

$$\textcircled{1} \log_c a^b = b \log_c a$$

$$\textcircled{2} a^{\log_c a} = c$$

$$T(N) = N + 2T(N/2)$$

$$2T(N/2) = 2(N/2) + 2T(N/4)$$

$$2^2 T(N/2^2) = 2^2(N/2^2) + 2^2 T(N/2^4)$$

$$2^k T(N/2^k) = 2^k(N/2^k) + 2^k T(1)$$

$$T(N) = KN + 2^k N$$

$$T(N) = N \lg(N) + 2 \cdot N$$

$$T(N) = O(N \lg(N))$$

$$\frac{N}{2}, \frac{N}{2}, \frac{N}{2}, \frac{N}{2}, \frac{N}{2}, \dots, 8, 4, 2, 1$$

$$a_0 = N$$

$$r = (1/2)$$

$$k = (KN)$$

$$a_k = a_0 \cdot r^{k+1}$$

$$1 = N \left(\frac{1}{2}\right)^k$$

$$2^k = N$$

$$|K = \lg_2(N)|$$

$$T(N) = N + T(N/2) + T(0)$$

$$T(N/2) = (N/2) + T(N/4) + T(0)$$

$$T(N/4) = (N/4) + T(N/8) + T(0)$$

$$\vdots$$

$$T(N/2^k) = 1 + T(N/2^{k+1}) + T(0)$$

$$T(N) = (N + N/2 + N/4 + \dots + 1) + N T(0)$$

$$= \frac{(N)(N+1)}{2} + N$$

$$T(N) = O(N^2)$$

(decreasing)

$$\left. \begin{matrix} BS \\ SS \\ TS \\ AS \end{matrix} \right\} N^2 \quad (B, A, W)$$

$$\rightarrow (N \lg N, N \lg N, N)$$