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Software for Automated Residual Plot Assessment: autovi and autovi.web

ANZJS Quarto Template

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Summary

Regression software is widely available, and there are many tools for generating diagnostics and computing conventional residual tests. However, the advice remains that the analyst should look at the residual plot to check the fit. Perhaps, one of the reasons is that conventional tests are too sensitive, strictly resulting in adequate models being abandoned. Visually assess the strength of patterns in residual plots requires human effort and suffers from the potential for inconsistent decisions from different analysts. Using a lineup protocol, where the residual plot is embedded among null plots, can help to alleviate inconsistency, but requires even more human effort. This is the type of task that in today's world might employ a robot to do the tedious work for a human. Here we describe a new R package that includes a computer vision model for automated assessment of residual plots, and an accompanying Shiny app for ease of use. For a user-provided sample of residuals, it predicts a measure of visual signal strength (VSS) and provides a suite of supporting information to assist the analyst decide on the appropriateness their model fit.

Key words: initial data analysis; statistical graphics; data visualization; visual inference; computer vision; machine learning; hypothesis testing; regression analysis

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1. Introduction

Regression analysis is a widely used statistical modeling technique widely for data in 11 many fields. There are a vast array of software for conducting regression modeling 12 and generating diagnostics. The package lmtest (Zeileis & Hothorn 2002) provides a 13 suite of conventional tests. The stats package (R Core Team 2022) offers standard 14 diagnostic plots such as residuals vs. fitted values, quantile-quantile (Q-Q) plots, and 15 residuals vs. leverage plots. Packages like jtools (Long 2022), olsrr (Hebbali 2024), 16 rockchalk (Johnson 2022), and ggResidpanel (Goode & Rey 2019) provide similar 17 graphical diagnostics, often with alternative aesthetics or interactive features. All of 18 these tools deliver the types of diagnostic plots outlined in the classical text by Cook 19 & Weisberg (1982). The ecostats package (Warton 2023) incorporates simulation 20 envelopes into residual plots, while DHARMa (Hartig 2022) compares empirical quantiles 21 (0.25, 0.5, and 0.75) of scaled residuals to their theoretical counterparts. DHARMa is 22 particularly focused on detecting model violations such as heteroscedasticity, incorrect 23 functional forms, and issues specific to generalized linear and mixed-effect models, like 24 over/under-dispersion. It also includes conventional test annotations to help avoid 25 misinterpretation. 26

However relying solely on subjective assessments of these plots can lead to issues, such as 27 over-interpreting random patterns as model violations. Li et al. (2024a) demonstrated 28 that visual methods using the lineup protocol (Buja et al. 2009) for assessing residuals 29 are more useful, and also perform more practically than conventional tests due to their 30 31 reduced sensitivity to minor departures. Packages such as nullabor (Wickham et al. 2020), HLMdiag (Loy & Hofmann 2014), and regressinator (Reinhart 2024), enable 32 users to compare observed residual plots with samples from null distributions, helping 33 to quantify the significance of any detected patterns. However, the 34

However, as discussed in Li et al. (2024b), the lineup protocol has significant limitations 35 in large-scale applications due dependence on human labor. Thus a computer vision 36 model was developed with an associated statistical testing procedure to automate 37 the assessment of residual plots. This model takes a residual plot and a vector of 38 auxiliary variables (such as the number of observations) as inputs and outputs the 39 predicted visual signal strength (VSS). This strength estimates the distance between 40 the residual distribution of the fitted regression model and the reference distribution 41 assumed under correct model specification. 42

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- To make the statistical testing procedure and trained computer vision model widely
- 44 accessible, we developed the R package autovi, and a web interface, autovi.web to
- 45 make it easy for users to automatically read their residual plots with the trained
- 46 computer vision model.
- 47 The remainder of this paper is structured as follows: Section 2 provides a detailed
- 48 documentation of the autovi package, including its usage and infrastructure. Section 3
- 49 focuses on the autovi.web interface, describing its design and usage, along with
- 50 illustrative examples. Finally, Section 4 presents the main conclusions of this work.

2. R package: autovi

- 52 The main purpose of autovi is to provide rejection decisions and p-values for testing
- 53 whether a regression model is correctly specified. The package introduces a novel
- 54 approach to automating statistical analysis, particularly in the interpretation of residual
- plots. The name autovi stands for automated visual inference.
- 56 There are two ways to access the package, directly using R or through a web interface,
- 57 autovi.web. The web interface has the advantage that it can be used without installing
- 58 Python, R and the relevant packages locally.

59 **2.1.** Why use it

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- 60 ?@fig-three-examples shows three sets of plots of residuals against fitted values. The
- 61 simulated example in (a) might be interpreted as a heteroscedastic pattern, however
- 62 the automated reading would predict this to have a visual signal strength (VSS) of
- 63 1.53, with a corresponding p-value of 0.25. This means it is would be interpreted
- as a good residual plot, that there is nothing in the data to indicate a violation of
- 65 model assumptions. Skewness in the predictor variables is generating the apparent
- 66 heteroscedasticity, where the smaller variance in residuals at larger fitted values is
- 67 due to smaller sample size only. The Breusch-Pagan test (Breusch & Pagan 1979) for
- 68 heteroscedasticity would also not reject this as good residual plot.
- 69 The data in (b) is generated by fitting a linear model predicting mpg based on hp
- 70 using the datasets::mtcars. It is a small data set, and there is a hint of nonlinear
- 71 structure not captured by the model. The automated plot reading would predict a
- 72 VSS of 3.57, which has a p-value less than 0.05. That is, the nonlinear structure is
- 73 most likely real, and indicates a problem with the model. The conventional test, a

Ramsey Regression Equation Specification Error Test (RESET) (Ramsey 1969) would also strongly detect the nonlinearity.

The third example is generated using the surreal package (Balamuta 2024) where 76 structured residuals are hidden in data, to be revealed if the correct model is specified. 77 Here a quote based on Tukev is used as the residual structure "visual summaries focus 78 on unexpected values". The automated plot reading predicts the VSS to be 5.87, with 70 a p-value less than 0.05. This structure is blindingly obvious visually, but a RESET 80 test for nonlinear structure would not report a problem. (It would be detected by 81 a Breusch-Pagan for heteroscedasticity and also Shapiro-Wilk test (Shapiro & Wilk 82 1965) for non-normality.) 83

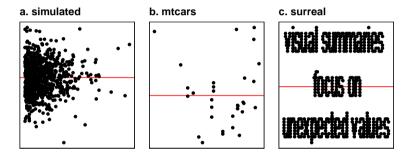


Figure 1. Reading residual plots can be a difficult task, particular for students new to statistical modeling. The autovi package makes it easier. Here are three examples of residual plots, which may appear to have structure. According to autovi, the visual signal strengths (VSS) of these three examples are approximately (a) 1.53, (b) 3.57, (c) 5.87, resulting in (b), (c) being significant violations of good residuals, but (a) is consistent with a good residual plot.

2.2. Implementation

The autovi package is built on the bandicoot object-oriented programming (OOP) system (Li 2024), marking a departure from R's traditional S3 generic system. This OOP architecture enhances flexibility and modularity, allowing users to redefine key functions through method overriding. While similar functionality could be achieved using R's S3 system with generic functions, the OOP framework offers a more structured and extensible foundation for the package.

The autovi infrastructure effectively integrates multiple programming languages and libraries into a comprehensive analytical tool. It relies on five core libraries from Python and R, each playing a critical role in the analysis pipeline. In Python, pillow (Clark et al. 2015) handles image processing tasks such as reading and resizing PNG

- files of residual plots, then converting them into input tensors for further analysis. The
 TensorFlow (Abadi et al. 2016) library, a key component of modern machine learning,
 is used to predict the VSS of these plots through a pre-trained convolutional neural
 network.
- In the R environment, autovi utilizes several libraries. ggplot2 (Wickham 2016) aa generates the initial residual plots, saved as PNG files for visual input. The cassowaryr 100 (Mason et al. 2022) library computes scagnostics (scatter plot diagnostics), providing 101 numerical features that capture statistical properties of the plots. These scagnostics 102 complement the visual analysis by offering quantitative metrics as secondary input to 103 the computer vision model. The reticulate (Ushey, Allaire & Tang 2024) package 104 bridges R and Python, enabling seamless communication between the two languages 105 and supporting the integrated infrastructure. 106

107 2.3. Installation

- The autovi package is available on CRAN. It is actively developed and maintained, with the latest updates accessible on GitHub at https://github.com/TengMCing/autovi.
- 110 The code discussed in this paper is based on autovi version 0.4.1.
- 111 The package includes internal functions to check the current Python environment used 112 by the reticulate package. If the necessary Python packages are not installed in the 113 Python interpreter, an error will be raised. If you want to select a specific Python 114 environment, you can do so by calling the reticulate::use_python() function before

using the autovi package.

