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Department of Computer Science & Engineering

SUBJECT: *Automata and Compiler Design*

Subject Code: **22PC1CB303**

***Topic Name: Phases of a compiler
III year-I sem, sec: B and D***

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<Web link of your created resource if any>

Syllabus



Semantics: Syntax directed translation, S-attributed and L-attributed grammars, Intermediate code – abstract syntax tree, translation of simple statements and control flow statements.

Agenda



4.1

- 1.Syntax-Directed Definitions and Translation schemes**
- 2.Synthesized and inherited attributes**
- 3.SDD for desk calculator**
- 4.Annotated parse tree**
- 5.Attributed grammar**
- 6.SDD for inherited attributes**
- 7.Dependency graph**
- 8.Abstract syntax trees and DAG**
- 9. Syntax tree creation using SDD**

Agenda



4.2

1. Intermediate code generation - benefits
2. Intermediate code representations – syntax tree, DAG, post fix notation and Three address code forms
3. Types of three address code
4. Implementation of three address code-quadruples, tripuls and indirect triples
5. Three address code for programming language constructs
 - 5.1 Three address code for assignment statement using SDD
 - 5.2 Three address code for Boolean expression using SDD
 - 5.3 Three address code for control flow statements using SDD

Syntax-Directed Definitions and Translation Schemes



- We can associate information with a language construct by attaching attributes to the grammar symbols.
- A syntax directed definition specifies the values of attributes by associating semantic rules with the grammar productions.
- Values of these attributes are evaluated by the **semantic rules** associated with the production rules.
- Evaluation of these semantic rules:
 - may generate intermediate codes
 - may put information into the symbol table
 - may perform type checking
 - may issue error messages
 - may perform some other activities
 - in fact, they may perform almost any activities.
- An attribute may hold almost any thing.
a string, a number, a memory location, a complex record.

Syntax-Directed Definitions and Translation Schemes



- When we associate semantic rules with productions, we use two notations:
 - **Syntax-Directed Definitions**
 - **Translation Schemes**
- **Syntax-Directed Definitions:**
 - give high-level specifications for translations
 - hide many implementation details such as order of evaluation of semantic actions.
 - We associate a production rule with a set of semantic actions, and we do not say when they will be evaluated.
- **Translation Schemes:**
 - indicate the order of evaluation of semantic actions associated with a production rule.
 - In other words, translation schemes give a little bit information about implementation details.

Syntax-Directed Definitions



- A syntax-directed definition is a generalization of a context-free grammar in which:
 - Each grammar symbol is associated with a set of attributes.
 - This set of attributes for a grammar symbol is partitioned into two subsets called **synthesized** and **inherited** attributes of that grammar symbol.
 - Each production rule is associated with a set of semantic rules.
- **SYNTHESIZED attributes** are computed from the values of the CHILDREN of a node in the parse tree.
- **INHERITED attributes** are computed from the attributes of the parents and/or siblings of a node in the parse tree.

Synthesized Attributes



A syntax directed definition that uses only synthesized attributes is said to be an **S-attributed** definition

A parse tree for an S-attributed definition can be annotated by evaluating semantic rules for attributes

Syntax-Directed Definition for Desk calculator -- Example



Production

$L \rightarrow E \text{ return}$

$E \rightarrow E_1 + T$

$E \rightarrow T$

$T \rightarrow T_1 * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow \text{digit}$

Semantic Rules

$\text{print}(E.\text{val})$

$E.\text{val} = E_1.\text{val} + T.\text{val}$

$E.\text{val} = T.\text{val}$

$T.\text{val} = T_1.\text{val} * F.\text{val}$

$T.\text{val} = F.\text{val}$

$F.\text{val} = E.\text{val}$

$F.\text{val} = \text{digit}.\text{lexval}$

- Symbols E, T, and F are associated with a synthesized attribute *val*.
- The token **digit** has a synthesized attribute *lexval* (it is assumed that it is evaluated by the lexical analyzer).

Annotated Parse Tree



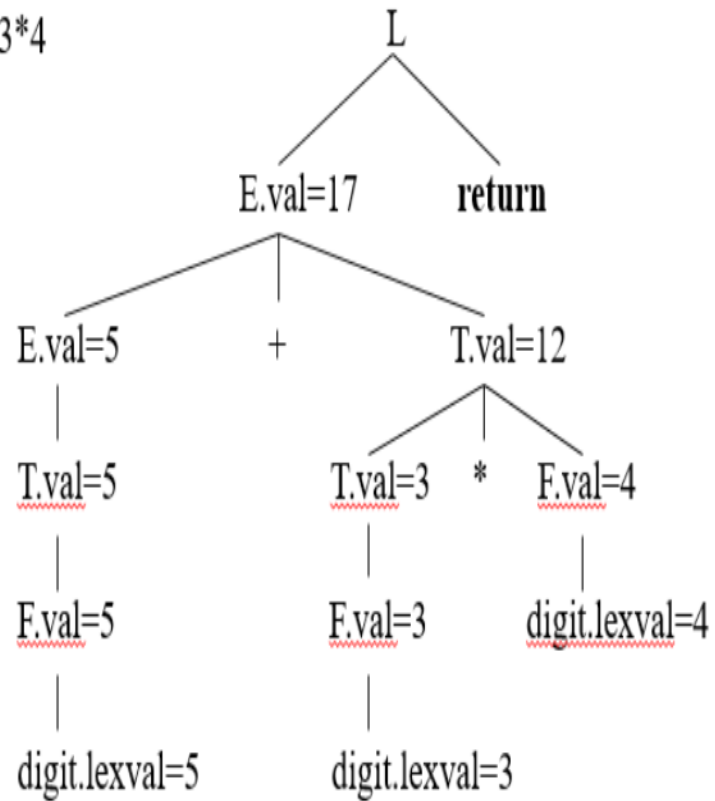
- A parse tree showing the values of attributes at each node is called an **annotated parse tree**.
- The process of computing the attributes values at the nodes is called **annotating** (or **decorating**) of the parse tree.

Parse tree for $5 + 3 * 5$



Annotated Parse Tree

Input: $5+3*4$



Syntax-Directed Definition – Inherited Attributes



Production

$D \rightarrow T L$

$T \rightarrow \text{int}$

$T \rightarrow \text{real}$

$L \rightarrow L_1 \text{ id}$

$L \rightarrow \text{id}$

Semantic Rules

$L.in = T.type$

$T.type = \text{integer}$

$T.type = \text{real}$

$L_1.in = L.in, \text{ addtype}(\text{id.entry}, L.in)$

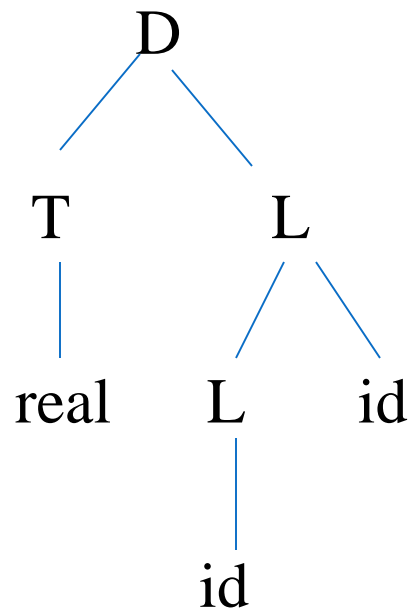
$\text{addtype}(\text{id.entry}, L.in)$

- Symbol T is associated with a synthesized attribute *type*.
- Symbol L is associated with an inherited attribute *in*.

