Maize Analysis English

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Introduction

 \mathbf{CME} - Ear length in cm

NTF - Total number of leaves

 \mathbf{ARF} - Leaf area cm^2

 \mathbf{ALP} - Plant height in cm

 \mathbf{PMG} - Thousand grain weight in g

 \mathbf{ALC} - Harvest site altitude in m

CDE - Endosperm color

NTN - Total number of nodes

FAS - Fasciation

The dataset used consists of mean values from regional corn populations, obtained over 3 decades through morphological characterization activities of the Portuguese Plant Germplasm Bank (BPGV). The variables in this dataset correspond to descriptors used for plant characterization before harvest, which corresponds to grain maturation, with the exception of the ALC descriptor, which corresponds to a passport descriptor obtained by technicians who collect this germplasm. We can classify the descriptors obtained from the characterization effort into 3 components: vegetative (ALP, NTN), foliar (NTF, ARF), productive (CME, PMG), and intrinsic (FAS, CDE).

Thus, for performing linear regression, we selected **ALP** as the dependent variable, since morphological studies have proven an interdependence between the various types of descriptors presented here. Therefore, we propose to demonstrate the association between these variables through the creation of a linear regression model for plant height using this dataset.

Import and Factorization

```
#Import the dataset
library(readxl)
data_milho <- read_excel("data_milho.xlsx")

#Factorize the variables
data_milho$CDE <-factor(data_milho$CDE,c("1", "2", "3", "4", "5"),labels=c("White", "Cream", "Light-yel
data_milho$FAS <-factor(data_milho$FAS,c("0", "1"),labels=c("Absent", "Present"))</pre>
```

Preliminary Analysis

```
## tibble [566 x 9] (S3: tbl_df/tbl/data.frame)

## $ CME: num [1:566] 8 10 10 11 11 10 13 7 9 11 ...

## $ NTF: num [1:566] 5 8 8 7 8 7 6 7 9 6 ...

## $ ARF: num [1:566] 30 60 60 57.8 66 ...

## $ ALP: num [1:566] 92 98 100 105 108 108 108 110 116 117 ...

## $ PMG: num [1:566] 240 270 230 300 335 250 370 250 210 325 ...

## $ ALC: num [1:566] 95 100 110 760 400 400 380 950 175 110 ...

## $ CDE: Factor w/ 5 levels "White", "Cream", ..: 4 1 1 3 3 4 5 4 3 1 ...

## $ NTN: num [1:566] 6 4 4 6 6 6 5 7 8 7 ...

## $ FAS: Factor w/ 2 levels "Absent", "Present": 1 1 1 1 1 1 1 1 1 1 1 ...
```

[1] FALSE

The dataset contains data from 566 populations, distributed across 9 variables explained above, with 6 continuous variables and 2 categorical variables. Within the categorical variables, the **CDE** variable has 5 levels (endosperm colors) and the **FAS** variable is a binary variable (Presence/Absence of fasciation). The dataset does not contain missing data (NA).

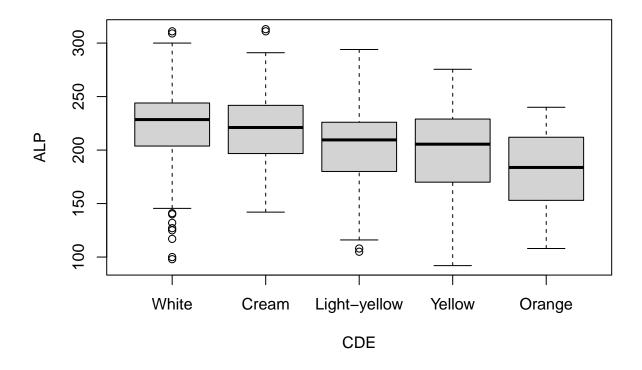
Exploratory Data Analysis

```
library(summarytools)
dfSummary(data_milho, na.col = F, valid.col = F)
## Data Frame Summary
## data milho
## Dimensions: 566 x 9
## Duplicates: 1
##
## ---
                    Stats / Values
                                                 Freqs (% of Valid)
## No
        Variable
                                                                        Graph
##
## 1
        CME
                    Mean (sd) : 15 (2.1)
                                                103 distinct values
                    min < med < max:</pre>
##
        [numeric]
##
                    7 < 15 < 22
                                                                                . : .
                    IQR (CV) : 2.1 (0.1)
##
                                                                              . : : :
##
                                                                           . . : : : : :
##
## 2
        NTF
                    Mean (sd): 10.2 (1.5)
                                            56 distinct values
##
        [numeric]
                    min < med < max:
                                                                                : .
##
                    5 < 10 < 14
                                                                              . : : .
                    IQR (CV) : 2 (0.1)
##
                                                                             . : : : :
```

