

# 附录

## 一、材料清单 BOM

项目号	零件号	说明	数量
1	机架		1
2	顶盖		1
3	70-35转角1球铰2转轴		3
4	圆球杆42mm		3
5	40-35转角2球铰1转轴		3
6	圆球杆158mm		3
7	三角板		1
8	凸轮		3

## 二、动学求解代码（通过执行器位置求解驱动空间参数）

```
clear;
L_tri=7.5;
%O1=(0,5,25);O2=(0,5,20);O3=(5*cos(pi/6),5*sin(pi/6),20);O4=(5*cos(pi/6),5*sin(pi/6),25)
xo=0;
yo=5;
zo=21;

xa=xo+L_tri/2;
ya=yo-L_tri/(2*3^0.5);
za=zo;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
```

```

zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;

```

```
eq9=xi-xf==(yi-yf)*3^0.5;
```

```
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];  
sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);  
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));  
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
```

```
L3=4.4;
```

```
L4=4.2;
```

```
L5=5.3;
```

```
xj=xg;
```

```
yj=yg+L3*(zd-zg)/L2;
```

```
zj=zg-L3*(yd-yg)/L2;
```

```
syms xk yk zk;
```

```
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
```

```
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
```

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xl,yl,zl]);
```

```
xl=double(sol.xl(sol.xl<0));
```

```
yl=double(sol.yl(sol.xl<0));
```

```
zl=double(sol.zl(sol.xl<0));
```

```
xs=6*sin(pi/6);
```

```
ys=-6*cos(pi/6);
```

```
zs=-1;
```

```
xu=-6;
```

```
yu=0;
```

```
zu=-1;
```

```
xv=xs;
```

```
yv=-ys;
```

```
zv=-1;
```

```
syms xm ym zm xp yp zp xq yq zq;
```

```
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
```

```
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
```

```

eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));

```

```
zu1=zp;  
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));  
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));  
zv1=zq;
```

```
rho_s=(xs1^2+ys1^2+zs1^2)^0.5;  
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;  
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;
```

```
positions.xo=xo;  
positions.yo=yo;  
positions.zo=zo;  
positions.xa=xa;  
positions.ya=ya;  
positions.za=za;  
positions.xb=xb;  
positions.yb=yb;  
positions.zb=zb;  
positions.xc=xc;  
positions.yc=yc;  
positions.zc=zc;  
positions.xd=xd;  
positions.yd=yd;  
positions.zd=zd;  
positions.xe=xe;  
positions.ye=ye;  
positions.ze=ze;
```

```
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl;
positions.zl=zl;
positions.xm=xm;
positions.ym=ym;
positions.zm=zm;
positions.xp=xp;
positions.yp=yp;
positions.zp=zp;
```

```
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
positions.rho_s=rho_s;
positions.rho_u=rho_u;
positions.rho_v=rho_v;
disp(positions);
```



### 三、运动学求解代码（凸轮方案运动功能设计）

```
clear;

L_tri=7.5;

%O1=(0,5,21);O2=(0,5,27);O3=(5*cos(pi/6),-5*sin(pi/6),21);O4=(5*cos(pi/6),-
5*sin(pi/6),27)

for i=27:-0.5:21

    xo=0;

    yo=5;

    zo=i;

    xa=xo+L_tri/2;

    ya=yo-L_tri/(2*3^0.5);

    za=zo;

    xb=xo-L_tri/2;

    yb=yo-L_tri/(2*3^0.5);

    zb=zo;

    xc=xo;

    yc=yo+L_tri/(3^0.5);

    zc=zo;

    xg=10*cos(pi/6);

    yg=-10*sin(pi/6);

    zg=0;

    xh=-xg;

    yh=yg;

    zh=zg;

    xi=0;
```

```

yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)^3^0.5;

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;
eq9=xi-xf==(yi-yf)^3^0.5;

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```

```
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
```

```
L3=4.4;
```

```
L4=4.2;
```

```
L5=5.3;
```

```
xj=xg;
```

```
yj=yg+L3*(zd-zg)/L2;
```

```
zj=zg-L3*(yd-yg)/L2;
```

```
syms xk yk zk;
```

```
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
```

```
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
```

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xl,yl,zl]);
```

```
xl=double(sol.xl(sol.xl<0));
```

```
yl=double(sol.yl(sol.xl<0));
```

```
zl=double(sol.zl(sol.xl<0));
```

```
xs=6*sin(pi/6);
```

```
ys=-6*cos(pi/6);
```

```
zs=-1;
```

```
xu=-6;
```

```
yu=0;
```

```
zu=-1;
```

```
xv=xS;
```

```
yv=-ys;
```

```
zv=-1;
```

```
syms xm ym zm xp yp zp xq yq zq;
```

```
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
```

```
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
```

```
eq3=zs==zm;
```

```
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
```

```
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
```

```
eq6=zp==zu;
```

```
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
```

```
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
```

```
eq9=zq==zv;
```

```
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
```

```
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
```

```
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
```

```
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
```

```

zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;

```

positions.zo=zo;  
positions.xa=xa;  
positions.ya=ya;  
positions.za=za;  
positions.xb=xb;  
positions.yb=yb;  
positions.zb=zb;  
positions.xc=xc;  
positions.yc=yc;  
positions.zc=zc;  
positions.xd=xd;  
positions.yd=yd;  
positions.zd=zd;  
positions.xe=xe;  
positions.ye=ye;  
positions.ze=ze;  
positions.xf=xf;  
positions.yf=yf;  
positions.zf=zf;  
positions.xg=xg;  
positions.yg=yg;  
positions.zg=zg;  
positions.xh=xh;  
positions.yh=yh;  
positions.zh=zh;  
positions.xi=xi;  
positions.yi=yi;

positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;  
positions.xs=xs;  
positions.ys=ys;  
positions.zs=zs;  
positions.xu=xu;  
positions.yu=yu;  
positions.zu=zu;  
positions.xv=xv;  
positions.yv=yv;





```

xo=i*5*cos(pi/6);
yo=5-i*(5*sin(pi/6)+5);
zo=21;

xa=xo+L_tri/2;
ya=yo-L_tri/(2*3^0.5);
za=zo;

xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;

xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;

xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;

xh=-xg;
yh=yg;
zh=zg;

xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;

syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;

```

$$eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;$$

$$eq3=xd==xg;$$

$$eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;$$

$$eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;$$

$$eq6=xe-xh==(yh-ye)^3^{0.5};$$

$$eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;$$

$$eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;$$

$$eq9=xi-xf==(yi-yf)^3^{0.5};$$

$$eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];$$

$$sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);$$

$$xd=double(sol.xd(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$yd=double(sol.yd(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$zd=double(sol.zd(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$xe=double(sol.xe(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$ye=double(sol.ye(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$ze=double(sol.ze(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$xf=double(sol.xf(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$yf=double(sol.yf(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$zf=double(sol.zf(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$L3=4.4;$$

$$L4=4.2;$$

$$L5=5.3;$$

$$xj=xg;$$

$$y_j = y_g + L_3 \cdot (z_d - z_g) / L_2;$$

$$z_j = z_g - L_3 \cdot (y_d - y_g) / L_2;$$

$$\text{syms } x_k \ y_k \ z_k;$$

$$\text{eq1} = (x_k - x_h)^2 + (y_k - y_h)^2 + (z_k - z_h)^2 == L_3^2;$$

$$\text{eq2} = (x_k - x_e)^2 + (y_k - y_e)^2 + (z_k - z_e)^2 == L_3^2 + L_2^2;$$

$$\text{eq3} = -\sin(\pi/6) \cdot (x_k - x_h) - \cos(\pi/6) \cdot (y_k - y_h) == 0;$$

$$\text{eqns} = [\text{eq1}, \text{eq2}, \text{eq3}];$$

$$\text{sol} = \text{solve}(\text{eqns}, [x_k, y_k, z_k]);$$

$$x_k = \text{double}(\text{sol}.x_k(\text{sol}.x_k > x_h));$$

$$y_k = \text{double}(\text{sol}.y_k(\text{sol}.x_k > x_h));$$

$$z_k = \text{double}(\text{sol}.z_k(\text{sol}.x_k > x_h));$$

$$\text{syms } x_l \ y_l \ z_l;$$

$$\text{eq1} = (x_l - x_i)^2 + (y_l - y_i)^2 + (z_l - z_i)^2 == L_3^2;$$

$$\text{eq2} = (x_l - x_f)^2 + (y_l - y_f)^2 + (z_l - z_f)^2 == L_2^2 + L_3^2;$$

$$\text{eq3} = -\sin(\pi/6) \cdot (x_l - x_i) + \cos(\pi/6) \cdot (y_l - y_i) == 0;$$

$$\text{eqns} = [\text{eq1}, \text{eq2}, \text{eq3}];$$

$$\text{sol} = \text{solve}(\text{eqns}, [x_l, y_l, z_l]);$$

$$x_l = \text{double}(\text{sol}.x_l(\text{sol}.x_l < 0));$$

$$y_l = \text{double}(\text{sol}.y_l(\text{sol}.x_l < 0));$$

$$z_l = \text{double}(\text{sol}.z_l(\text{sol}.x_l < 0));$$

$$x_s = 6 \cdot \sin(\pi/6);$$

$$y_s = -6 \cdot \cos(\pi/6);$$

$$z_s = -1;$$

$$x_u = -6;$$

```

yu=0;
zu=-1;
xv=xs;
yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;

```

```
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
```

positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;  
positions.xs=xs;  
positions.ys=ys;  
positions.zs=zs;  
positions.xu=xu;  
positions.yu=yu;  
positions.zu=zu;  
positions.xv=xv;  
positions.yv=yv;  
positions.zv=zv;  
positions.xs1=xs1;  
positions.ys1=ys1;  
positions.zs1=zs1;  
positions.xu1=xu1;  
positions.yu1=yu1;  
positions.zu1=zu1;

[illegible]

