

Caches

Reminders:

Quiz 2 Review: Tuesday, April 14, 7:30pm EST

Quiz 2: Thursday, April 16 7:30pm EST

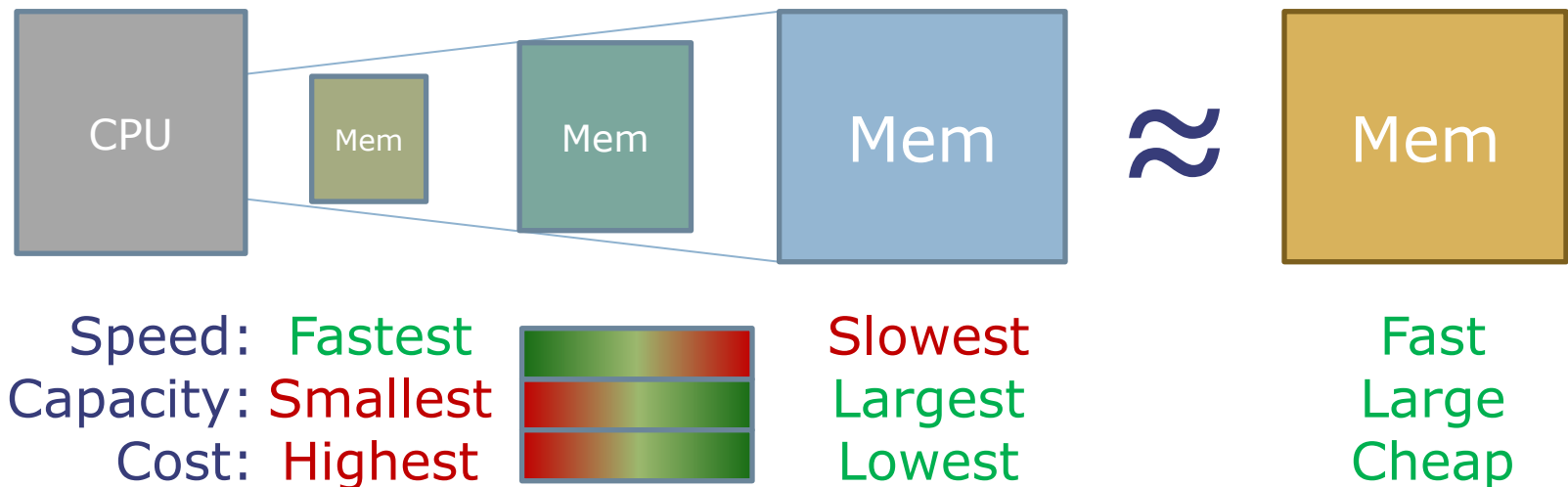
The Memory Hierarchy

Want large, fast, and cheap memory, but...

Large memories are slow (e.g., Hard Disk)

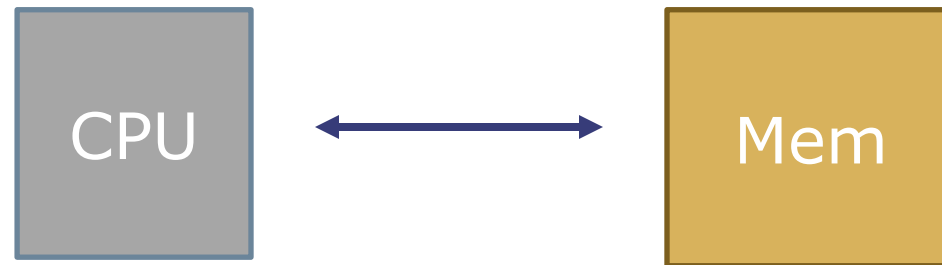
Fast memories are small and expensive (e.g., SRAM)

Solution: Use a **hierarchy** of memories with different tradeoffs to **fake** a large, fast, cheap memory