116 **2.4.** Usage

115

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To get started quickly, only three function calls are needed to obtain a summary of the automated residual assessment:

```
library(autovi)
checker <- residual_checker(lm(dist ~ speed, data = cars))
checker$check()</pre>
```

```
120 -- <AUTO_VI object>
121 Status:
122 - Fitted model: lm
```

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146

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```
- Keras model: UNKNOWN
123
        - Output node index: 1
124
     - Result:
125
        - Observed visual signal strength: 3.162 (p-value = 0.0396)
126
        - Null visual signal strength: [100 draws]
127
            - Mean: 1.274
128
            - Quantiles:
120
130
                   25%
                           50%
                                   75%
                                           80%
                                                   90%
                                                           95%
                                                                  99%
131
                0.8021 1.1109 1.5751 1.6656 1.9199 2.6564 3.3491
132
133
        - Bootstrapped visual signal strength: [100 draws]
134
            - Mean: 2.786 (p-value = 0.05941)
135
            - Quantiles:
136
137
                                             90%
                  25%
                         50%
                                75%
                                      80%
                                                    95%
                                                           99%
138
                2.452 2.925 3.173 3.285 3.463 3.505 3.652
139
140
        - Likelihood ratio: 0.7275 (boot) / 0.06298 (null) = 11.55
141
```

142 The three functions are explained as follows:

- 1. Load the autovi package using the library() function.
- 2. Create a checker object with a linear regression model.
 - 3. Call the check() method of the checker, which, by default, predicts the VSS for the true residual plot, 100 null plots, and 100 bootstrapped plots, storing the predictions internally. A concise report of the check results is then printed.

The summary reports key findings such as the VSS of the true residual plot and the p-value of the automated visual test. The p-value is the ratio of null plots that have VSS greater than or equal to that of the true residual plot. We typically reject the null hypothesis when the p-value is smaller than or equal to a desired significance level, such as 5%. The report also provides sample quantiles of VSS for null and bootstrapped plots, helping to explain the severity and likelihood of model violations.

Although the p-value is sufficient for automated decision-making, users can visually inspect the original residual plot alongside a sample null plot. This visual comparison can clarify why H_0 is either rejected or not, and help identify potential remedies. The plot_pair() and plot_lineup() methods facilitate this comparison.

checker\$plot_pair()

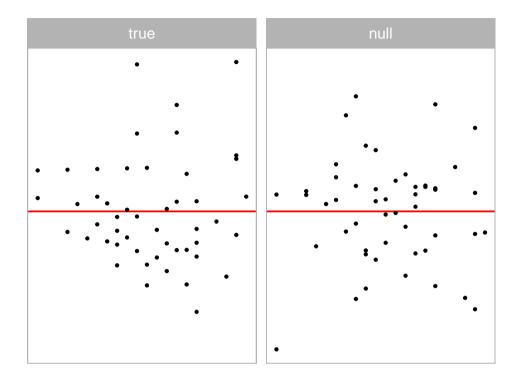


Figure 2. True plot alongside one null plot, for quick comparison.

The plot_pair() method (Figure 2) displays the true residual plot on the left and a single null plot on the right. If a full lineup was shown, the true residual plot would be embedded in a page of null plots. Users should look for any distinct visual patterns in the true residual plot that are absent in the null plot. Running these functions multiple times can help any visual suspicions, as each execution generates new random null plots for comparison.

The package offers a straightforward visualization of the assessment result through the summary_plot() function.

```
checker$summary_plot()
```

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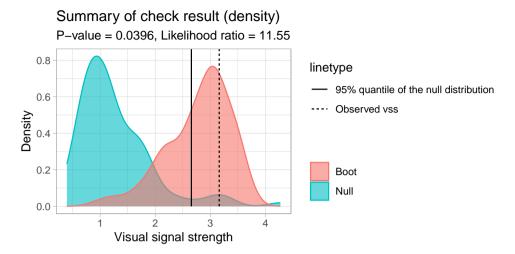


Figure 3. Summary plot comparing the densities of VSS for bootstrapped residual samples (red) relative to VSS for null plots (blue).

In the result, shown in Figure 3, the blue area represents the density of VSS for null residual plots, while the red area shows the density for bootstrapped residual plots. The dashed line indicates the VSS of the true residual plot, and the solid line marks the critical value at a 95% significance level. The p-value and the likelihood ratio are displayed in the subtitle. The likelihood ratio represents the ratio of the likelihood of observing the VSS of the true residual plot from the bootstrapped distribution compared to the null distribution.

Interpreting the plot involves several key aspects. If the dashed line falls to the right of
the solid line, it suggests rejecting the null hypothesis. The degree of overlap between
the red and blue areas indicates similarity between the true residual plot and null
plots; greater overlap suggests more similarity. Lastly, the portion of the red area to
the right of the solid line represents the percentage of bootstrapped models considered
to have model violations.

This visual summary provides an intuitive way to assess the model's fit and potential violations, allowing users to quickly grasp the results of the automated analysis.

2.5. Modularized Infrastructure

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The initial motivation for developing autovi was to create a convenient interface for sharing the models described and trained in Li et al. (2024b). However, recognizing that the classical normal linear regression model represents a restricted class of models,

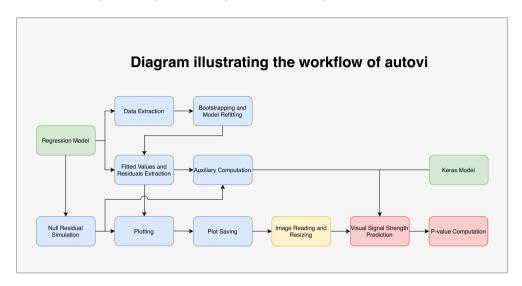


Figure 4. Diagram illustrating the infrastructure of the R package autovi. The modules in green are primary inputs provided by users. Modules in blue are overridable methods that can be modified to accommodate users' specific needs. The module in yellow is a pre-defined non-overridable method. The modules in red are primary outputs of the package.

we sought to avoid limiting the potential for future extensions, whether by the original developers or other users. As a result, the package was designed to function seamlessly with linear regression models with minimal modification and few required arguments, while also accommodating other classes of models through partial infrastructure substitution. This modular and customizable design allows autovi to handle a wide range of residual diagnostics tasks.

The infrastructure of autovi consists of ten core modules: data extraction, bootstrapping and model refitting, fitted values and residuals extraction, auxiliary computation, null residual simulation, plotting, plot saving, image reading and resizing, VSS prediction, and p-value computation. Each module is designed with minimal dependency on the preceding modules, allowing users to customize parts of the infrastructure without affecting its overall integrity. An overview of this infrastructure is illustrated in Figure 4.

The modules for VSS prediction and p-value computation are predefined and cannot be overridden, although users can interact with them directly through function arguments. Similarly, the image reading and resizing module is fixed but will adapt to different Keras models by checking their input shapes. The remaining seven modules are designed to be overridable, enabling users to tailor the infrastructure to their specific needs. These modules are discussed in detail in the following sections.

2.5.1. Initialization

An autovi checker can be initialized by supplying two primary inputs, including 205 a regression model object, such as an 1m object representing the result of a linear 206 regression model, and a trained computer vision model compatible with the Keras 207 (Chollet et al. 2015) Application Programming Interface (API), to the AUTO VI class 208 constructor auto vi(). The residual checker() introduced in Section 2.4 is a thin 209 wrapper around auto_vi(), which will call get_keras_model() during initialization. 210 get_keras_model() is a function to download a trained computer vision model 211 (described in Li et al. (2024b)) from GitHub. "vss phn 32" specifies a model that 212 predicts VSS and is trained on residuals with polynomial, heteroscedasticity, and 213 non-normality patterns (phn). More details about the hosted models will be provided 214 in Section 2.8. 215

The input of the constructor will be stored as attributes of the checker and can be accessed by the user through the \$ operator.

Optionally, the user may specify the node index of the output layer of the trained computer vision model to be monitored by the checker via the node_index argument if there are multiple output nodes. This is particularly useful for multiclass classifiers when the user wants to use one of the nodes as a VSS indicator.

222 After initializing the object, you can print the checker to view its status.