```
for i=21:0.5:26.5
```

24



```

za=zo;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

```

$$\text{eq7}=(\text{xc}-\text{xf})^2+(\text{yc}-\text{yf})^2+(\text{zc}-\text{zf})^2==\text{L1}^2;$$

$$\text{eq8}=(\text{xi}-\text{xf})^2+(\text{yi}-\text{yf})^2+(\text{zi}-\text{zf})^2==\text{L2}^2;$$

$$\text{eq9}=\text{xi}-\text{xf}==(\text{yi}-\text{yf})^3^{0.5};$$

$$\text{eqns}=[\text{eq1},\text{eq2},\text{eq3},\text{eq4},\text{eq5},\text{eq6},\text{eq7},\text{eq8},\text{eq9}];$$

$$\text{sol}=\text{solve}(\text{eqns},[\text{xd},\text{yd},\text{zd},\text{xe},\text{ye},\text{ze},\text{xf},\text{yf},\text{zf}]);$$

$$\text{xd}=\text{double}(\text{sol}.\text{xd}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{yd}=\text{double}(\text{sol}.\text{yd}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{zd}=\text{double}(\text{sol}.\text{zd}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{xe}=\text{double}(\text{sol}.\text{xe}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{ye}=\text{double}(\text{sol}.\text{ye}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{ze}=\text{double}(\text{sol}.\text{ze}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{xf}=\text{double}(\text{sol}.\text{xf}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{yf}=\text{double}(\text{sol}.\text{yf}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{zf}=\text{double}(\text{sol}.\text{zf}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{L3}=4.4;$$

$$\text{L4}=4.2;$$

$$\text{L5}=5.3;$$

$$\text{xj}=\text{xg};$$

$$\text{yj}=\text{yg}+\text{L3}^*(\text{zd}-\text{zg})/\text{L2};$$

$$\text{zj}=\text{zg}-\text{L3}^*(\text{yd}-\text{yg})/\text{L2};$$

$$\text{syms } \text{xk } \text{yk } \text{zk};$$

$$\text{eq1}=(\text{xk}-\text{xh})^2+(\text{yk}-\text{yh})^2+(\text{zk}-\text{zh})^2==\text{L3}^2;$$

$$\text{eq2}=(\text{xk}-\text{xe})^2+(\text{yk}-\text{ye})^2+(\text{zk}-\text{ze})^2==\text{L3}^2+\text{L2}^2;$$

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xl,yl,zl]);
```

```
xl=double(sol.xl(sol.xl<0));
```

```
yl=double(sol.yl(sol.xl<0));
```

```
zl=double(sol.zl(sol.xl<0));
```

```
xs=6*sin(pi/6);
```

```
ys=-6*cos(pi/6);
```

```
zs=-1;
```

```
xu=-6;
```

```
yu=0;
```

```
zu=-1;
```

```
xv=xS;
```

```
yv=-ys;
```

```
zv=-1;
```

```

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));

```

```

zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;

```

```
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl;
positions.zl=zl;
positions.xm=xm;
positions.ym=ym;
positions.zm=zm;
```







```

zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)^3^0.5;

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;
eq9=xi-xf==(yi-yf)^3^0.5;

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];

```

```

sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```

```
L3=4.4;
```

```
L4=4.2;
```

```
L5=5.3;
```

```
xj=xg;
```

```
yj=yg+L3*(zd-zg)/L2;
```

```
zj=zg-L3*(yd-yg)/L2;
```

```
syms xk yk zk;
```

```
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
```

```
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
```

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```

syms xl yl zl;
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xl,yl,zl]);
xl=double(sol.xl(sol.xl<0));
yl=double(sol.yl(sol.xl<0));
zl=double(sol.zl(sol.xl<0));

```

```

xs=6*sin(pi/6);
ys=-6*cos(pi/6);
zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=x;
yv=-y;
zv=-1;

```

```

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;

```

```

eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));

```

zv1=zq;

rho\_s=(xs1^2+ys1^2+zs1^2)^0.5;

rho\_u=(xu1^2+yu1^2+zu1^2)^0.5;

rho\_v=(xv1^2+yv1^2+zv1^2)^0.5;

positions.xo=xo;

positions.yo=yo;

positions.zo=zo;

positions.xa=xa;

positions.ya=ya;

positions.za=za;

positions.xb=xb;

positions.yb=yb;

positions.zb=zb;

positions.xc=xc;

positions.yc=yc;

positions.zc=zc;

positions.xd=xd;

positions.yd=yd;

positions.zd=zd;

positions.xe=xe;

positions.ye=ye;

positions.ze=ze;

positions.xf=xf;

positions.yf=yf;

positions.zf=zf;

positions.xg=xg;  
positions.yg=yg;  
positions.zg=zg;  
positions.xh=xh;  
positions.yh=yh;  
positions.zh=zh;  
positions.xi=xi;  
positions.yi=yi;  
positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;



```
s.yq,positions.zq,positions.xs,positions.ys,positions.zs,positions.xu,positions.yu,positions.zu,positions.xv,positions.yv,positions.zv,positions.xs1,positions.ys1,positions.zs1,positions.xu1,positions.yu1,positions.zu1,positions.xv1,positions.yv1,positions.zv1);
```

```
end;
```

```
for i=1/12:1/12:11/12
```

```
    xo=5*cos(pi/6)-i*2*5*cos(pi/6);
```

```
    yo=-5*sin(pi/6);
```

```
    zo=21;
```

```
    xa=xo+L_tri/2;
```

```
    ya=yo-L_tri/(2*3^0.5);
```

```
    za=zo;
```

```
    xb=xo-L_tri/2;
```

```
    yb=yo-L_tri/(2*3^0.5);
```

```
    zb=zo;
```

```
    xc=xo;
```

```
    yc=yo+L_tri/(3^0.5);
```

```
    zc=zo;
```

```
    xg=10*cos(pi/6);
```

```
    yg=-10*sin(pi/6);
```

```
    zg=0;
```

```
    xh=-xg;
```

```
    yh=yg;
```



```

zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)^3^0.5;

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;
eq9=xi-xf==(yi-yf)^3^0.5;

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```

```

ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```

```
L3=4.4;
```

```
L4=4.2;
```

```
L5=5.3;
```

```
xj=xg;
```

```
yj=yg+L3*(zd-zg)/L2;
```

```
zj=zg-L3*(yd-yg)/L2;
```

```
syms xk yk zk;
```

```
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
```

```
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
```

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```

sol=solve(eqns,[xl,yl,zl]);
xl=double(sol.xl(sol.xl<0));
yl=double(sol.yl(sol.xl<0));
zl=double(sol.zl(sol.xl<0));

xs=6*sin(pi/6);
ys=-6*cos(pi/6);
zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=x;
yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);

```

```

xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```
positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
```

positions.xi=xi;  
positions.yi=yi;  
positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;  
positions.xs=xs;  
positions.ys=ys;  
positions.zs=zs;  
positions.xu=xu;  
positions.yu=yu;  
positions.zu=zu;



```
for i=21:0.5:26.5
```

```
    xo=-5*cos(pi/6);
```

```
    yo=-5*sin(pi/6);
```

```
    zo=i;
```

```
    xa=xo+L_tri/2;
```

```
    ya=yo-L_tri/(2*3^0.5);
```

```
    za=zo;
```

```
    xb=xo-L_tri/2;
```

```
    yb=yo-L_tri/(2*3^0.5);
```

```
    zb=zo;
```

```
    xc=xo;
```

```
    yc=yo+L_tri/(3^0.5);
```

```
    zc=zo;
```

```
    xg=10*cos(pi/6);
```

```
    yg=-10*sin(pi/6);
```

```
    zg=0;
```

```
    xh=-xg;
```

```
    yh=yg;
```

```
    zh=zg;
```

```
    xi=0;
```

```
    yi=10;
```

```
    zi=0;
```

```
    L1=20.8;
```

```
    L2=10.8;
```



```

syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)^3^0.5;

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;
eq9=xi-xf==(yi-yf)^3^0.5;

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));

L3=4.4;
L4=4.2;

```

```

L5=5.3;

xj=xg;

yj=yg+L3*(zd-zg)/L2;

zj=zg-L3*(yd-yg)/L2;


syms xk yk zk;

eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;

eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;

eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;

eqns=[eq1,eq2,eq3];

sol=solve(eqns,[xk,yk,zk]);

xk=double(sol.xk(sol.xk>xh));

yk=double(sol.yk(sol.xk>xh));

zk=double(sol.zk(sol.xk>xh));


syms xl yl zl;

eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;

eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;

eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;

eqns=[eq1,eq2,eq3];

sol=solve(eqns,[xl,yl,zl]);

xl=double(sol.xl(sol.xl<0));

yl=double(sol.yl(sol.xl<0));

zl=double(sol.zl(sol.xl<0));


xs=6*sin(pi/6);

ys=-6*cos(pi/6);

```

```

zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=xs;
yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));  
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
```

```
alpha=pi*3/4;  
L6=2.5;  
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));  
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));  
zs1=zm;  
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));  
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));  
zu1=zp;  
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));  
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));  
zv1=zq;
```

```
rho_s=(xs1^2+ys1^2+zs1^2)^0.5;  
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;  
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;
```

```
positions.xo=xo;  
positions.yo=yo;  
positions.zo=zo;  
positions.xa=xa;  
positions.ya=ya;  
positions.za=za;  
positions.xb=xb;
```

```
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
```

positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;  
positions.xs=xs;  
positions.ys=ys;  
positions.zs=zs;  
positions.xu=xu;  
positions.yu=yu;  
positions.zu=zu;  
positions.xv=xv;  
positions.yv=yv;  
positions.zv=zv;  
positions.xs1=xs1;  
positions.ys1=ys1;  
positions.zs1=zs1;  
positions.xu1=xu1;

[illegible]

```
for i=27:-0.5:21
```

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```

ya=yo-L_tri/(2*3^0.5);
za=zo;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;

