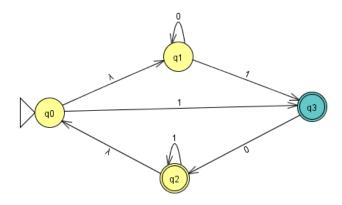
Submit a pdf in Canvas. Use a word processor and/or JFLAP. (30 pts)

1) (4 pts) Convert the following NFA into an equivalent DFA



- 2) (3 pts) Show that the language L = {  $vwv : v, w \in \{a,b\}^*, |v| = 2$ } is a regular language.
- 3) (4 pts) Prove that if L is regular language then L<sup>R</sup> is a regular language.
- 4) (9 pts) Give regular expressions for the following languages on  $\Sigma = \{a, b\}$ 
  - a)  $L_1 = \{ w : n_a(w) \mod 3 = 1 \}.$
  - b)  $L_2 = \{ w : w \text{ ends in } aa \}.$
  - c)  $L_3$  = all strings containing no more than three a's.
- 5) (4 pts) Consider a type of scientific notation for real numbers with the following rules:
  - a. A number can be preceded by a "+" or "-" sign or the sign may be absent.
  - b. Numeric values must be of the form  $cb_1b_2...b_n$  where  $b_i$  is any digit, but c must be nonzero.
  - c. The number may be followed by an exponent field of the form  $e''+''y_1y_2$  or  $e''-''y_1y_2$ , where  $y_i$  can be any digit  $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$ .

For example the strings -123e+10 and 257 represent real number in this scientific format. Give a regular expression for this scientific notation. Let  $\Sigma = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, "+", "-", e\}$ . (Note: With this convention "+" is the sign associated with the scientific number and + the operator of the regular expression.)

- 6) (6 pts) Find a regular grammars for the following languages on  $\Sigma = \{a, b\}$ :
  - a)  $L_0$  is all strings with exactly one  $\alpha$
  - b)  $L_1 = \{ w : n_a(w) \mod 3 = 1 \}.$