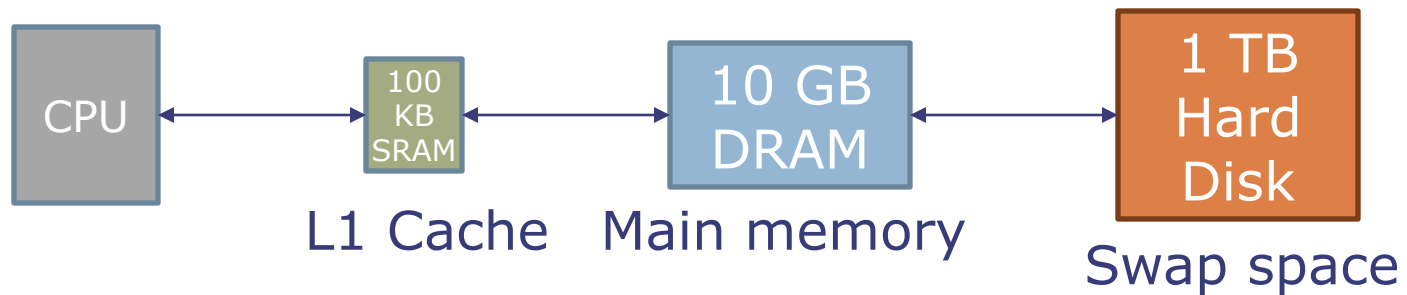
Memory Hierarchy Interface

- Programming model: Single memory, single address space



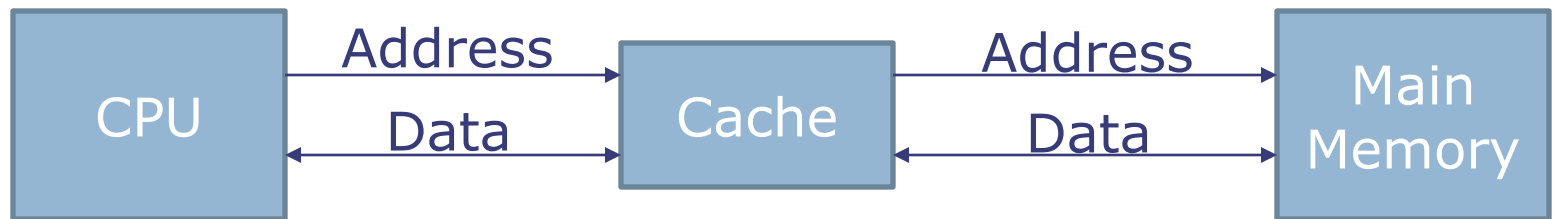
Memory Hierarchy Interface

- Programming model: Single memory, single address space
- Machine transparently stores data in fast or slow memory, depending on usage patterns



Caches

- Cache: A small, interim storage component that transparently retains (caches) data from recently accessed locations



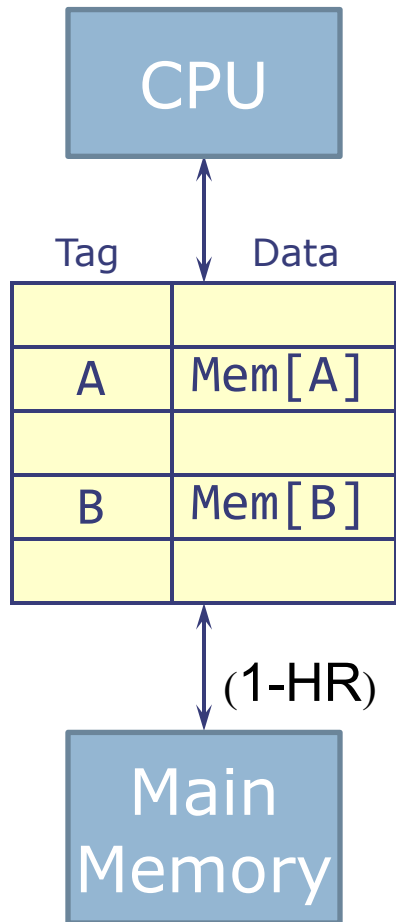
- Processor sends accesses to cache. Two options:
 - Cache hit**: Data for this address in cache, returned quickly
 - Cache miss**: Data not in cache
 - Fetch data from memory, send it back to processor
 - Retain this data in the cache (replacing some other data)
- Processor must deal with variable memory access time

Why Caches Work

- Two predictable properties of memory accesses:
 - **Temporal locality**: If a location has been accessed recently, it is likely to be accessed (reused) soon
 - **Spatial locality**: If a location has been accessed recently, it is likely that nearby locations will be accessed soon
- Result:
 - High hit rate (low miss ratio)
 - Reduced Average Memory Access Time (AMAT):

$$AMAT = HitTime + MissRatio \times MissPenalty$$

Basic Cache Algorithm (Reads)



On reference to Mem[X],
look for X among cache tags

HIT: $X = \text{Tag}(i)$
for some
cache line i

Return Data(i)