```
-- <AUTO_VI object>
Status:
- Fitted model: lm
- Keras model: (None, 32, 32, 3) + (None, 5) -> (None, 1)
- Output node index: 1
- Result: UNKNOWN
```

The status includes the list of regression model classes (as provided by the built-in class() function), the input and output shapes of the Keras model in the standard Numpy format (Harris et al. 2020), the output node index being monitored, and the assessment result. If no check has been run yet, the assessment result will display as "UNKNOWN".

228 2.5.2. Fitted Values and Residuals Extraction

To be able to predict VSS for a residual plot, both fitted values and residuals are 229 needed to be extracted from the regression model object supplied by the user. In R, 230 statistical models like 1m (linear model) and glm (generalized linear model) typically 231 support the use of generic functions such as fitted() and resid() to retrieve these 232 values. The get_fitted_and_resid() method, called by the checker, relies on these 233 generic functions by default. However, generic functions only work with classes that 234 have appropriate method implementations. Some regression modeling packages may 235 not fully adhere to the stats package guidelines for implementing these functions. In 236 such cases, overriding the method becomes necessary. 237

238 By design, the get_fitted_and_resid() method accepts a regression model object as input and returns a tibble (a modern presentation of the data.frame) with two 239 columns: .fitted and .resid, representing the fitted values and residuals, respectively. 240 If no input is supplied, the method uses the regression model object stored in the 241 checker. Although modules in the autovi infrastructure make minimal assumptions 242 about other modules, they do require strictly defined input and output formats to 243 ensure data validation and prevent fatal bugs. Therefore, any overridden method 244 245 should follow to these conventions.

checker\$get_fitted_and_resid()

```
# A tibble: 50 x 2
246
         .fitted .resid
247
           <dbl>
248
                   <dbl>
      1
           -1.85
                     3.85
249
           -1.85
      2
                   11.8
250
251
      3
            9.95
                   -5.95
      4
            9.95
                   12.1
252
      5
           13.9
                     2.12
253
      6
           17.8
                   -7.81
254
      7
           21.7
                    -3.74
255
      8
           21.7
                     4.26
256
      9
           21.7
                    12.3
257
           25.7
                    -8.68
258
     10
     # i 40 more rows
259
```

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260 2.5.3. Data Extraction

For linear regression model in R, the model frame contains all the data required by a 261 formula for evaluation. This is essential for bootstrapping and refitting the model when 262 constructing a bootstrapped distribution of VSS. Typically, the model frame can be 263 extracted from the regression model object using the model.frame() generic function, 264 which is the default method used by get data(). However, some regression models 265 do not use a formula or are evaluated differently, potentially lacking a model frame. In 266 such cases, users can either provide the data used to fit the regression model through 267 the data argument when constructing the checker, or customize the method to better 268 suit their needs. It's worth noting that this module is only necessary if bootstrapping 269 is required, as the model frame is not used in other modules of the infrastructure. 270

The get_data() method accepts a regression model object as input and returns a data.frame representing the model frame of the fitted regression model. If no input is supplied, the regression model stored in the checker will be used.

```
checker$get_data() |>
  head()
```

```
dist speed
274
             2
     1
                      4
275
     2
            10
                      4
276
     3
                      7
             4
277
     4
            22
                      7
278
     5
            16
                      8
279
     6
            10
                      9
280
```

2.5.4. Bootstrapping and Model Refitting

Bootstrapping a regression model typically involves sampling the observations with replacement and refitting the model with the bootstrapped data. The boot_method() method follows this bootstrapping scheme by default. It accepts a fitted regression model and a data.frame as inputs, and returns a tibble of bootstrapped residuals. If no inputs are provided, the method uses the regression model stored in the checker and the result of the get_data() method.

Note that instead of calling get_data() implicitly within the method, it is used as part of the default argument definition. This approach allows users to bypass the get data() method entirely and directly supply a data.frame to initiate the bootstrap process. Many other methods in autovi adopt this principle when possible, where dependencies are explicitly listed in the formal arguments. This design choice enhances the reusability and isolation of modules, offers better control for testing, and simplifies the overall process.

```
checker$boot_method(data = checker$get_data())
```

```
# A tibble: 50 x 2
295
296
        .fitted .resid
           <dbl>
                   <dbl>
297
          27.0
                   -2.96
      1
298
      2
          38.8
                  -12.8
299
      3
          34.8
                   -8.82
300
      4
          27.0
                  -13.0
301
302
      5
           11.2
                    4.76
      6
          42.7
                   -2.68
303
      7
          42.7
                   -2.68
304
      8
          38.8
                  -18.8
305
      9
          38.8
                   15.2
306
    10
           -4.47
                    6.47
307
    # i 40 more rows
308
```

309

2.5.5. Auxiliary Computation

As described in Li et al. (2024b), in some cases, a residual plot alone may not provide 310 enough information to accurately determine VSS. For instance, when the points in the 311 residual plot have significant overlap, the trend and shape of the residual pattern can be 312 difficult to discern. Including auxiliary variables, such as the number of observations, 313 as additional inputs to the computer vision model can be beneficial. To address 314 this, autovi includes internal functions within the checker that automatically detect 315 the number of inputs required by the provided Keras model. If multiple inputs are 316 317 necessary, the checker invokes the auxiliary() method to compute these additional inputs. 318

The auxiliary() method takes a data.frame containing fitted values and residuals as input and returns a data.frame with five numeric columns. These columns represent four scagnostics — "Monotonic", "Sparse", "Striped", and "Splines" — calculated using the cassowaryr package, as well as the number of observations. This approach is consistent with the training process of the computer vision models described in Li

et al. (2024b). If no data.frame is provided, the method will default to retrieving fitted values and residuals by calling get_fitted_and_resid().

Technically, any Keras-implemented computer vision model can be adapted to accept an image as the primary input and additional variables as secondary inputs by adding a data pre-processing layer before the actual input layer. If users wish to override auxiliary(), the output should be a data.frame with a single row and the number of columns such that its concatenation matches the number of parameters for the corresponding layer in the supplied Keras model.

checker\$auxiliary()

```
# A tibble: 1 x 5
332
      measure_monotonic measure_sparse measure_splines measure_striped
                                                                                   n
333
                    <dbl>
                                     <dbl>
                                                      <dbl>
                                                                        <dbl> <int>
334
    1
                  0.0621
                                     0.470
                                                     0.0901
                                                                         0.62
                                                                                  50
335
```

2.5.6. Null Residual Simulation

A fundamental element of the automated residual assessment described in Li et al. 337 (2024b) is comparing the VSS of null plots with that of the true residual plot. However, 338 due to the variety of regression models, there is no universal method for simulating null 339 residuals that are consistent with model assumptions. Fortunately, for classical normal 340 linear regression models, null residuals can be effectively simulated using the residual 341 rotation method, as outlined in Buja et al. (2009). This process involves generating 342 random draws from a standard normal distribution, regressing these draws on the 343 original predictors, and then rescaling the resulting residuals by the ratio of the residual 344 sum of squares to the that of the original linear regression model. Other regression 345 models, such as glm (generalized linear model) and gam (generalized additive model), 346 generally cannot use this method to efficiently simulate null residuals. Therefore, it is 347 recommended that users override the null_method() to suit their specific model. The 348 null_method() takes a fitted regression model as input, defaulting to the regression 349 model stored in the checker, and returns a tibble. 350

checker\$null method()

```
351 # A tibble: 50 x 2
352 .fitted .resid
353 <dbl> <dbl>
354 1 -1.85 18.2
```