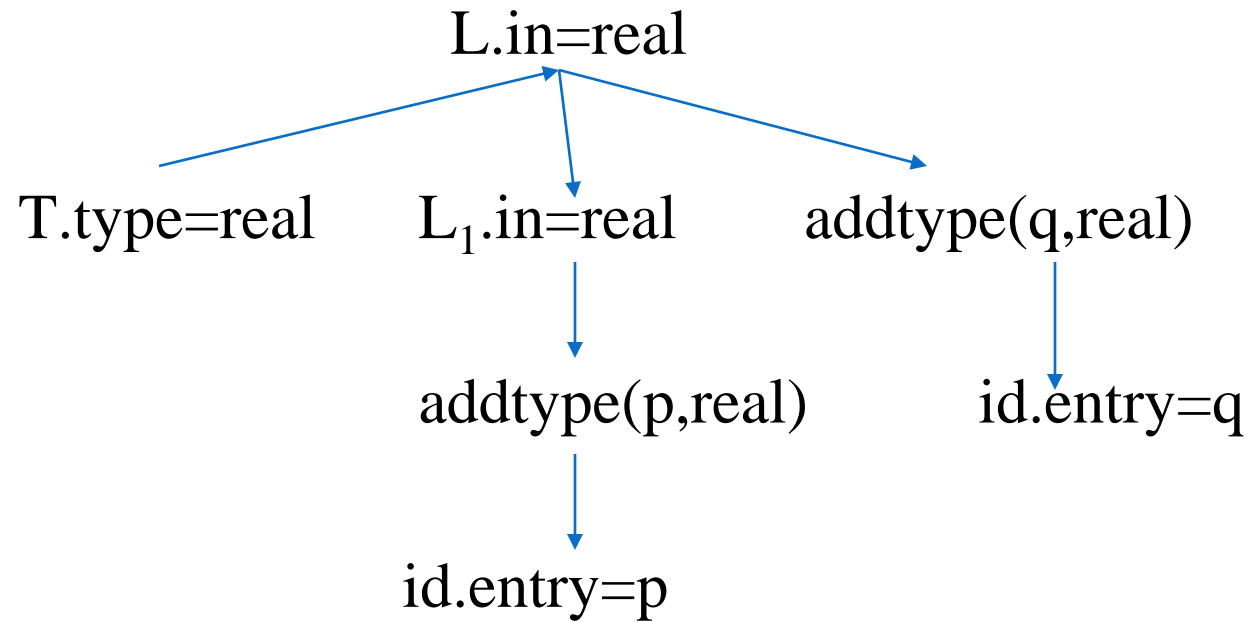
A Dependency Graph – Inherited Attributes



Input: real p q



parse tree



dependency graph

S-Attributed Definitions



- We will look at two sub-classes of the syntax-directed definitions:
 - **S-Attributed Definitions:** only synthesized attributes used in the syntax-directed definitions.
 - **L-Attributed Definitions:** in addition to synthesized attributes, we may also use inherited attributes in a restricted fashion.
- To implement S-Attributed Definitions and L-Attributed Definitions are easy (we can evaluate semantic rules in a single pass during the parsing).
- Implementations of S-attributed Definitions are a little bit easier than implementations of L-Attributed Definitions

Abstract Syntax tree



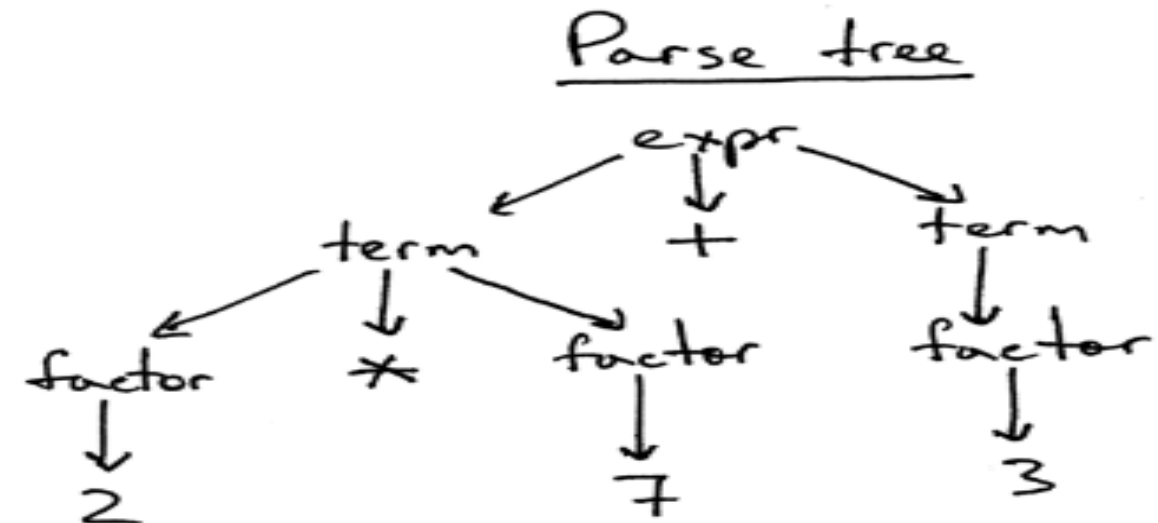
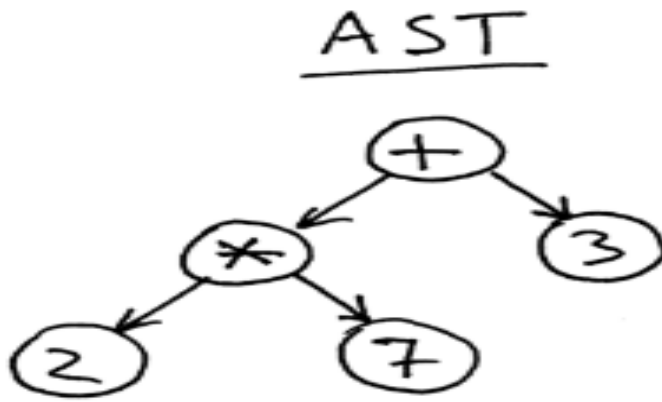
- ❑ Condensed form of parse tree
- ❑ useful for representing language constructs.
- ❑ A **concrete syntax** tree represents the source text exactly in parsed form.
- ❑ The **abstract syntax tree** is the result of simplifying the concrete syntax tree
- ❑ Uses of AST
- ❑ AST is used in Intermediate code representation(IR)

