

## Practical 2

The Grinch is given the job of partitioning  $2n$  players into two teams of  $n$  players each. Each player has a numerical rating that measures how good he/she is at the game. He seeks to divide the players as unfairly as possible, so as to create the biggest possible talent imbalance between team A and team B. Show how the Grinch can do the job in  $O(n \log n)$  time.

**Solution:**

| Player | Rating | Team A | Team B |
|--------|--------|--------|--------|
| P1     | 8      | Y      |        |
| P2     | 3      | Y      |        |
| P3     | 4      |        | Y      |
| P4     | 5      | Y      |        |
| P5     | 1      |        | Y      |
| P6     | 2      | Y      |        |
| P7     | 7      |        | Y      |
| P8     | 6      |        | Y      |
|        |        | 18     | 18     |

TeamA=1+2+3+4=10, Team B= 5+6+7+8=26 (Worst case)

Team A=8+3+5+2=18, Team B=4+1+7+6=18 (Best Case)

Sort the players using any sorting algorithm with  $O(n \log n)$  worst case time complexity(e.g. mergesort). The first  $n$  players will be on teamA, the second  $n$  players will be on teamB

| Sorting Algorithms | Time Complexity    |                    |               | Space Complexity |
|--------------------|--------------------|--------------------|---------------|------------------|
|                    | Best Case          | Average Case       | Worst Case    | Worst Case       |
| Bubble Sort        | $\Omega(N)$        | $\Theta(N^2)$      | $O(N^2)$      | $O(1)$           |
| Selection Sort     | $\Omega(N^2)$      | $\Theta(N^2)$      | $O(N^2)$      | $O(1)$           |
| Insertion Sort     | $\Omega(N)$        | $\Theta(N^2)$      | $O(N^2)$      | $O(1)$           |
| Quick Sort         | $\Omega(N \log N)$ | $\Theta(N \log N)$ | $O(N^2)$      | $O(N)$           |
| Merge Sort         | $\Omega(N \log N)$ | $\Theta(N \log N)$ | $O(N \log N)$ | $O(N)$           |
| Heap Sort          | $\Omega(N \log N)$ | $\Theta(N \log N)$ | $O(N \log N)$ | $O(1)$           |

Input: 

|    |   |   |   |   |    |   |   |
|----|---|---|---|---|----|---|---|
| 10 | 2 | 5 | 3 | 7 | 13 | 1 | 6 |
|----|---|---|---|---|----|---|---|