```
2
           -1.85
                   -0.765
355
      3
            9.95 - 12.8
356
            9.95
      4
                   18.6
357
      5
           13.9
                     2.57
358
      6
           17.8
                     7.03
359
      7
           21.7
                  -11.1
360
     8
           21.7
                  -13.2
361
      9
           21.7
                  -12.6
362
    10
           25.7
                     3.57
363
    # i 40 more rows
364
```

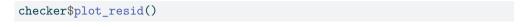
365 **2.5.7.** Plotting

Plotting is a crucial aspect of residual plot diagnostics because aesthetic elements like 366 marker size, marker color, and auxiliary lines impact the presentation of information. 367 There are computer vision models trained to handle images captured in various 368 scenarios. For example, the VGG16 model (Simonyan & Zisserman 2014) can classify 369 objects in images taken under different lighting conditions and is robust to image 370 rotation. However, data plots are a special type of image as the plotting style can 371 always be consistent if controlled properly. Therefore, we assume computer vision 372 models built for reading residual plots will be trained with residual plots of a specific 373 aesthetic style. In this case, it is best to predict plots using the same style for optimal 374 performance. The plotting method plot_resid() handles this aspect. 375

plot_resid() accepts a data.frame containing fitted values and residuals, along 376 with several customization options: a ggplot theme, an alpha value to control the 377 transparency of data points, a size value to set the size of data points, and a stroke 378 value to define the thickness of data point edges. Additionally, it includes four Boolean 379 arguments to toggle the display of axes, legends, grid lines, and a horizontal red line. 380 By default, it replicates the style we used to generate the training samples for the 381 computer vision models described in Li et al. (2024b). In brief, the residual plot omits 382 axis text and ticks, titles, and background grid lines, featuring only a red line at y=0. 383 It retains only the necessary components of a residual plot. If the computer vision 384 model is trained with a different but consistent aesthetic style, plot resid() should 385 be overridden. 386

The method returns a ggplot object (Figure 5), which can be saved as a PNG file in the following module. If no data is provided, the method will use get_fitted_and_resid()

to retrieve the fitted values and residuals from the regression model stored in the checker.



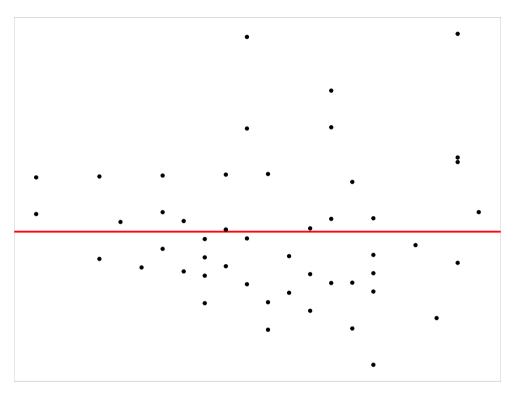


Figure 5. Residual plot of the regression model stored in the checker.

To manually generate true residual plots, null plots, or bootstrapped residual plots, you can pass the corresponding data.frame produced by the get_fitted_and_resid(), null_method(), and boot_method() methods to the plot_resid() method, respectively.

2.5.8. Plot Saving

395

Another key aspect of a standardized residual plot is its resolution. In Li et al. (2024b), we used an image format of 420 pixels in height and 525 pixels in width. This resolution was chosen because the original set, consisting of 20 residual plots arranged in a four by five grid, was represented by an image of 2100 by 2100 pixels. The save_plot() method accepts a ggplot object as input and saves it as a PNG file to the location specified by the path argument. If no path is provided, the PNG file is saved to a temporary file.

```
checker$plot_resid() |>
  checker$save_plot()
```

403 [1] "/var/folders/61/bv7_1qzs20x6fjb2rsv7513r0000gn/T//Rtmp6Lce76/file135f86b4a7b6

404 2.5.9. Image Reading and Resizing

When training computer vision models, it is common to test various input sizes 405 for the same architecture to identify the optimal setup. This involves preparing 406 the original training image at a higher resolution than required and then resizing 407 it to match the input size during training. The autovi package includes a class, 408 KERAS WRAPPER, to simplify this process. This Keras wrapper class features a method 409 called image_to_array(), which reads an image as a PIL image using the pillow 410 Python package, resizes it to the target input size required by the Keras model, and 411 converts it to a Numpy array. 412

To construct a KERAS_WRAPPER object, you need to provide the Keras model as the 413 main argument. However, users generally do not need to interact with this class 414 directly, as the autovi checker automatically invokes its methods when performing 415 VSS predictions. The image to array() method takes the path to the image file, 416 the target height, and the target width as inputs and returns a Numpy array. If not 417 specified, the target height and target width will be retrieved from the input layer 418 of the Keras model by the get_input_height() and get_input_width() method of 419 KERAS WRAPPER. 420

The following code example demonstrate the way to manually generate the true residual plot, save it as PNG file, and load it back as Numpy array.

```
wrapper <- keras_wrapper(keras_model = checker$keras_model)
input_array <- checker$plot_resid() |>
   checker$save_plot() |>
   wrapper$image_to_array()
input_array$shape
```

423 (1, 32, 32, 3)

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2.5.10. Visual Signal Strength (VSS) Prediction 424

- VSS, as discussed in Li et al. (2024b), estimates the distance between the input residual 425 plot and a theoretically good residual plot. It can be defined in various ways, much 426 like different methods for measuring the distance between two points. This will not 427 impact the autovi infrastructure as long as the provided Keras model can predict the 428 intended measure. 429
- There are several ways to obtain VSS from the checker, with the most direct being the 430 vss() method. By default, this method predicts the VSS for the true residual plot. If 431 a ggplot or a data.frame, such as null residuals generated by the null_method(), 432 is explicitly provided, the method will use that input to predict VSS accordingly. 433 Note that if a ggplot is provided, auxiliary inputs must be supplied manually via 434 the auxiliary argument, as we assume that auxiliary variables can not be computed 435 directly from a ggplot.
- Another way to obtain VSS is by calling the check() method. This comprehensive 437 method perform extensive diagnostics on the true residual plot and store the VSS in 438 the check result field of the checker. Additionally, for obtaining VSS for null residual 439 plots and bootstrapped residual plots, there are two specialized methods, null vss() 440 and boot vss(), designed for this purpose respectively. 441
- Calling the vss() method without arguments will predict the VSS for the true residual 442 plot and return the result as a single-element tibble. 443

checker\$vss()

```
# A tibble: 1 x 1
444
          vss
445
       <dbl>
446
        3.16
447
```

Providing a data.frame of null residuals or a null residual plot yields the same VSS. 448

```
null_resid <- checker$null_method()</pre>
checker$vss(null_resid)
```

```
# A tibble: 1 x 1
449
          VSS
450
451
       <dbl>
        1.23
452
     1
```

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```
null_resid |>
  checker$plot_resid() |>
  checker$vss()
```

```
453 # A tibble: 1 x 1
454 vss
455 <dbl>
456 1 1.23
```

The null_vss() helper method primarily takes the number of null plots as input. If
the user wants to use a ad hoc null simulation scheme, it can be provided via the
null_method argument. Intermediate results, including null residuals and null plots,
can be returned by enabling keep_null_data and keep_null_plot. The VSS, along
with null residuals and null plots, will be stored in a tibble with three columns. The
following code example demonstrates how to predict the VSS for five null residual
plots while keeping the intermediate results.

```
# A tibble: 5 x 3
464
        vss data
                             plot
465
      <dbl> <list>
                             t>
466
    1 0.982 <tibble [50 \times 2] > \langle gg >
467
    2 1.58 <tibble [50 x 2]> <gg>
468
    469
    4 0.742 <tibble [50 x 2]> <gg>
470
          <tibble [50 x 2]> <gg>
    5 2.21
471
```

The boot_vss() helper method is similar to null_vss(), with some differences in argument names. The following code example demonstrates how to predict the VSS for five bootstrapped residual plots while keeping the intermediate results.

```
475 # A tibble: 5 x 3
```

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```
vss data
                                    plot
476
       <dbl> <list>
                                    t>
477
        3.12 < tibble [50 x 2] > < gg>
        2.37 < tibble [50 x 2] > < gg >
479
        2.87 < \text{tibble } [50 \times 2] > < gg>
480
        1.85 <tibble [50 x 2]> <gg>
481
        3.66 < tibble [50 x 2] > < gg >
    5
482
```

483 2.5.11. p-value Computation

Once we have obtained the VSS from both the true residual plot and the null plots, we 484 can compute the p-value. This p-value represents the ratio of plots with VSS greater 485 than or equal to that of the true residual plot. We can perform this calculation using the 486 check() method. The main inputs for this method are the number of null plots and the 487 number of bootstrapped plots to generate. If you need to access intermediate residuals 488 and plots, you can enable the keep_data and keep_plot options. The method stores 480 the final result in the check_result field of the object. To obtain the p-value using 490 the check() method, you can use the following code. 491

```
checker$check(boot_draws = 100L, null_draws = 100L)
checker$check_result$p_value
```

492 [1] 0.02970297

493 2.6. Summary Plots

After executing the check() method, autovi offers two visualization options for the 494 assessment result through the summary_plot() method, including the density plot and 495 the rank plot. We have already discussed and interpreted the density plot in Section 2.4. 496 Here, we would like to highlight the flexibility in choosing which elements to display 497 in the density plot as shown in Figure 6. For instance, you can omit the bootstrapped 498 distribution by setting boot_dist to NULL. Similarly, you can hide the null distribution 499 (null_dist), the p-value (p_value), or the likelihood ratio (likelihood_ratio) as 500 needed. The following example demonstrates how to create a summary plot without 501 the results from bootstrapped plots. 502

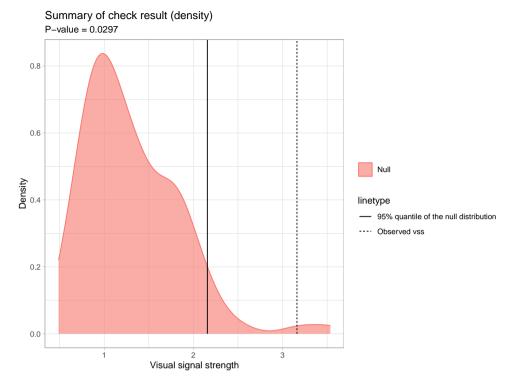


Figure 6. Density plot of the VSS for null plots.

This customization allows you to focus on specific aspects of the assessment, tailoring the visualization to your analytical needs.

The rank plot (Figure 7), creating by setting type to "rank", is a bar plot where the x-axis represents the rank and the y-axis shows the VSS. The bar that is coloured in red corresponding to the VSS of the true residual plot. By examining the rank plot, you can intuitively understand how the observed VSS compares to the null VSSs and identify any outliers in the null distribution.