Abstract Syntax tree-definition

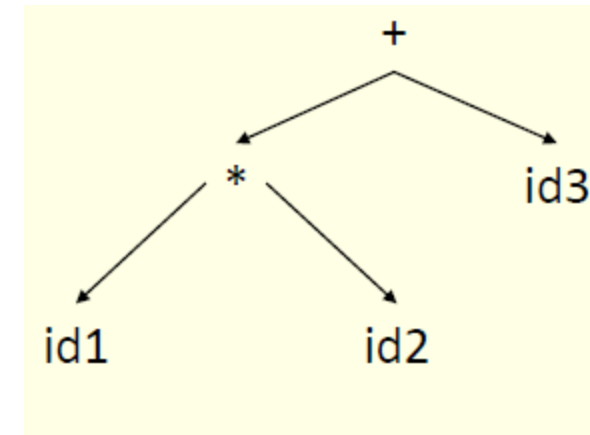
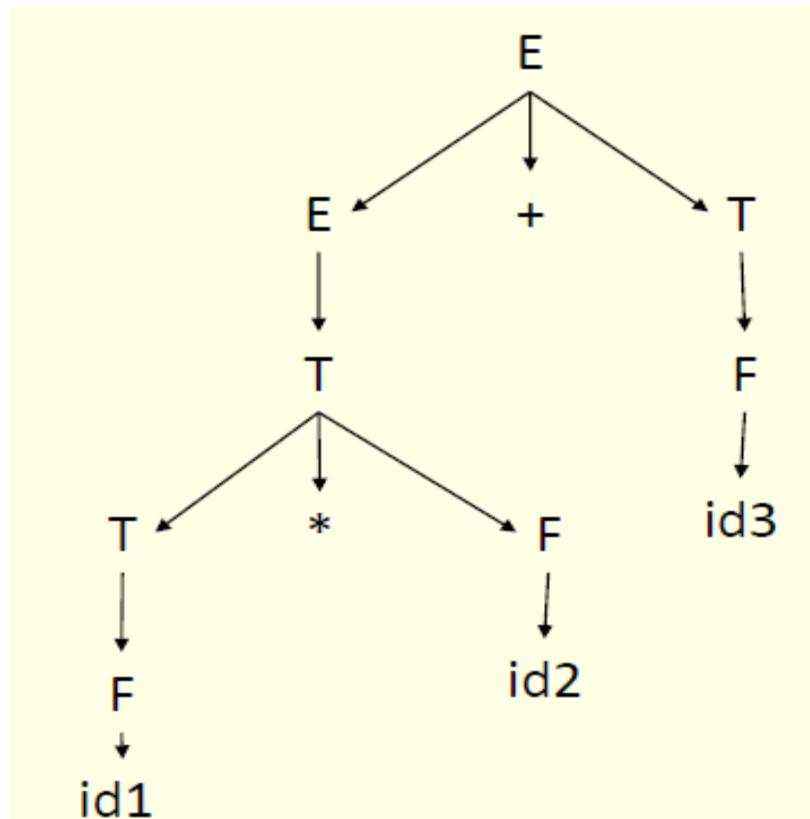


An **abstract syntax tree** (AST) is a tree that represents the abstract syntactic structure of a language construct where each **interior node** and the **root node** represents **an operator**, and the **children of the node** represent the **operands** of that operator.


$2 * 7 + 3$



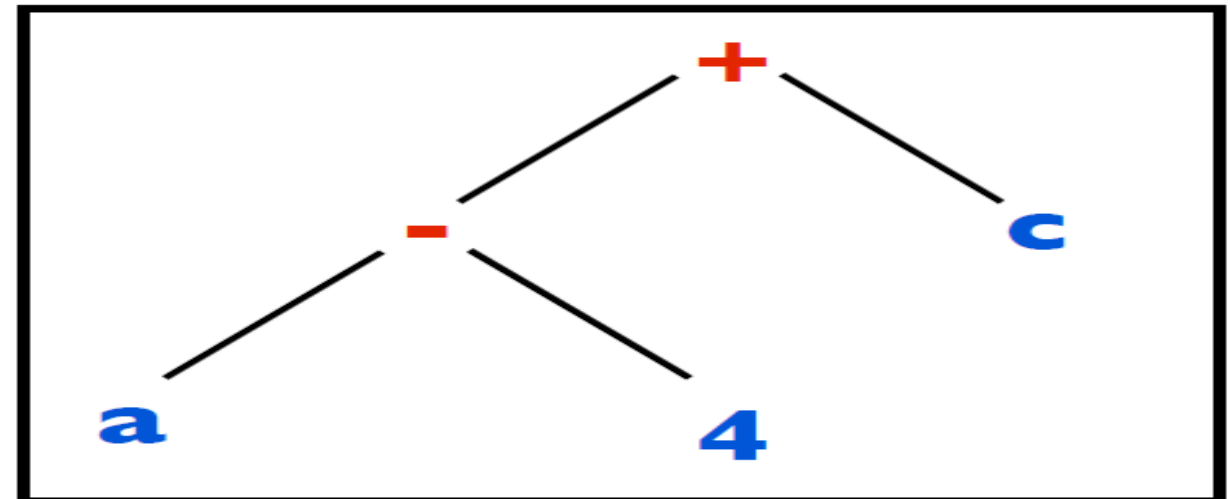
Abstract Syntax tree ...



Abstract Syntax tree ...

PRODUCTION	SEMANTIC RULES
1) $E \rightarrow E_1 + T$	
2) $E \rightarrow E_1 - T$	
3) $E \rightarrow T$	
4) $T \rightarrow (E)$	
5) $T \rightarrow \text{id}$	
6) $T \rightarrow \text{num}$	

a-4+c



Constructing Abstract Syntax Tree for expression



Each node can be represented as a record

- *operators*: one field for operator, remaining fields ptrs to operands `mknode(op,left,right)`
- *identifier*: one field with label id and another ptr to symbol table `mkleaf(id,entry)`
- *number*: one field with label num and another to keep the value of the number `mkleaf(num,val)`

Example

The following sequence of function calls creates a parse tree for $a - 4 + c$

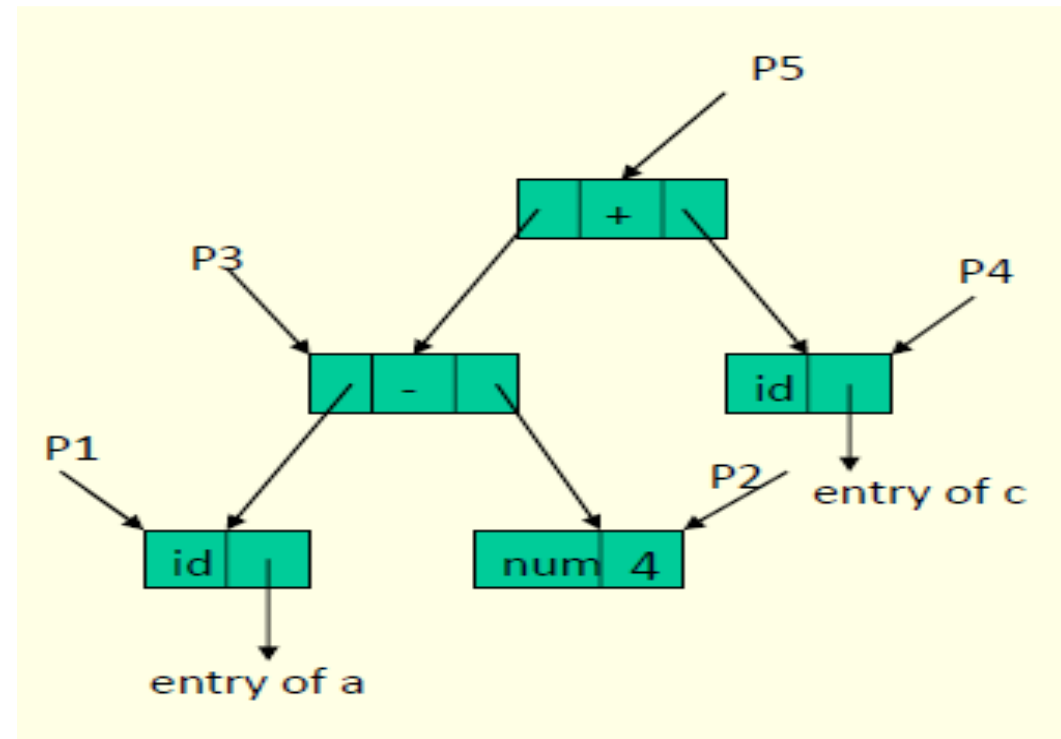
$P1 = \text{mkleaf}(\text{id}, \text{entry.a})$

