*2*pi)/(10**3)))
Out[53]: (array([-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
                 -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
```

```
-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
-0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j,\\
-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
-0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j,\\
-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
```

```
-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
-0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j,\\
-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
-0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j, -0.00207526 + 0.j,\\
-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
```

```
-0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j,
       -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j, -0.00207526+0.j]),
array([-0.18981489+0.j, -0.17532648+0.j, -0.14439776+0.j, -0.10824093+0.j,
       -0.09567925+0.j, -0.06659201+0.j, -0.05155044+0.j, -0.04496856+0.j,
       -0.05368121+0.j, -0.07263244+0.j, -0.05431784+0.j, -0.05235868+0.j,
       -0.04252277+0.j, -0.03262759+0.j, -0.00729903+0.j,
                                                             0.00634903+0.j,
                                           0.00464709+0.j,
                                                             0.0222782 + 0.j,
        0.00468536+0.j,
                         0.00513758+0.j,
        0.03112502+0.j,
                                                             0.03338055+0.j,
                         0.04024616+0.j,
                                           0.05110875+0.j,
        0.02501782+0.j,
                         0.00757774+0.j,
                                           0.01910582+0.j,
                                                             0.0345821 + 0.j,
        0.04931579+0.j,
                         0.06845434+0.j,
                                           0.07356085+0.j,
                                                             0.09481535+0.j,
        0.09752187+0.j,
                         0.12735617+0.j,
                                           0.1594223 + 0.j
                                                             0.18635566+0.j,
        0.20741238+0.j,
                         0.2127336 + 0.j,
                                           0.2182719 + 0.j,
                                                             0.22991645+0.j,
        0.22171453+0.j,
                         0.22386559+0.j,
                                           0.21391604+0.j,
                                                             0.22508712+0.j,
        0.23516238+0.j,
                         0.22820706+0.j,
                                           0.24660838+0.j,
                                                             0.25041709+0.j,
        0.25915332+0.j,
                         0.25550177+0.j,
                                           0.26695301+0.j,
                                                             0.28777818+0.j,
        0.31561954+0.j,
                         0.31105956+0.j,
                                           0.30460653+0.j,
                                                             0.32838411+0.j,
        0.33689041+0.j,
                         0.35886909+0.j,
                                           0.37071472+0.j,
                                                             0.37578945+0.j,
        0.38858389+0.j,
                         0.39025233+0.j,
                                           0.39307612+0.j,
                                                             0.41307595+0.j,
        0.40643024+0.j
                         0.41421651+0.j,
                                           0.40767244+0.j
                                                             0.41419967+0.j,
                         0.45977087+0.j,
        0.43756068+0.j,
                                           0.47657047+0.j,
                                                             0.4955884 +0.j,
        0.49683263+0.j,
                         0.50374738+0.j,
                                           0.52770218+0.j,
                                                             0.53742089+0.j,
        0.53896688+0.j,
                         0.55419342+0.j,
                                           0.56511304+0.j,
                                                             0.56207053+0.j,
        0.55901499+0.j,
                         0.56670222+0.j,
                                           0.56804928+0.j,
                                                             0.55437803+0.j,
        0.54600026+0.j
                         0.52936125+0.j,
                                           0.5401968 + 0.j
                                                             0.52835857+0.j,
        0.51328568+0.j,
                         0.51052897+0.j,
                                           0.52592567+0.j,
                                                             0.50906907+0.j,
        0.53135472+0.i
                         0.53863585+0.i
                                           0.54224582+0.i
                                                             0.57518988+0.j,
        0.58978452+0.j,
                         0.61021496+0.j,
                                           0.60556076+0.j,
                                                             0.61901571+0.j,
        0.62115889+0.j,
                         0.64235455+0.j,
                                           0.62434626+0.j,
                                                             0.62492177+0.j,
        0.63940489+0.j,
                         0.62798486+0.j,
                                           0.63644454+0.j,
                                                             0.63582665+0.j,
        0.6580747 + 0.j,
                         0.66799219+0.j,
                                           0.64966433+0.j,
                                                             0.63671267+0.j,
        0.65773049+0.j,
                         0.6757297 + 0.j
                                           0.66510398+0.j,
                                                             0.67480878+0.j,
        0.67360209+0.j,
                         0.67040668+0.j,
                                           0.6655067 + 0.j
                                                             0.64475393+0.j,
        0.65016572+0.j,
                         0.67338778+0.j,
                                           0.67794346+0.j,
                                                             0.66383772+0.j,
        0.6735167 + 0.j
                         0.66003833+0.j,
                                           0.636998 + 0.j,
                                                             0.64153596+0.j,
        0.65352443+0.j
                         0.67916867+0.j,
                                           0.70194022+0.j,
                                                             0.69556726+0.j,
        0.68653746+0.j,
                         0.68391691+0.j,
                                           0.67962941+0.j,
                                                             0.67423764+0.j,
        0.69368394+0.j,
                         0.67258774+0.j,
                                           0.67273545+0.j,
                                                             0.67315896+0.j,
        0.6517371 + 0.j
                         0.65721385+0.j,
                                           0.6663704 + 0.j,
                                                             0.65943668+0.j,
                         0.6820261 + 0.j
                                                             0.6767627 + 0.j
        0.6591273 + 0.j
                                           0.68187594+0.j,
```