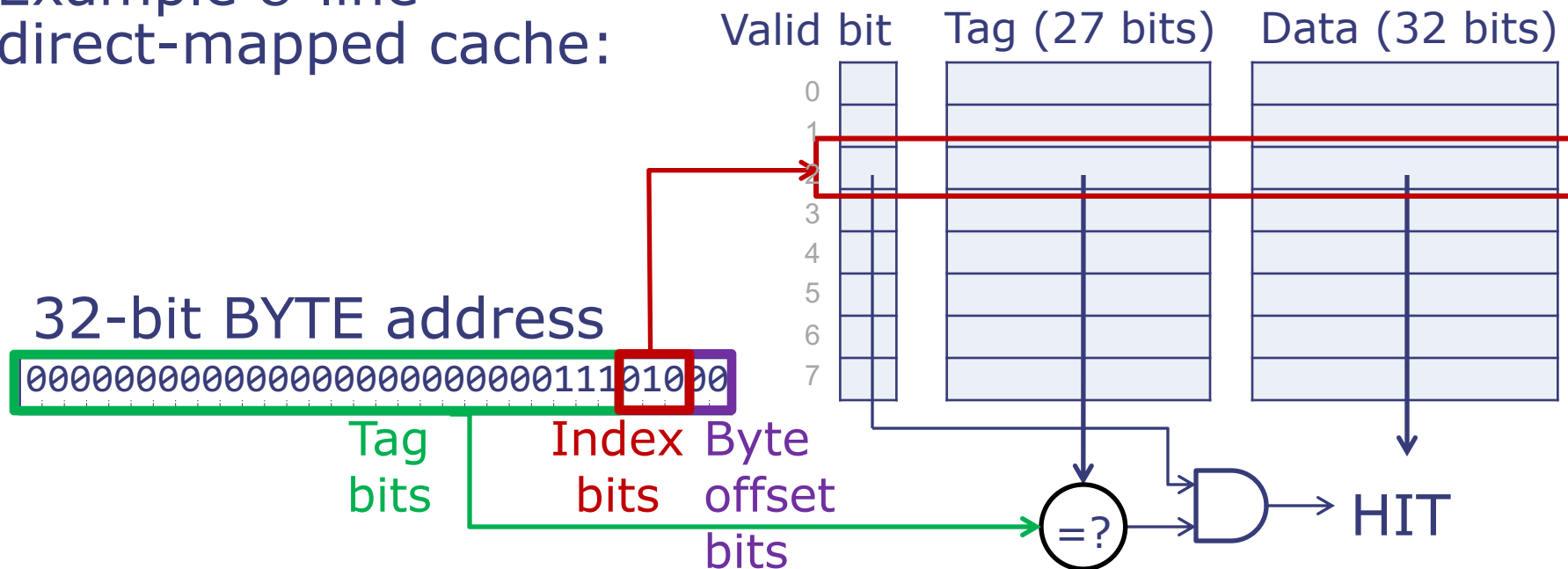
MISS: X not
found in Tag
of any cache line

Read Mem[X]
Return Mem[X]
Select a line k
to hold Mem[X]
Write Tag(k) = X,
Data(k) = Mem[X]

Q: How do we "search" the cache?

Direct-Mapped Caches

- Each word in memory maps into a single cache line
- Access (for cache with 2^W lines):
 - Index into cache with W address bits (the **index bits**)
 - Read out valid bit, tag, and data
 - If valid bit == 1 and tag matches upper address bits, HIT
- Example 8-line direct-mapped cache:



Example: Direct-Mapped Caches

64-line direct-mapped cache → 64 indices → 6 index bits

Read Mem[0x400C]

0100 0000 0000 1100
TAG: 0x40
INDEX: 0x3
BYTE OFFSET: 0x0

HIT, DATA 0x42424242

Would 0x4008 hit?

INDEX: 0x2 → tag mismatch
→ MISS

	Valid bit	Tag (24 bits)	Data (32 bits)
0	1	0x000058	0xDEADBEEF
1	1	0x000058	0x00000000
2	1	0x000058	0x00000007
3	1	0x000040	0x42424242
4	0	0x000007	0x6FBA2381
	⋮	⋮	⋮
63	1	0x000058	0xF7324A32