$P2 = \text{mkleaf}(\text{num}, 4)$

$P3 = \text{mknode}(-, P1, P2)$

$P4 = \text{mkleaf}(\text{id}, \text{entry.c})$

$P5 = \text{mknode}(+, P3, P4)$



A syntax directed definition for constructing syntax tree or DAG(directed acyclic graph)



Production

$E \rightarrow E1 + T$

$E \rightarrow T$

$T \rightarrow T1 * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow id$

$F \rightarrow num$

Semantic Rule

$E.ptr = \text{mknode}(+, E1.ptr, T.ptr)$

$E.ptr = T.ptr$

$T.ptr := \text{mknode}(*, T1.ptr, F.ptr)$

$T.ptr := F.ptr$

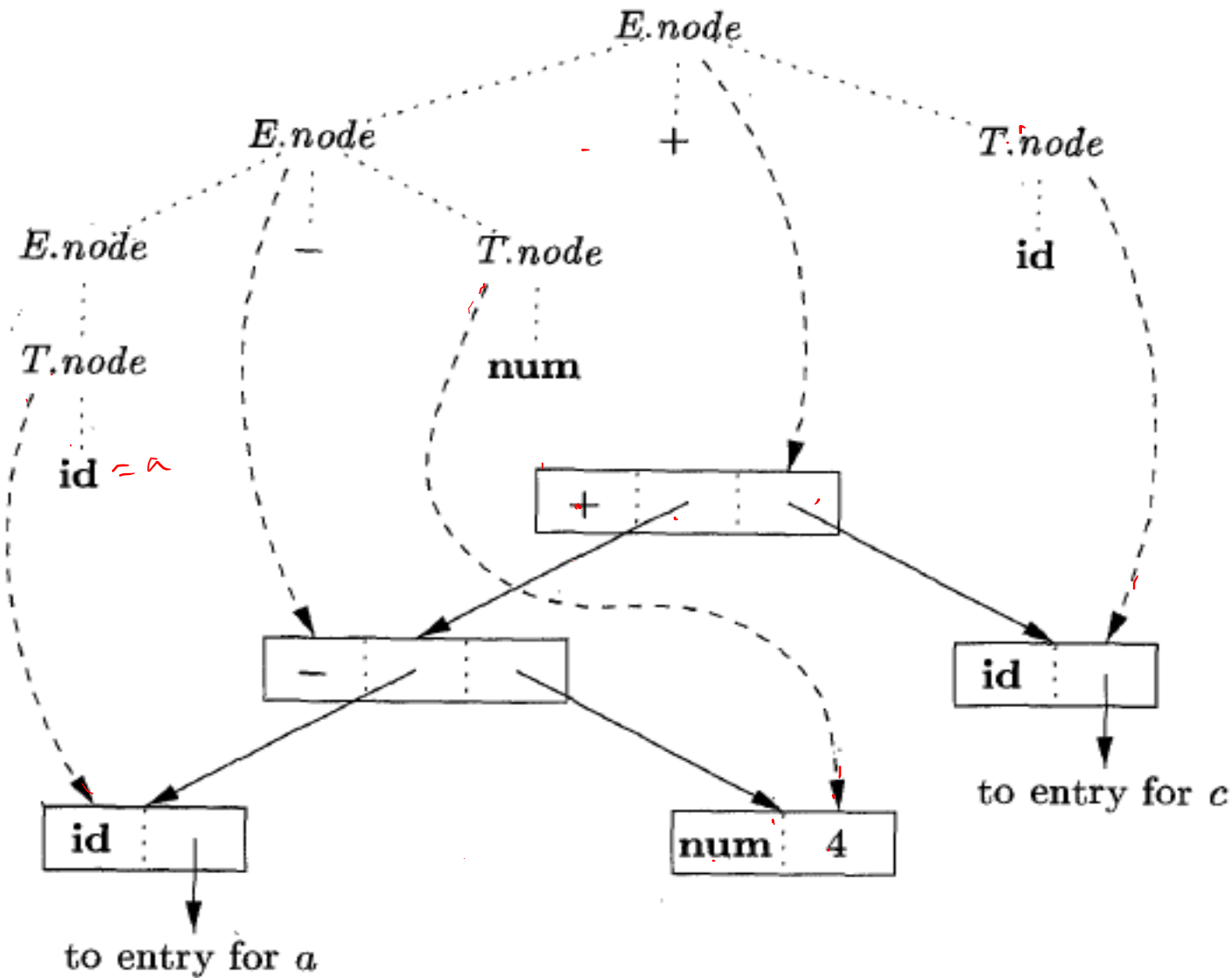
$F.ptr := E.ptr$

$F.ptr := \text{mkleaf}(id, \text{entry.id})$

$F.ptr := \text{mkleaf}(num, val)$

Syntax Tree Using SDD

for $a - 4 + c$



A syntax directed definition for constructing DAG(directed acyclic graph)



Production

$E \rightarrow E1 + T$

$E \rightarrow T$

$T \rightarrow T1 * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow id$

$F \rightarrow num$

Semantic Rule

$E.ptr = \text{mknode}(+, E1.ptr, T.ptr)$

$E.ptr$ = $T.ptr$

$T.ptr := \text{mknode}(*, T1.ptr, F.ptr)$

$T.ptr := F.ptr$

$F.ptr := E.ptr$

$F.ptr := \text{mkleaf}(id, \text{entry.id})$

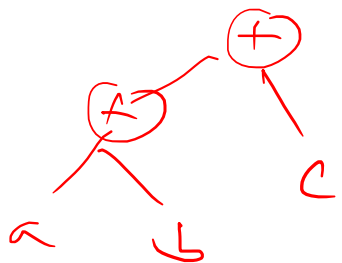
$F.ptr := \text{mkleaf}(num, val)$

Draw the DAG for the expression

$a + a * (b + c) + (b + c) * d$

Monday
(18/01/2021)