```



$$eq6 = x_e - x_h == (y_h - y_e) * 3^{0.5};$$

$$eq7 = (x_c - x_f)^2 + (y_c - y_f)^2 + (z_c - z_f)^2 == L1^2;$$

$$eq8 = (x_i - x_f)^2 + (y_i - y_f)^2 + (z_i - z_f)^2 == L2^2;$$

$$eq9 = x_i - x_f == (y_i - y_f) * 3^{0.5};$$

$$eqns = [eq1, eq2, eq3, eq4, eq5, eq6, eq7, eq8, eq9];$$

$$sol = solve(eqns, [x_d, y_d, z_d, x_e, y_e, z_e, x_f, y_f, z_f]);$$

$$x_d = double(sol.xd(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$y_d = double(sol.yd(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$z_d = double(sol.zd(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$x_e = double(sol.xe(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$y_e = double(sol.ye(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$z_e = double(sol.ze(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$x_f = double(sol.xf(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$y_f = double(sol.yf(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$z_f = double(sol.zf(sol.yd > 0 \& sol.xe > -5 \& sol.xf < 0));$$

$$L3 = 4.4;$$

$$L4 = 4.2;$$

$$L5 = 5.3;$$

$$x_j = x_g;$$

$$y_j = y_g + L3 * (z_d - z_g) / L2;$$

$$z_j = z_g - L3 * (y_d - y_g) / L2;$$

$$\text{syms } x_k \ y_k \ z_k;$$

$$eq1 = (x_k - x_h)^2 + (y_k - y_h)^2 + (z_k - z_h)^2 == L3^2;$$

$$eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;$$

$$eq3=-\sin(\pi/6)*(xk-xh)-\cos(\pi/6)*(yk-yh)==0;$$

$$eqns=[eq1,eq2,eq3];$$

$$sol=solve(eqns,[xk,yk,zk]);$$

$$xk=double(sol.xk(sol.xk>xh));$$

$$yk=double(sol.yk(sol.xk>xh));$$

$$zk=double(sol.zk(sol.xk>xh));$$

$$\text{syms } xl \ yl \ zl;$$

$$eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;$$

$$eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;$$

$$eq3=-\sin(\pi/6)*(xl-xi)+\cos(\pi/6)*(yl-yi)==0;$$

$$eqns=[eq1,eq2,eq3];$$

$$sol=solve(eqns,[xl,yl,zl]);$$

$$xl=double(sol.xl(sol.xl<0));$$

$$yl=double(sol.yl(sol.xl<0));$$

$$zl=double(sol.zl(sol.xl<0));$$

$$xs=6*\sin(\pi/6);$$

$$ys=-6*\cos(\pi/6);$$

$$zs=-1;$$

$$xu=-6;$$

$$yu=0;$$

$$zu=-1;$$

$$xv=x;$$

$$yv=-y;$$

$$zv=-1;$$

```

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));

```

```

ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;

```

positions.zd=zd;  
positions.xe=xe;  
positions.ye=ye;  
positions.ze=ze;  
positions.xf=xf;  
positions.yf=yf;  
positions.zf=zf;  
positions.xg=xg;  
positions.yg=yg;  
positions.zg=zg;  
positions.xh=xh;  
positions.yh=yh;  
positions.zh=zh;  
positions.xi=xi;  
positions.yi=yi;  
positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;

```
positions.zm=zm;
positions.xp=xp;
positions.yp=yp;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
fileID=fopen('spiderhand_positions.txt','a');
dispcontent=positions;
```



```

yc=yo+L_tri/(3^0.5);
zc=z0;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;
eq9=xi-xf==(yi-yf)*3^0.5;

```



```

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```

```
L3=4.4;
```

```
L4=4.2;
```

```
L5=5.3;
```

```
xj=xg;
```

```
yj=yg+L3*(zd-zg)/L2;
```

```
zj=zg-L3*(yd-yg)/L2;
```

```
syms xk yk zk;
```

```
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
```

```
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
```

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xl,yl,zl]);
```

```
xl=double(sol.xl(sol.xl<0));
```

```
yl=double(sol.yl(sol.xl<0));
```

```
zl=double(sol.zl(sol.xl<0));
```

```
xs=6*sin(pi/6);
```

```
ys=-6*cos(pi/6);
```

```
zs=-1;
```

```
xu=-6;
```

```
yu=0;
```

```
zu=-1;
```

```
xv=xu;
```

```
yv=-yu;
```

```
zv=-1;
```

```
syms xm ym zm xp yp zp xq yq zq;
```

```
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
```

```
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
```

```
eq3=zs==zm;
```

```
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
```

```

eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));

```

```
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
```

```
zv1=zq;
```

```
rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
```

```
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
```

```
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;
```

```
positions.xo=xo;
```

```
positions.yo=yo;
```

```
positions.zo=zo;
```

```
positions.xa=xa;
```

```
positions.ya=ya;
```

```
positions.za=za;
```

```
positions.xb=xb;
```

```
positions.yb=yb;
```

```
positions.zb=zb;
```

```
positions.xc=xc;
```

```
positions.yc=yc;
```

```
positions.zc=zc;
```

```
positions.xd=xd;
```

```
positions.yd=yd;
```

```
positions.zd=zd;
```

```
positions.xe=xe;
```

```
positions.ye=ye;
```

```
positions.ze=ze;
```

```
positions.xf=xf;
```

```
positions.yf=yf;
```

positions.zf=zf;  
positions.xg=xg;  
positions.yg=yg;  
positions.zg=zg;  
positions.xh=xh;  
positions.yh=yh;  
positions.zh=zh;  
positions.xi=xi;  
positions.yi=yi;  
positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;



```
tions.ym,positions.zm,positions.xp,positions.yp,positions.zp,positions.xq,positions.yq,positions.zq,positions.xs,positions.ys,positions.zs,positions.xu,positions.yu,positions.zu,positions.xv,positions.yv,positions.zv,positions.xs1,positions.ys1,positions.zs1,positions.xu1,positions.yu1,positions.zu1,positions.xv1,positions.yv1,positions.zv1);
```

```
end;
```

```
for i=21:0.5:26.5
```

```
    xo=0;
```

```
    yo=5;
```

```
    zo=i;
```

```
    xa=xo+L_tri/2;
```

```
    ya=yo-L_tri/(2*3^0.5);
```

```
    za=zo;
```

```
    xb=xo-L_tri/2;
```

```
    yb=yo-L_tri/(2*3^0.5);
```

```
    zb=zo;
```

```
    xc=xo;
```

```
    yc=yo+L_tri/(3^0.5);
```

```
    zc=zo;
```

```
    xg=10*cos(pi/6);
```

```
    yg=-10*sin(pi/6);
```

```
    zg=0;
```

```
    xh=-xg;
```

```
    yh=yg;
```

```

zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)^3^0.5;

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;
eq9=xi-xf==(yi-yf)^3^0.5;

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```



```

ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```

```
L3=4.4;
```

```
L4=4.2;
```

```
L5=5.3;
```

```
xj=xg;
```

```
yj=yg+L3*(zd-zg)/L2;
```

```
zj=zg-L3*(yd-yg)/L2;
```

```
syms xk yk zk;
```

```
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
```

```
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
```

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```

sol=solve(eqns,[xl,yl,zl]);
xl=double(sol.xl(sol.xl<0));
yl=double(sol.yl(sol.xl<0));
zl=double(sol.zl(sol.xl<0));

xs=6*sin(pi/6);
ys=-6*cos(pi/6);
zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=x;
yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);

```

```

xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```
positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
```

positions.xi=xi;  
positions.yi=yi;  
positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;  
positions.xs=xs;  
positions.ys=ys;  
positions.zs=zs;  
positions.xu=xu;  
positions.yu=yu;  
positions.zu=zu;



```
fclose(fileID);
```

## 四、逆运动学求解代码（电机方案运动功能设计）

```
clear;
L_tri=7.5;
%O1=(0,5,25);O2=(0,5,20);O3=(5*cos(pi/6),5*sin(pi/6),20);O4=(5*cos(pi/6),5*sin(pi/6),25)
xo=5*cos(pi/6);
yo=5*sin(pi/6);
zo=27;
x_target=0;
y_target=5;
z_target=27;
x_ball1=5;
y_ball1=10;
z_ball1=27;
x_ball2=-7;
y_ball2=-7;
z_ball2=27;
x_ball3=3;
y_ball3=6;
z_ball3=27;
x_ball4=6;
y_ball4=-4;
z_ball4=27;
xa=xo+L_tri/2;
ya=yo-L_tri/(2*3^0.5);
```

```

za=zo;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

```



```

eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;
eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;
eq9=xi-xf==(yi-yf)*3^0.5;

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);
xd=double(sol.xd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yd=double(sol.yd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zd=double(sol.zd(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xe=double(sol.xe(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ye=double(sol.ye(sol.yd>0 & sol.xe>-5 & sol.xf<0));
ze=double(sol.ze(sol.yd>0 & sol.xe>-5 & sol.xf<0));
xf=double(sol.xf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
yf=double(sol.yf(sol.yd>0 & sol.xe>-5 & sol.xf<0));
zf=double(sol.zf(sol.yd>0 & sol.xe>-5 & sol.xf<0));

```

```

L3=4.4;
L4=4.2;
L5=5.3;
xj=xg;
yj=yg+L3*(zd-zg)/L2;
zj=zg-L3*(yd-yg)/L2;

```

```

syms xk yk zk;
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;

```

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xl,yl,zl]);
```

```
xl=double(sol.xl(sol.xl<0));
```

```
yl=double(sol.yl(sol.xl<0));
```

```
zl=double(sol.zl(sol.xl<0));
```

```
xs=6*sin(pi/6);
```

```
ys=-6*cos(pi/6);
```

```
zs=-1;
```

```
xu=-6;
```

```
yu=0;
```

```
zu=-1;
```

```
xv=xu;
```

```
yv=-yu;
```

```
zv=-1;
```

```

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));

```

```

zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;