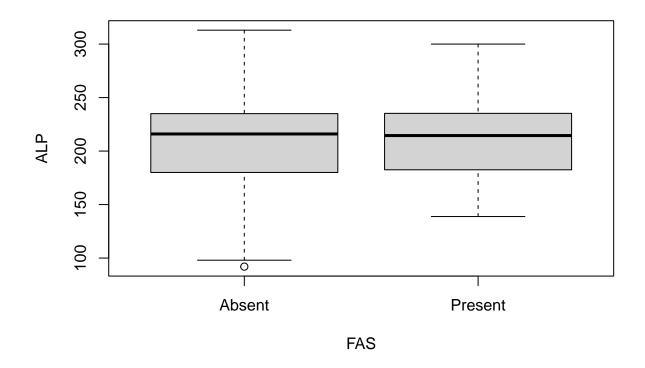
```
##
                                                                          . : : : : :
##
                                                 241 distinct values
## 3
                    Mean (sd): 115.2 (28)
##
                    min < med < max:
        [numeric]
##
                    30 < 114.4 < 189
                                                                             : : : :
##
                    IQR (CV): 38.9 (0.2)
                                                                            . : : : :
##
                                                                          . : : : : : .
##
## 4
        ALP
                    Mean (sd) : 208 (39.7)
                                                 264 distinct values
                    min < med < max:
##
        [numeric]
                                                                                 : :
##
                    92 < 215.5 < 313
                                                                             . ::
                    IQR (CV) : 55 (0.2)
##
                                                                            . : : : : :
                                                                        . . : : : : : . .
##
##
## 5
        PMG
                    Mean (sd): 302.5 (60.8) 118 distinct values
##
        [numeric]
                    min < med < max:</pre>
                                                                              : :
##
                    112 < 310 < 525
                                                                            . : : .
##
                    IQR (CV) : 77 (0.2)
                                                                           : : : :
##
                                                                          . : : : : .
##
## 6
        ALC
                    Mean (sd): 404.2 (268.5) 155 distinct values
##
        [numeric]
                    min < med < max:
                    5 < 400 < 1150
##
                                                                        : . : : : .
##
                    IQR (CV): 407.5 (0.7)
                                                                        ::::::
##
                                                                        : : : : : : : . .
##
                    1. White
## 7
        CDE
                                                 148 (26.1%)
                                                                        IIIII
##
                    2. Cream
                                                 108 (19.1%)
        [factor]
                                                                        III
##
                    3. Light-yellow
                                                  94 (16.6%)
                                                                        III
                                                 194 (34.3%)
##
                    4. Yellow
                                                                        IIIIII
##
                    5. Orange
                                                  22 (3.9%)
##
                    Mean (sd) : 9.6 (1.5)
## 8
        NTN
                                                 47 distinct values
##
        [numeric]
                    min < med < max:
                                                                               : : :
                    4 < 10 < 13
##
                                                                              . : : :
                    IQR (CV) : 2 (0.2)
##
                                                                              : : : : :
##
                                                                          . . : : : : : .
##
## 9
        FAS
                    1. Absent
                                                 491 (86.7%)
                                                                        IIIIIIIIIIIIIII
##
                    2. Present
                                                  75 (13.3%)
        [factor]
                                                                        TT
```

The descriptive statistics for the descriptors used are shown above. Appealing to the Central Limit Theorem, we will assume normality of the distributions.

```
boxplot(ALP~CDE, data = data_milho)
```



boxplot(ALP~FAS, data = data_milho)



```
\#ANOVA analysis between the dependent variable and the categorical variable CDE
#Verify homogeneity of variances
fligner.test(ALP~CDE, data = data_milho)
##
##
   Fligner-Killeen test of homogeneity of variances
## data: ALP by CDE
## Fligner-Killeen:med chi-squared = 4.9117, df = 4, p-value = 0.2965
#Assuming normality
model = aov(ALP~CDE, data = data_milho)
summary(model)
##
                Df Sum Sq Mean Sq F value
                                            Pr(>F)
                 4 66381
                            16595
                                     11.3 7.93e-09 ***
## CDE
## Residuals
               561 823721
                             1468
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
TukeyHSD(model)
     Tukey multiple comparisons of means
```