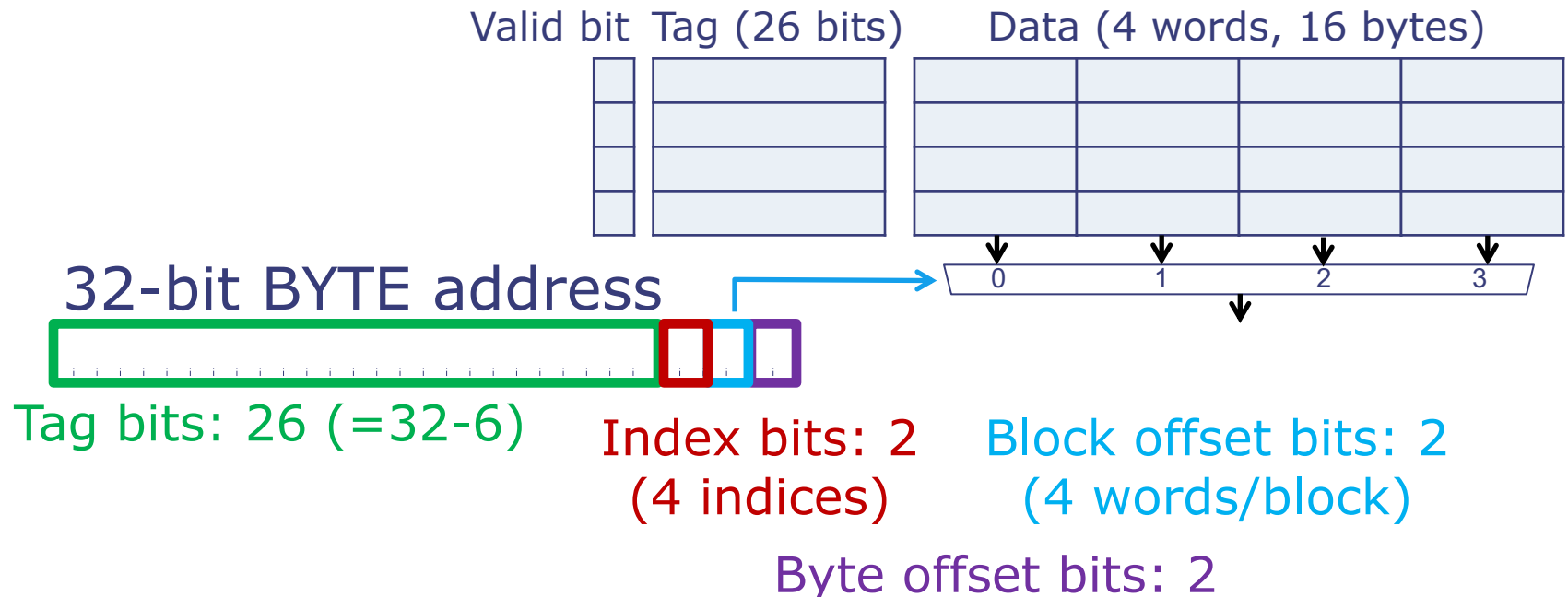
Part of the address (index bits) is encoded in the location
Tag + Index bits unambiguously identify the data's address

Selection of Index Bits

- Why do we chose low order bits for index?
 - Allows consecutive memory locations to live in the cache simultaneously
 - Reduces likelihood of replacing data that may be accessed again in the near future
 - Helps take advantage of locality

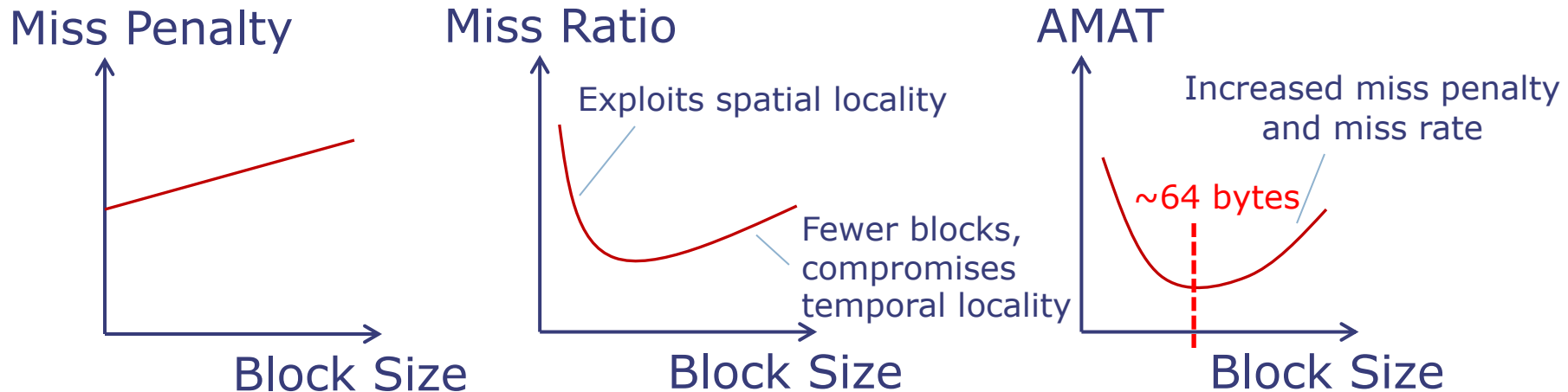
Block Size

- Take advantage of spatial locality: Store multiple words per data line
 - Always fetch entire block (multiple words) from memory
 - Another advantage: Reduces size of tag memory!
 - Potential disadvantage: Fewer indices in the cache
- Example: 4-block, 16-word direct-mapped cache



Block Size Tradeoffs

- Larger block sizes...
 - Take advantage of spatial locality
 - Incur larger miss penalty since it takes longer to transfer the block from memory
 - Can increase the average hit time and miss ratio
- $AMAT = HitTime + MissPenalty * MissRatio$



Direct-Mapped Cache Problem: Conflict Misses

Loop A:
Code at
1024,
data at
37

Word Address	Cache Line index	Hit/ Miss
1024	0	HIT
37	37	HIT
1025	1	HIT
38	38	HIT
1026	2	HIT
39	39	HIT
1024	0	HIT
37	37	HIT
...		