```
checker$summary_plot(type = "rank")
```

505

506

507

508

509

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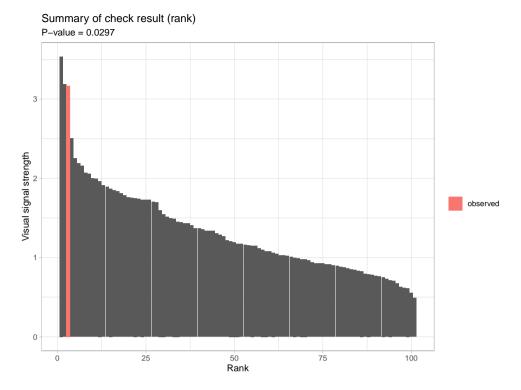


Figure 7. Rank plot of the VSS for null plots.

510 2.7. Feature Extraction

In addition to predicting VSS and computing p-values, autovi offers methods to extract features from any layer of the Keras model. To see which layers are available in the current Keras model, you can use the list_layer_name() method from the KERAS_WRAPPER class.

515 The following code example lists the layer names of the currently used Keras model:

```
wrapper <- keras_wrapper(checker$keras_model)
wrapper$list_layer_name()</pre>
```

```
[1] "input 1"
516
                                       "tf.__operators__.getitem"
     [3] "tf.nn.bias add"
                                       "grey scale"
517
     [5] "block1_conv1"
                                       "batch_normalization"
518
     [7] "activation"
                                       "block1_conv2"
519
     [9] "batch normalization 1"
                                       "activation 1"
520
    [11] "block1_pool"
                                       "dropout"
521
```

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```
[13] "block2 conv1"
                                       "batch normalization 2"
522
    [15] "activation 2"
                                       "block2 conv2"
523
    [17] "batch normalization 3"
                                       "activation 3"
524
    [19] "block2 pool"
                                       "dropout 1"
525
526
    [21] "block3 conv1"
                                       "batch normalization 4"
    [23] "activation_4"
                                       "block3 conv2"
527
    [25] "batch_normalization_5"
                                       "activation 5"
528
    [27] "block3 conv3"
                                       "batch_normalization_6"
529
    [29] "activation 6"
                                       "block3 pool"
530
    [31] "dropout 2"
                                       "block4 conv1"
531
    [33] "batch_normalization_7"
                                       "activation 7"
532
    [35] "block4 conv2"
                                       "batch_normalization_8"
533
    [37] "activation 8"
                                       "block4 conv3"
534
    [39] "batch normalization 9"
                                       "activation 9"
535
                                       "dropout_3"
    [41] "block4_pool"
536
    [43] "block5_conv1"
                                       "batch_normalization_10"
537
                                       "block5 conv2"
    [45] "activation 10"
538
539
    [47] "batch_normalization_11"
                                       "activation 11"
    [49] "block5_conv3"
                                       "batch_normalization_12"
540
    [51] "activation_12"
                                       "block5_pool"
541
    [53] "dropout_4"
                                       "global_max_pooling2d"
542
    [55] "additional input"
                                       "concatenate"
543
    [57] "dense"
                                       "dropout_5"
544
    [59] "activation_13"
                                       "dense_1"
545
```

Among these layers, the "global_max_pooling2d" layer is a 2D global max pooling layer that outputs the results from the last convolutional blocks. As Simonyan & Zisserman (2014) noted, all preceding convolutional blocks can be viewed as a large feature extractor. Consequently, the output from this layer provides features that can be utilized for various purposes, such as performing transfer learning.

То obtain the features. provide the laver using the name 551 extract_feature_from_layer argument in the predict() method. This will 552 return a tibble with the VSS and all features extracted from that layer. Each row 553 corresponds to one plot. The features will be flattened into 2D and named with the 554 prefix "f" if ollowed by a number from one to the total number of features. 555

```
# A tibble: 1 x 257
556
              f 1
                    f_2
                           f_3
                                 f_4
                                       f_5
                                               f_6
                                                     f_7
                                                            f_8
                                                                   f_9
                                                                         f_10 f_11
557
      <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                           <dbl> <dbl>
                                                          <dbl> <dbl>
                                                                        <dbl> <dbl>
558
      3.16 0.151
                      0
                             0
                                   0
                                         0 0.0203 0.109 0.0203
                                                                     0 0.0834
                                                                                  0
559
    # i 245 more variables: f 12 <dbl>, f 13 <dbl>, f 14 <dbl>, f 15 <dbl>,
560
        f_16 <dbl>, f_17 <dbl>, f_18 <dbl>, f_19 <dbl>, f_20 <dbl>, f_21 <dbl>,
561
        f_22 <dbl>, f_23 <dbl>, f_24 <dbl>, f_25 <dbl>, f_26 <dbl>, f_27 <dbl>,
562
        f 28 <dbl>, f 29 <dbl>, f 30 <dbl>, f 31 <dbl>, f 32 <dbl>, f 33 <dbl>,
563
        f_34 <dbl>, f_35 <dbl>, f_36 <dbl>, f_37 <dbl>, f_38 <dbl>, f_39 <dbl>,
564
        f_40 <dbl>, f_41 <dbl>, f_42 <dbl>, f_43 <dbl>, f_44 <dbl>, f_45 <dbl>,
565
        f_46 <dbl>, f_47 <dbl>, f_48 <dbl>, f_49 <dbl>, f_50 <dbl>, f_51 <dbl>, ...
566
```

Alternatively, the AUTO_VI class provides a way to extract features using the vss() method. This method is essentially a high-level wrapper around the predict() method of KERAS_WRAPPER, but it offers a more straightforward interface and better default arguments.

The results from the previous code example can be replicated with a single line of code as shown below.

```
checker$vss(extract_feature_from_layer = "global_max_pooling2d")
```

```
# A tibble: 1 x 257
573
                                                                                   f 2
                                                                                                            f 3
                                                                                                                                      f 4
                                                                                                                                                               f 5
                                                                                                                                                                                            f 6
                                                                                                                                                                                                                      f 7
                                                                                                                                                                                                                                                   f 8
                                                                                                                                                                                                                                                                             f 9
                                                                                                                                                                                                                                                                                                      f 10 f 11
574
                         <dbl> 
                                                                                                                                                                                                                                                                                                  <dbl> <dbl>
575
                         3.16 0.151
                                                                                            0
                                                                                                                                               0
                                                                                                                                                                       0 0.0203 0.109 0.0203
                                                                                                                                                                                                                                                                                     0 0.0834
                                                                                                                                                                                                                                                                                                                                            0
576
                # i 245 more variables: f 12 <dbl>, f 13 <dbl>, f 14 <dbl>, f 15 <dbl>,
577
                                 f 16 <dbl>, f 17 <dbl>, f 18 <dbl>, f 19 <dbl>, f 20 <dbl>, f 21 <dbl>,
578
                                 f_22 <dbl>, f_23 <dbl>, f_24 <dbl>, f_25 <dbl>, f_26 <dbl>, f_27 <dbl>,
579
                                 f_28 <dbl>, f_29 <dbl>, f_30 <dbl>, f_31 <dbl>, f_32 <dbl>, f_33 <dbl>,
580
                                 f_34 <dbl>, f_35 <dbl>, f_36 <dbl>, f_37 <dbl>, f_38 <dbl>, f_39 <dbl>,
581
                                 f_40 <dbl>, f_41 <dbl>, f_42 <dbl>, f_43 <dbl>, f_44 <dbl>, f_45 <dbl>,
582
```

```
f 46 <dbl>, f 47 <dbl>, f 48 <dbl>, f 49 <dbl>, f 50 <dbl>, f 51 <dbl>, ...
583
    The argument extract_feature_from_layer is also available in other functions that
584
```