##

##

95% family-wise confidence level

```
##
## Fit: aov(formula = ALP ~ CDE, data = data_milho)
##
## $CDE
##
                             diff
                                        lwr
                                                   upr
                                                           p adj
## Cream-White
                        -3.694645 -16.96579
                                              9.576498 0.9413324
## Light-yellow-White -19.989779 -33.82047
                                             -6.159085 0.0008179
## Yellow-White
                       -21.281367 -32.72628
                                             -9.836457 0.0000049
## Orange-White
                       -38.352641 -62.31410 -14.391179 0.0001375
## Light-yellow-Cream -16.295134 -31.08727
                                             -1.502997 0.0224832
## Yellow-Cream
                       -17.586722 -30.17661
                                             -4.996836 0.0013770
## Orange-Cream
                       -34.657997 -59.18698 -10.129015 0.0011609
## Yellow-Light-yellow -1.291588 -14.46998 11.886806 0.9988623
## Orange-Light-yellow -18.362863 -43.19904
                                              6.473316 0.2560756
## Orange-Yellow
                       -17.071275 -40.66224
                                              6.519691 0.2769280
#ANOVA analysis between the dependent variable and the categorical variable FAS
#Verify homogeneity of variances
fligner.test(ALP~FAS, data = data_milho)
##
   Fligner-Killeen test of homogeneity of variances
##
## data: ALP by FAS
## Fligner-Killeen:med chi-squared = 1.0155, df = 1, p-value = 0.3136
#Assuming normality
model = aov(ALP~FAS, data = data_milho)
summary(model)
##
                Df Sum Sq Mean Sq F value Pr(>F)
## FAS
                 1
                      115
                            115.4
                                    0.073 0.787
## Residuals
               564 889986 1578.0
```

Since the dependent variable we intend to study corresponds to **ALP**, we chose to analyze the distribution of this variable against the categorical variables.

We observe the occurrence of outliers in the **ALP/CDE** box plots for the 'White', 'Cream', and 'Light-yellow' factors. Among all, the 'Orange' factor presents itself as the one with the lowest mean relative to **ALP**, also being the factor with the smallest number of individuals (3.9%).

The ANOVA analysis results indicate that the differences between the 'Light-Yellow', 'Yellow', and 'Orange' factors are not significant, as well as between the 'White' and 'Cream' factors, with all others being significant. For the **FAS** variable, we verify that the ANOVA analysis does not reveal significant differences between its levels (Presence/Absence) and the dependent variable, which is observable in the **ALP/FAS** box plot.

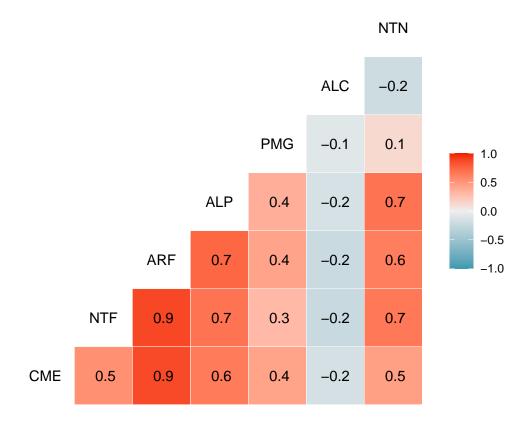
Correlations

```
#create dataset with only numeric variables
data_milho_num <- data_milho
data_milho_num$FAS <- NULL
data_milho_num$CDE <- NULL</pre>
```

```
#Correlations
library(GGally)
```

Loading required package: ggplot2

```
library(ggplot2)
ggcorr(data_milho_num, geom="tile", label = T, label_alpha = F)
```



The correlations between continuous variables were computed using Pearson's correlation coefficient. Defining correlations above 0.5 as relevant, we observe the occurrence of strong and positive correlations between the following descriptors:

CME - NTF, ARF, ALP and NTN NTF - CME, ARF, ALP, NTN ARF - CME, NTF, ALP, NTN ALP - CME, NTF, ARF, NTN

We also observe lighter and positive correlations between the \mathbf{PMG} descriptor and the vegetative and foliar descriptors that are strongly correlated among themselves.