Loop B:
Code at
1024,
data at
2048

1024	0	MISS
2048	0	MISS
1025	1	MISS
2049	1	MISS
1026	2	MISS
2050	2	MISS
1024	0	MISS
2048	0	MISS
...		

Assume:

1024-line DM cache

Block size = 1 word

Consider looping code, in
steady state

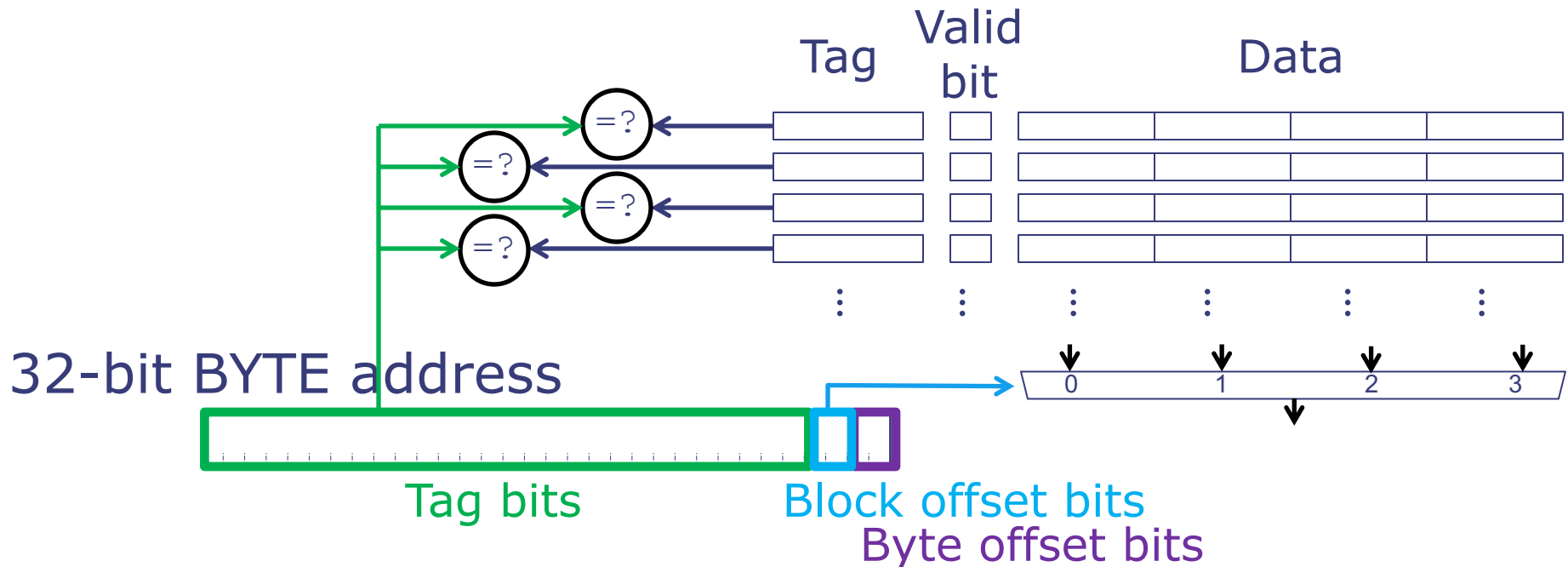
Assume WORD, not BYTE,
addressing

Inflexible mapping
(each address can only be
in one cache location) →
**Conflict misses (multiple
addresses map to same
cache index)!**

Fully-Associative Cache

Opposite extreme: Any address can be in any location

- No cache index!
- **Flexible** (no conflict misses)
- **Expensive**: Must compare tags of all entries in parallel to find matching one