for $a + b + c$



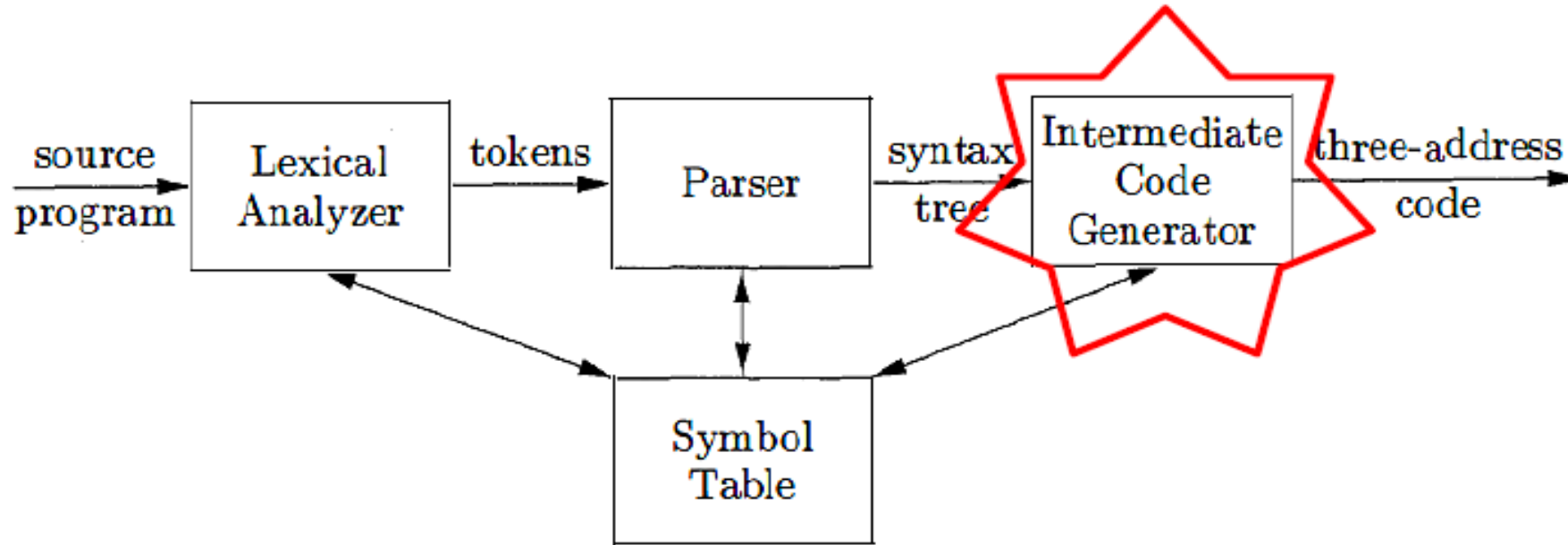
Instructions

$p_1 = \text{mkleaf}(\text{id}, \text{entry}.a)$
 $p_2 = \text{mkleaf}(\text{id}, \text{entry}.b)$
 $p_3 = \text{mknode}(+, p_1, p_2)$
 $p_4 = \text{mkleaf}(\text{id}, \text{entry}.c)$
 $p_5 = \text{mknode}(+, p_3, p_4)$

- 1) $p_1 = \text{Leaf}(\text{id}, \text{entry}.a)$
- 2) $p_2 = \text{Leaf}(\text{id}, \text{entry}.a) = p_1$
- 3) $p_3 = \text{Leaf}(\text{id}, \text{entry}.b)$
- 4) $p_4 = \text{Leaf}(\text{id}, \text{entry}.c)$
- 5) $p_5 = \text{Node}('-', p_3, p_4)$
- 6) $p_6 = \text{Node}('*', p_1, p_5)$
- 7) $p_7 = \text{Node}('+', p_1, p_6)$
- 8) $p_8 = \text{Leaf}(\text{id}, \text{entry}.b) = p_3$
- 9) $p_9 = \text{Leaf}(\text{id}, \text{entry}.c) = p_4$
- 10) $p_{10} = \text{Node}('-', p_3, p_4) = p_5$
- 11) $p_{11} = \text{Leaf}(\text{id}, \text{entry}.d)$
- 12) $p_{12} = \text{Node}('*', p_5, p_{11})$
- 13) $p_{13} = \text{Node}('+', p_7, p_{12})$

Steps for constructing the DAG

Intermediate code generation



The front end translates a source program into an intermediate representation from which the back end generates target code.

Intermediate code generation



Benefits of using a machine-independent intermediate form are:

1. Retargeting is facilitated. That is, a compiler for a different machine can be created by attaching a back end for the new machine to an existing front end.
2. A machine-independent code optimizer can be applied to the intermediate representation.

Intermediate code representations



Three ways of intermediate representation:

- ☐ Syntax tree and DAG
- ☐ Postfix notation
- ☐ Three address code

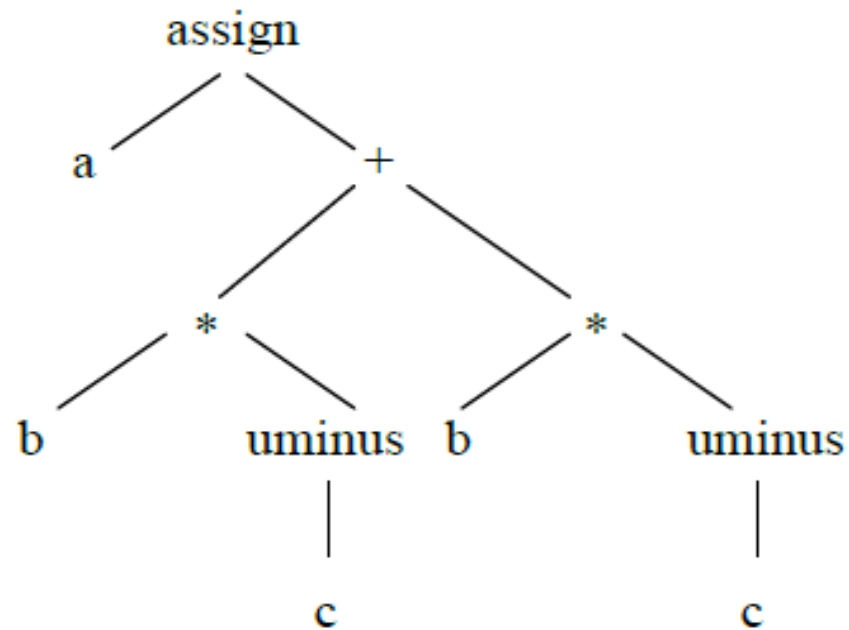
Syntax tree and DAG



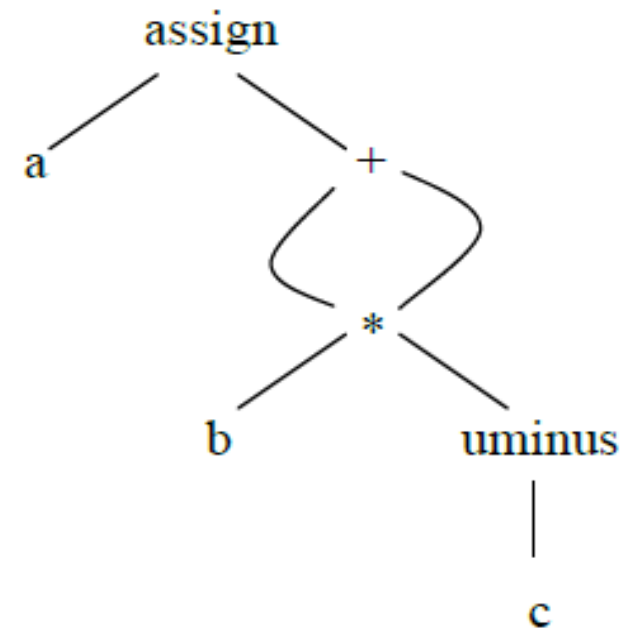
A syntax tree depicts the natural hierarchical structure of a source program. A dag (Directed Acyclic Graph) gives the same information but in a more compact way because common subexpressions are identified.

