

COMP27112

Computer
Graphics
and
Image Processing

8: Rendering (2)

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Recap

- We now have a local illumination model

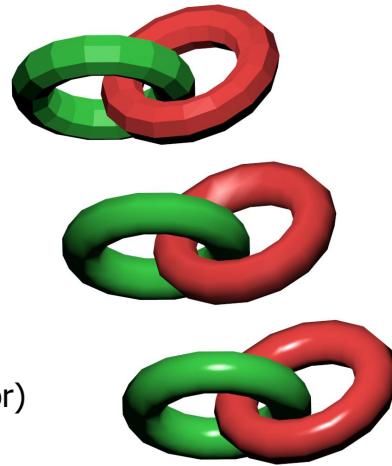
$$I_R = k_{aR}I_{aR} + \frac{I_{pR}}{d'} \left[k_{dR}(\hat{\mathbf{N}} \cdot \hat{\mathbf{L}}) + k_s(\hat{\mathbf{R}} \cdot \hat{\mathbf{V}})^n \right]$$

- How do we use it for a triangle mesh?

Shading a surface

- We'll look at three shading methods:

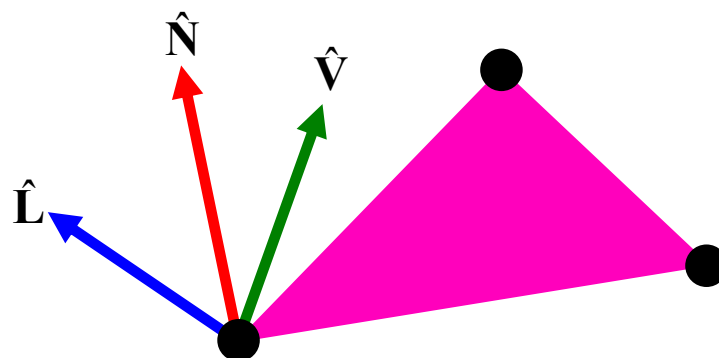
1. Flat
(aka constant)
2. Gouraud
(aka intensity)
3. Phong
(aka normal-vector)



Vic Baker

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Flat (aka constant) shading



- This is the simplest approach
- We compute colour C at one vertex and use it for all pixels in the polygon

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Flat (aka constant) shading



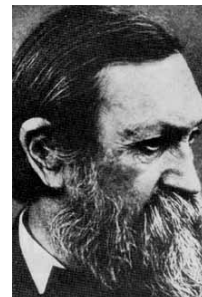
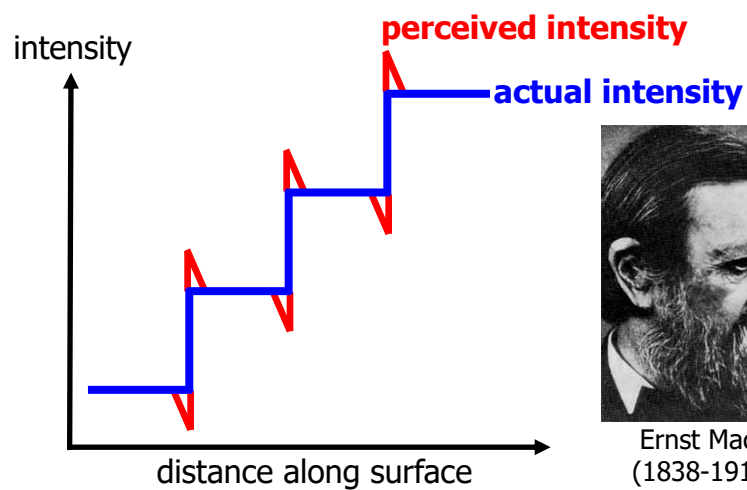
Henri Gouraud

- Each polygon is uniformly coloured according to its orientation
- We clearly see the mesh
- This is made worse by the Mach Band effect

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Mach banding

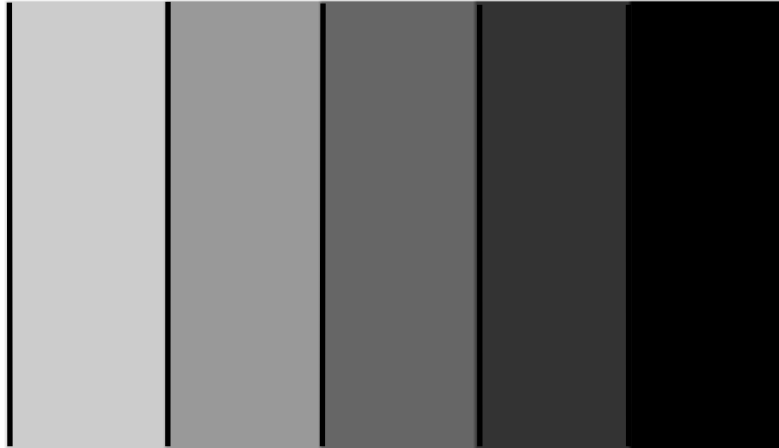
- Our eyes are very good at finding edges



Ernst Mach
(1838-1916)

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Mach banding



Here, we see separate strips, each with a different intensity

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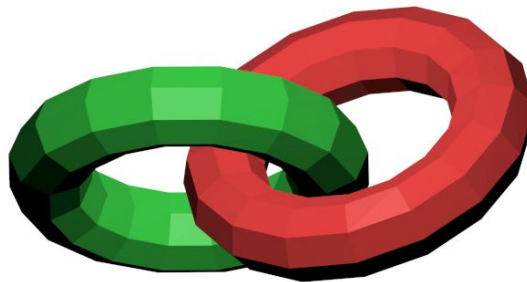
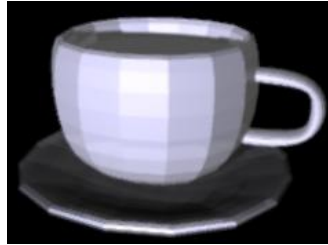
Mach banding



Now, we still see separate strips, but the edges between them stand out

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Examples of flat shading

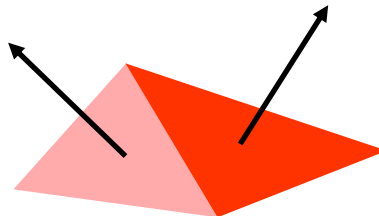


Vic Baker

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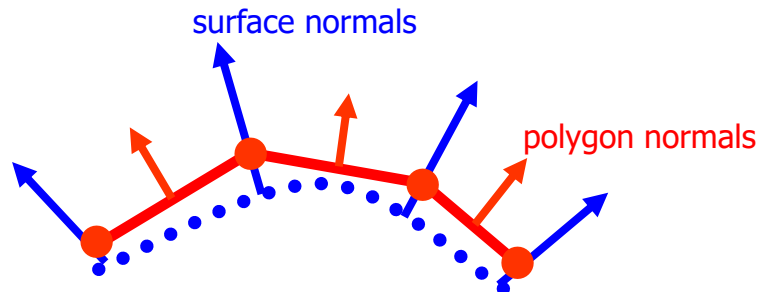
Gouraud (aka intensity) shading

- Invented by Henri Gouraud in 1971
- Gouraud shading uses interpolation, to smooth out the discontinuities between polygons



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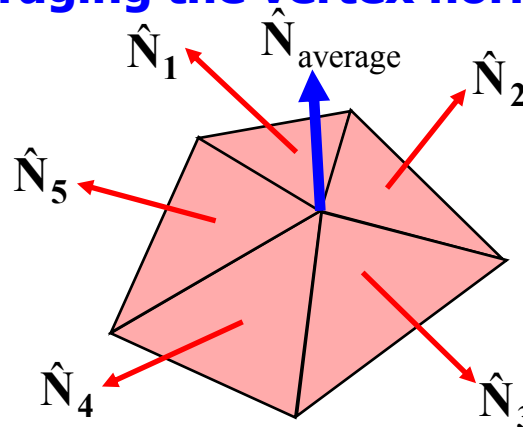
Approximating a surface



- We can approximate the normals of the underlying "surface" the polygons are modelling
- by averaging the normals where polygons share vertices

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Averaging the vertex normals

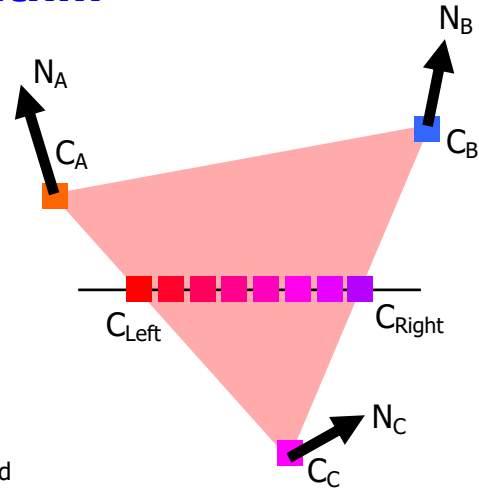


$$\hat{N}_{\text{average}} = \frac{\hat{N}_1 + \hat{N}_2 + \hat{N}_3 + \hat{N}_4 + \hat{N}_5}{|\hat{N}_1 + \hat{N}_2 + \hat{N}_3 + \hat{N}_4 + \hat{N}_5|}$$

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Gouraud algorithm

- compute average vertex normals at A, B and C
- compute pixel colours C_A , C_B , C_C
- for each scanline {
 - average colour C_{Left} from C_A and C_C
 - average colour C_{Right} from C_B and C_C
 - average between C_{Left} and C_{Right} along the scanline

