```
In [ ]: word break
In [16]: def wbreak(s,wdict):
             wset= set(wdict)
             dp=[False]*(len(s)+1)
             dp[0]=True
             for i in range(1, len(s)+1):
                 for j in range(i):
                      if dp[j] and s[j:i] in wset:
                          dp[i]=True
                          break
             return dp
         s="goodday"
         wdict=["go","good", "day"]
         print(wbreak(s,wdict))
         [True, False, True, False, True, False, False, True]
In [ ]: | assembly line scheduling
In [20]: def assemblyLineScheduling(a,t,e,x):
             n = len(a[0])
             T1 = [0]*n
             T2 = [0]*n
             T3 = [0]*n
             T1[0]=e[0]+a[0][0]
             T2[0]=e[1]+a[1][0]
             T3[0]=e[2]+a[2][0]
             for i in range(1, n):
                 T1[i]=min(T1[i-1] + a[0][i], T2[i-1] + t[1][i] + a[0][i], T3[i-1] +
                 T2[i]=min(T2[i-1] + a[1][i], T1[i-1] + t[0][i] + a[1][i], T3[i-1] +
                 T3[i]=min(T3[i-1] + a[2][i], T1[i-1] + t[0][i] + a[2][i], T2[i-1] +
             final_time=min(T1[n-1] + x[0], T2[n-1] + x[1], T3[n-1] + x[2])
             return final time
         a = [[1,1,1,1],
              [2,1,2,1],
              [0,0,0,0]
         t = [[0,2,1,3],
              [0,3,5,6],
              [0,4,3,1]]
         e = [10, 10, 10]
         x = [18, 7, 11]
         print(assemblyLineScheduling(a, t, e, x))
```

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In [22]: class DisjointSet:
             def __init__(self, n):
                 self.parent=list(range(n))
                 self.rank=[0]*n
             def find(self, u):
                 if self.parent[u]!=u:
                      self.parent[u]=self.find(self.parent[u])
                 return self.parent[u]
             def union(self, u, v):
                 root_u=self.find(u)
                 root_v=self.find(v)
                 if root_u!=root_v:
                      if self.rank[root_u]>self.rank[root_v]:
                          self.parent[root_v]=root_u
                      elif self.rank[root_u]<self.rank[root_v]:</pre>
                          self.parent[root_u]=root_v
                          self.parent[root_v]=root_u
                          self.rank[root u]+=1
         def kruskal(n, edges):
             edges.sort(key=lambda x: x[2])
             ds=DisjointSet(n)
             mst_weight=0
             for u, v, weight in edges:
                 if ds.find(u)!= ds.find(v):
                      ds.union(u, v)
                      mst_weight+= weight
             return mst_weight
         import heapq
         def prim(n, edges):
             adj={i: [] for i in range(n)}
             for u, v, weight in edges:
                 adj[u].append((weight, v))
                 adj[v].append((weight, u))
             mst_weight=0
             visited=[False *n
             min heap=[(0, 0)]
             while min heap:
                 weight, u=heapq.heappop(min_heap)
                 if visited[u]:
                      continue
                 visited[u]= True
                 mst weight+= weight
                 for next weight, v in adj[u]:
                      if not visited[v]:
                          heapq.heappush(min_heap, (next_weight, v))
             return mst_weight
         def boruvka(n, edges):
             ds=DisjointSet(n)
             mst weight=0
             num_components=n
             while num components>1:
                 cheapest=[-1]*n
                 for u, v, weight in edges:
                      set u=ds.find(u)
                      set v=ds.find(v)
                      if set u!= set v:
                          if cheapest[set_u]==-1 or cheapest[set_u][2]>weight:
                              cheapest[set_u]=(u, v, weight)
                          if cheapest[set_v]==-1 or cheapest[set_v][2]>weight:
                              cheapest[set v]=(u, v, weight)
```

```
for node in range(n):
            if cheapest[node]!=-1:
                u, v, weight=cheapest[node]
                if ds.find(u)!= ds.find(v):
                    ds.union(u, v)
                    mst_weight+=weight
                    num_components-= 1
    return mst_weight
n=4
edges=[
    (0, 1, 10),
    (0, 2, 6),
    (0, 3, 5),
    (1, 3, 15),
    (2, 3, 4)
print("Kruskal's MST weight:", kruskal(n, edges))
print("Prim's MST weight:", prim(n, edges))
print("Boruvka's MST weight:", boruvka(n, edges))
```

Kruskal's MST weight: 19
Prim's MST weight: 19
Boruvka's MST weight: 19