A syntax tree and dag for the assignment statement $a := b * -c + b * -c$ are as follows:

Syntax tree and DAG



(a) Syntax tree



(b) Dag

Postfix notation



Postfix notation is a linearized representation of a syntax tree; it is a list of the nodes of the tree in which a node appears immediately after its children.

The postfix notation for the syntax tree given above is

a b c uminus * b c uminus * + assign

Three-Address Code:

Three-address code is a sequence of statements of the general form

$$x := y \text{ op } z$$

where x , y and z are names, constants, or compiler-generated temporaries; op stands for any operator, such as a fixed- or floating-point arithmetic operator, or a logical operator on boolean valued data. Thus a source language expression like $x + y * z$ might be translated into a sequence

$$t1 := y * z$$

$$t2 := x + t1$$

where $t1$ and $t2$ are compiler-generated temporary names

Three-address code corresponding to the syntax tree and DAG the statement : $a := b * -c + b * -c$



$t_1 := -c$

$t_2 := b * t_1$

$t_3 := -c$

$t_4 := b * t_3$

$t_5 := t_2 + t_4$

$a := t_5$

(a) Code for the syntax tree

$t_1 := -c$

$t_2 := b * t_1$

$t_5 := t_2 + t_2$

$a := t_5$

(b) Code for the dag

Types of Three-Address Statements



Assignments:

Two possible forms:

1. \square $x := y \text{ op } z$ where op is a binary arithmetic or logical operation,
2. \square $x := \text{op } y$ where op is a unary operation (minus, negation)

(1) $x = y \text{ op } z$

(2) $x = \text{op } z$

(3) $x = y$

(4) $\text{goto } L$

(5) $\text{if } x \text{ relop } y \text{ goto } L$

Copy statements:

3. \square They have the form $x := y$

Un-conditional jumps:

4. \square They have the form $\text{goto } L$ where L is a symbolic label of a statement.

Conditional jumps:

5. \square They have the form $\text{if } x \text{ relop } y \text{ goto } L$ where statement L is executed if x and y are in relation relop .

Types of Three-Address Statements



Procedure calls:

They have the form

param x_1

param x_2

•
•
•

param x_n

call p, n corresponding to the procedure $\text{call } p(x_1, x_2, \dots, x_n)$

Return statement:

They have the form **return y** where **y** representing a returned value is optional.

Types of Three-Address Statements



Indexed assignments:

- They have the form $x := y[i]$ or $x[i] := y$

Address assignments:

- They have the form $x := \&y$ which sets x to the location of y .

Pointer assignments:

- They have the form
 - $x := *y$ where y is a pointer and which sets x to the value pointed to by y
 - $*x := y$ which changes the location of the value pointed to by x .

Data structures to hold Three address code
OR



Three address code implementation Techniques

Three address code implementations methods:

- ☐ Quadruples
- ☐ Triples
- ☐ Indirect triples

Three address code implementation Techniques



In **quadruples** representation, each instruction is split into the following 4 different fields : **op**, **arg1**, **arg2**, **result**

The **op** field is used for storing the internal code of the operator. The **arg1** and **arg2** fields are used for storing the two operands used. The **result** field is used for storing the result of the expression.

For example: $x = y + z$

- ☐ Op (+)
- ☐ Arg1 (y)
- ☐ Arg2 (z)
- ☐ Result (x)

Triples-

In triples representation,

- ☐ References to the instructions are made.
- ☐ Temporary variables are not used.

Indirect Triples-

- ❑ This representation is an enhancement over triples representation.
- ❑ It uses an additional instruction array to list the pointers to the triples in the desired order.
- ❑ Thus, instead of position, pointers are used to store the results.
- ❑ It allows the optimizers to easily re-position the sub-expression for producing the optimized code.

Translate the following expression to quadruple, triple and indirect triple: $a + b \times c / e \uparrow f + b \times a$



Three Address Code for the given expression is-

$T1 = e \uparrow f$
 $T2 = b \times c$
 $T3 = T2 / T1$
 $T4 = b \times a$
 $T5 = a + T3$
 $T6 = T5 + T4$

Quadruple Representation-

Location	Op	Arg1	Arg2	Result
(0)	\uparrow	e	f	T1
(1)	\times	b	c	T2
(2)	/	T2	T1	T3
(3)	\times	b	a	T4
(4)	+	a	T3	T5
(5)	+	T5	T4	T6

Triple Representation-

Location	Op	Arg1	Arg2
(0)	↑	e	f
(1)	x	b	c
(2)	/	(1)	(0)
(3)	x	b	a
(4)	+	a	(2)
(5)	+	(4)	(3)

Indirect Triple Representation-

	Statement
35	(0)
36	(1)
37	1869-9391
38	(3)
39	(4)
40	(5)

Location	Op	Arg1	Arg2
(0)	↑	e	f
(1)	x	b	e
(2)	/	(1)	(0)
(3)	x	b	a
(4)	+	a	(2)
(5)	+	(4)	(3)

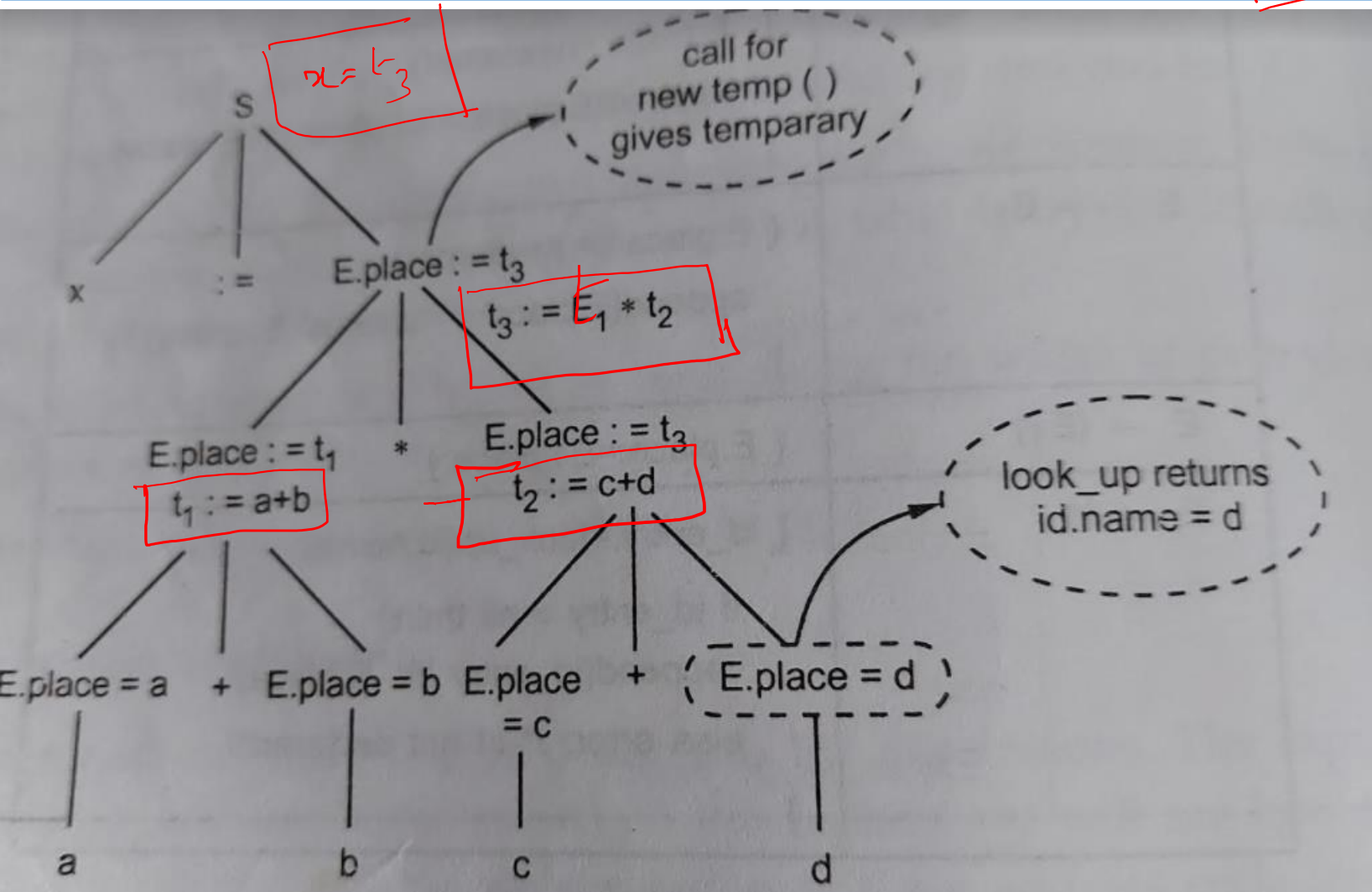
Homework problem :