build on the vss() method, including null_vss(), boot_vss(), and check(). 585

2.8. Trained Model Hosting 586

The trained computer vision models described in Li et al. (2024b) are hosted on a 587 GitHub repository at https://github.com/TengMCing/autovi data. Currently, there 588 are six models available. You can view them by calling list_keras_model(), which 589 will return a tibble showing the input shape and a description of each model. 590

```
list keras model() |>
  str()
```

```
tibble [6 x 11] (S3: tbl_df/tbl/data.frame)
                                                                                                           : chr [1:6] "vss_32" "vss_64" "vss_128" "vss_phn_32" ...
                   $ model_name
592
                   $ path
                                                                                                           : chr [1:6] "keras_model/vss_32.keras.zip" "keras_model/vss
593
                                                                                                           : chr [1:6] "keras_model_volumes/vss_32.zip.001" "keras_model_volumes/vss_32.zip.001"
                   $ volume_path
594
                                                                                                           : int [1:6] 4 1 8 2 8 8
                   $ volume_size
595
                                                                                                           : chr [1:6] "keras_model_npz/vss_32.npz" "keras_model_npz/v
                   $ npz_path
596
                   $ npz_py
                                                                                                           : chr [1:6] "keras_model_npz/vss_32_rebuild.py" "keras_model
597
                   $ input_height
                                                                                                           : int [1:6] 32 64 128 32 64 128
598
                   $ input_width
                                                                                                          : int [1:6] 32 64 128 32 64 128
599
                   $ input_channels
                                                                                                          : int [1:6] 3 3 3 3 3 3
600
                   $ auxiliary_input_size: int [1:6] 0 0 0 5 5 5
601
                   $ description
                                                                                                           : chr [1:6] "A Keras model trained with residual plots cont
602
```

The get_keras_model() function can be used to download a model to a temporary 603 directory and load it into memory using TensorFlow. It requires only the model name, 604 which is the value in the first column of the tibble returned by list_keras_model().

3. Web interface: autovi.web

The autovi.web package extends the functionality of autovi by offering a user-607 friendly web interface for automated residual plot assessment. This eliminates the 608 common challenges associated with software installation, so users can avoid managing 609 Python environments or handling version requirements for R libraries. The platform 610 is cross-platform and accessible on various devices and operating systems, making it 611

605

606

suitable even for users without R programming experience. Additionally, updates are managed centrally, ensuring that users always have access to the latest features.

The autovi.web interface is available at autoviweb.netlify.app. This section discusses the implementation based on autovi.web version 0.1.0.

616 3.1. Implementation

The package autovi.web is built using the shiny (Chang et al. 2022) and shinydashboard (Chang & Borges Ribeiro 2021) R packages. Hosted on the shinyapps.io domain, the application is accessible through any modern web browser. The R packages htmltools (Cheng et al. 2024) and shinycssloaders (Sali & Attali 2020) are used to render markdown documentation in shiny application, and for loading animations for shiny widgets, respectively.

Determining the best way to implement the interface was difficult. In our initial 623 planning for autovi. web, we considered implementing the entire web application using 624 the webr framework (Moon 2020), which would have allowed the entire application 625 to run directly in the user's browser. However, this approach was not feasible at the 626 time of writing this paper. The reason is that one of the R packages autovi depends 627 on the R package splancs (Rowlingson & Diggle 2023), which uses compiled Fortran 628 code. A working Emscripten (Zakai 2011) version of this package, which would be 629 required for webr, was not available. 630

We also explored the possibility of implementing the web interface using frameworks 631 built on other languages, such as Python. However, server hosting domains that 632 natively support Python servers typically do not have the latest version of R installed. 633 Additionally, calling R from Python is typically done using the rpy2 Python library 634 (Gautier 2024), but this approach can be awkward when dealing with language syntax 635 related to non-standard evaluation. Another option we considered was renting a server 636 where we could have full control, such as those provided by cloud platforms like Google 637 Cloud Platform (GCP) or Amazon Web Services (AWS). However, correctly setting up 638 the server and ensuring a secure deployment requires significant expertise. Ultimately, 639 the most practical solution was to use the shiny and shinydashboard frameworks, 640 which are well-established in the R community and offer a solid foundation for web 641 application development. 642

The server-side configuration of autovi.web is carefully designed to support its functionality. Most required Python libraries, including pillow and NumPy, are preinstalled on the server. These libraries are integrated into the Shiny application using the reticulate package, which provides an interface between R and Python.

Due to the resource allocation policy of shinyapps.io, the server enters a sleep mode during periods of inactivity, resulting in the clearing of the local Python virtual environment. Consequently, when the application "wakes up" for a new user session, these libraries need to be reinstalled. While this ensures a clean environment for each session, it may lead to slightly longer loading times for the first user after a period of inactivity.

In contrast to autovi, autovi.web does not use the native Python version of
TensorFlow. Instead, it leverages TensorFlow.js, a JavaScript library that allows
the execution of machine learning models directly in the browser. This choice enables
native browser execution, enhancing compatibility across different user environments,
and shifts the computational load from the server to the client-side. TensorFlow.js
also offers better scalability and performance, especially when dealing with resourceintensive computer vision models on shinyapps.io.

While autovi requires downloading the pre-trained computer vision models from GitHub, these models in ".keras" file format are incompatible with TensorFlow.js. Therefore, we extract and store the model weights in JSON files and include them as extra resources in the Shiny application. When the application initializes, TensorFlow.js rebuilds the computer vision model using these pre-stored weights.

To allow communication between TensorFlow.js and other components of the Shiny application, the shinyjs R package is used. This package allows calling custom JavaScript code within the Shiny framework. The specialized JavaScript code for initializing TensorFlow.js and calling TensorFlow.js for VSS prediction is deployed alongside the Shiny application as additional resources.

670 3.2. Design

While the R package autovi aims to provide tools that can be extended to broader visual inference applications, autovi.web is only focus on providing a straightforward and clean user interface. An overview of the graphical user interface of autovi.web is provided in Figure 8. This is the default view of the web application, and there are five regions that user can mainly interact with. Region 1 of Figure 8 is a sidebar menu

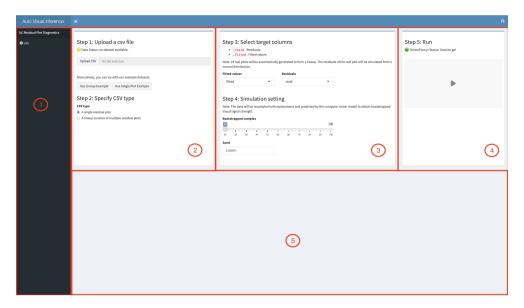


Figure 8. Overview of the autovi.web graphical user interface (GUI). This default view may change based on user interactions. Region 1 is the sidebar menu, containing the residual assessment tab and the information tab. Region 2 is the data upload panel, where users can provide a CSV file and specify the type of data it contains. Region 3 includes dropdown menus for selecting the columns to be analyzed, a slider to control the number of bootstrapping samples, and a numeric input box for setting the simulation seed. Region 4 displays the initialization status and offers a button to start the analysis. Region 5 is empty in the default view but will be populated with results once the analysis is started.

which can switch between the analysis page and the information page. The analysis page is the focus of this section.

Region 2 of Figure 8 is a panel for data uploading and CSV type selection. Clicking 678 the "upload CSV" button opens a window where the user can select a file from their 679 local system. The data status displayed above the button provides information about 680 the number of rows and columns in the current dataset. Additionally, there are two 681 example datasets available beneath the "upload CSV" button: one is a lineup example 682 using a CSV file with three columns, and the other is a single plot example using a 683 CSV file with two columns. More details about these example datasets are be discussed 684 in Section 3.3. 685

While the autovi package typically expects a fitted regression model object provided by the user, this approach is impractical for a web interface. Saving the R model object to the filesystem involves extra steps and requires users to have specific knowledge, which does not align with the goal of the web application. Moreover, the regression model object may contain sensitive, non-shareable data, making it unsuitable for uploading. Additionally, model objects are often unnecessarily large, containing extra information not needed for residual diagnostics. In contrast, a CSV file is easier to generate using various software programs, not just R. CSV files are widely accepted and can be easily viewed and modified using common desktop applications like Excel. They are generally less sensitive than raw data, as they exclude most information about the predictors.

The web application is designed to assess either a single residual plot or a lineup of residual plots. Therefore, it accepts only two types of CSV files: one with at least two columns representing the fitted values and residuals of a single residual plot, and another with at least three columns, where the additional column serves as the label or identifier for a lineup of multiple residual plots. For a single residual plot, 19 null plots are generated by simulating normal random draws from a distribution with the same variance as the original residual plot, and comparisons are made with the original residual plot. For a lineup, comparisons are made among the plots within the lineup. After uploading the CSV file, the user must select the correct format to ensure the web interface interprets the data correctly.