```
0.67666127+0.j,
                  0.65271957+0.j,
                                   0.65719275+0.j,
                                                     0.64269157+0.j,
 0.61799018+0.j,
                  0.64585746+0.j,
                                   0.64096547+0.j,
                                                     0.61059959+0.j,
 0.58608396+0.j,
                  0.5828865 +0.j,
                                   0.56566646+0.j,
                                                     0.57097945+0.j
 0.57005031+0.j,
                  0.55414373+0.j,
                                   0.55113743+0.j,
                                                     0.52995004+0.j,
 0.53701348+0.i
                  0.56019091+0.i
                                   0.55632425+0.i
                                                     0.55700318+0.i
 0.55923798+0.j,
                  0.56549333+0.j,
                                   0.57183764+0.j,
                                                     0.58336759+0.j,
 0.59904106+0.j,
                  0.60235593+0.j,
                                   0.59984626+0.j,
                                                     0.58725173+0.j,
 0.60824822+0.j,
                  0.61737596+0.j,
                                   0.59629448+0.j,
                                                     0.57428821+0.j,
 0.55415343+0.j,
                  0.54625146+0.j,
                                   0.53344648+0.j,
                                                     0.53231955+0.j,
 0.50845455+0.j,
                  0.48195091+0.j,
                                   0.44540157+0.j,
                                                     0.431681 + 0.j
                  0.42375361+0.j
 0.43315001+0.j,
                                   0.41621515+0.j,
                                                     0.3955753 + 0.j
 0.39640428+0.j
                  0.37644841+0.j
                                   0.39082553+0.j
                                                     0.39521496+0.j
                                                     0.40918534+0.j,
 0.41723454+0.j
                  0.40546437+0.j
                                   0.40224657+0.j
 0.39232748+0.j
                  0.38234751+0.j
                                   0.35156531+0.j,
                                                     0.35604805+0.j,
 0.32827676+0.j,
                  0.33507236+0.j,
                                   0.30427105+0.j,
                                                     0.30450557+0.j,
 0.30689309+0.j,
                  0.27978009+0.j,
                                   0.27105834+0.j,
                                                     0.25863889+0.j,
 0.24762204+0.j,
                  0.21309759+0.j,
                                   0.21591281+0.j,
                                                     0.18342081+0.j,
 0.19755019+0.j,
                  0.20039123+0.j,
                                   0.18176412+0.j,
                                                     0.17447886+0.j,
 0.17833621+0.j,
                  0.18445272+0.j,
                                   0.17677694+0.j,
                                                     0.17748326+0.j,
 0.17436188+0.j,
                  0.16547039+0.i
                                   0.13095384+0.j,
                                                     0.09986995+0.i
 0.08378487+0.j,
                  0.09739656+0.j,
                                   0.09928475+0.j,
                                                     0.08361583+0.j,
 0.09399917+0.j,
                  0.0821147 + 0.j
                                   0.07285404+0.j,
                                                     0.0901184 + 0.j
 0.0966029 + 0.j,
                  0.10258161+0.j,
                                   0.09233394+0.j,
                                                     0.07494531+0.j,
 0.05082207+0.j,
                  0.05515701+0.j,
                                   0.04219505+0.j,
                                                     0.05339267+0.j,
 0.04012904+0.j,
                  0.01383232+0.j, -0.00712591+0.j, -0.01745221+0.j,
-0.02624092+0.j, -0.02260088+0.j, -0.02365738+0.j, -0.03455945+0.j,
-0.03533082+0.j, -0.0416341 +0.j, -0.06203955+0.j, -0.06997482+0.j,
-0.07400132+0.j, -0.09460447+0.j, -0.09705045+0.j, -0.12786286+0.j,
-0.12596214+0.j, -0.14412826+0.j, -0.15418246+0.j, -0.1641098 +0.j,
-0.1724538 +0.j, -0.16240899+0.j, -0.17430401+0.j, -0.18499652+0.j,
-0.18248914+0.j, -0.18834567+0.j, -0.21361626+0.j, -0.21345717+0.j,
-0.23175122+0.j, -0.25453091+0.j, -0.23481785+0.j, -0.24346882+0.j,
-0.24454802+0.j, -0.2273565 +0.j, -0.23238386+0.j, -0.21868758+0.j,
-0.22534731+0.j, -0.23055593+0.j, -0.22992686+0.j, -0.21628585+0.j,
-0.22227603+0.j, -0.22823219+0.j, -0.24028802+0.j, -0.26882924+0.j,
-0.30038103+0.j, -0.31030821+0.j, -0.31250408+0.j, -0.32376877+0.j,
-0.3360826 +0.j, -0.35195222+0.j, -0.35783441+0.j, -0.36177639+0.j,
-0.36322666+0.j, -0.36044068+0.j, -0.35642047+0.j, -0.37626743+0.j,
-0.38360475+0.j, -0.39863258+0.j, -0.40260139+0.j, -0.40757727+0.j,
-0.43508512+0.j, -0.46062144+0.j, -0.46158914+0.j, -0.45860549+0.j,
-0.45739458+0.j, -0.45805327+0.j, -0.44543141+0.j, -0.44611099+0.j,
-0.4597519 +0.j, -0.46556551+0.j, -0.46845635+0.j, -0.45402347+0.j,
-0.44909344+0.j, -0.45986071+0.j, -0.44755705+0.j, -0.44952101+0.j,
-0.47978275+0.j, -0.4746718 +0.j, -0.46359934+0.j, -0.47138964+0.j,
-0.453233 +0.j, -0.47930815+0.j, -0.47957041+0.j, -0.47160536+0.j,
-0.4910898 +0.j, -0.49666723+0.j, -0.48895116+0.j, -0.49631566+0.j,
-0.50992145+0.j, -0.50034438+0.j, -0.50063023+0.j, -0.49669364+0.j,
-0.5191154 +0.j, -0.52364944+0.j, -0.52884114+0.j, -0.53148841+0.j,
```