A slight negative correlation is also verified between the **ALC** descriptor and all others.

Linear Regression (Full-model)

```
#Complete fit
full.model <- lm(ALP ~., data = data_milho)</pre>
summary(full.model)
##
## Call:
## lm(formula = ALP ~ ., data = data_milho)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -74.130 -13.806 -0.116 14.842 64.623
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  -2.034e+02 4.217e+01 -4.825 1.81e-06 ***
                   1.570e+01 2.847e+00 5.515 5.37e-08 ***
## CME
                   2.278e+01 4.428e+00 5.146 3.70e-07 ***
## NTF
## ARF
                  -1.417e+00 3.854e-01 -3.676 0.000259 ***
## PMG
                  7.776e-02 1.960e-02 3.968 8.21e-05 ***
                   2.296e-03 3.840e-03 0.598 0.550045
## ALC
## CDECream
                  -1.939e+00 2.942e+00 -0.659 0.510035
## CDELight-yellow 1.206e+00 3.428e+00 0.352 0.725112
## CDEYellow
                  -7.348e+00 2.627e+00 -2.797 0.005340 **
                  -1.470e+01 5.536e+00 -2.656 0.008138 **
## CDEOrange
## NTN
                   8.980e+00 8.830e-01 10.169 < 2e-16 ***
## FASPresent
                  4.470e+00 2.925e+00
                                        1.528 0.127003
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 23.06 on 554 degrees of freedom
## Multiple R-squared: 0.6691, Adjusted R-squared: 0.6625
## F-statistic: 101.8 on 11 and 554 DF, p-value: < 2.2e-16
#Test for multicollinearity
car::vif(full.model)
            GVIF Df GVIF^(1/(2*Df))
##
## CME 39.436548 1
                           6.279853
## NTF 44.443851 1
                           6.666622
## ARF 123.331154 1
                          11.105456
## PMG
        1.507722 1
                          1.227893
        1.129155 1
## ALC
                          1.062617
## CDE
        1.478180 4
                           1.050064
## NTN
        1.984576 1
                          1.408750
## FAS
        1.046837 1
                          1.023151
#Remove ARF
data_milho$ARF <- NULL</pre>
#New complete fit
```

```
full.model <- lm(ALP ~., data = data_milho)</pre>
summary(full.model)
##
## Call:
## lm(formula = ALP ~ ., data = data_milho)
##
##
  Residuals:
##
                1Q
                                 3Q
       Min
                     Median
                                         Max
   -84.138 -14.475
                      0.279
                             14.730
                                     65.701
##
##
##
  Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                                           -5.227 2.45e-07 ***
## (Intercept)
                    -52.851483
                                10.111563
## CME
                      5.455422
                                 0.590183
                                             9.244 < 2e-16 ***
## NTF
                      6.923725
                                 1.006716
                                             6.878 1.65e-11 ***
                                             3.669 0.000267 ***
## PMG
                      0.072522
                                 0.019767
## ALC
                      0.002880
                                 0.003879
                                             0.742 0.458230
## CDECream
                     -1.534346
                                 2.972627
                                            -0.516 0.605949
## CDELight-yellow
                      1.457687
                                 3.466087
                                             0.421 0.674241
                                            -2.948 0.003336 **
## CDEYellow
                     -7.821781
                                 2.653498
## CDEOrange
                    -12.639860
                                 5.569023
                                            -2.270 0.023610 *
                                            10.279 < 2e-16 ***
## NTN
                      9.163944
                                 0.891499
## FASPresent
                      5.150903
                                 2.951549
                                             1.745 0.081512 .
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 23.32 on 555 degrees of freedom
## Multiple R-squared: 0.661, Adjusted R-squared: 0.6549
## F-statistic: 108.2 on 10 and 555 DF, \, p-value: < 2.2e-16
#New test for multicollinearity
car::vif(full.model)
##
           GVIF Df GVIF^(1/(2*Df))
## CME 1.657244
                 1
                           1.287340
## NTF 2.247043
                           1.499014
## PMG 1.499747
                           1.224642
## ALC 1.127227
                           1.061709
## CDE 1.446683
                  4
                           1.047241
## NTN 1.978192
                           1.406482
## FAS 1.042638
                           1.021096
#Diagnostic measures
\#R^2 \rightarrow 1 (value tending to 1 implies that the predictor variables are well fitted in the model)
#RSE -> 0 (A smaller value implies a smaller model error)
```

Performing the complete fit of the dependent variable **ALP** to a linear model with the remaining 8 variables from the dataset, we verify that the coefficients of variables **CME**, **NTF**, **ARF**, **PMG**, **NTN**, and the intercept are recognized as significant at a significance level of 0, and the 'Yellow' and 'Orange' levels of variable **CDE** at a significance level of 0.001. Thus, for the intercept and predictor variables, we can reject H and accept the alternative hypothesis that there is a significant association between the predictor

variables and the dependent variable.