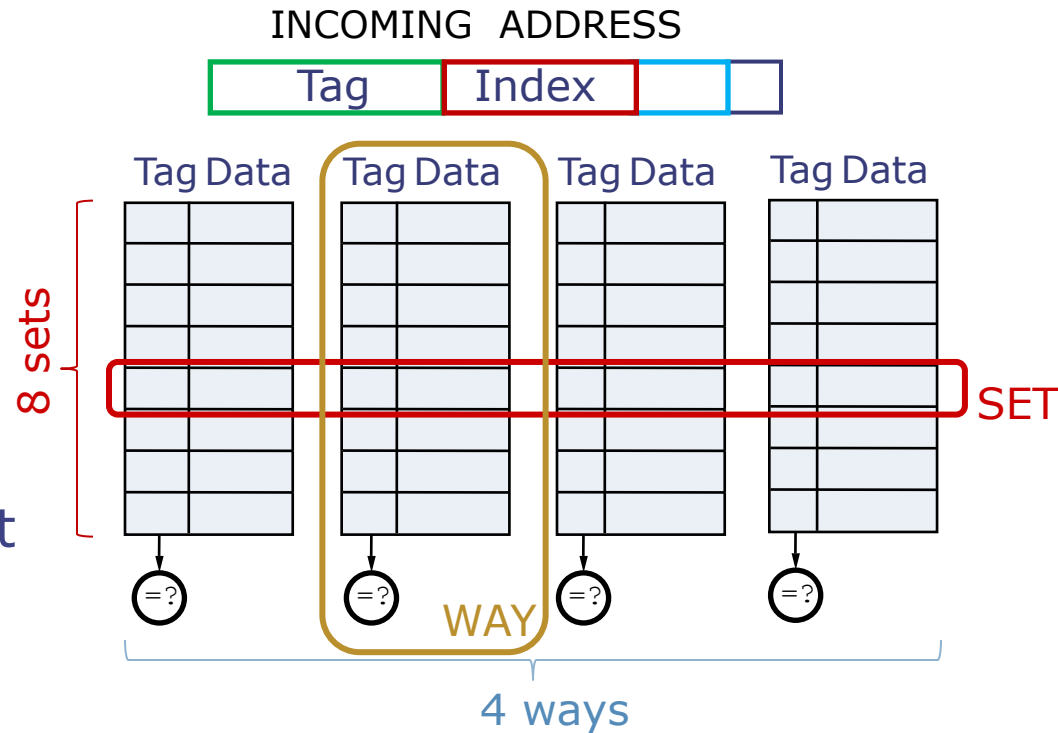


N-way Set-Associative Cache

- Use multiple direct-mapped caches in parallel to reduce conflict misses

- Nomenclature:

- # Rows = # Sets
- # Columns = # Ways
- Set size = #ways
= "set associativity"
(e.g., 4-way → 4 lines/set)
- Each address maps to only one set, but can be in any way within the set
- Tags from all ways are checked in parallel

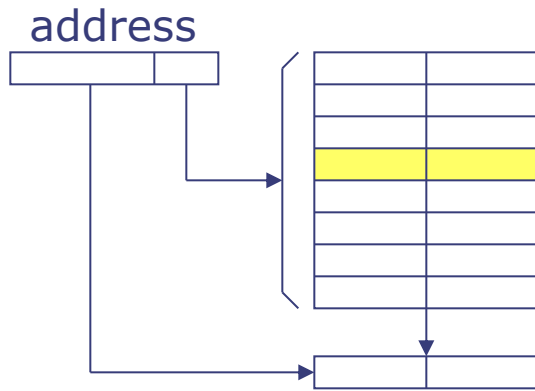


- Fully-associative cache: Extreme case with a single set and as many ways as cache lines

Associativity Implies Choices

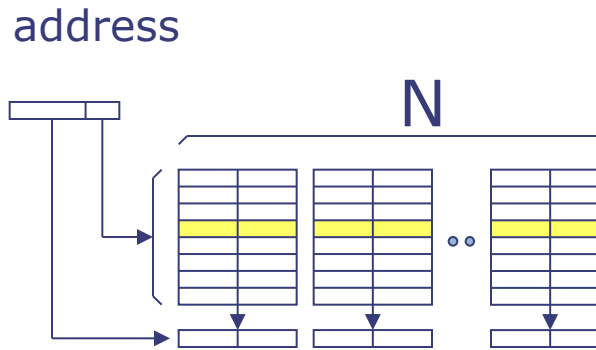
Issue: Replacement Policy

Direct-mapped



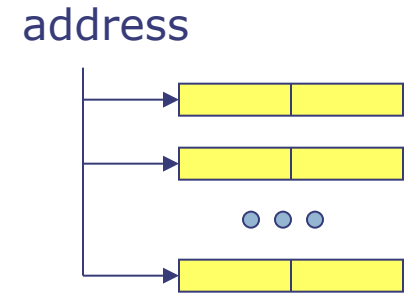
- Compare addr with only one tag
- Location A can be stored in exactly one cache line

N-way set-associative



- Compare addr with N tags simultaneously
- Location A can be stored in exactly one set, but in any of the N cache lines belonging to that set

Fully associative



- Compare addr with each tag simultaneously
- Location A can be stored in any cache line

Replacement Policies

- Optimal policy: Replace the line that is accessed furthest in the future
 - Requires knowing the future...
- Idea: Predict the future from looking at the past
 - If a line has not been used recently, it's often less likely to be accessed in the near future (a locality argument)
- **Least Recently Used (LRU)**: Replace the line that was accessed furthest in the past
 - Works well in practice
 - Need to keep ordered list of N items $\rightarrow N!$ orderings $\rightarrow O(\log_2 N!) = O(N \log_2 N)$ "LRU bits" + complex logic
 - Caches often implement cheaper approximations of LRU
- Other policies:
 - First-In, First-Out (least recently replaced)
 - Random: Choose a candidate at random
 - Not very good, but does not have adversarial access patterns

