

1. (a) Mutant #3 Mutant #4
 (b) Case #3 Case #4
 (c) Case #3 only strongly kill Mutant #2, So $|killed\ mutants| = 1$
 Since $|mutants| = 5$
 Then mutation score = $\frac{|killed\ mutants|}{|mutants|} = \frac{1}{5}$

The surviving mutants are Mutant #1, #3, #4, #5

(d) Case #4 strongly kills Mutant #1, #2, #4, #5

Case #5 strongly kills only Mutant #4

So the complete test suit strongly kills Mutant #1, #2, #4, #5

$$\begin{aligned} |killed\ mutants| &= 4 & |mutants| &= 5 \\ \text{mutation score} &= \frac{|killed\ mutants|}{|mutants|} = \frac{4}{5} \end{aligned}$$

The surviving mutant is Mutant #3

(e)

Case# \ Mutant#	1	2	3	4	5
1				killed	
2			killed	killed	
3	killed				
4	killed			killed	killed
5				killed	

"killed" means some mutant is killed by some case.

Mutant #4

(f) Mutant #1, #3, #5

2. (a) Yes, it is.

Directly analyze the source code of caesar_cipher, or compare the two source codes

(b) Yes, it is.

Blackbox testing and compare the outputs of the two functions with the same inputs

(c) Yes, it is

Blackbox testing and compare the outputs of the two functions with the same inputs

(d) No, it isn't.

3. (a)

$$Z = F(y) = y$$

Since there are 26 characters in alphabet, then any character with bias 26 will be itself.

Besides, Line #6: $output += chr((ascii_val - 65 + b) \% 26 + 65)$

$$\begin{aligned} \text{Here, } chr((ascii_val - 65 + b) \% 26 + 65) &\text{ is defined as original expression} \\ \text{change } b \text{ into } b+26: &chr((ascii_val - 65 + b + 26) \% 26 + 65) \\ &= chr((ascii_val - 65 + b) \% 26 + 26 \% 26 + 65) \\ &= chr((ascii_val - 65 + b) \% 26 + 26 \% 26 + 65) \\ &= chr((ascii_val - 65 + b) \% 26 + 65) = \text{original expression} \end{aligned}$$

So does Line #8.

Therefore, $Z = f(g(x)) = f(c(s, b+26)) = f(c(s, b)) = f(x) = y$

(b) No test case can detect the defects.

Mutants #4: $\Delta 7$. output $\neq \text{chr}((\text{ascii_val} - 97 - b) \% 26 + 97)$

Here, $\text{chr}((\text{ascii_val} - 97 - b) \% 26 + 97)$ is defined as original expression
change b into $b+26$: $\text{chr}((\text{ascii_val} - 97 - (b+26)) \% 26 + 97)$

$$= \text{chr}((\text{ascii_val} - 97 - b) \% 26 - 26 \% 26 + 97)$$

$$= \text{chr}((\text{ascii_val} - 97 - b) \% 26 - 0 + 97)$$

$$= \text{chr}((\text{ascii_val} - 97 - b) \% 26 + 97) = \text{original expression}$$

Outputs before transformed and after transformed are the same.

So any defects can't be detected.

4. (a) O#1: "bcd"

O#2: "C"

O#3: "VWX"

O#4: "Hello, World!"

O#5: "Vlbrhal"

(b) No test case can detect the defects.

Mutants #4 is $\Delta 7$. output $\neq \text{chr}((\text{ascii_val} - 97 - b) \% 26 + 97)$

Here, $\text{chr}((\text{ascii_val} - 97 - b) \% 26 + 97)$ is defined as original expression

After inserting $b = -(26 - b) \% 26$,

we have $\text{chr}((\text{ascii_val} - 97 - (-(26 - b) \% 26)) \% 26 + 97)$

$$= \text{chr}((\text{ascii_val} - 97 + (26 - b) \% 26) \% 26 + 97)$$

$$= \text{chr}((\text{ascii_val} - 97 + (26 \% 26) - (b \% 26)) \% 26 + 97)$$

$$= \text{chr}((\text{ascii_val} - 97 + 0 - b) \% 26 + 97) \quad \text{notice that } (b \% 26) \% 26 = b \% 26$$

$$= \text{chr}((\text{ascii_val} - 97 - b) \% 26 + 97) = \text{original expression}$$

The outputs before inserting and after inserting are the same.