```
-0.54058291+0.j, -0.5175859 +0.j, -0.51908031+0.j, -0.51596762+0.j,
-0.53122122+0.j, -0.51429092+0.j, -0.50679759+0.j, -0.50784827+0.j,
-0.51053065+0.j, -0.50386027+0.j, -0.48679365+0.j, -0.51366852+0.j,
-0.48936605+0.j, -0.4847466+0.j, -0.4717867+0.j, -0.47308547+0.j,
-0.448743 +0.j, -0.46236233+0.j, -0.44830721+0.j, -0.45245764+0.j,
-0.46613791+0.j, -0.44112902+0.j, -0.46318575+0.j, -0.46816873+0.j,
-0.47431248+0.j, -0.47075347+0.j, -0.47090423+0.j, -0.46445162+0.j,
-0.45531539+0.j, -0.46135392+0.j, -0.45954568+0.j, -0.47870619+0.j,
-0.45460867+0.j, -0.46672081+0.j, -0.46381593+0.j, -0.45643221+0.j,
-0.4763782 + 0.j, -0.46129372 + 0.j, -0.46007989 + 0.j, -0.43579596 + 0.j,
-0.40148667+0.j, -0.39174005+0.j, -0.39807442+0.j, -0.39233033+0.j,
-0.3877545 +0.j, -0.39226954+0.j, -0.37223244+0.j, -0.35965203+0.j,
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-0.35607355+0.j, -0.33364665+0.j, -0.33722397+0.j, -0.33484492+0.j,
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-0.23495823+0.j, -0.22911451+0.j, -0.22553002+0.j, -0.23473038+0.j,
-0.22629084+0.j, -0.21230721+0.j, -0.20516253+0.j, -0.20141265+0.j,
-0.20986307+0.j, -0.21305115+0.j, -0.19524946+0.j, -0.18412027+0.j,
-0.20009322+0.j, -0.1847023 +0.j, -0.18612701+0.j, -0.19856394+0.j,
-0.20870019+0.j, -0.20057487+0.j, -0.17211355+0.j, -0.15266146+0.j,
-0.14846749+0.j, -0.15543135+0.j, -0.12555856+0.j, -0.11770019+0.j,
-0.10729537+0.j, -0.08631548+0.j, -0.07557817+0.j, -0.0905244 +0.j,
-0.08694717+0.j, -0.07980948+0.j, -0.08187849+0.j, -0.07066793+0.j,
-0.08680067+0.j, -0.09605075+0.j, -0.09707327+0.j, -0.09537512+0.j,
-0.09074836+0.j, -0.07462175+0.j, -0.06276156+0.j, -0.06299608+0.j,
-0.04911118+0.j, -0.03409736+0.j, -0.00615456+0.j, 0.02209517+0.j,
 0.05108223+0.j, 0.06537526+0.j,
                                   0.07100315+0.j,
                                                    0.07573659+0.j
 0.07504343+0.j
                 0.08132914+0.j,
                                   0.09689284+0.j,
                                                    0.11331409+0.j,
 0.10366834+0.j,
                  0.11598682+0.j,
                                   0.10581205+0.j,
                                                    0.09926045+0.j,
 0.12010182+0.j,
                  0.13565544+0.j
                                   0.13851948+0.j,
                                                    0.13185644+0.j,
 0.13570809+0.j,
                  0.14309554+0.j,
                                   0.16754299+0.j,
                                                    0.15015905+0.j,
 0.16899458+0.j,
                  0.1742532 + 0.j
                                   0.18322914+0.j,
                                                    0.19877095+0.j,
 0.21635625+0.j,
                  0.24828109+0.j,
                                   0.24469296+0.j,
                                                    0.24112582+0.j,
 0.25057636+0.i
                  0.26814865+0.j,
                                   0.27635856+0.j,
                                                    0.30581701+0.i
 0.306278 + 0.i
                  0.30771324+0.i
                                   0.29597105+0.i
                                                    0.28247674+0.j,
 0.30050984+0.i
                  0.30248706+0.j,
                                   0.31071373+0.j,
                                                    0.3346877 + 0.i
 0.35408918+0.j,
                  0.35429758+0.j,
                                   0.38406155+0.j,
                                                    0.40172216+0.j,
                                                    0.46993703+0.j,
 0.42902731+0.j,
                  0.45260232+0.j,
                                   0.44896578+0.j,
                                                    0.41342787+0.j]))
 0.45508956+0.j,
                  0.43671676+0.j,
                                   0.41342787+0.j,
```

In [54]: times[-1]

Out [54]: 6.283185307179586

In [55]: total_time_evo

Out [55]: 6.283185307179586

2.6 joining qutip to my code

NameError Traceback (most recent call last) in () ----> 1 total_time

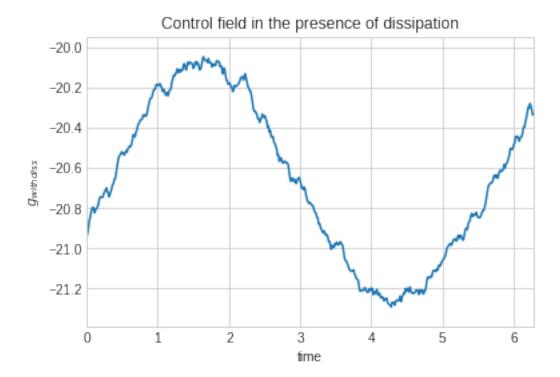
2.7 ##### total_time

```
NameError: name 'total_time' is not defined
In [56]: len(times)
Out[56]: 500
   def terminator(max_iter, time_steps=len(times), total_time= total_time_evo, epsilon= 2pi1):
r"""Brief description of the function"""
xi_initial = result.u[-1, 0, : ]
#1000*random_sample((time_steps,))
dt = (2*pi)/500 #total_time/time_steps
xi_diff, xi_new_vec = updater(xi_initial, dt, epsilon)
for i in range(max_iter):
    if amax(xi_diff) < epsilon**2 :</pre>
        xi_final = xi_new_vec
        break
    else :
        xi_diff, xi_new_vec = updater(xi_new_vec, dt, epsilon)
        print(i)
        print(amax(xi_diff))
xi_final = xi_new_vec
return xi final
In [59]: def terminator(max_iter, time_steps=len(times),
                        total_time=total_time_evo,
                        epsilon=2*pi*1):
             r"""Brief description of the function"""
             xi_initial = result.u[-1, 0, :]
              # 1000*random_sample((time_steps,))
             dt = (2*pi)/500 #total_time/time_steps
             xi_diff, xi_new_vec = updater(xi_initial, dt, epsilon)
             for i in range(max_iter):
                  if amax(xi_diff) < epsilon**2 :</pre>
                      xi_final = xi_new_vec
                      print("Tejas is unlucky")
                      break
                  else :
                      xi_diff, xi_new_vec = updater(xi_new_vec, dt, epsilon)
                      print("Tejas is a good boy")
```