The multicollinearity assumption was tested and it was discovered that the \mathbf{ARF} variable had a GVIF > 10 value, which indicates a strong correlation of this variable with other independent variables, breaking this assumption. Therefore, the \mathbf{ARF} variable was removed from the dataset and the model was recalculated. The new model contained the same significance levels for the variables that remained, with the \mathbf{R}^2 value decreasing slightly to 0.661.

Stepwise Selection

```
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
              1.1.4
                         v readr
                                     2.1.5
## v dplyr
## v forcats 1.0.0
                         v stringr
                                     1.5.1
## v lubridate 1.9.4
                         v tibble
                                     3.2.1
## v purrr
              1.1.0
                         v tidyr
                                     1.3.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
## x tibble::view() masks summarytools::view()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
library(caret)
## Loading required package: lattice
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
##
      lift
library(leaps)
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
step.model <- stepAIC(full.model, direction = "both", trace = FALSE)</pre>
summary(step.model)
##
## Call:
## lm(formula = ALP ~ CME + NTF + PMG + CDE + NTN + FAS, data = data_milho)
```

```
##
## Residuals:
      Min
                1Q Median
## -84.425 -14.966
                    0.124 14.708 65.479
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
                                9.42224 -5.321 1.50e-07 ***
## (Intercept)
                   -50.13497
## CME
                     5.43814
                                0.58949
                                          9.225 < 2e-16 ***
## NTF
                     6.87414
                                1.00409
                                          6.846 2.01e-11 ***
## PMG
                     0.07244
                                0.01976
                                          3.666 0.00027 ***
                                        -0.508
## CDECream
                    -1.50961
                                2.97124
                                                0.61160
                   1.69147
                                3.45035
                                         0.490
                                                0.62416
## CDELight-yellow
## CDEYellow
                   -7.94778
                                2.64699
                                        -3.003
                                                0.00280 **
## CDEOrange
                                5.49718 -2.418
                   -13.29146
                                                0.01593 *
## NTN
                     9.08775
                                0.88521
                                         10.266
                                                < 2e-16 ***
## FASPresent
                     5.10415
                                2.94968
                                         1.730 0.08411 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 23.31 on 556 degrees of freedom
## Multiple R-squared: 0.6607, Adjusted R-squared: 0.6552
## F-statistic: 120.3 on 9 and 556 DF, p-value: < 2.2e-16
step.modelf <- stepAIC(full.model, direction = "forward", trace = FALSE)</pre>
summary(step.modelf)
##
## Call:
## lm(formula = ALP ~ CME + NTF + PMG + ALC + CDE + NTN + FAS, data = data_milho)
##
## Residuals:
##
                1Q Median
      Min
                                3Q
                                       Max
## -84.138 -14.475
                    0.279 14.730
                                   65.701
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -52.851483 10.111563 -5.227 2.45e-07 ***
                                           9.244 < 2e-16 ***
## CME
                     5.455422
                               0.590183
## NTF
                     6.923725
                               1.006716
                                           6.878 1.65e-11 ***
## PMG
                     0.072522
                               0.019767
                                           3.669 0.000267 ***
## ALC
                     0.002880
                                0.003879
                                           0.742 0.458230
## CDECream
                    -1.534346
                                2.972627
                                         -0.516 0.605949
## CDELight-yellow
                                           0.421 0.674241
                    1.457687
                                3.466087
## CDEYellow
                   -7.821781
                                2.653498
                                         -2.948 0.003336 **
## CDEOrange
                                         -2.270 0.023610 *
                   -12.639860
                                5.569023
## NTN
                     9.163944
                                0.891499
                                         10.279 < 2e-16 ***
                                          1.745 0.081512 .
                     5.150903
                                2.951549
## FASPresent
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 23.32 on 555 degrees of freedom
## Multiple R-squared: 0.661, Adjusted R-squared: 0.6549
## F-statistic: 108.2 on 10 and 555 DF, p-value: < 2.2e-16
```

```
summary(step.modelb)
##
## Call:
## lm(formula = ALP ~ CME + NTF + PMG + CDE + NTN + FAS, data = data milho)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
  -84.425 -14.966
                     0.124
                            14.708
                                     65.479
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   -50.13497
                                9.42224 -5.321 1.50e-07 ***
## CME
                     5.43814
                                0.58949
                                           9.225 < 2e-16 ***
## NTF
                     6.87414
                                1.00409
                                           6.846 2.01e-11 ***
## PMG
                     0.07244
                                0.01976
                                           3.666
                                                 0.00027 ***
                                 2.97124
                                          -0.508
## CDECream
                    -1.50961
                                                  0.61160
## CDELight-yellow
                     1.69147
                                 3.45035
                                           0.490
                                                  0.62416
## CDEYellow
                    -7.94778
                                2.64699
                                         -3.003
                                                  0.00280 **
## CDEOrange
                   -13.29146
                                 5.49718
                                                  0.01593 *
                                          -2.418
## NTN
                     9.08775
                                 0.88521
                                          10.266
                                                  < 2e-16 ***
## FASPresent
                     5.10415
                                 2.94968
                                           1.730
                                                  0.08411 .
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 23.31 on 556 degrees of freedom
## Multiple R-squared: 0.6607, Adjusted R-squared: 0.6552
## F-statistic: 120.3 on 9 and 556 DF, p-value: < 2.2e-16
AIC(step.model)
## [1] 5182.498
AIC(step.modelf)
## [1] 5183.936
AIC(step.modelb)
```