Implement a three address code for $a = b * -c + b * -c$ using quadrapuples,triples and indirect tripples

Production Rule	Semantic actions
$S \rightarrow id := E$	<pre> { id_entry:=look_up(id.name); if id_entry \neq nil then gen (id_entry ':=' E.place) else error; /* id not declared*/ }</pre>
$E \rightarrow E_1 + E_2$	<pre> { E.place:=newtemp(); gen (E.place ':=' E₁.place '+' E₂.place) }</pre>
$E \rightarrow E_1 * E_2$	<pre> { E.place:=newtemp(); gen (E.place ':=' E₁.place '*' E₂.place) }</pre>
$E \rightarrow - E_1$	<pre> { E.place := newtemp(); gen (E.place ':=' 'uminus' E₁.place) }</pre>
$E \rightarrow (E_1)$	<pre> { E.place:=E₁.place }</pre>
$E \rightarrow id$	<pre> { id_entry:=look_up(id.name); if id_entry \neq nil then E.place := id_entry else error; /* id not declared*/ }</pre>

Three address code for $x = (a+b) * (c+d)$



3 AC

$t_1 = a+b$
 $t_2 = c+d$
 $t_3 = t_1 * t_2$
 $x = t_3$

Three address code(3AC) for Boolean expressions using SDD



Production

$E \rightarrow E1 \text{ or } E2$ ✓

$E \rightarrow E1 \text{ and } E2$ ✓

$E \rightarrow \text{not } E1$ ✓

$E \rightarrow (E1)$ ✓

$E \rightarrow id1 \text{ relop } id2$ ✓

$E \rightarrow \text{true}$ ✓

$E \rightarrow \text{false}$ ✓

Semantic

```
{ E.place := newtemp;  
  gen( E.place ':=' E1.place 'or' E2.place ) }
```

```
{ E.place := newtemp;  
  gen( E.place ':=' E1.place 'and' E2.place ) }
```

```
{ E.place := newtemp;  
  gen( E.place ':=' 'not' E1.place ) }
```

```
{ E.place := E1.place }
```

```
{ E.place := newtemp;  
  gen ( 'if' id1.place relop.op id2.place 'goto' nextstat + 3); gen ( E.place ':=' '0' );  
  gen ( 'goto' nextstat + 2);
```

```
  gen( E.place ':=' '1' ) }
```

```
{ E.place := newtemp;  
  gen ( E.place ':=' '1' ) }
```

```
{ E.place := newtemp;  
  gen ( E.place ':=' '0' ) }
```


Translation scheme using a numerical representation for booleans

$E \rightarrow E1 \text{ or } E2$	<pre>{ E.place := newtemp; emit(E.place ':=' E1.place 'or' E2.place) }</pre>
$E \rightarrow E1 \text{ and } E2$	<pre>{ E.place := newtemp; emit(E.place ':=' E1.place 'and' E2.place) }</pre>
$E \rightarrow \text{not } E1$	<pre>{ E.place := newtemp; emit(E.place ':=' 'not' E1.place) }</pre>
$E \rightarrow (E1)$	<pre>{ E.place := E1.place }</pre>
$E \rightarrow id1 \text{ relop } id2$	<pre>{ E.place := newtemp; emit('if' id1.place relop.op id2.place 'goto' nextstat + 3); emit(E.place ':=' '0'); emit('goto' nextstat + 2); emit(E.place ':=' '1') }</pre>
$E \rightarrow \text{true}$	<pre>{ E.place := newtemp; emit(E.place ':=' '1') }</pre>
$E \rightarrow \text{false}$	<pre>{ E.place := newtemp; emit(E.place ':=' '0') }</pre>

Example: translating $(a < b \text{ or } c < d \text{ and } e < f)$ into 3AC



Three address code

$E \rightarrow id_1 \text{ relop } id_2$

- $\{E.place := newtemp();$
- $gen("if", id_1.place, relop.op, id_2.place, "goto", nextstat+3);$
- $gen(E.place, ":", "0");$
- $gen("goto", nextstat+2);$
- $gen(E.place, ":", "1");\}$

```
100: if a < b goto 103
101: t1 := 0
102: goto 104
103: t1 := 1 /* true */
104: if c < d goto 107
105: t2 := 0 /* false */
106: goto 108
107: t2 := 1
108: if e < f goto 111
109: t3 := 0
110: goto 112
111: t3 := 1
112: t4 := t2 and t3
113: t3 := t1 or t4
```

Handwritten annotations in red:

- $a < b$ points to line 100.
- $c < d$ points to line 104.
- $e < f$ points to line 108.
- t_1 points to line 103.
- t_2 points to line 106.
- t_3 points to line 110.
- and points to line 112.
- or points to line 113.