```

```
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl;
positions.zl=zl;
positions.xm=xm;
positions.ym=ym;
positions.zm=zm;
```

```
positions.xp=xp;
positions.yp=yp;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
positions.rho_s=rho_s;
positions.rho_u=rho_u;
positions.rho_v=rho_v;
```

```
positions.x_target=x_target;  
positions.y_target=y_target;  
positions.z_target=z_target;
```

```
for i=-10:0.5:0
```

```
    positions.xo=xo+i;  
    positions.yo=yo-10;  
    positions.zo=zo;  
    positions.xa=xa+i;  
    positions.ya=ya-10;  
    positions.za=za;  
    positions.xb=xb+i;  
    positions.yb=yb-10;  
    positions.zb=zb;  
    positions.xc=xc+i;  
    positions.yc=yc-10;  
    positions.zc=zc;  
    positions.xd=xd+i;  
    positions.yd=yd-10;  
    positions.zd=zd;  
    positions.xe=xe+i;  
    positions.ye=ye-10;  
    positions.ze=ze;  
    positions.xf=xf+i;  
    positions.yf=yf-10;  
    positions.zf=zf;  
    positions.xg=xg+i;
```

```
positions.yg=yg-10;
positions.zg=zg;
positions.xh=xh+i;
positions.yh=yh-10;
positions.zh=zh;
positions.xi=xi+i;
positions.yi=yi-10;
positions.zi=zi;
positions.xj=xj+i;
positions.yj=yj-10;
positions.zj=zj;
positions.xk=xk+i;
positions.yk=yk-10;
positions.zk=zk;
positions.xl=xl+i;
positions.yl=yl-10;
positions.zl=zl;
positions.xm=xm+i;
positions.ym=ym-10;
positions.zm=zm;
positions.xp=xp+i;
positions.yp=yp-10;
positions.zp=zp;
positions.xq=xq+i;
positions.yq=yq-10;
positions.zq=zq;
positions.xs=xs+i;
```







```
positions.zd=zd;
positions.xe=xe;
positions.ye=ye+i;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf+i;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg+i;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh+i;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi+i;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj+i;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk+i;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl+i;
positions.zl=zl;
positions.xm=xm;
positions.ym=ym+i;
```

```
positions.zm=zm;
positions.xp=xp;
positions.yp=yp+i;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq+i;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys+i;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu+i;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv+i;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1+i;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1+i;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1+i;
positions.zv1=zv1;
positions.rho_s=rho_s;
positions.rho_u=rho_u;
```



```

za=zo;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

```

$$\text{eq7}=(\text{xc}-\text{xf})^2+(\text{yc}-\text{yf})^2+(\text{zc}-\text{zf})^2==\text{L1}^2;$$

$$\text{eq8}=(\text{xi}-\text{xf})^2+(\text{yi}-\text{yf})^2+(\text{zi}-\text{zf})^2==\text{L2}^2;$$

$$\text{eq9}=\text{xi}-\text{xf}==(\text{yi}-\text{yf})^3^{0.5};$$

$$\text{eqns}=[\text{eq1},\text{eq2},\text{eq3},\text{eq4},\text{eq5},\text{eq6},\text{eq7},\text{eq8},\text{eq9}];$$

$$\text{sol}=\text{solve}(\text{eqns},[\text{xd},\text{yd},\text{zd},\text{xe},\text{ye},\text{ze},\text{xf},\text{yf},\text{zf}]);$$

$$\text{xd}=\text{double}(\text{sol}.\text{xd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{yd}=\text{double}(\text{sol}.\text{yd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{zd}=\text{double}(\text{sol}.\text{zd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{xe}=\text{double}(\text{sol}.\text{xe}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{ye}=\text{double}(\text{sol}.\text{ye}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{ze}=\text{double}(\text{sol}.\text{ze}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{xf}=\text{double}(\text{sol}.\text{xf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{yf}=\text{double}(\text{sol}.\text{yf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{zf}=\text{double}(\text{sol}.\text{zf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{L3}=4.4;$$

$$\text{L4}=4.2;$$

$$\text{L5}=5.3;$$

$$\text{xj}=\text{xg};$$

$$\text{yj}=\text{yg}+\text{L3}^*(\text{zd}-\text{zg})/\text{L2};$$

$$\text{zj}=\text{zg}-\text{L3}^*(\text{yd}-\text{yg})/\text{L2};$$

$$\text{syms } \text{xk } \text{yk } \text{zk};$$

$$\text{eq1}=(\text{xk}-\text{xh})^2+(\text{yk}-\text{yh})^2+(\text{zk}-\text{zh})^2==\text{L3}^2;$$

$$\text{eq2}=(\text{xk}-\text{xe})^2+(\text{yk}-\text{ye})^2+(\text{zk}-\text{ze})^2==\text{L3}^2+\text{L2}^2;$$

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xl,yl,zl]);
```

```
xl=double(sol.xl(sol.xl<0));
```

```
yl=double(sol.yl(sol.xl<0));
```

```
zl=double(sol.zl(sol.xl<0));
```

```
xs=6*sin(pi/6);
```

```
ys=-6*cos(pi/6);
```

```
zs=-1;
```

```
xu=-6;
```

```
yu=0;
```

```
zu=-1;
```

```
xv=xS;
```

```
yv=-ys;
```

```
zv=-1;
```



```

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));

```

```

zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;

```

```
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl;
positions.zl=zl;
positions.xm=xm;
positions.ym=ym;
positions.zm=zm;
```

```
positions.xp=xp;
positions.yp=yp;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
positions.x_target=x_target;
positions.y_target=y_target;
positions.z_target=z_target;
```



```

za=zo;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

```

$$\text{eq7}=(\text{xc}-\text{xf})^2+(\text{yc}-\text{yf})^2+(\text{zc}-\text{zf})^2==\text{L1}^2;$$

$$\text{eq8}=(\text{xi}-\text{xf})^2+(\text{yi}-\text{yf})^2+(\text{zi}-\text{zf})^2==\text{L2}^2;$$

$$\text{eq9}=\text{xi}-\text{xf}==(\text{yi}-\text{yf})^3^{0.5};$$

$$\text{eqns}=[\text{eq1},\text{eq2},\text{eq3},\text{eq4},\text{eq5},\text{eq6},\text{eq7},\text{eq8},\text{eq9}];$$

$$\text{sol}=\text{solve}(\text{eqns},[\text{xd},\text{yd},\text{zd},\text{xe},\text{ye},\text{ze},\text{xf},\text{yf},\text{zf}]);$$

$$\text{xd}=\text{double}(\text{sol}.\text{xd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{yd}=\text{double}(\text{sol}.\text{yd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{zd}=\text{double}(\text{sol}.\text{zd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{xe}=\text{double}(\text{sol}.\text{xe}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{ye}=\text{double}(\text{sol}.\text{ye}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{ze}=\text{double}(\text{sol}.\text{ze}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{xf}=\text{double}(\text{sol}.\text{xf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{yf}=\text{double}(\text{sol}.\text{yf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{zf}=\text{double}(\text{sol}.\text{zf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{L3}=4.4;$$

$$\text{L4}=4.2;$$

$$\text{L5}=5.3;$$

$$\text{xj}=\text{xg};$$

$$\text{yj}=\text{yg}+\text{L3}^*(\text{zd}-\text{zg})/\text{L2};$$

$$\text{zj}=\text{zg}-\text{L3}^*(\text{yd}-\text{yg})/\text{L2};$$

$$\text{syms } \text{xk } \text{yk } \text{zk};$$

$$\text{eq1}=(\text{xk}-\text{xh})^2+(\text{yk}-\text{yh})^2+(\text{zk}-\text{zh})^2==\text{L3}^2;$$

$$\text{eq2}=(\text{xk}-\text{xe})^2+(\text{yk}-\text{ye})^2+(\text{zk}-\text{ze})^2==\text{L3}^2+\text{L2}^2;$$

```
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xk,yk,zk]);
```

```
xk=double(sol.xk(sol.xk>xh));
```

```
yk=double(sol.yk(sol.xk>xh));
```

```
zk=double(sol.zk(sol.xk>xh));
```

```
syms xl yl zl;
```

```
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
```

```
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
```

```
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
```

```
eqns=[eq1,eq2,eq3];
```

```
sol=solve(eqns,[xl,yl,zl]);
```

```
xl=double(sol.xl(sol.xl<0));
```

```
yl=double(sol.yl(sol.xl<0));
```

```
zl=double(sol.zl(sol.xl<0));
```

```
xs=6*sin(pi/6);
```

```
ys=-6*cos(pi/6);
```

```
zs=-1;
```

```
xu=-6;
```

```
yu=0;
```

```
zu=-1;
```

```
xv=xS;
```

```
yv=-ys;
```

```
zv=-1;
```



```

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));

```

```

zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;

```

```
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl;
positions.zl=zl;
positions.xm=xm;
positions.ym=ym;
positions.zm=zm;
```

```
positions.xp=xp;
positions.yp=yp;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
positions.x_target=x_target;
positions.y_target=y_target;
positions.z_target=z_target;
```



```

xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

```

$$\text{eq7}=(\text{xc}-\text{xf})^2+(\text{yc}-\text{yf})^2+(\text{zc}-\text{zf})^2==\text{L1}^2;$$

$$\text{eq8}=(\text{xi}-\text{xf})^2+(\text{yi}-\text{yf})^2+(\text{zi}-\text{zf})^2==\text{L2}^2;$$

$$\text{eq9}=\text{xi}-\text{xf}==(\text{yi}-\text{yf})^3^{0.5};$$

$$\text{eqns}=[\text{eq1},\text{eq2},\text{eq3},\text{eq4},\text{eq5},\text{eq6},\text{eq7},\text{eq8},\text{eq9}];$$

$$\text{sol}=\text{solve}(\text{eqns},[\text{xd},\text{yd},\text{zd},\text{xe},\text{ye},\text{ze},\text{xf},\text{yf},\text{zf}]);$$

$$\text{xd}=\text{double}(\text{sol}.\text{xd}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{yd}=\text{double}(\text{sol}.\text{yd}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{zd}=\text{double}(\text{sol}.\text{zd}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{xe}=\text{double}(\text{sol}.\text{xe}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{ye}=\text{double}(\text{sol}.\text{ye}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{ze}=\text{double}(\text{sol}.\text{ze}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{xf}=\text{double}(\text{sol}.\text{xf}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{yf}=\text{double}(\text{sol}.\text{yf}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{zf}=\text{double}(\text{sol}.\text{zf}(\text{sol}.\text{yd}>0 \ \& \ \text{sol}.\text{xe}>-5 \ \& \ \text{sol}.\text{xf}<0));$$

$$\text{L3}=4.4;$$

$$\text{L4}=4.2;$$

$$\text{L5}=5.3;$$

$$\text{xj}=\text{xg};$$

$$\text{yj}=\text{yg}+\text{L3}*(\text{zd}-\text{zg})/\text{L2};$$

$$\text{zj}=\text{zg}-\text{L3}*(\text{yd}-\text{yg})/\text{L2};$$

$$\text{syms } \text{xk } \text{yk } \text{zk};$$

$$\text{eq1}=(\text{xk}-\text{xh})^2+(\text{yk}-\text{yh})^2+(\text{zk}-\text{zh})^2==\text{L3}^2;$$

$$\text{eq2}=(\text{xk}-\text{xe})^2+(\text{yk}-\text{ye})^2+(\text{zk}-\text{ze})^2==\text{L3}^2+\text{L2}^2;$$

$$\text{eq3}=-\sin(\pi/6)*(\text{xk}-\text{xh})-\cos(\pi/6)*(\text{yk}-\text{yh})==0;$$