```
print(i)
                                                                   print(amax(xi_diff))
                                         return xi_final
2.8 sub topic 3
In [60]: new_label = [r'$g_{with diss}$']
2.8.1 try
In [61]: xi_opt = terminator(10)
Tejas is unlucky
In [62]: time_steps=len(times)
                             total_time= total_time_evo
                             epsilon= 2*pi*1
In [63]: dt = (2*pi)/500
                            F(xi_opt, dt)
Out[63]: -4.223952468753483
In [64]: L_full_maker(xi_opt, dt)
         Out [64]:
         Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
          0.637
In [65]: ax = axes()
                            ax.plot(times, xi_opt)
                            xi_max = amax(xi_opt) + 0.1
                            xi_min = amin(xi_opt) - 0.1
                            ax.set(xlim=(0, total_time_evo), ylim=(xi_min, xi_max),
                                                   xlabel='time', ylabel= r'$g_{with diss}$',
                                                   title='Control field in the presence of dissipation');
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Control of the cont
      return array(a, dtype, copy=False, order=order)
```

self._points[:, 1] = interval

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968:



2.8.2 try

In [66]: xi_opt = terminator(1000)

Tejas is unlucky

In [68]: dt = (2*pi)/500 $F(xi_opt, dt)$

Out[68]: -4.223952468753483

In [69]: L_full_maker(xi_opt, dt)

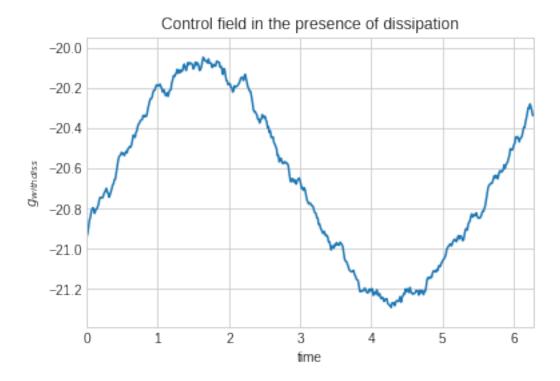
Out[69]:

Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False

$$\begin{pmatrix} 0.363 & (0.228 + 0.007j) & (0.228 - 0.007j) & 0.637 \\ (-0.228 - 0.007j) & (0.004 + 0.011j) & (-0.280 + 1.747 \times 10^{-04}j) & (0.228 + 0.007j) \\ (-0.228 + 0.007j) & (-0.280 - 1.747 \times 10^{-04}j) & (0.004 - 0.011j) & (0.228 - 0.007j) \\ 0.637 & (-0.228 - 0.007j) & (-0.228 + 0.007j) & 0.363 \end{pmatrix}$$

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval



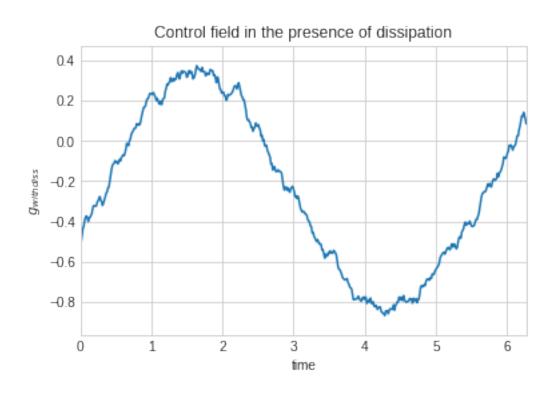
2.8.3 try

Tejas is unlucky

```
In [73]: dt = (2*pi)/500
           F(xi_opt, dt)
Out[73]: -2.2265924567489033
In [74]: L_full_maker(xi_opt, dt)
   Out [74]:
   Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
                                (0.088 - 0.088j)
                                                    (0.088 + 0.088j)
                                                                               0.680
             \begin{array}{lll} (0.243+0.060j) & (-0.051+0.006j) & (0.175+0.265j) & (-0.243-0.060j) \\ (0.243-0.060j) & (0.175-0.265j) & (-0.051-0.006j) & (-0.243+0.060j) \end{array} 
                               (-0.088 + 0.088j) (-0.088 - 0.088j)
                                                                               0.320
In [75]: ax = axes()
           ax.plot(times, xi_opt)
           xi_max = amax(xi_opt) + 0.1
           xi_min = amin(xi_opt) - 0.1
           ax.set(xlim=(0, total_time_evo), ylim=(xi_min, xi_max),
                    xlabel='time', ylabel= r'$g_{with diss}$',
                    title='Control field in the presence of dissipation');
```

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)

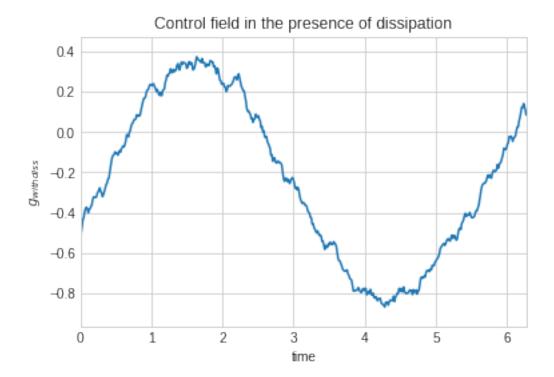
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval



```
In [76]: xi_opt = terminator(10,time_steps=len(times), total_time= total_time_evo,
                                                                               epsilon= ((0.1*2*pi)/(times[-1]))
Tejas is unlucky
In [77]: time_steps=len(times)
                             total_time= total_time_evo
                             epsilon = ((0.1*2*pi)/(times[-1]))
In [78]: dt = (2*pi)/500
                             F(xi_opt, dt)
Out[78]: -2.2265924567489033
In [79]: L_full_maker(xi_opt, dt)
         Out[79]:
         Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
                              \begin{array}{cccc} 0.320 & (0.088-0.088j) & (0.088+0.088j) & 0.680 \\ (0.243+0.060j) & (-0.051+0.006j) & (0.175+0.265j) & (-0.243-0.060j) \\ (0.243-0.060j) & (0.175-0.265j) & (-0.051-0.006j) & (-0.243+0.060j) \\ 0.680 & (-0.088+0.088j) & (-0.088-0.088j) & 0.320 \end{array}
In [80]: ax = axes()
                             ax.plot(times, xi_opt)
                             xi_max = amax(xi_opt) + 0.1
                             xi_min = amin(xi_opt) - 0.1
                             ax.set(xlim=(0, total_time_evo), ylim=(xi_min, xi_max),
                                                    xlabel='time', ylabel= r'$g_{with diss}$',
                                                    title='Control field in the presence of dissipation');
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Control of the cont
      return array(a, dtype, copy=False, order=order)
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968:
```

2.8.4 try

self._points[:, 1] = interval



Out[85]:

Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False