Generate a three address code for $x = a \&\& b || c$

Three address code for flow of control statements



Production	Semantic Rules
$S \rightarrow \text{if } E \text{ then } S1$	$E.\text{true} := \text{newlabel}()$ $E.\text{false} := s.\text{next}$ $S1.\text{next} := s.\text{next}$ $S.\text{code} := E.\text{code} \text{gen}(E.\text{true} ":") s1.\text{code}$
$S \rightarrow \text{if } E \text{ then } S1 \text{ else } S2$	$E.\text{true} := \text{newlabel}()$ $E.\text{false} := \text{newlabel}()$ $S1.\text{next} := s.\text{next}$ $S2.\text{next} := s.\text{next}$ $S.\text{code} := E.\text{code} \text{gen}(E.\text{true} ":") s1.\text{code} $ $\quad \text{gen}(\text{"goto" } S.\text{next}) $ $\quad \text{gen}(E.\text{false} ":") s2.\text{code}$
$S \rightarrow \text{while } E \text{ then } S1$	$S.\text{begin} := \text{newlabel}()$ $E.\text{true} := \text{newlabel}()$ $E.\text{false} := s.\text{next}$ $S1.\text{next} := S.\text{begin}$ $S.\text{code} := \text{gen}(S.\text{begin} ":") E.\text{code} $ $\quad \text{gen}(E.\text{true} ":") s1.\text{code} $ $\quad \text{gen}(\text{"goto" } S.\text{begin})$

flow of control statements

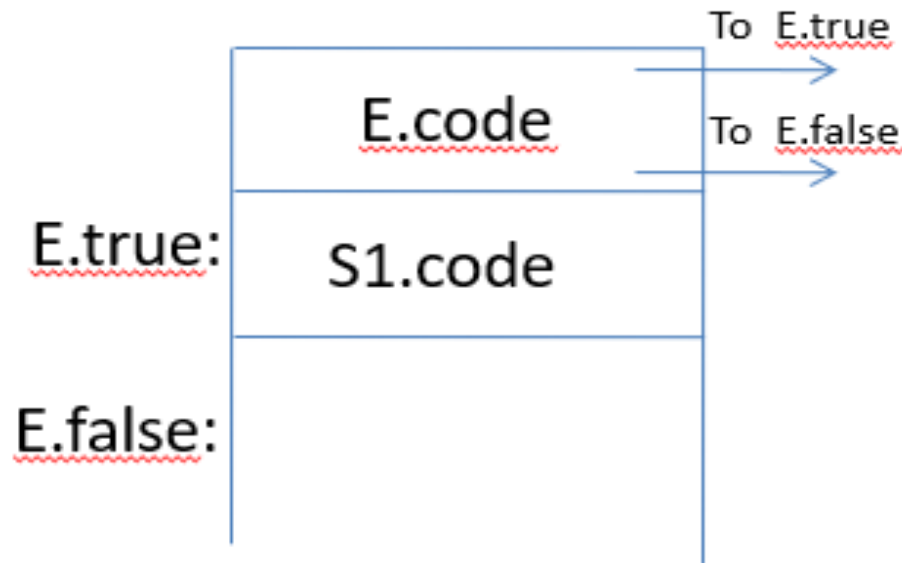


fig (a): if - then

flow of control statements

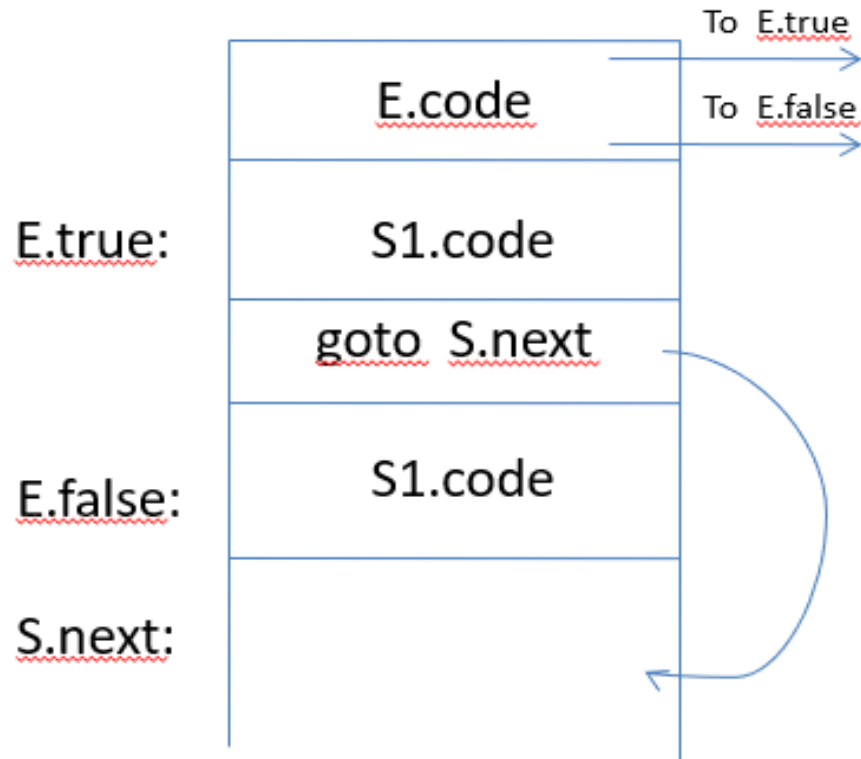


fig (b): if - then - else

flow of control statements

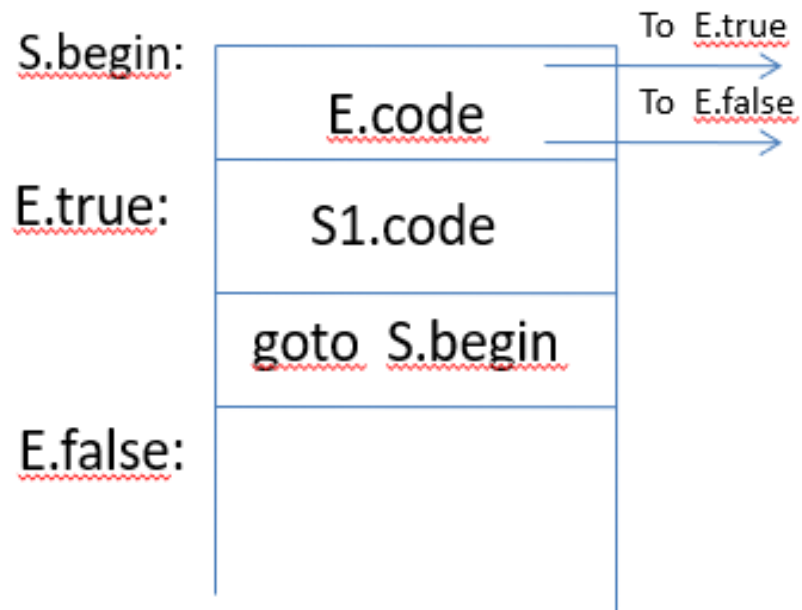


fig (c): while - do

HW submit on or before 23/01/2021

(1) Write a Three Address code for the following code fragment using SDD

```
c = 0
do {
    if (a < b)
    {
        x = x + 1
    }
    else {
        x = x - 1
    }

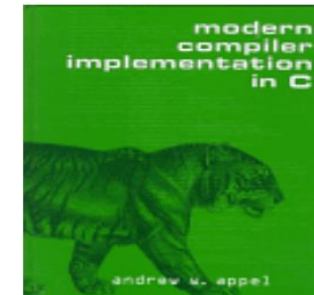
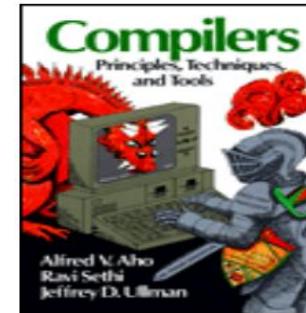
```

```
    c = c + 1
} while (c < 5)
```

(2) Write a 3AC for
for (i = 1; i < 10; i++)
{
 a[i] = x * 5
}

References

- Compilers principles ,tools and techniques by Aho, Sethi, and Ullman, Chapters 1, 2, 3
- S. Muchnick, Advanced Compiler Design and Implementation, Morgan Kaufman, 1997
- Andrew W. Appel : Modern Compiler Implementation in C



End of Unit -3

THANK YOU