```

eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xk,yk,zk]);
xk=double(sol.xk(sol.xk>xh));
yk=double(sol.yk(sol.xk>xh));
zk=double(sol.zk(sol.xk>xh));

syms xl yl zl;
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xl,yl,zl]);
xl=double(sol.xl(sol.xl<0));
yl=double(sol.yl(sol.xl<0));
zl=double(sol.zl(sol.xl<0));

xs=6*sin(pi/6);
ys=-6*cos(pi/6);
zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=xS;
yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;

```



```

eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;

```

```
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));  
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));  
zu1=zp;  
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));  
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));  
zv1=zq;
```

```
rho_s=(xs1^2+ys1^2+zs1^2)^0.5;  
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;  
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;
```

```
positions.xo=xo;  
positions.yo=yo;  
positions.zo=zo;  
positions.xa=xa;  
positions.ya=ya;  
positions.za=za;  
positions.xb=xb;  
positions.yb=yb;  
positions.zb=zb;  
positions.xc=xc;  
positions.yc=yc;  
positions.zc=zc;  
positions.xd=xd;  
positions.yd=yd;  
positions.zd=zd;  
positions.xe=xe;
```

```
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl;
positions.zl=zl;
positions.xm=xm;
positions.ym=ym;
positions.zm=zm;
positions.xp=xp;
```

```
positions.yq=yq;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
positions.x_target=x_target;
positions.y_target=y_target;
positions.z_target=z_target;
disp(positions);
```



```

xb=xo-L/2;
yb=yo-L/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;
eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;
eq6=xe-xh==(yh-ye)*3^0.5;

```

$$\text{eq7}=(x_c-x_f)^2+(y_c-y_f)^2+(z_c-z_f)^2==L1^2;$$

$$\text{eq8}=(x_i-x_f)^2+(y_i-y_f)^2+(z_i-z_f)^2==L2^2;$$

$$\text{eq9}=x_i-x_f==(y_i-y_f)^3^{0.5};$$

$$\text{eqns}=[\text{eq1},\text{eq2},\text{eq3},\text{eq4},\text{eq5},\text{eq6},\text{eq7},\text{eq8},\text{eq9}];$$

$$\text{sol}=\text{solve}(\text{eqns},[\text{xd},\text{yd},\text{zd},\text{xe},\text{ye},\text{ze},\text{xf},\text{yf},\text{zf}]);$$

$$\text{xd}=\text{double}(\text{sol.xd}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{yd}=\text{double}(\text{sol.yd}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{zd}=\text{double}(\text{sol.zd}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{xe}=\text{double}(\text{sol.xe}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{ye}=\text{double}(\text{sol.ye}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{ze}=\text{double}(\text{sol.ze}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{xf}=\text{double}(\text{sol.xf}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{yf}=\text{double}(\text{sol.yf}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$\text{zf}=\text{double}(\text{sol.zf}(\text{sol.yd}>0 \& \text{sol.xe}>-5 \& \text{sol.xf}<0));$$

$$L3=4.4;$$

$$L4=4.2;$$

$$L5=5.3;$$

$$x_j=x_g;$$

$$y_j=y_g+L3*(z_d-z_g)/L2;$$

$$z_j=z_g-L3*(y_d-y_g)/L2;$$

$$\text{syms } x_k \ y_k \ z_k;$$

$$\text{eq1}=(x_k-x_h)^2+(y_k-y_h)^2+(z_k-z_h)^2==L3^2;$$

$$\text{eq2}=(x_k-x_e)^2+(y_k-y_e)^2+(z_k-z_e)^2==L3^2+L2^2;$$

$$\text{eq3}=-\sin(\pi/6)*(x_k-x_h)-\cos(\pi/6)*(y_k-y_h)==0;$$

```

eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xk,yk,zk]);
xk=double(sol.xk(sol.xk>xh));
yk=double(sol.yk(sol.xk>xh));
zk=double(sol.zk(sol.xk>xh));

syms xl yl zl;
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xl,yl,zl]);
xl=double(sol.xl(sol.xl<0));
yl=double(sol.yl(sol.xl<0));
zl=double(sol.zl(sol.xl<0));

xs=6*sin(pi/6);
ys=-6*cos(pi/6);
zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=xS;
yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;

```



```

eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;

```

```

xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;
positions.xe=xe;

```

positions.ye=ye;  
positions.ze=ze;  
positions.xf=xf;  
positions.yf=yf;  
positions.zf=zf;  
positions.xg=xg;  
positions.yg=yg;  
positions.zg=zg;  
positions.xh=xh;  
positions.yh=yh;  
positions.zh=zh;  
positions.xi=xi;  
positions.yi=yi;  
positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zk;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;

```
positions.yq=yq;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
positions.x_target=x_target;
positions.y_target=y_target;
positions.z_target=z_target;
disp(positions);
```



```

xa=xo+L_tri/2;
ya=yo-L_tri/(2*3^0.5);
za=z0;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=z0;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=z0;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;

```

$$\text{eq5}=(x_h-x_e)^2+(y_h-y_e)^2+(z_h-z_e)^2==L2^2;$$

$$\text{eq6}=x_e-x_h==(y_h-y_e)^3^{0.5};$$

$$\text{eq7}=(x_c-x_f)^2+(y_c-y_f)^2+(z_c-z_f)^2==L1^2;$$

$$\text{eq8}=(x_i-x_f)^2+(y_i-y_f)^2+(z_i-z_f)^2==L2^2;$$

$$\text{eq9}=x_i-x_f==(y_i-y_f)^3^{0.5};$$

$$\text{eqns}=[\text{eq1},\text{eq2},\text{eq3},\text{eq4},\text{eq5},\text{eq6},\text{eq7},\text{eq8},\text{eq9}];$$

$$\text{sol}=\text{solve}(\text{eqns},[x_d,y_d,z_d,x_e,y_e,z_e,x_f,y_f,z_f]);$$

$$x_d=\text{double}(\text{sol}.x_d(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$y_d=\text{double}(\text{sol}.y_d(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$z_d=\text{double}(\text{sol}.z_d(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$x_e=\text{double}(\text{sol}.x_e(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$y_e=\text{double}(\text{sol}.y_e(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$z_e=\text{double}(\text{sol}.z_e(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$x_f=\text{double}(\text{sol}.x_f(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$y_f=\text{double}(\text{sol}.y_f(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$z_f=\text{double}(\text{sol}.z_f(\text{sol}.y_d>0 \& \text{sol}.x_e>-5 \& \text{sol}.x_f<0));$$

$$L3=4.4;$$

$$L4=4.2;$$

$$L5=5.3;$$

$$x_j=x_g;$$

$$y_j=y_g+L3*(z_d-z_g)/L2;$$

$$z_j=z_g-L3*(y_d-y_g)/L2;$$

$$\text{syms } x_k \ y_k \ z_k;$$

```

eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xk,yk,zk]);
xk=double(sol.xk(sol.xk>xh));
yk=double(sol.yk(sol.xk>xh));
zk=double(sol.zk(sol.xk>xh));

```

```

syms xl yl zl;
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xl,yl,zl]);
xl=double(sol.xl(sol.xl<0));
yl=double(sol.yl(sol.xl<0));
zl=double(sol.zl(sol.xl<0));

```

```

xs=6*sin(pi/6);
ys=-6*cos(pi/6);
zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=xS;
yv=-ys;

```



zv=-1;

syms xm ym zm xp yp zp xq yq zq;

eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;

eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;

eq3=zs==zm;

eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;

eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;

eq6=zp==zu;

eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;

eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;

eq9=zq==zv;

eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];

sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);

xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

alpha=pi\*3/4;

L6=2.5;

```

xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;

```

positions.yd=yd;  
positions.zd=zd;  
positions.xe=xe;  
positions.ye=ye;  
positions.ze=ze;  
positions.xf=xf;  
positions.yf=yf;  
positions.zf=zf;  
positions.xg=xg;  
positions.yg=yg;  
positions.zg=zg;  
positions.xh=xh;  
positions.yh=yh;  
positions.zh=zh;  
positions.xi=xi;  
positions.yi=yi;  
positions.zi=zi;  
positions.xj=xj;  
positions.yj=yj;  
positions.zj=zj;  
positions.xk=xk;  
positions.yk=yk;  
positions.zk=zg;  
positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;

```
positions.ym=ym;
positions.zm=zm;
positions.xp=xp;
positions.yp=yp;
positions.zp=zp;
positions.xq=xq;
positions.yq=yq;
positions.zq=zq;
positions.xs=xs;
positions.ys=ys;
positions.zs=zs;
positions.xu=xu;
positions.yu=yu;
positions.zu=zu;
positions.xv=xv;
positions.yv=yv;
positions.zv=zv;
positions.xs1=xs1;
positions.ys1=ys1;
positions.zs1=zs1;
positions.xu1=xu1;
positions.yu1=yu1;
positions.zu1=zu1;
positions.xv1=xv1;
positions.yv1=yv1;
positions.zv1=zv1;
positions.x_target=x_target;
```



```

z_target=zo;
xa=xo+L_tri/2;
ya=yo-L_tri/(2*3^0.5);
za=zo;
xb=xo-L_tri/2;
yb=yo-L_tri/(2*3^0.5);
zb=zo;
xc=xo;
yc=yo+L_tri/(3^0.5);
zc=zo;
xg=10*cos(pi/6);
yg=-10*sin(pi/6);
zg=0;
xh=-xg;
yh=yg;
zh=zg;
xi=0;
yi=10;
zi=0;

