

PRE PSPM SET 1 (ANSWER SCHEME)

NO.	ANSWER SCHEME	MARK (S)
1	$[J] = [F][t]$ $= [m][a][t]$ $= (M)(LT^{-2})(T)$ $= MLT^{-1}$ \therefore Unit of impulse = $kg\ m\ s^{-1}$	<p>K1</p> <p>J1</p>
	TOTAL	2

NO.	ANSWER SCHEME	MARK (S)
2(a)(i)	$u = 0\ m\ s^{-1}$ $v^2 = u^2 + 2as$ $v^2 = 0^2 + 2(2.0)850$ $v = 58.31\ m\ s^{-1}$	<p>K1</p> <p>GJU1</p>
(a)(ii)	$v = u + at$ $58.31 = 0 + 2.0t$ $t = 29.16\ s$	<p>G1 JU1</p>
(b)(i)	$u_x = u \cos 45^\circ, u_y = u \sin 45^\circ$ $S_y = 3.05 - 2 = 1.05\ m$ $S_x = u_x t$ $S_x = (u \cos 45^\circ) t$ $t = \frac{10}{u \cos 45^\circ} \dots\dots\dots(1)$	<p>K1</p> <p>G1</p>

	$S_y = u_y t - \frac{1}{2} g t^2$ $1.05 = (u \sin 45^\circ) t - \frac{1}{2} (9.81) t^2 \dots\dots\dots (2)$ $1.05 = (u \sin 45^\circ) \left(\frac{10}{u \cos 45^\circ} \right) - \frac{1}{2} (9.81) \left(\frac{10}{u \cos 45^\circ} \right)^2$ $u = 10.47 \text{ m s}^{-1}$	<p>G1</p> <p>JU1</p>
(b)(ii)	$S_x = (u \cos 45^\circ) t$ $10 = (10.47 \cos 45^\circ) t$ $t = 1.35 \text{ s}$	<p>G1</p> <p>JU1</p>
	TOTAL	10

NO.	ANSWER SCHEME	MARKS
3(a)	$m = 40 \text{ kg}, u = 6.2 \text{ m s}^{-1}, v = 5.7 \text{ m s}^{-1}$ $\Delta P = m(v - u)$ $\Delta P = \text{area under } F - t \text{ graph}$ $40(7 - 6.2) = \frac{1}{2} \times F_{\max} \times (6 + 10)$ $F_{\max} = 4 \text{ N}$	<p>K1</p> <p>GJU1</p>
3(b)	$m_A = m_B = m, u_A = 55 \text{ m s}^{-1}, u_{Ax} = 55 \sin 20^\circ, u_{Ay} = 55 \cos 20^\circ$ $u_B = 55 \text{ m s}^{-1}, u_{Bx} = 55 \text{ m s}^{-1}, u_{By} = 0$ $\sum P_{ix} = \sum P_{fx}$ $m_A u_{Ax} + m_B u_{Bx} = (m_A + m_B) v_x$ $m(55 \sin 20^\circ) + m(55) = (m + m) v_x$ $v_x = 36.91 \text{ m s}^{-1}$ $\sum P_{iy} = \sum P_{fy}$ $m_A u_{Ay} + m_B u_{By} = (m_A + m_B) v_y$ $m(55 \cos 20^\circ) + m(0) = (m + m) v_y$ $v_y = 25.84 \text{ m s}^{-1}$ $v = \sqrt{v_x^2 + v_y^2}$ $v = \sqrt{36.91^2 + 25.84^2} = 45.06 \text{ m s}^{-1}$	<p>K1</p> <p>G1</p> <p>G1</p> <p>GJU1</p>

	$\theta = \tan^{-1} \left(\frac{v_y}{v_x} \right)$ $\theta = \tan^{-1} \left(\frac{25.84}{36.91} \right) = 35^\circ$	GJU1
3(c)	<p> $m_1 = 8 \text{ kg}, m_2 = 4 \text{ kg}, \theta = 35^\circ, \mu_k = 0.2$ </p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> <p><u>Object 1</u></p> <p> $W_{1y} = W_1 \cos 35^\circ$ $W_{1x} = W_1 \sin 35^\circ$ </p> </div> <div style="text-align: center;"> <p><u>Object 2</u></p> <p> T W_2 </p> </div> </div> <p> $\sum F_y = 0$ $N_1 = W_1 \cos 35^\circ = (4)(9.81) \cos 35^\circ = 32.14 \text{ N}$ </p> <p> $\sum F_x = m_1 a$ $T - f_1 - W_1 \sin 35^\circ = m_1 a$ $T - (0.2)(32.14) - (4)(9.81) \sin 35^\circ = 4a$ $T - 4a = 28.94$ </p> <p> $\sum F_y = m_2 a$ $W_2 - T = m_2 a$ $(8)(9.81) - T = 8a$ $T + 8a = 78.48$ </p> <p> $T = 45.44 \text{ N}$ $a = 4.13 \text{ m s}^{-2}$ </p>	<p>G1</p> <p>K1</p> <p>G1</p> <p>G1</p> <p>JU1 JU1</p>
	TOTAL	13