step.modelb <- stepAIC(full.model, direction = "backward", trace = FALSE)</pre>

```
## [1] 5182.498
```

We performed the stepwise selection method from the complete model fit, using the 'both', 'forward', and 'backward' methods. After comparing the AIC values of the 3 selections, we opted for the 'backward' method (lowest AIC). In this method, the coefficients of variables **CME**, **NTF**, **PMG**, **NTN**, and the intercept are considered significant at a significance level of 0, the 'Yellow' and 'Orange' levels of variable **CDE** at a significance level of 0.001, and the **FAS** variable at a significance level of 0.05. Thus, for the intercept and predictor variables, we can reject H and accept the alternative hypothesis that there is a significant association between the predictor variables and the dependent variable.

The residual standard error takes the value of approximately 0.66, which we consider sufficiently significant to proceed with the regression.

Conclusions

```
#Evaluate residual normalization
shapiro.test(residuals(step.modelb))

##

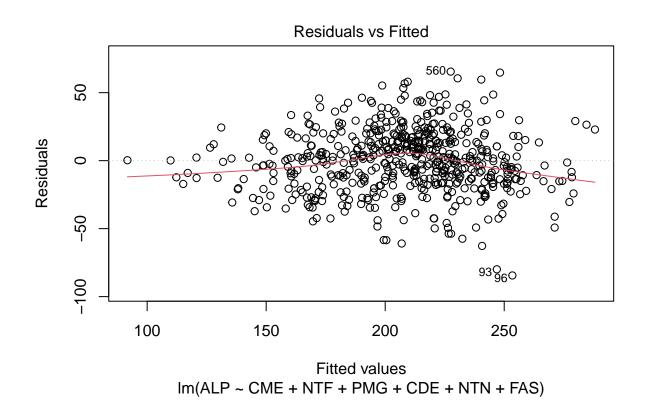
## Shapiro-Wilk normality test
##

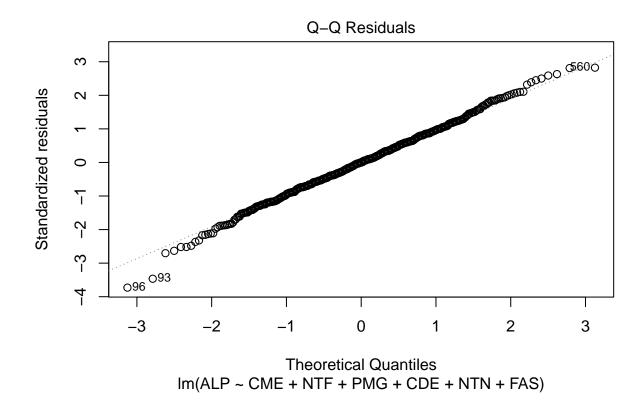
## data: residuals(step.modelb)
## W = 0.99714, p-value = 0.4295

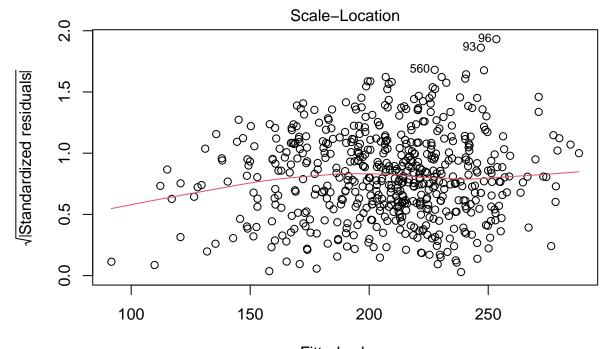
#Residual standard error
sigma(step.modelb)/mean(data_milho$ALP)

## [1] 0.1120357

#Diagnostic plots
# Test for homoscedasticity assumption
plot(step.modelb)
```

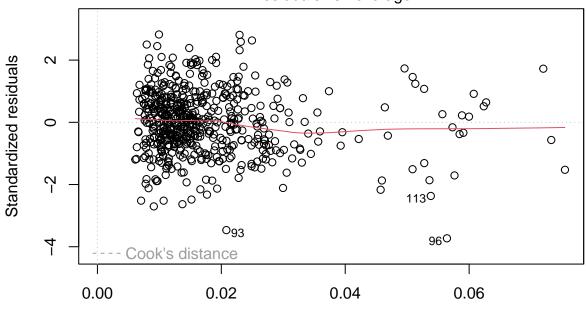






Fitted values
Im(ALP ~ CME + NTF + PMG + CDE + NTN + FAS)

Residuals vs Leverage



Leverage Im(ALP ~ CME + NTF + PMG + CDE + NTN + FAS)

#Model confidence interval confint(step.modelb)

```
2.5 %
                                       97.5 %
##
                    -68.64251284 -31.6274193
## (Intercept)
##
  CME
                      4.28025225
                                   6.5960335
                      4.90186319
                                   8.8464149
## NTF
## PMG
                      0.03363078
                                   0.1112514
## CDECream
                     -7.34584060
                                   4.3266130
## CDELight-yellow
                    -5.08584978
                                   8.4687938
## CDEYellow
                                   -2.7484502
                    -13.14711014
## CDEOrange
                    -24.08924496
                                   -2.4936813
## NTN
                      7.34898060
                                   10.8265189
## FASPresent
                     -0.68973826
                                   10.8980377
```

#Model ANOVA

anova(step.modelb)

```
## Analysis of Variance Table
##
## Response: ALP
##
              Df Sum Sq Mean Sq F value
                                             Pr(>F)
## CME
               1 368547
                         368547 678.5021 < 2.2e-16 ***
## NTF
               1 139824
                         139824 257.4184 < 2.2e-16 ***
## PMG
                   2536
                            2536
                                   4.6687
                                            0.03114 *
```

```
## CDE
                  19762
                            4940
                                   9.0953 4.024e-07 ***
## NTN
                  55800
                           55800 102.7287 < 2.2e-16 ***
               1
## FAS
                    1626
                            1626
                                   2.9943
                                             0.08411 .
## Residuals 556 302007
                             543
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

The normality assumption of residuals was verified through a Shapiro-Wilk test, obtaining a p-value > 0.05, thus proving the normality of residuals. The 95% confidence intervals for the intercept and predictor variables were computed.

The homoscedasticity assumption was tested using the residuals vs fitted values scatter plot. Since the dispersion does not present a conical shape, we consider this assumption satisfied.

The quality of the final linear model was assessed through the R-squared and Residual Standard Error metrics, obtaining a value of approximately 0.6689 for the first and an estimated error rate of 11% for the second.

Satisfying all requirements, we define as our final model $\mathbf{ALP} \sim \mathbf{CME} + \mathbf{NTF} + \mathbf{PMG} + \mathbf{CDE} + \mathbf{NTN} + \mathbf{FAS}$, with the stepwise selection method only excluding the \mathbf{ALC} variable. The ANOVA analysis of the final model supports these conclusions.

We conclude that from a set of morphological descriptors it is possible to establish linear regression models for plant height, with this model having utility from the perspective of eliminating missing data through its prediction using this model, on the datasets of regional corn populations conserved in the BPGV.