L1=20.8;
L2=10.8;
syms xd yd zd xe ye ze xf yf zf;
eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;
eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;
eq3=xd==xg;

```

$$\text{eq4}=(\text{xb}-\text{xe})^2+(\text{yb}-\text{ye})^2+(\text{zb}-\text{ze})^2==\text{L1}^2;$$

$$\text{eq5}=(\text{xh}-\text{xe})^2+(\text{yh}-\text{ye})^2+(\text{zh}-\text{ze})^2==\text{L2}^2;$$

$$\text{eq6}=\text{xe}-\text{xh}==(\text{yh}-\text{ye})^3^{0.5};$$

$$\text{eq7}=(\text{xc}-\text{xf})^2+(\text{yc}-\text{yf})^2+(\text{zc}-\text{zf})^2==\text{L1}^2;$$

$$\text{eq8}=(\text{xi}-\text{xf})^2+(\text{yi}-\text{yf})^2+(\text{zi}-\text{zf})^2==\text{L2}^2;$$

$$\text{eq9}=\text{xi}-\text{xf}==(\text{yi}-\text{yf})^3^{0.5};$$

$$\text{eqns}=[\text{eq1},\text{eq2},\text{eq3},\text{eq4},\text{eq5},\text{eq6},\text{eq7},\text{eq8},\text{eq9}];$$

$$\text{sol}=\text{solve}(\text{eqns},[\text{xd},\text{yd},\text{zd},\text{xe},\text{ye},\text{ze},\text{xf},\text{yf},\text{zf}]);$$

$$\text{xd}=\text{double}(\text{sol}.\text{xd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{yd}=\text{double}(\text{sol}.\text{yd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{zd}=\text{double}(\text{sol}.\text{zd}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{xe}=\text{double}(\text{sol}.\text{xe}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{ye}=\text{double}(\text{sol}.\text{ye}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{ze}=\text{double}(\text{sol}.\text{ze}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{xf}=\text{double}(\text{sol}.\text{xf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{yf}=\text{double}(\text{sol}.\text{yf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{zf}=\text{double}(\text{sol}.\text{zf}(\text{sol}.\text{yd}>0 \& \text{sol}.\text{xe}>-5 \& \text{sol}.\text{xf}<0));$$

$$\text{L3}=4.4;$$

$$\text{L4}=4.2;$$

$$\text{L5}=5.3;$$

$$\text{xj}=\text{xg};$$

$$\text{yj}=\text{yg}+\text{L3}*(\text{zd}-\text{zg})/\text{L2};$$

$$\text{zj}=\text{zg}-\text{L3}*(\text{yd}-\text{yg})/\text{L2};$$

```

syms xk yk zk;
eq1=(xk-xh)^2+(yk-yh)^2+(zk-zh)^2==L3^2;
eq2=(xk-xe)^2+(yk-ye)^2+(zk-ze)^2==L3^2+L2^2;
eq3=-sin(pi/6)*(xk-xh)-cos(pi/6)*(yk-yh)==0;
eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xk,yk,zk]);
xk=double(sol.xk(sol.xk>xh));
yk=double(sol.yk(sol.xk>xh));
zk=double(sol.zk(sol.xk>xh));

```

```

syms xl yl zl;
eq1=(xl-xi)^2+(yl-yi)^2+(zl-zi)^2==L3^2;
eq2=(xl-xf)^2+(yl-yf)^2+(zl-zf)^2==L2^2+L3^2;
eq3=-sin(pi/6)*(xl-xi)+cos(pi/6)*(yl-yi)==0;
eqns=[eq1,eq2,eq3];
sol=solve(eqns,[xl,yl,zl]);
xl=double(sol.xl(sol.xl<0));
yl=double(sol.yl(sol.xl<0));
zl=double(sol.zl(sol.xl<0));

```

```

xs=6*sin(pi/6);
ys=-6*cos(pi/6);
zs=-1;
xu=-6;
yu=0;
zu=-1;
xv=xS;

```



```

yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

alpha=pi*3/4;

```

```

L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

```

```

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

```

```

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;

```

```
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
positions.xl=xl;
positions.yl=yl;
positions.zl=zl;
```

positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;  
positions.xs=xs;  
positions.ys=ys;  
positions.zs=zs;  
positions.xu=xu;  
positions.yu=yu;  
positions.zu=zu;  
positions.xv=xv;  
positions.yv=yv;  
positions.zv=zv;  
positions.xs1=xs1;  
positions.ys1=ys1;  
positions.zs1=zs1;  
positions.xu1=xu1;  
positions.yu1=yu1;  
positions.zu1=zu1;  
positions.xv1=xv1;  
positions.yv1=yv1;  
positions.zv1=zv1;



```

zo=21;

L=L_tri-i;

z_target=zo+(3.5-i)^2


xa=xo+L/2;

ya=yo-L/(2*3^0.5);

za=zo;

xb=xo-L/2;

yb=yo-L/(2*3^0.5);

zb=zo;

xc=xo;

yc=yo+L/(3^0.5);

zc=zo;

xg=10*cos(pi/6);

yg=-10*sin(pi/6);

zg=0;

xh=-xg;

yh=yg;

zh=zg;

xi=0;

yi=10;

zi=0;


L1=20.8;

L2=10.8;

syms xd yd zd xe ye ze xf yf zf;

eq1=(xd-xa)^2+(yd-ya)^2+(za-zd)^2==L1^2;

```

$$eq2=(xd-xg)^2+(yd-yg)^2+(zd-zg)^2==L2^2;$$

$$eq3=xd==xg;$$

$$eq4=(xb-xe)^2+(yb-ye)^2+(zb-ze)^2==L1^2;$$

$$eq5=(xh-xe)^2+(yh-ye)^2+(zh-ze)^2==L2^2;$$

$$eq6=xe-xh==(yh-ye)^3^{0.5};$$

$$eq7=(xc-xf)^2+(yc-yf)^2+(zc-zf)^2==L1^2;$$

$$eq8=(xi-xf)^2+(yi-yf)^2+(zi-zf)^2==L2^2;$$

$$eq9=xi-xf==(yi-yf)^3^{0.5};$$

$$eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];$$

$$sol=solve(eqns,[xd,yd,zd,xe,ye,ze,xf,yf,zf]);$$

$$xd=double(sol.xd(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$yd=double(sol.yd(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$zd=double(sol.zd(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$xe=double(sol.xe(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$ye=double(sol.ye(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$ze=double(sol.ze(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$xf=double(sol.xf(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$yf=double(sol.yf(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$zf=double(sol.zf(sol.yd>0 \& sol.xe>-5 \& sol.xf<0));$$

$$L3=4.4;$$

$$L4=4.2;$$

$$L5=5.3;$$

$$xj=xg;$$

$$y_j = y_g + L_3 \cdot (z_d - z_g) / L_2;$$

$$z_j = z_g - L_3 \cdot (y_d - y_g) / L_2;$$

$$\text{syms } x_k \ y_k \ z_k;$$

$$\text{eq1} = (x_k - x_h)^2 + (y_k - y_h)^2 + (z_k - z_h)^2 == L_3^2;$$

$$\text{eq2} = (x_k - x_e)^2 + (y_k - y_e)^2 + (z_k - z_e)^2 == L_3^2 + L_2^2;$$

$$\text{eq3} = -\sin(\pi/6) \cdot (x_k - x_h) - \cos(\pi/6) \cdot (y_k - y_h) == 0;$$

$$\text{eqns} = [\text{eq1}, \text{eq2}, \text{eq3}];$$

$$\text{sol} = \text{solve}(\text{eqns}, [x_k, y_k, z_k]);$$

$$x_k = \text{double}(\text{sol}.x_k(\text{sol}.x_k > x_h));$$

$$y_k = \text{double}(\text{sol}.y_k(\text{sol}.x_k > x_h));$$

$$z_k = \text{double}(\text{sol}.z_k(\text{sol}.x_k > x_h));$$

$$\text{syms } x_l \ y_l \ z_l;$$

$$\text{eq1} = (x_l - x_i)^2 + (y_l - y_i)^2 + (z_l - z_i)^2 == L_3^2;$$

$$\text{eq2} = (x_l - x_f)^2 + (y_l - y_f)^2 + (z_l - z_f)^2 == L_2^2 + L_3^2;$$

$$\text{eq3} = -\sin(\pi/6) \cdot (x_l - x_i) + \cos(\pi/6) \cdot (y_l - y_i) == 0;$$

$$\text{eqns} = [\text{eq1}, \text{eq2}, \text{eq3}];$$

$$\text{sol} = \text{solve}(\text{eqns}, [x_l, y_l, z_l]);$$

$$x_l = \text{double}(\text{sol}.x_l(\text{sol}.x_l < 0));$$

$$y_l = \text{double}(\text{sol}.y_l(\text{sol}.x_l < 0));$$

$$z_l = \text{double}(\text{sol}.z_l(\text{sol}.x_l < 0));$$

$$x_s = 6 \cdot \sin(\pi/6);$$

$$y_s = -6 \cdot \cos(\pi/6);$$

$$z_s = -1;$$

$$x_u = -6;$$



```

yu=0;
zu=-1;
xv=xs;
yv=-ys;
zv=-1;

syms xm ym zm xp yp zp xq yq zq;
eq1=(xm-xj)^2+(ym-yj)^2+(zm-zj)^2==L4^2;
eq2=(xm-xs)^2+(ym-ys)^2+(zm-zs)^2==L5^2;
eq3=zs==zm;
eq4=(xp-xk)^2+(yp-yk)^2+(zp-zk)^2==L4^2;
eq5=(xp-xu)^2+(yp-yu)^2+(zp-zu)^2==L5^2;
eq6=zp==zu;
eq7=(xq-xl)^2+(yq-yl)^2+(zq-zl)^2==L4^2;
eq8=(xq-xv)^2+(yq-yv)^2+(zq-zv)^2==L5^2;
eq9=zq==zv;
eqns=[eq1,eq2,eq3,eq4,eq5,eq6,eq7,eq8,eq9];
sol=solve(eqns,[xm,ym,zm,xp,yp,zp,xq,yq,zq]);
xm=double(sol.xm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
ym=double(sol.ym(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zm=double(sol.zm(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xp=double(sol.xp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yp=double(sol.yp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zp=double(sol.zp(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
xq=double(sol.xq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
yq=double(sol.yq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));
zq=double(sol.zq(sol.ym>-3 & sol.xp>-6.3 & sol.yq<8.2));

```