```
 \begin{pmatrix} 0.219 & (0.033-0.027j) & (0.033+0.027j) & 0.781 \\ (-0.038+0.006j) & (-0.065-0.049j) & (0.394+0.015j) & (0.038-0.006j) \\ (-0.038-0.006j) & (0.394-0.015j) & (-0.065+0.049j) & (0.038+0.006j) \\ 0.781 & (-0.033+0.027j) & (-0.033-0.027j) & 0.219 \end{pmatrix}
```

In [86]: len(times)

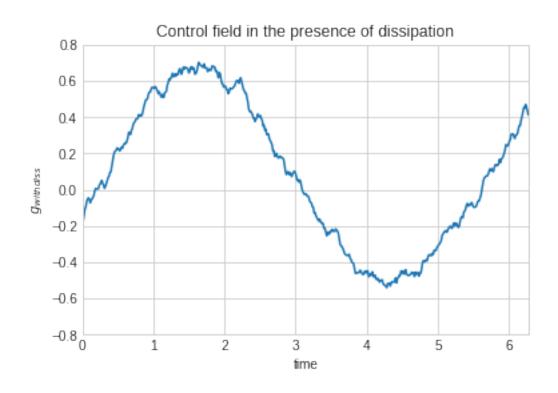
Out[86]: 500

```
In [87]: new_label = [r'$g_{with diss}$']
```

"'plot_grape_control_fields(times, xi_opt / (2 * np.pi), new_label, uniform_axes=True); ValueError Traceback (most recent call last) in () 1 plot_grape_control_fields(times, ----> 2 xi_opt / (2 * np.pi), new_label, uniform_axes=True);

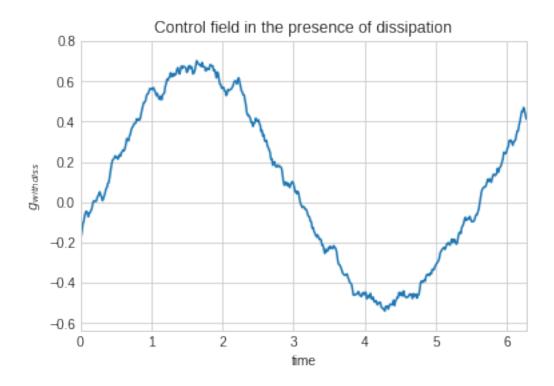
/anaconda3/envs/qutip-env/lib/python3.6/site-packages/qutip/control/grape.py in plot_grape_control_fields(times, u, labels, uniform_axes) 101 import matplotlib.pyplot as plt 102 --> 103 R, J, M = u.shape 104 105 fig, axes = plt.subplots(J, 1, figsize=(8, 2 * J), squeeze=False) ValueError: not enough values to unpack (expected 3, got 1) "'

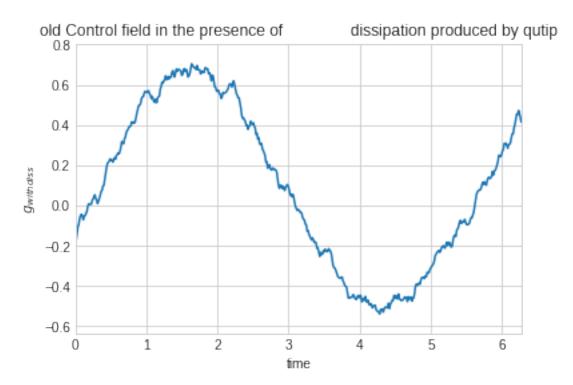
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)



/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Con return array(a, dtype, copy=False, order=order)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval





2.8.6 try

Tejas is unlucky

In [92]: dt = (2*pi)/500 $F(xi_opt, dt)$

Out[92]: -0.9548389887847603

In [93]: L_full_maker(xi_opt, dt)

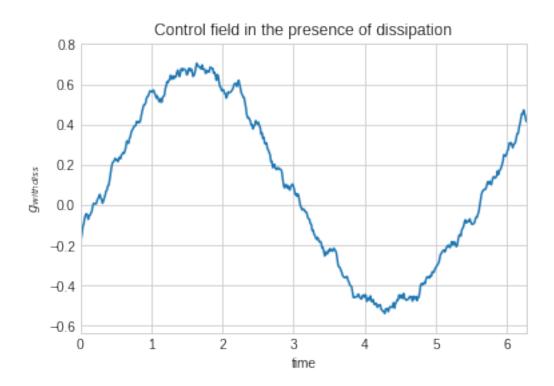
Out [93]:

Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False

$$\begin{pmatrix} 0.219 & (0.035 - 0.028j) & (0.035 + 0.028j) & 0.781 \\ (-0.038 + 0.006j) & (-0.064 - 0.049j) & (0.394 + 0.012j) & (0.038 - 0.006j) \\ (-0.038 - 0.006j) & (0.394 - 0.012j) & (-0.064 + 0.049j) & (0.038 + 0.006j) \\ 0.781 & (-0.035 + 0.028j) & (-0.035 - 0.028j) & 0.219 \end{pmatrix}$$

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval



2.8.7 try

Tejas is unlucky

```
Out [96]: -0.9549811435604786
```

In [97]: L_full_maker(xi_opt, dt)

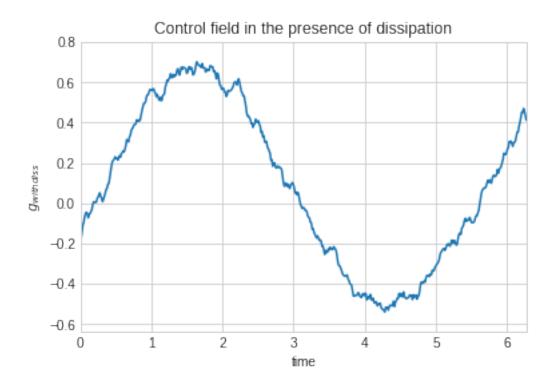
Out [97]:

Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False

$$\begin{pmatrix} 0.219 & (0.033 - 0.027j) & (0.033 + 0.027j) & 0.781 \\ (-0.038 + 0.006j) & (-0.065 - 0.049j) & (0.394 + 0.015j) & (0.038 - 0.006j) \\ (-0.038 - 0.006j) & (0.394 - 0.015j) & (-0.065 + 0.049j) & (0.038 + 0.006j) \\ 0.781 & (-0.033 + 0.027j) & (-0.033 - 0.027j) & 0.219 \end{pmatrix}$$

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)

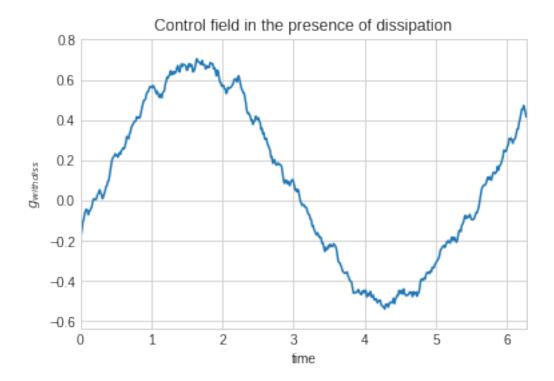
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval



```
2.8.8 try
```

self._points[:, 1] = interval

```
In [99]: xi_opt = terminator(10**4,time_steps=len(times), total_time= total_time_evo,
                             epsilon= ((0.1*2*pi)/(10**4)))
Tejas is unlucky
In [100]: dt = (2*pi)/500
            F(xi_opt, dt)
Out[100]: -0.9548389887847603
In [101]: L_full_maker(xi_opt, dt)
   Out[101]:
   Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False
          \begin{array}{ccc} 0.219 & (0.035-0.028j) & (0.035+0.028j) \\ (-0.038+0.006j) & (-0.064-0.049j) & (0.394+0.012j) \\ (-0.038-0.006j) & (0.394-0.012j) & (-0.064+0.049j) \\ 0.781 & (-0.035+0.028j) & (-0.035-0.028j) \end{array}
                                                                              0.781
                                                                         (0.038 - 0.006i)
                                                                         (0.038 + 0.006j)
In [102]: ax = axes()
            ax.plot(times, xi_opt)
            xi_max = amax(xi_opt) + 0.1
            xi_min = amin(xi_opt) - 0.1
            ax.set(xlim=(0, total_time_evo), ylim=(xi_min, xi_max),
                     xlabel='time', ylabel= r'$g_{with diss}$',
                    title='Control field in the presence of dissipation');
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Con
  return array(a, dtype, copy=False, order=order)
/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968:
```



2.8.9 try

Tejas is unlucky

In [104]: dt = (2*pi)/500 $F(xi_opt, dt)$

Out[104]: -0.9548286833510965

In [105]: L_full_maker(xi_opt, dt)

Out[105]:

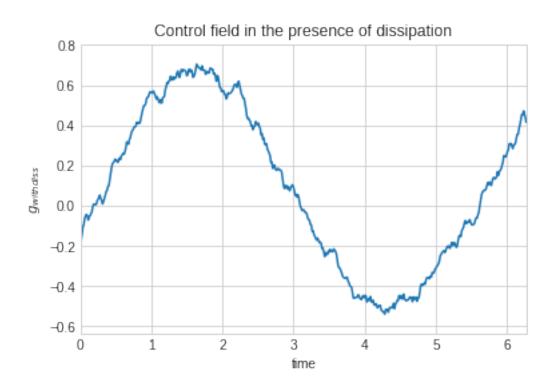
Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False

$$\begin{pmatrix} 0.219 & (0.035 - 0.028j) & (0.035 + 0.028j) & 0.781 \\ (-0.038 + 0.006j) & (-0.064 - 0.049j) & (0.394 + 0.012j) & (0.038 - 0.006j) \\ (-0.038 - 0.006j) & (0.394 - 0.012j) & (-0.064 + 0.049j) & (0.038 + 0.006j) \\ 0.781 & (-0.035 + 0.028j) & (-0.035 - 0.028j) & 0.219 \end{pmatrix}$$

In [106]: ax = axes()
 ax.plot(times, xi_opt)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval



2.8.10 try

```
In [107]: xi_{opt} = terminator(10**4,time_steps=10**3, total_time= total_time_evo, epsilon= ((0.1*2*pi)/(10**3)))
```

Tejas is unlucky

```
In [108]: dt = (2*pi)/(10**3)#(2*pi)/500
# probaly happened because of hard coding of dt inside terminator
# must try it again after changing that
F(xi_opt, dt)
```

```
Out[108]: -4.870058606858147
```

```
In [109]: L_full_maker(xi_opt, dt)
```

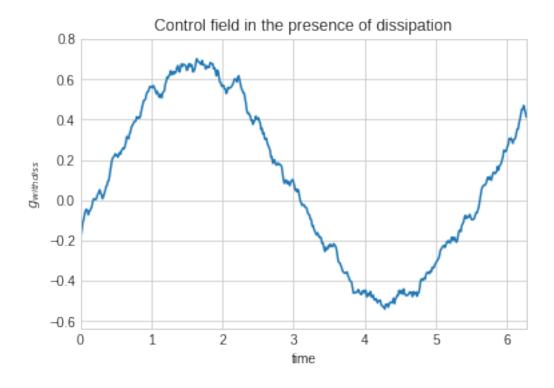
Out[109]:

Quantum object: dims = [[2, 2], [2, 2]], shape = (4, 4), type = oper, isherm = False

$$\begin{pmatrix} 0.755 & (-0.333 - 0.092j) & (-0.333 + 0.092j) & 0.245 \\ (-0.256 + 0.074j) & (-0.402 + 0.137j) & (0.146 - 0.056j) & (0.256 - 0.074j) \\ (-0.256 - 0.074j) & (0.146 + 0.056j) & (-0.402 - 0.137j) & (0.256 + 0.074j) \\ 0.245 & (0.333 + 0.092j) & (0.333 - 0.092j) & 0.755 \end{pmatrix}$$

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval



2.9 APS stuff

2.9.1 infidelity function tryouts

2.10 ##### ket2bra

```
NameError Traceback (most recent call last) in () ----> 1 ket2bra
NameError: name 'ket2bra' is not defined
```

```
In [113]: (sigmax()).matrix_element(qone, qzero)
Out[113]: (1+0j)
In [114]: abs((sigmax()).matrix_element(qone, qzero))
Out[114]: 1.0
In [115]: abs(2 + 3j)
Out[115]: 3.605551275463989
In [116]: abs(3 + 4j)
Out[116]: 5.0
In [117]: def infidelity_to_one(U):
              r"""infidelity to state one"""
              fidelity = (abs(U.matrix_element(qone, qzero)))**2
              infidelity = 1 - fidelity
              return infidelity
In [118]: infidelity_to_one(sigmax())
          # 1 - abs((sigmax()).matrix_element(qone, qzero))
          #1 - 1 = 0
```