NO.	ANSWER SCHEME	MARK (S)
4 (a)	<p><i>work done = area under Force – displacement graph</i></p> $W = \frac{1}{2}(0.02)(200) + \frac{1}{2}(0.06 - 0.02)(200 + 300) + \frac{1}{2}(0.08 - 0.06)(300 + 500) + \frac{1}{2}(0.14 - 0.08)(500) = 35 \text{ J}$	<p>K1</p> <p>GJU1</p>
4(b)(i)	$mgh_A = \frac{1}{2}mv_B^2 \quad \text{OR} \quad U_A = K_B$ $(0.14)(9.81)(0.7) = \frac{1}{2}(0.14)v_B^2$ $v_B = 3.71 \text{ m s}^{-1}$	<p>K1</p> <p>GJU1</p>
4(b)(ii)	<p><i>potential energy at point C = mgh_c</i></p> $h_c = L - L \cos 35^\circ$ $h_c = 0.7 - 0.7 \cos 35^\circ = 0.13 \text{ m}$ $U_c = mgh_c = (0.14)(9.81)(0.13) = 0.179 \text{ J}$	<p>G1</p> <p>GJU1</p>
4(c)	$P_{AV} = \frac{\text{energy}}{\text{time}} = \frac{mgh}{t}$ $P_{AV} = \frac{(65)(9.81)(342)}{(30)(60)}$ $P_{AV} = 121.15 \text{ W}$	<p>G1</p> <p>JU1</p>
	TOTAL	8

NO.	ANSWER SCHEME	MARK (S)
5(a) (i)	$a_c = \frac{v^2}{R} = \frac{5^2}{0.5} = 50 \text{ m s}^{-2}$	GJU1
5(a)(ii)	$\sum F = F_c$ $T = ma_c$ $T = (0.2)(50) = 10 \text{ N}$	GJU1
5(b)	<div style="text-align: center;"> </div> $T \sin \theta = \frac{mv^2}{R} \dots\dots\dots (1)$ $T \cos \theta = mg \dots\dots\dots (2)$ <div style="text-align: center;"> $(2) \div (1)$ $\tan \theta = \frac{v^2}{Rg} = \frac{(3^2)}{(40 \times 10^{-2})(9.81)}$ $\theta = 66.4^\circ$ </div>	<div style="text-align: center;">K1</div> <div style="text-align: center;">G1</div> <div style="text-align: center;">JU1</div>
	TOTAL	5

NO.	ANSWER SCHEME	MARK (S)
6(a)(i)	$y = 4\sin 1.2t = 4\sin 1.2(3) = -1.77 \text{ cm}$	GJU1
6(a)(ii)	$v = \omega A \cos \omega t$ $= (1.2)(4) \cos 1.2(3)$ $= -4.30 \text{ cm s}^{-1}$ OR $y = A \sin \omega t$ $y = 4 \sin 1.2t$ $\omega = 1.2 \text{ rad s}^{-1}$ and $A = 4 \text{ cm}$ $v = \pm \omega \sqrt{A^2 - y^2}$ $v = \pm (1.2) \sqrt{(4)^2 - (-1.77)^2}$ $v = \pm 4.30 \text{ cm s}^{-1}$	G1 JU1
6(a)(iii)	$a = -\omega^2 A \sin \omega t$ $= -(1.2)^2 4 \sin 1.2(3)$ $a = 2.55 \text{ cm s}^{-2}$ OR $a = -\omega^2 y$ $= -(1.2)^2 (-1.77)$ $= 2.55 \text{ cm s}^{-2}$	G1 JU1
6(b)(i)	$T = 2\pi \sqrt{\frac{m}{k}} = 2\pi \sqrt{\frac{0.25}{50}}$ $= 0.44 \text{ s}$ $f = \frac{1}{T} = \frac{1}{0.44}$ $= 2.27 \text{ Hz}$	G1 GJU1
6(b)(ii)	$E = \frac{1}{2} k A^2$ $= \frac{1}{2} (50) (0.06)^2$ $= 0.09 \text{ J}$	G1 JU1