```

alpha=pi*3/4;
L6=2.5;
xs1=xs+L6*cos(alpha+atan2(ym-ys,xm-xs));
ys1=ys+L6*sin(alpha+atan2(ym-ys,xm-xs));
zs1=zm;
xu1=xu+L6*cos(alpha+atan2(yp-yu,xp-xu));
yu1=yu+L6*sin(alpha+atan2(yp-yu,xp-xu));
zu1=zp;
xv1=xv+L6*cos(alpha+atan2(yq-yv,xq-xv));
yv1=yv+L6*sin(alpha+atan2(yq-yv,xq-xv));
zv1=zq;

rho_s=(xs1^2+ys1^2+zs1^2)^0.5;
rho_u=(xu1^2+yu1^2+zu1^2)^0.5;
rho_v=(xv1^2+yv1^2+zv1^2)^0.5;

positions.xo=xo;
positions.yo=yo;
positions.zo=zo;
positions.xa=xa;
positions.ya=ya;
positions.za=za;
positions.xb=xb;
positions.yb=yb;
positions.zb=zb;

```

```
positions.xc=xc;
positions.yc=yc;
positions.zc=zc;
positions.xd=xd;
positions.yd=yd;
positions.zd=zd;
positions.xe=xe;
positions.ye=ye;
positions.ze=ze;
positions.xf=xf;
positions.yf=yf;
positions.zf=zf;
positions.xg=xg;
positions.yg=yg;
positions.zg=zg;
positions.xh=xh;
positions.yh=yh;
positions.zh=zh;
positions.xi=xi;
positions.yi=yi;
positions.zi=zi;
positions.xj=xj;
positions.yj=yj;
positions.zj=zj;
positions.xk=xk;
positions.yk=yk;
positions.zk=zk;
```

positions.xl=xl;  
positions.yl=yl;  
positions.zl=zl;  
positions.xm=xm;  
positions.ym=ym;  
positions.zm=zm;  
positions.xp=xp;  
positions.yp=yp;  
positions.zp=zp;  
positions.xq=xq;  
positions.yq=yq;  
positions.zq=zq;  
positions.xs=xs;  
positions.ys=ys;  
positions.zs=zs;  
positions.xu=xu;  
positions.yu=yu;  
positions.zu=zu;  
positions.xv=xv;  
positions.yv=yv;  
positions.zv=zv;  
positions.xs1=xs1;  
positions.ys1=ys1;  
positions.zs1=zs1;  
positions.xu1=xu1;  
positions.yu1=yu1;  
positions.zu1=zu1;

[illegible]

```
fclose(fileID);
```

## 五、凸轮设计

% 导入数据并计算

```
c = 15;

phi = linspace(0, 2*pi, 630);

filepath = 'C:\Users\Dell\Desktop\机设大作业\spiderhand_rho_s1.txt';

rho = readmatrix(filepath);

x = zeros(length(phi), 1);
y = zeros(length(phi), 1);
z = zeros(length(phi), 1);

for i = 1:length(phi)
    x(i) = rho(i) * cos(phi(i));
    y(i) = rho(i) * sin(phi(i));
end

%输出 solidworks 中生成凸轮需要的数据

output_data = [x, y, z] * c;

writematrix(output_data, 'closed_cam_profile.txt');

disp('闭合凸轮曲线数据已保存为 closed_cam_profile.txt');
```

%绘制凸轮轮廓

```
figure;

hold on;

plot(x, y, 'r', 'LineWidth', 2);

plot(x(1:11), y(1:11), 'blue', 'LineWidth', 2);

plot(x(71:81), y(71:81), 'green', 'LineWidth', 2);

plot(x(200:221), y(200:221), 'blue', 'LineWidth', 2);

plot(x(281:291), y(281:291), 'green', 'LineWidth', 2);

plot(x(410:431), y(410:431), 'blue', 'LineWidth', 2);
```

```

plot(x(551:561), y(551:561), 'green', 'LineWidth', 2);
plot(x(620:630), y(620:630), 'blue', 'LineWidth', 2);
hold off;
axis equal;
title('凸轮轮廓');
xlabel('X');
ylabel('Y');
grid on;

```

%绘制 rho 与 phi 的关系图像

```

figure;
plot(phi, rho, 'b', 'LineWidth', 3);
title('$\rho$($\phi$)', 'Interpreter', 'latex');
xlabel('$\phi$', 'Interpreter', 'latex');
ylabel('$\rho$', 'Interpreter', 'latex');
xticks(0:0.25:2*pi);
grid on;

```

## 六、仿真代码

### (一)、蜘蛛手

#### 1. 主代码块

功能：对蜘蛛手的运动仿真

```

import numpy as np
import matplotlib.pyplot as plt
import mode

with open('spiderhand.txt', 'r') as file:
    data = []
    for line in file:

```

```

        line_data = line.strip().split() # 去掉换行符并按空格分割
        data.append([float(i) for i in line_data]) # 转换为浮动类型

# 创建一个三维图形
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')

# 设置图形属性
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')

angle_sum = 0
# 开始绘制循环
while True:
    # 清空当前坐标轴

    for para in data:
        ax.clear()
        coords = np.array(para).reshape(-1, 3)

        point_o = coords[0]
        # 定义三条路径
        line_1 = coords[1:19:3]

        line_2 = coords[2:19:3]

        line_3 = coords[3:19:3]

        line_sum = [line_1, line_2, line_3]

        for line in line_sum:
            for i in range(len(line)):
                ax.scatter(line[i][0], line[i][1], line[i][2], color='r', s=3) # 绘制点
            for i in range(2):
                ax.plot([line[i][0], line[i + 1][0]], [line[i][1], line[i + 1][1]], [line[i][2], line[i + 1][2]], color='#00FFFF', linewidth=1) # 绘制线

            for i in range(2, len(line) - 1):
                ax.plot([line[i][0], line[i + 1][0]], [line[i][1], line[i + 1][1]], [line[i][2], line[i + 1][2]], color='black', linewidth=1) # 绘制线

```



```

# 绘制两点连接线
for i in range(-1, 2):
    ax.plot([line_sum[i][-1][0], line_sum[i + 1][-1][0]],
            [line_sum[i][-1][1], line_sum[i + 1][-1][1]],
            [line_sum[i][-1][2], line_sum[i + 1][-1][2]], color
            ='b', linewidth=1)

    for i in range(-1, 2):
        ax.plot([line_sum[i][0][0], line_sum[i + 1][0][0]],
                [line_sum[i][0][1], line_sum[i + 1][0][1]],
                [line_sum[i][0][2], line_sum[i + 1][0][2]], color='
orange', linewidth=1)

mode.plot_triangle_and_circle_3d(ax,[line_sum[0][2][0], line_su
m[0][2][1],line_sum[0][2][2]],
    [line_sum[1][2][0], line_sum[1][2][1],line_sum[1][2]
[2]],
    [line_sum[2][2][0], line_sum[2][2][1],line_sum[2][2]
[2]])

for i in range(-1,2):
    angle_new = mode.calculate_angle(line_sum[i][2] - line_sum
[i][1], line_sum[i][3] - line_sum[i][2])
    if angle_sum:
        # 精度
        if abs(abs(angle_sum) - abs(angle_new)) > 0.0001:
            angle_sum = angle_new
            print(angle_sum)
    else:
        angle_sum = angle_new
        print(angle_new)

# 绘制原点

ax.scatter(point_o[0], point_o[1], point_o[2], color='r', s=5)

ax.set_xlim([-20, 20]) # 设置 x 轴的范围
ax.set_ylim([-20, 20]) # 设置 y 轴的范围
ax.set_zlim([-5, 35]) # 设置 z 轴的范围
# 更新图形
plt.draw()
ax.invert_zaxis() # 反转Z轴方向
plt.pause(0.01) # 暂停0.1秒, 允许更新

```

## 2. 模块 mode

功能：画出给定三点的外接圆

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
import math
def calculate_angle(v1, v2):
    """
    计算两个三维向量 v1 和 v2 的夹角（以度为单位）
    :param v1: 第一个三维向量 (x1, y1, z1)
    :param v2: 第二个三维向量 (x2, y2, z2)
    :return: 夹角 (单位: 度)
    """
    # 计算点积
    dot_product = np.dot(v1, v2)

    # 计算模长
    magnitude_v1 = np.linalg.norm(v1)
    magnitude_v2 = np.linalg.norm(v2)

    # 计算夹角的余弦值
    cos_theta = dot_product / (magnitude_v1 * magnitude_v2)

    # 防止数值误差导致的溢出, 限制范围
    cos_theta = np.clip(cos_theta, -1.0, 1.0)

    # 计算夹角 (弧度)
    theta_rad = np.arccos(cos_theta)

    # 转换为度
    theta_deg = np.degrees(theta_rad)

    return theta_deg

def calculate_circle_3d(p1, p2, p3):
    """
    计算三维空间中通过三点的圆心、半径和法向量
    :param p1, p2, p3: 三个点的坐标 (x, y, z)
    :return: 圆心 center, 半径 radius, 法向量 normal
    """
    # 转换为 numpy 数组
    p1, p2, p3 = np.array(p1), np.array(p2), np.array(p3)

    # 向量定义
```

```

v1 = p2 - p1
v2 = p3 - p1

# 法向量 (平面法向量) 通过叉积计算
normal = np.cross(v1, v2)
normal = normal / np.linalg.norm(normal) # 单位化

# 三角形边的中点
mid1 = (p1 + p2) / 2
mid2 = (p1 + p3) / 2

# 两边中垂线的方向
dir1 = np.cross(normal, v1)
dir2 = np.cross(normal, v2)

# 解方程找到中垂线的交点, 即圆心
A = np.array([dir1, -dir2, normal]).T # 系数矩阵
b = mid2 - mid1
t = np.linalg.solve(A, b)
center = mid1 + t[0] * dir1 # 圆心坐标

# 计算半径
radius = np.linalg.norm(center - p1)
return center, radius, normal

def plot_triangle_and_circle_3d(ax, p1, p2, p3):
    """
    绘制给定三点构成的三角形, 并画出外接圆
    :param p1, p2, p3: 三个点的坐标 (x, y, z)
    """
    # 计算圆心和半径
    center, radius, normal = calculate_circle_3d(p1, p2, p3)

    # 绘制圆
    # 生成圆的参数方程
    # 选择一个与 normal 垂直的向量作为基向量 u
    u = np.array([1, 0, 0]) if abs(normal[0]) < 1 else np.array([0, 1,
0])

    # 计算两个基向量 v1 和 v2, 确保它们垂直于法向量并且平行于圆的平面
    v1 = np.cross(normal, u)
    v1 = v1 / np.linalg.norm(v1) # 单位化
    v2 = np.cross(normal, v1) # 另一垂直向量

    # 生成圆上的点