Write Policy

Write-through: CPU writes are cached, but also written to main memory immediately (stalling the CPU until write is completed). Memory always holds current contents

- Simple, slow, wastes bandwidth

Write-back: CPU writes are cached, but not written to main memory until we replace the line. Memory contents can be “stale”

- Fast, low bandwidth, more complex
- Commonly implemented in current systems

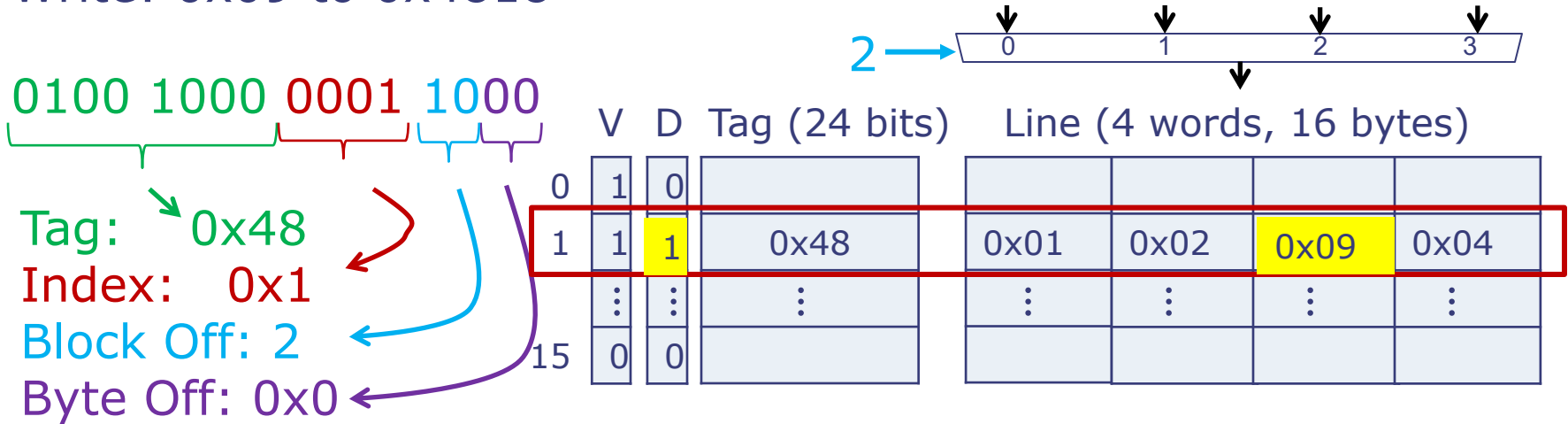
Example: Cache Write-Hit

16-line direct-mapped cache \rightarrow 4 index bits

Block size = 4 \rightarrow 2 block offset bits

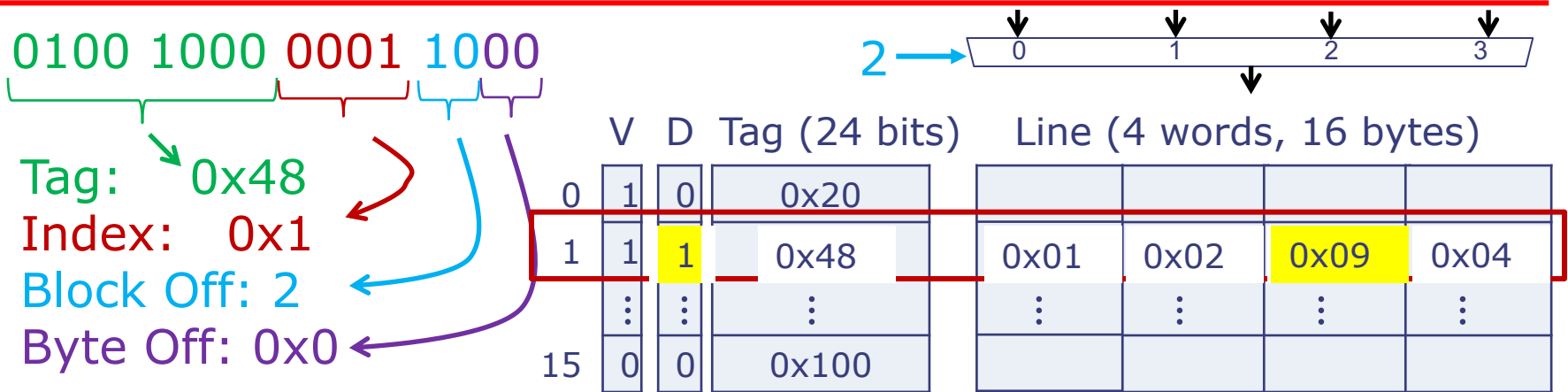
Write Policy = Write Back

Write: 0x09 to 0x4818



D=1: cache contents no longer match main memory so write back line to memory upon replacement

Example: Cache Write-Miss



Write: 0x09 to 0x4818

1. Tags don't match -> Miss

- D=1: Write cache line 1 (tag = 0x280: addresses 0x28010-0x2801C) back to memory
- If D=0: Don't need to write line back to memory.

2. Load line (tag = 0x48: addresses 0x4810-0x481C) from memory

3. Write 0x09 to 0x4818 (block offset 2), set D=1.

Summary: Cache Tradeoffs

$$AMAT = HitTime + MissRatio \times MissPenalty$$

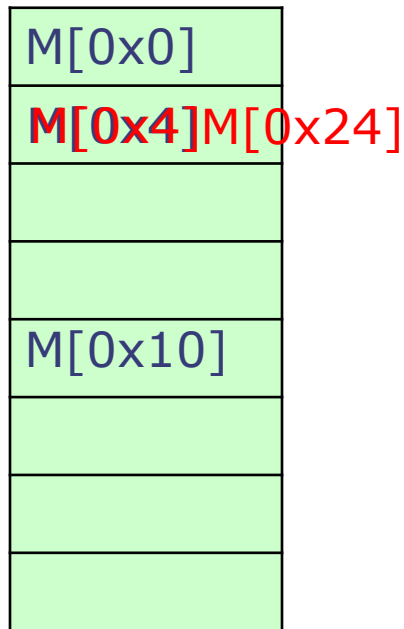
- Cache size
- Block size
- Associativity
- Replacement policy
- Write policy

Example: Comparing Hit Rates

3 Caches: DM, 2-Way, FA: each has 8 words, block size=1, LRU

Access following addresses repeatedly: 0x0, 0x10, 0x4, 0x24

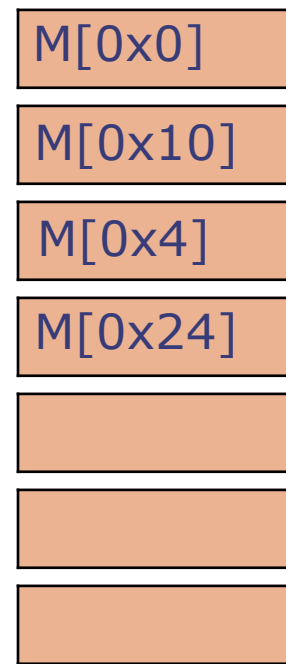
DM



2-Way



FA



DM: 50% hit rate
2-Way: 100% hit rate
FA: 100% hit rate

0x0 = 0b000000

DM index = 000

2-Way index = 00

0x10 = 0b010000

DM index = 100

2-Way index = 01

0x4 = 0b000100

DM index = 001

2-Way index = 01

0x24 = 0b100100

DM index = 001

2-Way index = 01

Example 2: Comparing Hit Rates

Access: 0x0, 0x4, 0x8, 0xC, 0x10, 0x14, 0x18, 0x1C, 0x20 repeatedly

DM

M[0x0]
M[0x20]
M[0x4]
M[0x8]
M[0xC]
M[0x10]
M[0x14]
M[0x18]
M[0x1C]

2-Way

M[0x0]	M[0x10]
M[0x20]	M[0x0]
M[0x10]	M[0x20]
M[0x4]	M[0x14]
M[0x8]	M[0x18]
M[0xC]	M[0x1C]

FA

M[0x0] M[0x20]
M[0x4] M[0x0]
M[0x8] M[0x4]
M[0xC] M[0x8]
M[0x10] M[0xC]
M[0x14] M[0x10]
M[0x18] M[0x14]
M[0x1C] M[0x18]

DM: Hit rate = 7/9

2-Way: Hit rate = 6/9

FA: Hit rate = 0%

Example 3: Comparing Hit Rates

Access: 0x0, 0x4, 0x8, 0xC, 0x20, 0x24, 0x28, 0x2C, 0x10
repeatedly

DM

M[0x0]
M[0x20]
M[0x4]
M[0x24]
M[0x8]
M[0x28]
M[0xC]
M[0x2C]
M[0x10]

2-Way

M[0x0]	M[0x20]
M[0x10]	M[0x0]
M[0x20]	M[0x10]
M[0x4]	M[0x24]
M[0x8]	M[0x28]
M[0xC]	M[0x2C]

FA

M[0x0]	M[0x10]
M[0x4]	M[0x0]
M[0x8]	M[0x4]
M[0xC]	M[0x8]
M[0x20]	M[0xC]
M[0x24]	M[0x20]
M[0x28]	M[0x24]
M[0x2C]	M[0x28]

DM: Hit rate = 1/9

2-Way: Hit rate = 6/9

FA: Hit rate = 0%

Thank you!

*Next lecture: Operating
Systems*