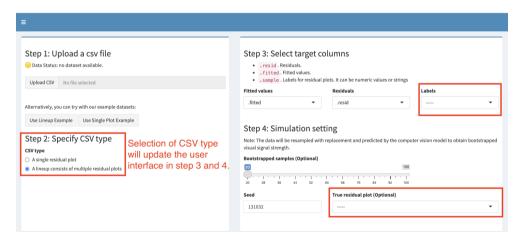


Figure 9. The panels for selecting target columns and simulation settings are updated when a different CSV type is selected in the left panel. Compared to Figure 8, where the CSV type is a single residual plot, choosing a CSV type that includes a lineup of multiple residual plots adds a dropdown menu for specifying a column for the residual plot identifier. Additionally, an optional dropdown menu for specifying the true residual plot identifier will appear under the simulation settings.

Region 3 of Figure 8 is a panel for column selection and simulation settings. As shown in Figure 8, if the CSV type is set to a single residual plot, there will be two dropdown menus for specifying the columns for fitted values and residuals, respectively. The default variable names for these columns are .fitted and .resid. After uploading the

CSV file, the content of these dropdown menus will be updated to reflect the existing 711 columns in the dataset. As displayed in Figure 9, for the CSV type that is a lineup of 712 multiple residual plots, an additional dropdown menu will appear for specifying the 713 column of residual plot labels. The default variable name for this column is .sample. If 714 this variable name does not exist in the dataset, the dropdown menu will remain empty, 715 allowing the user to specify the correct column. The number of levels for each option 716 in this dropdown menu will be displayed to help avoid the selection of a variable with 717 too many levels, which could significantly slow down the application due to extensive 718 computation. 719

Under the simulation settings, there is a slider for specifying the number of 720 bootstrapped samples needed for the assessment. A higher value on this slider will 721 result in a more accurate bootstrap distribution estimation, though it will require 722 more computation time. The simulation seed can be set in a numeric input box below 723 the slider to control the reproducibility of the assessment. By default, a random seed 724 is set each time the web page is refreshed. When the CSV type is a lineup of multiple 725 residual plots, an optional dropdown menu will appear next to the simulation seed 726 input box, allowing the user to specify an identifier for the true residual plot. If no 727 label is provided for the true residual plot, the assessment will only estimate the 728 VSS for each residual plot in the lineup, without providing a p-value, as it cannot 729 be computed. Consequently, some result panels may be missing due to insufficient 730 information. This option is useful when the lineup consists solely of null plots or if the 731 user simply wants to obtain the VSS for multiple residual plots. 732

Region 4 of Figure 8 is the panel for triggering the assessment. It contains a large play button to start the assessment. Above the play button, a text message displays the status of TensorFlow.js, allowing users to monitor whether the JavaScript library and Keras model have been loaded correctly. The play button will remain disabled until both the data status in Region 1 and the TensorFlow.js status in Region 4 indicate that everything is ready, with both showing a green status.

Once the play button is clicked, region 5 of Figure 8 will be populated with panels displaying the assessment results. Generally, there will be four result panels, as shown in Figure 10 and Figure 11.

Region 6 of Figure 10 contains an interactive table created with the R package DT (Xie, Cheng & Tan 2024), which provides the VSS. This table includes four columns:

.sample, vss, rank, and null. The .sample column shows the residual plot labels.

For a CSV type that is a lineup, these labels are taken from an identifier column in

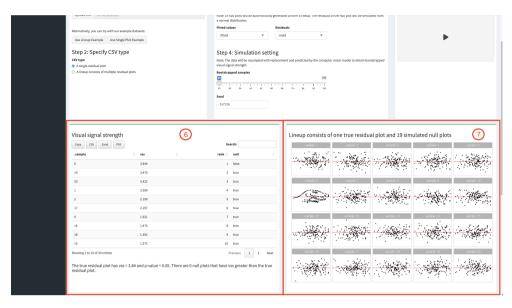


Figure 10. The first two panels of results from the automated residual assessment are shown. The application provides four results panels in total, and these screenshots display the first two. In region 1, there is an interactive table detailing the VSS, with a summary of the analysis provided in the paragraph below. Region 2 displays a lineup of residual plots.



Figure 11. The last two panels of results from the automated residual assessment are shown. The application provides four results panels in total, and these screenshots display the final two. Region 1 presents a density plot comparing the bootstrapped VSS with the null VSS. Region 2 includes an attention map of the true residual plot.

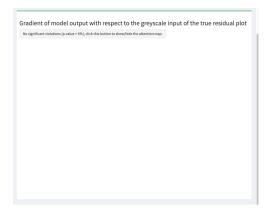


Figure 12. The attention map is hidden if the assessment indicates a p-value greater than 0.05. A button is available to toggle the display of the attention map.

the dataset specified by the user. In the case of the CSV type is a single residual plot, 746 labels are automatically generated from 1 to 20, with the true residual plot receiving 747 a randomly assigned label. The vss column displays the VSS for each residual plot, 748 749 rounded to three decimal places. The rank column indicates the ranking of each residual plot based on VSS. The null column reveals whether the plot is a null plot. 750 For the CSV type that is a single residual plot, only the true residual plot will have 751 "false" in this column, while all other plots will be marked "true." For the CSV type 752 that is a lineup, if the true residual plot identifier has not been provided, this column 753 will show "NA" to represent missing values. If the identifier is provided by user, the 754 column behaves as if the CSV type is a single residual plot. 755

The DT table provides several interactive features. Users can download the table in four formats, including text, CSV, Excel, and PDF, using the buttons located above the table. Additionally, the table is searchable via the text input field also positioned above it. Below the table, a text message displays the *p*-value of the assessment for the true residual plot and summarizes the number of null plots with VSS greater than that of the true residual plot. This helps the user determine whether the true residual plot shows visual patterns that suggest model violations.

Region 7 of Figure 10 provides a lineup of plots corresponding to each .sample value from the table in Region 6. Due to space limitations, a maximum of 20 residual plots will be displayed, ensuring that the true residual plot, if known, will be included in the lineup. The plots are generated using ggplot2, the same as in autovi. Users can perform a visual test with this lineup to check if the true residual plot is distinguishable from the other plots, helping to determine the significance of model violations.

Region 8 of Figure 11 displays the density plot for bootstrapped VSS and null VSS. 769 The densities are shown in distinct colors that are friendly for colorblind users. A solid 770 vertical line marks the VSS of the true residual plot, while rug lines at the bottom 771 of the plot provide a clearer view of individual cases. Below the plot, a text message 772 indicates the number and percentage of bootstrapped residual plots that would be 773 rejected by the visual test when compared to the null plots. Note that the bootstrapped 774 residual plots in this application are generated differently from autovi. Since we do 775 not have the R model object, we can not refit the regression model with bootstrapped 776 data. Instead, we bootstrap the residuals of the true residual plot directly to obtain 777 bootstrapped residual plots. As as result, this panel will disappear when the true 778 residual plot is unknown. 779

Region 9 of Figure 11 displays an attention map for the true residual plot, generated 780 by computing the gradient of the Keras model's output with respect to the greyscale 781 input of the plot. The attention map helps to understand how the Keras model predicts 782 VSS and which areas it is focusing on. We use a greyscale input because it is easier to 783 generate a clear attention map in this format, and it usually conveys all the essential 784 information, as most of the important details of the plot are drawn in black. If the 785 p-value of the true residual plot is greater than 0.05, checking the attention map is 786 not necessary. However, to provide users with the option to review it if they wish, a 787 button will be available, as shown in Figure 12. This button allows users to toggle the 788 display of the attention map. 789

790 **3.3. Workflow**

The workflow of autovi.web is designed to be straightforward, with numbered steps displayed in each panel shown in Figure 8. There are two example datasets provided by the web application, as mentioned in Section 3.2. The single residual plot example uses the dino dataset from the R package datasauRus (Davies, Locke & D'Agostino McGowan 2022). The lineup example uses residuals from a simulated regression model that has a non-linearity issue. We will walk through the lineup example to further demonstrate the workflow of the web application.

As shown in Figure 13, to use the lineup example data, click the "Use Lineup Example" button. The data status will then update to show the number of rows and columns in the dataset, and the CSV type will automatically be selected to the correct option. Since the example dataset follows the variable naming conventions assumed by the web application, the columns for fitted values, residuals, and labels of residual plots

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are set automatically (Figure 14). If the user is working with a custom dataset, these options must be set accordingly. Regardless of the dataset, the user must manually select the label for the true residual plot, as the web application allows assessments without this label. The next step is to click the play button to start the assessment.