```
In [23]: # Prim's Algorithm in Python
         def prims(G):
              INF=9999999
              V=5
              selected=[0, 0, 0, 0, 0]
              no_edge=0
              selected[0]=True
              print("Edge : Weight")
              while (no_edge < V - 1):</pre>
                  minimum=INF
                  x=0
                  y=0
                  for i in range(V):
                      if selected[i]:
                          for j in range(V):
                               if ((not selected[j]) and G[i][j]):
                                   if minimum>G[i][j]:
                                       minimum=G[i][j]
                                       x=i
                                       y=j
                  print(str(x) + " - " + str(y) + " : " + str(G[x][y]))
                  selected[y]=True
                  no_edge +=1
          #kruskals algorithm
         def find(parent, i):
              if parent[i]==i:
                  return i
              return find(parent, parent[i])
          def union(parent, rank, x, y):
              xroot=find(parent, x)
              yroot=find(parent, y)
              if rank[xroot]<rank[yroot]:</pre>
                  parent[xroot]=yroot
              elif rank[xroot]>rank[yroot]:
                  parent[yroot]=xroot
              else:
                  parent[yroot]=xroot
                  rank[xroot]+=1
          def kruskals(G):
              V=len(G)
              edges=[]
              for i in range(V):
                  for j in range(i+1, V):
                      if G[i][j] != 0:
                          edges.append((G[i][j], i, j))
              edges.sort()
              parent=[]
              rank=[]
              for node in range(V):
                  parent.append(node)
                  rank.append(0)
              MST=[]
              edge_count= 0
              index=0
              while edge_count<V-1:</pre>
                  w, u, v=edges[index]
                  index=index+1
                  x=find(parent, u)
                  y=find(parent, v)
                  if x!= y:
                      edge count = edge count + 1
```

```
MST.append((u, v, w))
            union(parent, rank, x, y)
   print("Edge : Weight")
   for u, v, weight in MST:
        print(str(u) + "-" + str(v) + " : " + str(weight))
#boruvkas algorithm
def findi(parent, i):
    if parent[i] == i:
        return i
    return findi(parent, parent[i])
def unioni(parent, rank, x, y):
   xroot = findi(parent, x)
   yroot = findi(parent, y)
   if rank[xroot]<rank[yroot]:</pre>
        parent[xroot]=yroot
   elif rank[xroot]>rank[yroot]:
        parent[yroot]=xroot
   else:
        parent[yroot]=xroot
        rank[xroot]+= 1
def boruvkas(G):
   V = len(G)
   parent = []
    rank=[]
    cheapest=[]
   for node in range(V):
        parent.append(node)
        rank.append(0)
        cheapest.append([-1, float('inf')])
    numTrees=V
   print("Edge : Weight")
   while numTrees>1:
        for i in range(V):
            for j in range(V):
                if G[i][j]!= 0:
                    u=findi(parent, i)
                    v=findi(parent, j)
                    if u!=v:
                         if G[i][j]<cheapest[u][1]:</pre>
                             cheapest[u]=[j, G[i][j]]
                         if G[i][j]<cheapest[v][1]:</pre>
                             cheapest[v]=[i, G[i][j]]
        for i in range(V):
            if cheapest[i][0]!=-1:
                u=i
                v=cheapest[i][0]
                w=cheapest[i][1]
                set u=findi(parent, u)
                set_v=findi(parent, v)
                if set u!= set v:
                    print(str(u) + " - " + str(v) + " : " + str(w))
                    unioni(parent, rank, set u, set v)
                    numTrees-= 1
        cheapest=[[-1, float('inf')] for _ in range(V)]
G = [[0, 9, 75, 0, 0],
     [9, 0, 95, 19, 42],
     [75, 95, 0, 51, 66],
     [0, 19, 51, 0, 31],
     [0, 42, 66, 31, 0]]
print("Prims Algorithm:")
prims(G)
```

```
print("\nkruskals Algorithm:")
kruskals(G)
print("\nBoruvkas Algorithm:")
boruvkas(G)
```

```
Prims Algorithm:
```

Edge : Weight

0 - 1 : 9 1 - 3 : 19 3 - 4 : 31 3 - 2 : 51

## kruskals Algorithm:

Edge : Weight 0-1 : 9

1-3 : 19 3-4 : 31 2-3 : 51

## Boruvkas Algorithm:

Edge : Weight

0 - 1 : 9 2 - 3 : 51 3 - 1 : 19 4 - 3 : 31

In [ ]: