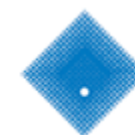


Arrays in Matlab

- ▶ NEF1104 – Problem Solving for Engineers
 - ▶ Week 2 Session 4



Operations on matrices and arrays

Matlab supports the standard operations of addition, subtraction, transposition and multiplication.

Recall that these operations are defined only when the matrices involved satisfy certain properties:

| | |
|---------|--|
| $A + B$ | A and B must be the same size (same numbers of rows and columns). |
| $A - B$ | A and B must be the same size. |
| AB | The number of columns in A must be equal to the number of rows of B. |
| A^2 | A must be a square matrix. |
| A^T | No restrictions. |

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```
>> A = [1 2 3 4;5 6 7 8;9 10 11 12]
```

A =

```
1 2 3 4
5 6 7 8
9 10 11 12
```

```
>> B = magic(3)
```

B =

```
8 1 6
3 5 7
4 9 2
```

```
>> C = [10 11 12;13 14 15;16 17 18]
```

C =

```
10 11 12
13 14 15
16 17 18
```

```
>> B+C
```

ans =

```
18 12 18
16 19 22
20 26 20
```

```
>> B*A
```

ans =

```
67 82 97 112
91 106 121 136
67 82 97 112
```

```
>> A'*C
```

ans =

```
219 234 249
258 276 294
297 318 339
336 360 384
```

```
>> B^2
```

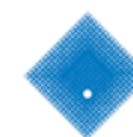
ans =

```
91 67 67
67 91 67
67 67 91
```

```
>> C^4
```

ans =

```
782730 842292 901854
993492 1069092 1144692
1204254 1295892 1387530
```



Dot operators

The “dot” operators (“array operators”) are a special class of commands which operate on every element of an array independently.

$A*B$: multiply A by B using the usual matrix definition

$A.*B$: multiply every element of A by the corresponding element of B

So this command is defined when A and B are the same size

```
>> A = [1 2 3 4;5 6 7 8]
A =
     1     2     3     4
     5     6     7     8

>> B = [1 1 -1 -1;2 -2 3 -3]
B =
     1     1    -1    -1
     2    -2     3    -3

>> A.*B
ans =
     1     2    -3    -4
    10   -12    21   -24
```

Dot operators

Dot division (divides corresponding elements) and Dot powers:

```
>> A = [1 2 3 4;5 6 7 8]
```

A =

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 5 | 6 | 7 | 8 |

```
>> B = [1 1 -1 -1;2 -2 3 -3]
```

B =

| | | | |
|---|----|----|----|
| 1 | 1 | -1 | -1 |
| 2 | -2 | 3 | -3 |

Some other operations:

```
>> 1./A
```

ans =

| | | | |
|--------|--------|--------|--------|
| 1.0000 | 0.5000 | 0.3333 | 0.2500 |
| 0.2000 | 0.1667 | 0.1429 | 0.1250 |

```
>> A.^3
```

ans =

| | | | |
|-----|-----|-----|-----|
| 1 | 8 | 27 | 64 |
| 125 | 216 | 343 | 512 |

```
>> A./B
```

ans =

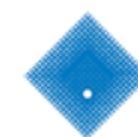
| | | | |
|--------|---------|---------|---------|
| 1.0000 | 2.0000 | -3.0000 | -4.0000 |
| 2.5000 | -3.0000 | 2.3333 | -2.6667 |

```
>> A.^B
```

ans =

| | | | |
|---------|--------|----------|--------|
| 1.0000 | 2.0000 | 0.3333 | 0.2500 |
| 25.0000 | 0.0278 | 343.0000 | 0.0020 |

If you enter these commands without a dot you'll get an error message: try them and see!

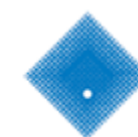


Relational operators

Much of Matlab usage is concerned with testing values.

There are six “relational operators”:

| | |
|----|--------------------------|
| > | Greater than |
| < | Less than |
| >= | Greater than or equal to |
| <= | Less than or equal to |
| == | Equal |
| ~= | Not equal |



Relational operators

```
>> A = [1 2 3 4;5 6 7 8]
```

A =

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 5 | 6 | 7 | 8 |

```
>> B = [1 1 -1 -1;2 -2 3 -3]
```

B =

| | | | |
|---|----|----|----|
| 1 | 1 | -1 | -1 |
| 2 | -2 | 3 | -3 |

```
>> A>B
```

ans =

2×4 logical array

| | | | |
|---|---|---|---|
| 0 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 |