Results are provided in multiple panels as displayed in Figure 15, Figure 16, Figure 17 807 ຂດຂ and Figure 18. In Figure 15, the first row of the table is the most crucial to check, as it provides the VSS and the rank of the true residual plot among the other plots. The 809 summary text beneath the table provides the p-value, which can be used for quick 810 decision-making. In Figure 16, the lineup is for manual inspection, and the user should 811 see if the true residual plot is visually distinguishable from the other plots, to confirm 812 if the model violation is serious. The density plot in Figure 17 offers a more robust 813 result, allowing the user to compare the distribution of bootstrapped VSS with the 814 distribution of null VSS. Finally, the grayscale attention map shown in Figure 18 can 815 be used to check if the target visual features, like the non-linearity present in the 816 lineup example, are captured by the computer vision model, ensuring the quality of 817 the assessment. 818

4. Conclusions

This paper presents new regression diagnostics software, the R package autovi and its accompanying web interface package, autovi.web. It addresses a critical gap in the current landscape of statistical software. While regression tools are widely available, effective and efficient diagnostic methods have lagged behind, particularly in the field of residual plot interpretation.

The autovi R package, introduced in this paper, automates the assessment of residual plots by incorporating a computer vision model, eliminating the need for time-consuming and potentially inconsistent human interpretation. This automation improves the efficiency of the diagnostic process and promotes consistency in model evaluation across different users and studies.

The development of the accompanying Shiny app, autovi.web, expands access to these advanced diagnostic tools, by providing a user-friendly interface. It makes automated residual plot assessment accessible to a broader audience, including those who may not have extensive programming experience. This web-based solution effectively addresses the potential barriers to adoption, such as complex dependencies and installation requirements, that are often associated with advanced statistical software.

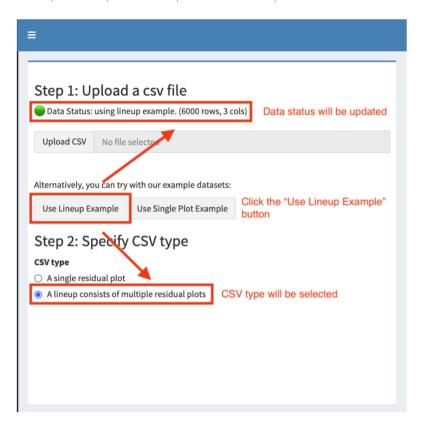


Figure 13. To begin the workflow for autovi using the lineup example dataset, the user clicks the "Use Lineup Example" button to load the example dataset, during which the data status and CSV type will be automatically updated.

The combination of autovi and autovi.web offers a comprehensive solution to the challenges of residual plot interpretation in regression analysis. These tools have the potential to significantly improve the quality and consistency of model diagnostics across various fields, from academic research to industry applications. By automating a critical aspect of model evaluation, they allow researchers and analysts to focus more on interpreting results and refining models, rather than grappling with the intricacies of plot assessment.

The framework established by autovi and autovi.web opens up exciting possibilities for further research and development. Future work could explore the extension of these automated assessment techniques to other types of diagnostic plots and statistical models, potentially revolutionizing how we approach statistical inference using visual displays more broadly.

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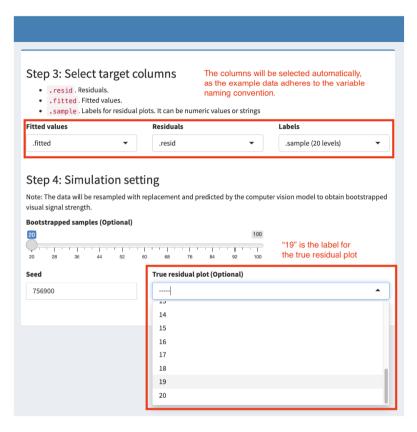


Figure 14. After clicking the button in Figure 13, the target columns are selected automatically, though the user must manually select the label for the true residual plot, as the web application permits assessment without this label.

5. Resources and Supplementary Material

The the current version of autovi can be installed from CRAN, and source code for both packages are available at https://github.com/TengMCing/autovi. The web interface is available from autoviweb.netlify.app.

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These R packages were used for the work: tidyverse (Wickham et al. 2019), lmtest (Zeileis & Hothorn 2002), kableExtra (Zhu 2021), patchwork (Pedersen 2022), rcartocolor (Nowosad 2018), glue (Hester & Bryan 2022), here (Müller 2020), magick (Ooms 2023), yardstick (Kuhn, Vaughan & Hvitfeldt 2024) and reticulate (Ushey, Allaire & Tang 2024).
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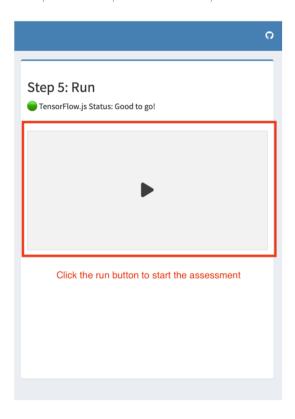


Figure 15. After finishing the required steps in Figure 13 and Figure 14, the user initiates the assessment of the lineup example data by clicking the run button.

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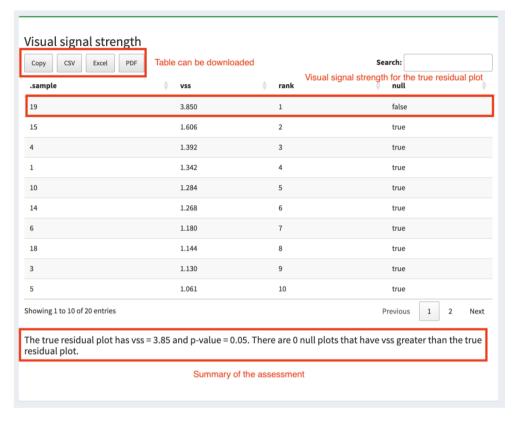


Figure 16. The VSS of the true residual plot is displayed in the first row of the table, with a summary text beneath the table providing the p-value to aid in decision-making.

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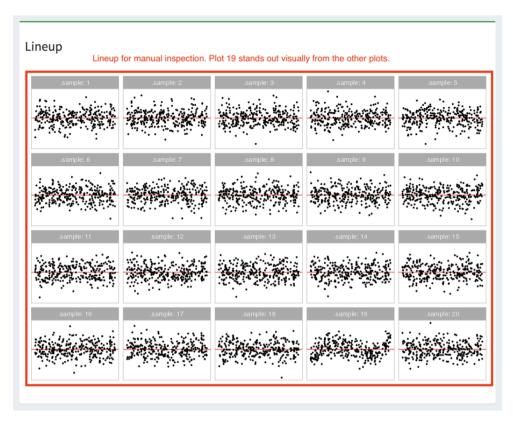


Figure 17. A lineup of residual plots allows for manual inspection.

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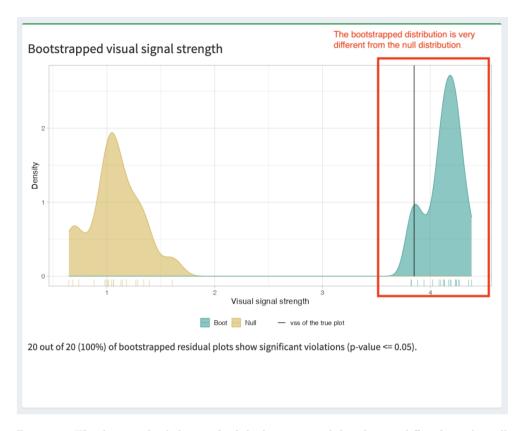


Figure 18. The density plot helps verify if the bootstrapped distribution differs from the null distribution.

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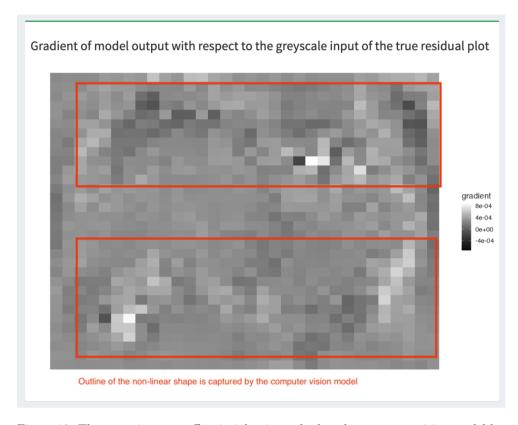


Figure 19. The attention map offers insights into whether the computer vision model has captured the intended visual features of the true residual plot.

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