```
Out[118]: 0.0
   result.u, result.u but lindbladian evolution, xi_opt
In [119]: qone.overlap(qzero)
Out[119]: 0j
In [120]: qzero.overlap(qzero)
Out[120]: (1+0j)
In [121]: qone.overlap(qone)
Out[121]: (1+0j)
In [122]: def infidelity_to_state(psi):
               r"""infidelity to state one"""
               fidelity = (abs(qone.overlap(psi)))**2
               infidelity = 1 - fidelity
               return infidelity
In [123]: infidelity_to_state(qzero)
Out[123]: 1.0
In [124]: infidelity_to_state(qone)
Out[124]: 0.0
In [125]: #mesolve
2.10.1 state building
In [126]: H_no_diss = [H_0, [H_1, result.u[-1, 0, :] ]]
           grape_no_diss = mesolve(H_no_diss, qzero, times, c_ops=[], e_ops=[],
                                     args={}, options=None,
                                     progress_bar=EnhancedTextProgressBar() )
                    0.60s*] Elapsed 0.60s / Remaining 00:00:00:00[*******57%*
 Total run time:
In [127]: len(grape_no_diss.states)
Out[127]: 500
In [128]: Lin
   Out[128]:
   Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True
                                      \left(\begin{array}{cc} 1.0 & 0.0 \\ 0.0 & -1.0 \end{array}\right)
```

] Elap

```
In [129]: sqrt(gamma)
Out[129]: 0.31622776601683794
In [130]: c_ops_tejas = sqrt(gamma)*Lin
          c_ops_tejas
   Out[130]:
   Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True
                                 \begin{pmatrix} 0.316 & 0.0 \\ 0.0 & -0.316 \end{pmatrix}
In [131]: H_{diss} = [H_0, [H_1, result.u[-1, 0, :]]]
          grape_diss = mesolve(H_no_diss, qzero, times, c_ops=[c_ops_tejas], e_ops=[],
                                    args={}, options=None,
                                   progress_bar=EnhancedTextProgressBar() )
Total run time:
                    0.39s*] Elapsed 0.39s / Remaining 00:00:00:00
In [132]: len(grape_diss.states)
Out[132]: 500
In [133]: H_diss_optimized = [H_0, [H_1, xi_opt ]]
          grape_diss_optimized = mesolve(H_no_diss, qzero, times, c_ops=[c_ops_tejas],
                                           e_ops=[], args={}, options=None,
                                           progress bar=TextProgressBar() )
                    0.01s. Est. time left: 00:00:00:00
10.0%. Run time:
20.0%. Run time:
                   0.02s. Est. time left: 00:00:00:00
30.0%. Run time:
                    0.03s. Est. time left: 00:00:00:00
40.0%. Run time:
                    0.04s. Est. time left: 00:00:00:00
50.0%. Run time:
                   0.05s. Est. time left: 00:00:00:00
60.0%. Run time:
                   0.06s. Est. time left: 00:00:00:00
70.0%. Run time:
                    0.06s. Est. time left: 00:00:00:00
80.0%. Run time:
                    0.07s. Est. time left: 00:00:00:00
90.0%. Run time:
                    0.08s. Est. time left: 00:00:00:00
Total run time:
                   0.10s
In [134]: len(grape_diss_optimized.states)
Out[134]: 500
```

2.10.2 states list to fidelity list

```
In [135]: infidelity_to_state_vec = vectorize(infidelity_to_state)
In [136]: infid_grape_no_diss = infidelity_to_state_vec(grape_no_diss.states)
In [137]: '''fid_grape_diss = infidelity_to_state_vec(grape_diss.states)
                                                    Traceback (most recent call last)
          TypeError
          <ipython-input-101-fbabc06eff84> in <module>()
          ----> 1 fid_grape_diss = infidelity_to_state_vec(grape_diss.states)
          /anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/lib/function_base.py in
             2753
                              vargs.extend([kwargs[_n] for _n in names])
             2754
          -> 2755
                          return self._vectorize_call(func=func, args=vargs)
             2756
             2757
                      def _qet_ufunc_and_otypes(self, func, args):
          /anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/lib/function_base.py in
             2823
                              res = func()
             2824
                          else:
          -> 2825
                              ufunc, otypes = self._qet_ufunc_and_otypes(func=func, args=args)
             2826
             2827
                              # Convert args to object arrays first
          /anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/lib/function_base.py in
             2783
             2784
                              inputs = [arg.flat[0] for arg in args]
          -> 2785
                              outputs = func(*inputs)
             2786
             2787
                              # Performance note: profiling indicates that -- for simple
          <ipython-input-96-32321f8d8a33> in infidelity_to_state(psi)
                1 def infidelity_to_state(psi):
                     r"""infidelity to state one"""
                2
          ---> 3
                     fidelity = (abs(qone.overlap(psi)))**2
                      infidelity = 1 - fidelity
                4
                      return infidelity
                5
          /anaconda3/envs/qutip-env/lib/python3.6/site-packages/qutip/qobj.py in overlap(self,
             1486
                                      return (self.data.H * state.data)[0, 0]
             1487
          -> 1488
                          raise TypeError("Can only calculate overlap for state vector Qobjs")
             1489
             1490
                      def eigenstates(self, sparse=False, sort='low',
          TypeError: Can only calculate overlap for state vector Qobjs
```

IIIIOut[137]: 'fid_grape_diss = infidelity_to_state_vec(grape_diss.states)\nTypeError fid_grape_no_diss = infidelity_to_state_vec(grape_no_diss.states) In [138]: fidelity(sigmax(), sigmax()) Out[138]: 1.999999999999996 In [139]: zero_dm = ket2dm(qzero) zero_dm Out[139]: Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True $\left(\begin{array}{cc} 0.0 & 0.0 \\ 0.0 & 1.0 \end{array}\right)$ In [140]: one_dm = ket2dm(qone) one_dm Out[140]: Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True $\left(\begin{array}{cc} 1.0 & 0.0 \\ 0.0 & 0.0 \end{array}\right)$ In [141]: fidelity(zero_dm, zero_dm) Out[141]: 1.0 In [142]: fidelity(zero_dm, one_dm) Out[142]: 0.0 In [143]: fidelity(one_dm, zero_dm) Out[143]: 0.0 In [144]: grape_no_diss.states[5] Out[144]: Quantum object: dims = [[2], [1]], shape = (2, 1), type = ket $\left(\begin{array}{c}
(0.008 - 4.378 \times 10^{-05}j) \\
(0.999 + 0.031j)
\end{array}\right)$

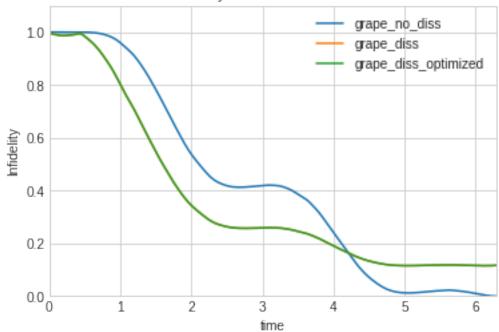
In [145]: grape_diss.states[5]