```
>> A<=B+4
```

ans =

2×4 logical array

| | | | |
|---|---|---|---|
| 1 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |

```
>> A==abs(B)+3
```

ans =

2×4 logical array

| | | | |
|---|---|---|---|
| 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 |

If you type in those at this point, you'll find that *ans* is a matrix of type "Logical".

In Matlab, a *logical* matrix consists of two values: **true** and **false**, which are printed as **1** and **0** respectively.

Logical operators

Results of testing can be joined together using “logical operators”:

| | |
|------------------------|---|
| <code>x & y</code> | x and y : true if both x and y are true, and false if at least one of x and y are false. |
| <code>x y</code> | x or y : true if either or both of x and y are true, and false only when both of x and y are false. |
| <code>xor(x,y)</code> | exclusive or of x and y : true if one of x and y is true and the other false, and false if both x and y are true, or both are false. |
| <code>~x</code> | not x : true if x is false, and false if x is true. |

Here's how we might use these operators to implement the function:

$$f(x, y) = \begin{cases} x + y, & \text{if } x \geq 0 \text{ or } y \geq 0 \\ x^2 + y^2, & \text{if } x < 0 \text{ and } y < 0 \\ 0, & \text{other} \end{cases}$$

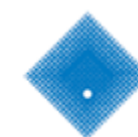
```
function out = f(x,y)
```

```
if x>=0 || y>=0  
    out = x+y;
```

```
else if x<0 & y<0  
    out = x^2+y^2;
```

```
else  
    out = 0;  
end
```

```
end  
end
```



The commands *any*, *all* and *find*

Results of testing can be joined together using “logical operators”:

| | |
|----------------------------|--|
| <code>any(test(v))</code> | Returns 1 if <i>any</i> of the elements of the vector <i>v</i> are true for the test |
| <code>all(test(v))</code> | Returns 1 if <i>all</i> of the elements of the vector <i>v</i> are true for the test |
| <code>find(test(v))</code> | Returns the list of indices of <i>v</i> for which the test is true. |

```
>> A = 1:8
```

```
A =
```

```
1 2 3 4 5 6 7 8
```

```
>> any(A==5)
```

```
ans =
```

```
logical
```

```
1
```

```
>> any(A>5)
```

```
ans =
```

```
logical
```

```
1
```

```
>> any(A>9)
```

```
ans =
```

```
logical
```

```
0
```

```
>> all(A>3)
```

```
ans =
```

```
logical
```

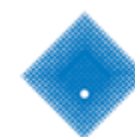
```
0
```

```
>> all(A<9)
```

```
ans =
```

```
logical
```

```
1
```



The commands *any*, *all* and *find*

To apply these operators to an array, you first need to make the array into one big vector.

The colon in brackets takes all the elements of A, and lists them as one long column vector.

```
>> A=magic(4)
```

```
A =
```

```
16   2   3  13
 5  11  10   8
 9   7   6  12
 4  14  15   1
```

```
>> any(A(:)>10)
```

```
ans =
```

```
logical
```

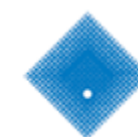
```
1
```

```
>> all(A(:)<20)
```

```
ans =
```

```
logical
```

```
1
```



The commands *any*, *all* and *find*

The results of **find** will be given as single numbers, indicating the position using the single number indexing system.

```
>> A=magic(4)
```

A =

| | | | |
|----|----|----|----|
| 16 | 2 | 3 | 13 |
| 5 | 11 | 10 | 8 |
| 9 | 7 | 6 | 12 |
| 4 | 14 | 15 | 1 |

```
>> find(A>10)
```

ans =

1
6
8
12
13
15

```
>> find(A>4 & A<8)
```

ans =

2
7
11

```
>> X = find(A > 10)
```

X =

1
6
8
12
13
15

```
>> A(X) = A(X)*100
```

A =

| | | | |
|------|------|------|------|
| 1600 | 2 | 3 | 1300 |
| 5 | 1100 | 10 | 8 |
| 9 | 7 | 6 | 1200 |
| 4 | 1400 | 1500 | 1 |

Find can be used to change all values of an array satisfying some criterion.

i.e. to multiply all values of A which are greater than 10, by 100