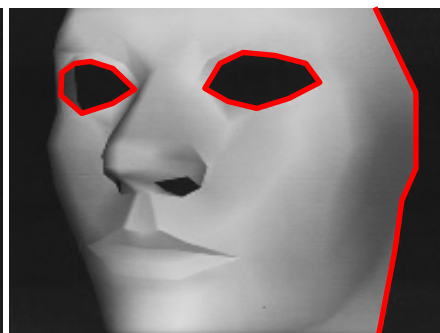


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Gouraud results



flat shading



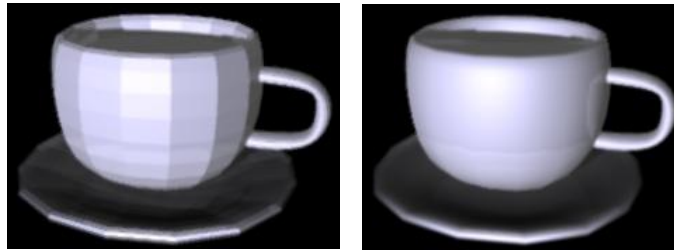
Gouraud shading

Henri Gouraud

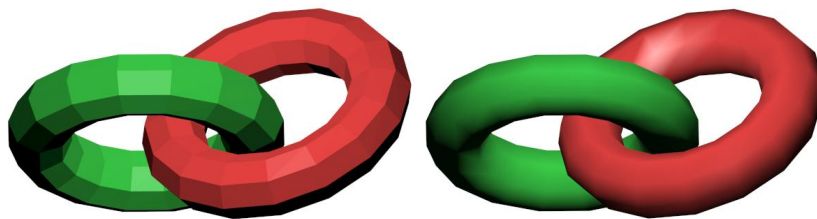
- Mesh now appears smooth
- But notice the silhouette edges, still polygonal

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Flat shading versus Gouraud

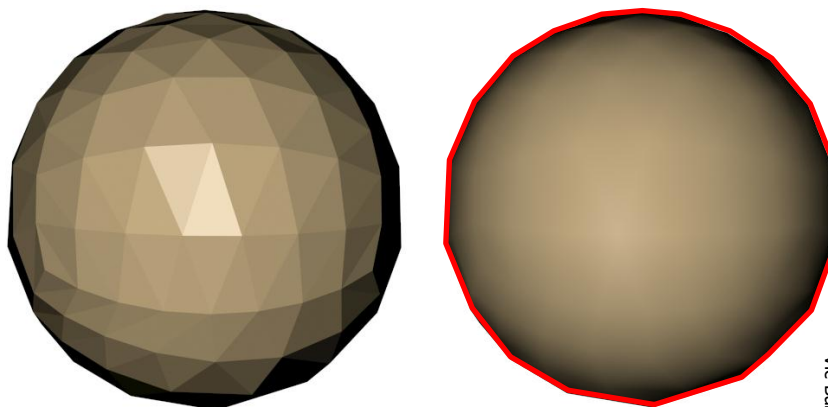


Vic Baker



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Flat shading versus Gouraud



Vic Baker

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Implementing Gouraud

- We need to optimise the computation as much as possible
- For each scanline we compute the colour increment between pixels:

```
deltaCol= (CRight - CLeft) / (XRight - XLeft);  
Col= CLeft;  
for (x= XLeft; X <= XRight; x++) {  
    TestAndSetPixel(x, y, Col);  
    Col= Col + deltaCol;  
}
```

- Similarly, we can also optimise by computing C_{Right} and C_{Left} incrementally

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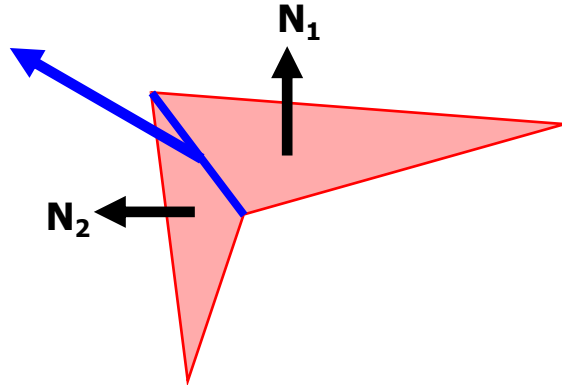
Gouraud shading: problems

- While it's fast and efficient, the method has drawbacks:
 - Specular highlights may be distorted or averaged away altogether (because Gouraud shading averages between **vertex** colours)
 - Mach banding may still be visible