```

```

theta = np.linspace(0, 2 * np.pi, 100)
circle_points = np.array([
    center + radius * (np.cos(t) * v1 + np.sin(t) * v2)
    for t in theta
])

# 绘制圆
ax.plot(circle_points[:, 0], circle_points[:, 1], circle_points[:,
2], color='grey', linestyle='--', linewidth=2)

# 绘制圆心
ax.scatter(center[0], center[1], center[2], color='red')

```

## (二)、抓娃娃机

### 1. 主代码块

功能：对娃娃机的运动仿真

```

import numpy as np
import matplotlib.pyplot as plt
import mode
import mode_ball
with open('claw_machine.txt', 'r') as file:
    data = []
    for line in file:
        line_data = line.strip().split() # 去掉换行符并按空格分割
        data.append([float(i) for i in line_data]) # 转换为浮动类型

# 创建一个三维图形
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')

# 设置图形属性
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')

ax.set_xlim([-20, 20]) # 设置 x 轴的范围
ax.set_ylim([-20, 20]) # 设置 y 轴的范围
ax.set_zlim([-15, 30]) # 设置 z 轴的范围
# 开始绘制循环
while True:
    # 清空当前坐标轴

```

```

for para in data:
    ax.clear()
    coords = np.array(para).reshape(-1, 3)

    ball = coords[23:]
    point_o = coords[0]
    # 定义三条路径
    line_1 = coords[1:19:3]

    line_2 = coords[2:19:3]

    line_3 = coords[3:19:3]
    target = coords[22]

    line_sum = [line_1, line_2, line_3]

    for line in line_sum:
        x = line[:,0]
        y = line[:,1]
        z = line[:,2]
        ax.scatter(x,y,z, color='r', s=3) # 绘制点
        ax.plot(x,y,z, color='black', linewidth = 1) # 绘制线

    # 绘制两点连接线
    for i in range(-1, 2):
        ax.plot([line_sum[i][-1][0], line_sum[i + 1][-1][0]],
                [line_sum[i][-1][1], line_sum[i + 1][-1][1]],
                [line_sum[i][-1][2], line_sum[i + 1][-1][2]], color
                = '#FF5733', linewidth=1)

        for i in range(-1, 2):
            ax.plot([line_sum[i][0][0], line_sum[i + 1][0][0]],
                    [line_sum[i][0][1], line_sum[i + 1][0][1]],
                    [line_sum[i][0][2], line_sum[i + 1][0][2]], color='
orange', linewidth=1)

    mode.plot_triangle_and_circle_3d(ax,[line_1[2][0], line_1[2][1],
line_1[2][2]],
    [line_2[2][0], line_2[2][1],line_2[2][2]],
    [line_3[2][0], line_3[2][1],line_3[2][2]])

    # 追踪球
    mode_ball.plot_sphere(ax,[target[0], target[1], target[2]],4 /
(3 ** 0.5))

```

```

mode_ball.plot_xy_plane_1(ax,0,0,line_1[2][2])

for i in ball:
    mode_ball.plot_sphere(ax, i, 4 / (3 ** 0.5))
mode_ball.plot_xy_plane(ax,ball[0][0],ball[0][1],ball[0][2])

# 绘制原点
ax.scatter(point_o[0], point_o[1], point_o[2], color='r', s=5)
ax.set_xlim([-30, 30]) # 设置 x 轴的范围
ax.set_ylim([-30, 30]) # 设置 y 轴的范围
ax.set_zlim([-15, 40]) # 设置 z 轴的范围
# 更新图形
plt.draw()
ax.invert_zaxis() # 反转Z轴方向
plt.pause(0.1) # 暂停0.1秒, 允许更新

```

## 2. 模块 mode

功能：画出给定三点的外接圆

```

import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
import math
def calculate_angle(v1, v2):
    """
    计算两个三维向量 v1 和 v2 的夹角（以度为单位）
    :param v1: 第一个三维向量 (x1, y1, z1)
    :param v2: 第二个三维向量 (x2, y2, z2)
    :return: 夹角 (单位: 度)
    """
    # 计算点积
    dot_product = np.dot(v1, v2)

    # 计算模长
    magnitude_v1 = np.linalg.norm(v1)
    magnitude_v2 = np.linalg.norm(v2)

    # 计算夹角的余弦值
    cos_theta = dot_product / (magnitude_v1 * magnitude_v2)

    # 防止数值误差导致的溢出, 限制范围
    cos_theta = np.clip(cos_theta, -1.0, 1.0)

    # 计算夹角 (弧度)

```

```

theta_rad = np.arccos(cos_theta)

# 转换为度
theta_deg = np.degrees(theta_rad)

return theta_deg

def calculate_circle_3d(p1, p2, p3):
    """
    计算三维空间中通过三点的圆心、半径和法向量
    :param p1, p2, p3: 三个点的坐标 (x, y, z)
    :return: 圆心 center, 半径 radius, 法向量 normal
    """
    # 转换为 numpy 数组
    p1, p2, p3 = np.array(p1), np.array(p2), np.array(p3)

    # 向量定义
    v1 = p2 - p1
    v2 = p3 - p1

    # 法向量 (平面法向量) 通过叉积计算
    normal = np.cross(v1, v2)
    normal = normal / np.linalg.norm(normal) # 单位化

    # 三角形边的中点
    mid1 = (p1 + p2) / 2
    mid2 = (p1 + p3) / 2

    # 两边中垂线的方向
    dir1 = np.cross(normal, v1)
    dir2 = np.cross(normal, v2)

    # 解方程找到中垂线的交点, 即圆心
    A = np.array([dir1, -dir2, normal]).T # 系数矩阵
    b = mid2 - mid1
    t = np.linalg.solve(A, b)
    center = mid1 + t[0] * dir1 # 圆心坐标

    # 计算半径
    radius = np.linalg.norm(center - p1)
    return center, radius, normal

def plot_triangle_and_circle_3d(ax, p1, p2, p3):
    """
    绘制给定三点构成的三角形, 并画出外接圆

```

```

:param p1, p2, p3: 三个点的坐标 (x, y, z)
"""
# 计算圆心和半径
center, radius, normal = calculate_circle_3d(p1, p2, p3)

# 绘制圆
# 生成圆的参数方程
# 选择一个与normal 垂直的向量作为基向量u
u = np.array([1, 0, 0]) if abs(normal[0]) < 1 else np.array([0, 1,
0])

# 计算两个基向量 v1 和 v2, 确保它们垂直于法向量并且平行于圆的平面
v1 = np.cross(normal, u)
v1 = v1 / np.linalg.norm(v1) # 单位化
v2 = np.cross(normal, v1) # 另一垂直向量

# 生成圆上的点
theta = np.linspace(0, 2 * np.pi, 100)
circle_points = np.array([
    center + radius * (np.cos(t) * v1 + np.sin(t) * v2)
    for t in theta
])

# 绘制圆
ax.plot(circle_points[:, 0], circle_points[:, 1], circle_points[:,
2], color='grey', linestyle='--', linewidth=2)

# 绘制圆心
ax.scatter(center[0], center[1], center[2], color='red')

```

### 3. 模块 mode\_ball

功能：绘制球的轮廓、所有球的初始平面以及抓娃娃机的平面。



```

import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

def plot_sphere(ax, center, radius):
    """
    在 3D 坐标系中绘制一个以给定中心和半径的球
    :param ax: 3D 坐标轴
    :param center: 球心 (x0, y0, z0)
    :param radius: 球的半径
    """
    u = np.linspace(0, 2 * np.pi, 100) # 方位角
    v = np.linspace(0, np.pi, 100) # 极角

    # 使用球坐标公式生成球面上的点
    x = center[0] + radius * np.outer(np.cos(u), np.sin(v))
    y = center[1] + radius * np.outer(np.sin(u), np.sin(v))
    z = center[2] + radius * np.outer(np.ones(np.size(u)), np.cos(v))

    # 绘制球面
    ax.plot_surface(x, y, z, color='b', alpha=0.3) # 绘制透明的球面
    ax.scatter(center[0], center[1], center[2], color='r', s=3) # 绘制
点

def plot_xy_plane(ax, x0, y0, z0): # 解包输入点的坐标

    # 创建网格数据
    x = np.linspace(-30, +30, 100)
    y = np.linspace(-30, +30, 100)
    X, Y = np.meshgrid(x, y)

    # Z 值为 z0, 表示平面高度
    Z = np.full(X.shape, z0)

    # 绘制XY 平面
    ax.plot_surface(X, Y, Z, alpha=0.3, color='yellow')

def plot_xy_plane_1(ax, x0, y0, z0): # 解包输入点的坐标

```

```
# 创建网格数据
x = np.linspace(-30, + 30, 100)
y = np.linspace(-30, + 30, 100)
X, Y = np.meshgrid(x, y)

# Z 值为 z0, 表示平面高度
Z = np.full(X.shape, z0)

# 绘制XY 平面
ax.plot_surface(X, Y, Z, alpha=0.3, color='green')
```