```
Out[145]:
   Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True
                     \left(\begin{array}{cc} 6.496\times 10^{-05} & (0.008-2.952\times 10^{-04}j) \\ (0.008+2.952\times 10^{-04}j) & 1.000 \end{array}\right)
In [146]: grape_diss.states[7]
   Out[146]:
   Quantum object: dims = [[2], [2]], shape = (2, 2), type = oper, isherm = True
                      \left( \begin{array}{cc} 8.740 \times 10^{-05} & (0.009 - 5.120 \times 10^{-04} j) \\ (0.009 + 5.120 \times 10^{-04} j) & 1.000 \end{array} \right) 
In [147]: fidelity(grape_diss.states[7], one_dm)
Out[147]: 0.00934875656096058
In [148]: #0.0122.347Œ10**05j)
In [149]: def infidelity_tejas(dm, d=2):
                r"""Brief description of the function"""
                 infid = 1 - fidelity(one dm, dm)
                 return infid
In [150]: infid_dm_vec = vectorize(infidelity_tejas)
In [151]: infid_grape_diss = infid_dm_vec(grape_diss.states)
In [152]: len(infid_grape_diss)
Out[152]: 500
In [153]: infid_grape_diss_optimized = infid_dm_vec(grape_diss_optimized.states)
In [154]: len(infid_grape_diss_optimized)
Out[154]: 500
2.10.3 plots
In [155]: ax = axes()
            ax.plot(times, infid_grape_no_diss, label='grape_no_diss')
            ax.plot(times, infid_grape_diss, label='grape_diss')
            ax.plot(times, infid grape_diss_optimized, label='grape_diss_optimized')
            \#ax.plot(x, cos(x), ':b', label='cos(x)')'-g',
            #ax.axis('equal')
            ax.legend()
            ax.set(xlim=(times[0],times[-1]), ylim=(0, 1.1),
```

title='Infidelity as a function of time ');

xlabel='time', ylabel='Infidelity',

Infidelity as a function of time





5

6

10

0.8

0.6

0.4

0.2

0.0

Infidelity

```
In [157]: ax = axes()
    ax.plot(times, infid_grape_no_diss, label='grape_no_diss')
    #ax.plot(times, infid_grape_diss, label='grape_diss')
    ax.plot(times, infid_grape_diss_optimized, label='grape_diss_optimized')
    #ax.plot(x, cos(x), ':b', label='cos(x)')'-g',
    #ax.axis('equal')
    ax.legend()

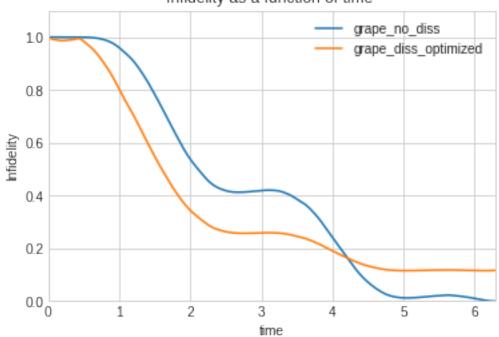
ax.set(xlim=(times[0],times[-1]), ylim=(0, 1.1),
    xlabel='time', ylabel='Infidelity',
```

title='Infidelity as a function of time ');

3

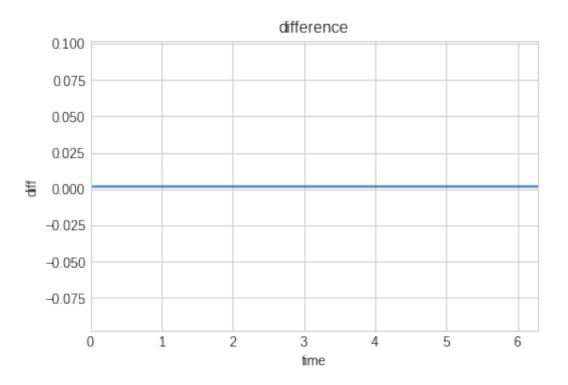
time

Infidelity as a function of time



/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Correturn array(a, dtype, copy=False, order=order)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval

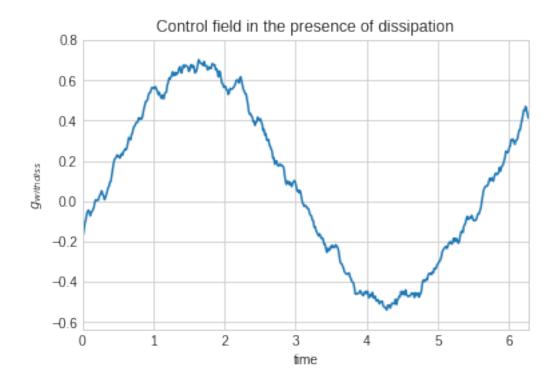


```
In [159]: ax = axes()
          ax.plot(times, xi_opt)
          xi_max = amax(xi_opt) + 0.1
          xi_min = amin(xi_opt) - 0.1

ax.set(xlim=(0, total_time_evo), ylim=(xi_min, xi_max),
          xlabel='time', ylabel= r'$g_{with diss}$',
          title='Control field in the presence of dissipation');
```

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/numpy/core/numeric.py:501: Con return array(a, dtype, copy=False, order=order)

/home/tejas/anaconda3/envs/qutip-env/lib/python3.6/site-packages/matplotlib/transforms.py:968: self._points[:, 1] = interval



2.11 Versions