	$f_a = \left(\frac{v}{v - v_s}\right) f_s$ $= \left(\frac{340}{340 - 46}\right) 550$ $= 636.05 \text{ Hz}$	G1 JU1
6(e)(ii)	$f_a = \left(\frac{v \pm v_o}{v \pm v_s}\right) f \quad \begin{matrix} \text{-O S+} \\ \longrightarrow \end{matrix}$ $f_a = \left(\frac{v}{v + v_s}\right) f_s$ $= \left(\frac{340}{340 + 46}\right) 550$ $= 484.46 \text{ Hz}$	G1 JU1
	TOTAL	23

NO.	ANSWER SCHEME	MARK (S)
7.(a)(i)	$\left(\frac{Q}{t}\right)_{brick} = \left(\frac{Q}{t}\right)_{concrete}$ $-KA\left(\frac{T - 40}{0.12}\right) = -KA\left(\frac{20 - T}{0.24}\right)$ $-(0.6)\left(\frac{T - 40}{0.12}\right) = -(0.8)\left(\frac{20 - T}{0.24}\right)$ $5(T - 40) = 3.33(20 - T)$ $T = 32^{\circ}\text{C}$	<p>K1</p> <p>G1</p> <p>JU1</p>
7.(a)(ii)	$\left(\frac{Q}{t}\right)_{concrete} = -KA\left(\frac{\Delta T}{L}\right)$ $\left(\frac{Q}{1 \times 60 \times 60}\right) = -0.6(55)\left(\frac{32 - 40}{0.12}\right)$ $Q = 7.92 \times 10^6 \text{J}$	<p>G1</p> <p>JU1</p>
7(b)	$V_t = V_o(1 + \gamma\Delta T)$ $V_t = 3(1 + 3\alpha\Delta T)$ $V_t = 3(1 + 3(1.1 \times 10^{-4}(18 - 32)))$ $V_t = 2.98614 \text{ m}^3$ $V_g = V_o(1 + \gamma\Delta T)$ $V_g = 3(1 + (4.8 \times 10^{-4}(18 - 32)))$ $V_g = 2.97984 \text{ m}^3$ $\Delta V = 2.98614 - 2.97984)$ $\Delta V = 0.0063 \text{ m}^3$ <p>OR</p>	<p>G1</p> <p>G1</p> <p>JU1</p>

	$\Delta V_t = 3\alpha_t V_{ot} \Delta T$ $= 3(1.1 \times 10^{-4})(3.0)(18 - 32)$ $= -0.01386 \text{ m}^3$ $\Delta V_g = \gamma_g V_{og} \Delta T$ $= (4.8 \times 10^{-4})(3.0)(18 - 32)$ $= -0.02016 \text{ m}^3$ $\Delta V_{add} = \Delta V_t - \Delta V_g$ $= -0.01386 - (-0.02016)$ $= 0.0063 \text{ m}^3$	
	TOTAL	8

NO.	ANSWER SCHEME	MARK (S)
8.(a)	$v_{rms} = 600 \text{ m s}^{-1}$ $v_{rms} = \sqrt{\frac{3RT}{M}}$ $600 = \sqrt{\frac{3(8.31)T}{28 \times 10^{-3}}}$ $T = 404.33 \text{ K}$ $f = 5$ $U = \frac{1}{2}fnRT$ $= \frac{1}{2}(5)(0.2)(8.31)(404.33)$ $= 1680 \text{ J}$	<p>G1</p> <p>K1</p> <p>G1</p> <p>JU1</p>

(b)	$P = \frac{1}{3} \rho v_{rms}^2$ $= \frac{1}{3} (0.1)(1.85 \times 10^3)^2$ $= 1.14 \times 10^5 \text{ N m}^{-2} \text{ or Pa}$	<p>G1</p> <p>JU1</p>
8(c)	$\Delta U = 0 \text{ J}$ $W = nRT \ln \left(\frac{V_f}{V_i} \right)$ $= (2)(8.31)(295) \ln \left(\frac{0.050}{0.025} \right)$ $= 3.398 \times 10^3 \text{ J}$ $\Delta U = Q - W$ $Q = 0 + (3.398 \times 10^3)$ $= 3.398 \times 10^3 \text{ J}$ <p>System absorb heat</p>	<p>K1</p> <p>G1</p> <p>G1</p> <p>JU1</p> <p>J1</p>
	TOTAL	11