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Gouraud shading: problems

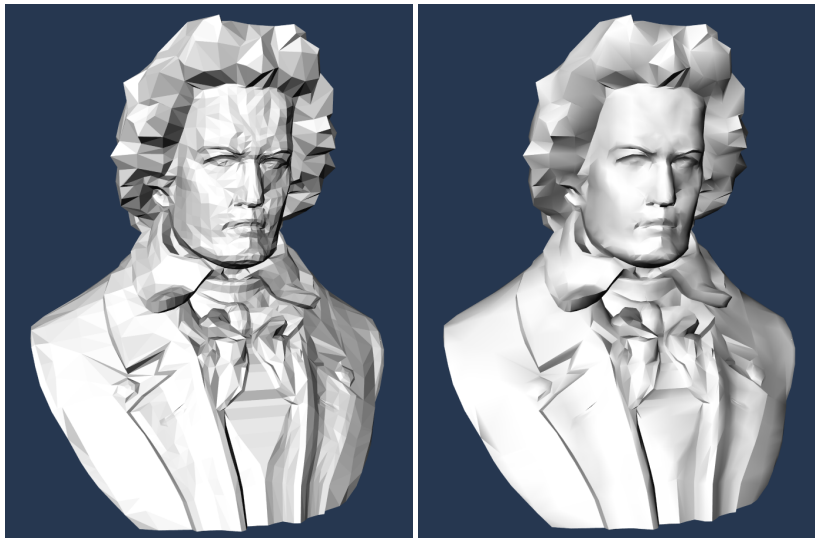
- Sometimes edges are "shaded away"



- Edge must be tagged in data structure to avoid interpolation across it

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Tagged edges to stop interpolation



Simon Gibson

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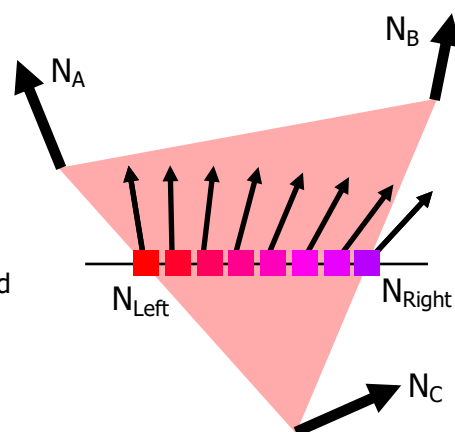
Phong (aka normal vector) interpolation

- Instead of interpolating colours, Phong suggested interpolating normal vectors
- We interpolate the normal vector along the scanline
- Compute illumination model for every pixel

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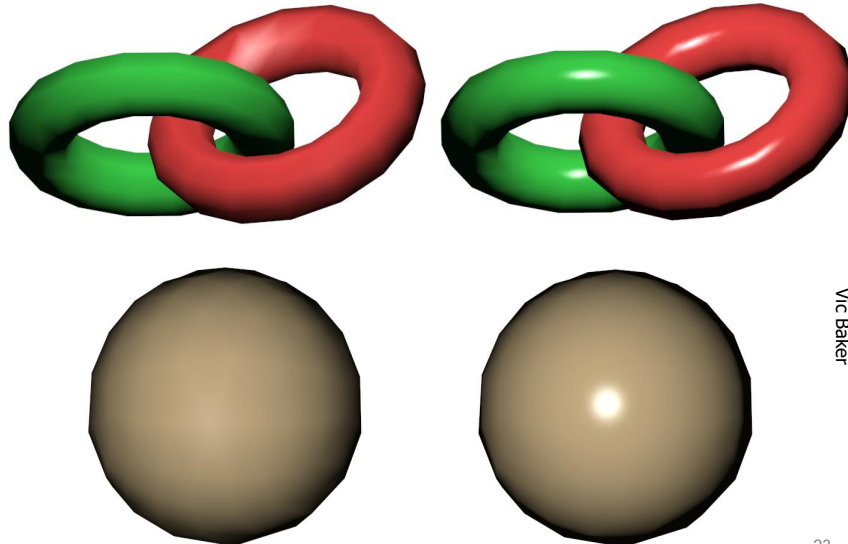
Phong (aka normal vector) interpolation

- for each scanline {
 - compute average normal \mathbf{N}_{Left} from \mathbf{N}_A and \mathbf{N}_C
 - compute average normal $\mathbf{N}_{\text{Right}}$ from \mathbf{N}_B and \mathbf{N}_C
 - average between \mathbf{N}_{Left} and $\mathbf{N}_{\text{Right}}$ along the scanline, and compute colour C using illumination model
- }



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Gouraud shading versus Phong



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Comparison of shading methods



flat

Gouraud

Phong

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Rendering expense

- Roughly, our local illumination model takes about **60** floating-point operations to compute a colour for a pixel
- For a Gouraud-shaded triangle, that's **180** flops, then about **2** per pixel
- For a Phong-shaded triangle, that's **60 flops for every pixel**

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